## **Building the Column Generation Loop**

**Step 0** Compute the parameters  $u_i^q$  and  $\delta_{ir}^q$ . There are helper functions to do this.

**Step 1** Solve the RMP.

Step 2 Modify the dual for this RMP.

If we look at our dual formulation, we notice that all constraints except one don't depend on what Q is. Instead they are functions on i and t, which means they don't need to be updated if we change Q etc. The one exception, of course, is that one constraint which involves Q:  $\sum_i \pi_i u_i^q + \rho + \sum_i \sum_t \mu_{it} \delta_{it}^q \leq C^q \ \forall q.$  Since our variable for the model of the dual,

modual, has already been calculated, we only need to update this one constraint.

- **Step 3** Solve the dual and extract the values of  $\rho$ ,  $\pi_i$ , and  $\mu_{ii}$ .
- **Step 4** Plug in these values and other parameters to the sp\_lsa.
- **Step 5** Extract the single best route with the most negative reduced cost from the LSA.
- **Step 6** Find the timestamps associated with the route, as well as the distances. The route should no longer be of the form [location, location, location...] but [[[location, time], [location, time], dist]...]
- **6.1** The first step is getting the identity of the route which can be done by checking feasibility and changing cost if necessary.

(no longer necessary)

- **6.2** The second step is to get time information which proceeds as follows:
- First, set all times to be 0. There are as many 0's as there are elements in the best route.
- Then, for each node from 2 to the length of the best route (because the 1 will of course start at time 0):
  - Start with the initial time of the previous node which we will add to.
  - Obtain the location of the previous node.
  - Obtain the load of work from the previous node. If not the depot (which currently says 1), indicate the true workload of the previous node.
  - Now, gather the new location.
  - Compute the total: prev\_time + prev\_load + distance\_to\_travel\_from\_prev\_to\_new.
  - Finally the maximum of this new total and the window start of the new location is your time info for this time.

**Step 7** Add this route to Q.

**Step 8** Update all the parameters: every constraint, the objective, Q, n\_routes...