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# Multiagent Reinforcement Learning in a Synchronous Strategy Game

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## Abstract

A lot of studies have been done on reinforcement learning recently. Q learning, or DQN tries to solve the single agent vs environment problem, where some other approaches such as AlphaGo attempt the double agent game. In this project, we try to find an algorithm to generate an agent that performs well in a multiagent synchronous strategy game.

Note: Version 2 changes are highlighted in yellow.

## 1 Introduction

Battlesnake is a synchronous strategy game. It is simply a multiplayer version of the classic game Snake. The version we are training with is a 11x11 game board with 4 snakes. In each round, players choose an action from the space *left, right, up, down*, the snake's head and body will then move accordingly. If a snake's head runs into any obstacle (a snake's body or wall), it dies. If it runs into another snake's head, the shorter snake dies (in a tied situation both snakes die). If it runs into a food, its length will grow by 1, and its health point resets to 100. Every turn, all snake's health will decrease by 1, and once it reaches 0 the snake dies. The last snake alive becomes the winner of the game. If no snakes live, it is considered a draw. See the reference for a more detailed description [1]. An image of such a game is shown below in figure 1.

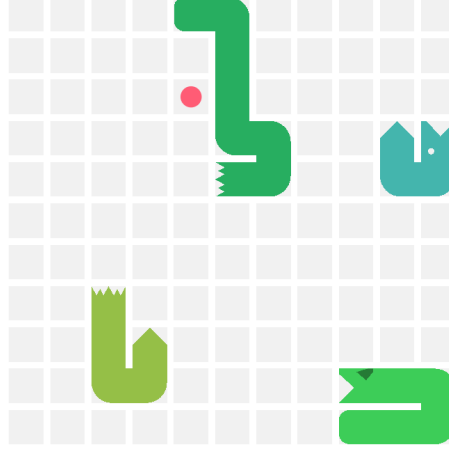


Figure 1: A game of battlesnake in-progress.

## 2 Related Work

AlphaSnake Zero uses the same approach that AlphaGo Zero used [2], where the training algorithm consists of 3 stages, self-play, training and pit. Due to the lack of a powerful computing device (a TPU), the network for AlphaSnake is simplified. AlphaGo uses a two headed network to compute the value (roughly interpreted as win rate) of the current game board, and also a policy to guide the next action. As this is a reinforcement learning problem, there is no true label that we can assign to the training data. Instead, a Monte Carlo Tree Search is used to get a good estimate of the optimal policy. See figure 2 to see the steps of the Monte Carlo tree search algorithm.

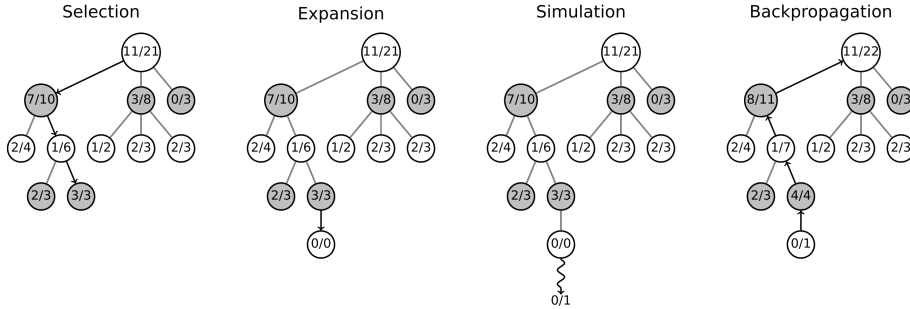


Figure 2: Steps of the MCTS algorithm

## 3 Method

In each iteration, a number of games are played using the current neural network, with data being recorded for training. For each turn of the game, we keep the information of the game board (the

state), the move each snake made (the action), the computed Q values, the transition probability (expanded on later). Then we use the data to train the network. After training, the new network competes against the old one and further replace it if performance is better. A general overview of this process is shown in figure 3 below.

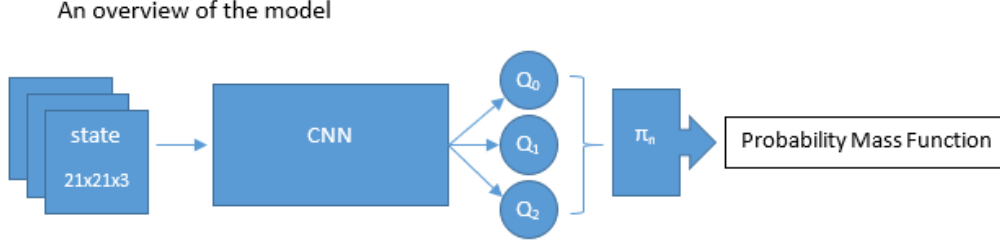


Figure 3: AlphaSnake Zero Model

For the input of the network, we need something that can recover enough information of the game board. The designed state representation is as follows: The state is a  $21 \times 21 \times 3$  tensor. The game board is only  $11 \times 11$ , thus the snake will quickly struggle to identify where it's head lies. To combat this, the view of the game is centered at the snake's head, allowing immediate recognition of relative position. Imagine you are the snake and you view the world around you, so a  $21 \times 21$  board is needed to perceive the original board in the worst case (if we are at the edge). Additionally, every snake has its own view of the board so this is replicated 3 more times.

There are essentially three fundamental things in the game; if you run into you die (body and wall), if you run into you grow (food), and if you run into another snake will die (head). Thus, the game board is classified into 3 channels. The first layer is the picture of all the snakes' heads. The second one is for all the 'deadly' obstacles (bodies and walls). And the last one shows all the food on the board. In all layers, 0 means an empty cell.

In the first layer, the value of a snake's head is the snake's length relative to the current player, so a negative value means a shorter snake's head and vice versa. Since a snake of the same length as you also kills you, the value of its head is also negative. Overall, the value roughly tells you how dangerous a block is. The formula for computing the head value is simply

$$value = (\text{length of the snake} - \text{length of you} + 0.5) \times \text{multiplier} \quad (1)$$

where the multiplier is to keep the value in the range of  $[-1, 1]$  for training purposes. The 0.5 solves two problems, one mentioned earlier about the snake of same length, and it avoids the value inside the brackets defaulting to zero, causing an "invisible head".

In the second layer, the wall is simply represented with 1. We also need something to recover the direction of a body block, since it holds the information about how the snake moves on the board. But what is really essential is how long a body block will remain at its position. If we represent the body as the number of turns until it will be away, then we can roughly recover the information of a snake by tracing the increasing value of the body blocks. The number of turns until it will be removed is simply the body length measured from that body block to the tail of the snake. The value is calculated using the following formula

$$value = (\text{number of turns until it's removed}) \times \text{multiplier} \quad (2)$$

There are degenerate cases where it is not possible to tell which body belongs to which snake, but body blocks all work the same way, so it does not matter.

In the last layer, all the food is labeled according to the snake's health points. This has a huge benefit to reducing the difficulty of learning. It strongly relates the food to health, and no explicit information for health needs to be stored.

$$value = (101 - \text{your health}) \times \text{multiplier} \quad (3)$$

Note that it is impossible to recover the health of other snakes, but according to the experience of Battlesnake tournaments, it is not a useful information, as death due to starvation almost never happens in high level games. We use 101 instead of 100 to avoid the value inside the brackets to be zero, resulting in “invisible food”.

For the output of the network, we need something that can guide the action to take. A policy could be a good choice, but unlike the game of Go, where a move usually just adds another piece on the board, MCTS is too expensive for Battlesnake, because a move will drastically change the game board and thus be very slow to compute. Instead of approximating the optimal policy, it is easier to obtain a good estimation of the Q values. Assume the optimal function for Q value is  $Q(s, a)$ , where it takes as input the current state  $s$  and the action  $a$ , and it outputs the value (win rate) of the player if that action  $a$  is chosen under state  $s$ . An obvious fact is that a game board of Battlesnake is equivalent to its rotation and reflections (with actions also rotated or reflected, of course). Thus, we can rotate the board so that the snake is always facing upwards. This mainly has two benefits. First, it automatically treats all rotations as one, thus reducing overfitting. Second, there is always a backward move that immediately kills you (run into your own body), so this action is meaningless to evaluate. If the snake is always facing up, the output space can be transformed into *turn left, go straight, turn right*, represented by numeric values 0,1,2. It simplifies the network and training. Although it is true that only for the very first move, there are technically four choices, but we don’t care about that one move so much that we want to expand the output space. During the training, we can also make the reflections of the board and Q value vectors to force the network to realize symmetry, and hopefully reduce overfitting. Once we have the 3 dimensional vector  $\langle Q(s, 0), Q(s, 1), Q(s, 2) \rangle$ , namely the Q value of each action  $a_i$  given the current state  $s$ , a softmax-like function is going to generate a probability mass function based on the values, which is the policy. The softmax-like function, denoted  $\pi$ , is simply softmax with exponent  $n$  instead of  $e$ .

$$\pi_n(\vec{v}) = \vec{v}^{\circ n} \cdot (\sum_i \vec{v}^{\circ n}_i)^{-1} \quad (4)$$

Here,  $\vec{v}$  is a vector and  $n$  is a constant.  $\vec{v}^{\circ n}$  denotes the element-wise power. By picking the  $n$ , we can control how explorative the snake is, the higher  $n$  is, the more it highlights the higher values in  $\vec{v}$ , and thus it would not bother to pick the lower valued actions.

To get a good estimate of the value function without MCTS, we label the Q values according to the following criteria. From the point of view of any snake, the transition between states is not deterministic. The transition is a Markov process because it depends on how other snake moves. Let the function  $\Psi(s_0, a, s_1)$  represents the probability of entering state  $s_1$ , if you take the action  $a$  at current state  $s_0$ . Let the Q value vector of state  $s_0$  be  $\langle Q(s_0, 0), Q(s_0, 1), Q(s_0, 2) \rangle$ . Say  $Q(s_0, a)$  is high and you pick this action  $a$ . Now with probability  $\Psi(s_0, a, s_1)$ , we then have entered the next state  $s_1$ , and we now get the Q values  $\langle Q(s_1, 0), Q(s_1, 1), Q(s_1, 2) \rangle$ . Since the Q values represent win rate, the optimal strategy is to pick  $\arg \max_{a_i} Q(s_1, a_i)$ . Then we can say that, at state  $s_0$ , if we pick action  $a$ , with probability  $\Psi(s_0, a, s_1)$ , we end up with a win rate of  $\max_{a_i} Q(s_1, a_i)$ . Obviously, we can see that the Q value is a weighted sum of the max Q values of its successor states, thus we have

$$Q(s_0, a) = \sum_{s_i} \Psi(s_0, a, s_i) \max_{a_j} Q(s_i, a_j) \quad (5)$$

This equation is the core part of AlphaSnake Zero’s training algorithm. We can now refine the Q value vector by updating its explored entry  $Q(s_0, a)$ . A complete record of a game play gives a chain of states for each snake. We update the Q values recursively, from the very last state to the first. We know what  $\max_{a_i} Q(s_1, a_i)$  is, namely the max value of the successor of  $s_0$  recorded in the chain of states. Assuming the network is already somewhat accurate, we don’t want to change  $Q(s_0, a)$  unless  $\max_{a_i} Q(s_1, a_i)$  has been refined. If  $\max_{a_i} Q(s_1, a_i)$  was updated to  $\max_{a_i} Q^*(s_1, a_i)$  during the previous step, then we want the new  $Q^*(s_0, a)$  to be

$$\begin{aligned}
& \Psi(s_0, a, s_1) \times \max_{a_i} Q^*(s_1, a_i) + \sum_{s_i \neq s_1} \Psi(s_0, a, s_i) \max_{a_j} Q(s_i, a_j) \\
&= \Psi(s_0, a, s_1) \times \max_{a_i} Q^*(s_1, a_i) + \sum_{s_i} \Psi(s_0, a, s_i) \max_{a_j} Q(s_i, a_j) \\
&\quad - \Psi(s_0, a, s_1) \times \max_{a_i} Q(s_1, a_i) \\
&= \Psi(s_0, a, s_1) \times [\max_{a_i} Q^*(s_1, a_i) - \max_{a_i} Q(s_1, a_i)] + \sum_{s_i} \Psi(s_0, a, s_i) \max_{a_j} Q(s_i, a_j) \\
&= \Psi(s_0, a, s_1) \times [\max_{a_i} Q^*(s_1, a_i) - \max_{a_i} Q(s_1, a_i)] + Q(s_0, a)
\end{aligned} \tag{6}$$

We can see that if the max of its successor was unchanged then the new value  $Q^*(s_0, a)$  just remains unchanged, too. There is, however, a flaw in this updating method. It has no guarantee on that the new Q value staying in the range  $[0, 1]$ , which is the practical range for win rate, and also the range for the sigmoid function. In practice, if the network is already somewhat good, a bad value should almost never happen, but we are still supposed to set the bound manually. If it does happen, say the new  $Q^*(s_0, a) \geq 1$ , then this one is guaranteed to be the new maximum since all other Q values is computed by sigmoid and thus less than 1. Then, it very likely will shoot up its parent state's Q value over 1 and recursively messes up the whole chain of states. Thus, we assign the following bounded value to  $Q^*(s_0, a)$ .

$$\min(\max(\Psi(s_0, a, s_1) \times [\max_{a_i} Q^*(s_1, a_i) - \max_{a_i} Q(s_1, a_i)] + Q(s_0, a), 0), 1) \tag{7}$$

To complete the final piece of our estimation of Q values, we need to know  $\Psi$ , the transition probability. If we get the actions of every snake, then the transition is almost deterministic, except the food spawns randomly, but that is a minor factor. Obviously, since the game is synchronous, the probability of any snake taking an action is independent from others.  $\Psi(s_0, a, s_1)$  is almost equal to the product of some entry of each policy calculated by other snakes. Let the transition function  $\Gamma(s, \vec{A})$  computes the successor state of  $s$  given  $\vec{A}$ , a vector of actions of snakes (omitting the randomness of food).

$$\Psi(s_o, a, \Gamma(s_o, \langle a, a_1, \dots, a_k \rangle)) \approx \prod_{i=1}^k \pi_n(\langle Q(s_i, 0), Q(s_i, 1), Q(s_i, 2) \rangle)_{a_i} \tag{8}$$

Here  $\pi_n$  is the softmax-like function,  $s_i$  is the  $i$ th snake's view of state  $s_0$  (not including you since you explicitly made action  $a$ ), and  $a_i \in 0, 1, 2$  is the action it chose. There is one exception; if a snake made an action and died right after, then the assigned value is simply 0 since it is usually not relevant to what last moves other snakes chose unless it died due to head on head collision.

Since the training data is massive, a good trick is to obtain a sample from the training data. There are various ways to sample the data, but one thing to realize is that late game might be far more important than the early game. The sampling method used in the training algorithm makes an exponentially growing gap between samples counting from the last move, to the first. Another trick is to use batch normalization between layers in the network because reinforcement learning tends to change the input distribution, it introduces instability to the learning, and batch normalization can address that problem. Another problem we encountered during training is that after some number of iterations, the snakes realize that if it runs into something they die, so they come up with the so-called "chicken snake" strategy, where one snake just moves in circles and does nothing. In other words, it is stuck at a local optimum. To avoid this, we let the snake learn in a modified environment where every turn the health is reduced by 9, so it will quickly die from starvation and force it to go look for food. After that, we put it into the original environment. We call that "learn to walk before you run". Be careful with the choice of the decrement value. We still want it to realize that once the health gets to 1, it will die next turn, so the decrement must be a factor of 99. If we prime factorize 99, we can see the only options are 1, 3, 9, 11, 33, 99.

After training, the newly trained network is to be compared with the old network. Several games are played between them (can use different competing rules, 1v3 or 2v2, etc.). If the new network's win rate surpasses a threshold, it will replace the old one. A good way to select the threshold is to use a binomial distribution to figure out a value such that a worse network (say a win rate less than 50% in 2v2 games) has a negligible chance of surpassing it.

## 4 Experiments and Discussion

With limited computational power, we tried the algorithm on a small CNN. It consists of 6 convolutional hidden layers, with 32, 32, 64, 64, 128, 128 filters of size 3x3, respectively. It used "selu" as activation function [3], and batch normalization layers are added between the weights and activation functions. After running for 154 iterations, we obtained the following results as seen in figure 4 and figure 5 below.

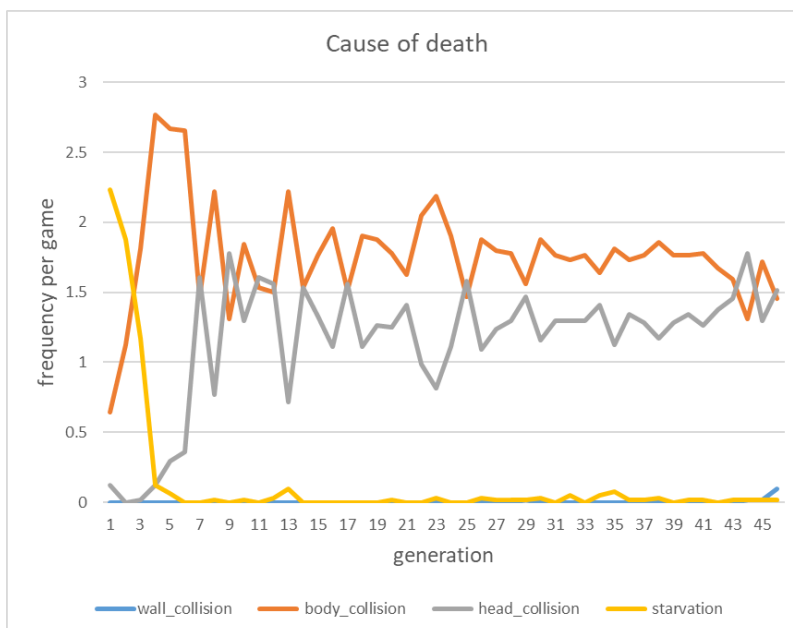


Figure 4: Cause of Death

Figure 4 above, further analyses the cause of death for the first 45 generations. The algorithm quickly learns the basics of the game as the deaths by starvation and wall collisions are close to zero following the 6th generation. However, interestingly, the number of deaths by head collisions is quite high. This is likely due to the algorithm not being able to control its aggressiveness between smaller and larger snakes.

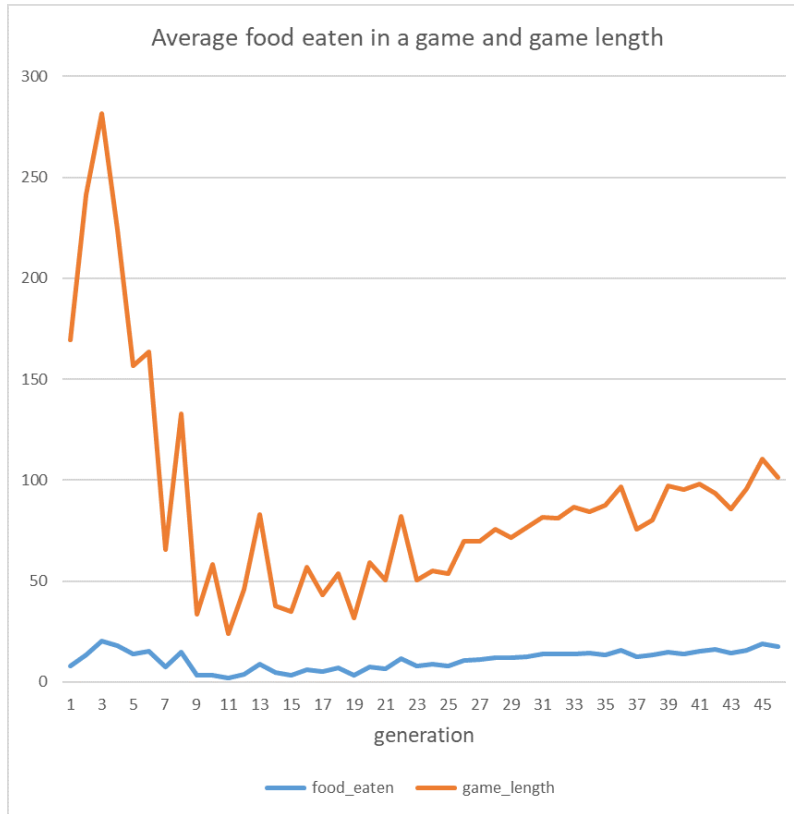


Figure 5: Average Food Eaten

Figure 5 above depicts the average food eaten per game as well as the game length. We see an upward trend on the game length, suggesting that further training would result in an overall smarter AI for the snake.

Other experiments that we have conducted were to compare 16 different generations against the best training snake provided by the battlesnake team. We compared the winrate, the average time steps in a game, the average food eaten in a game, the average number of collisions in a game, and the average number of heads hunted in a game in figure 6, 7, 8, 9, 10 respectively. Generally, we noticed that as the number of model generations/ training iterations increased the winrate, average time steps, food eaten, and heads hunted increased, while the average number of collisions decreased which are all consistent with what we'd predict with the increasing winrate as it is getting a better understanding of the rules of the game.

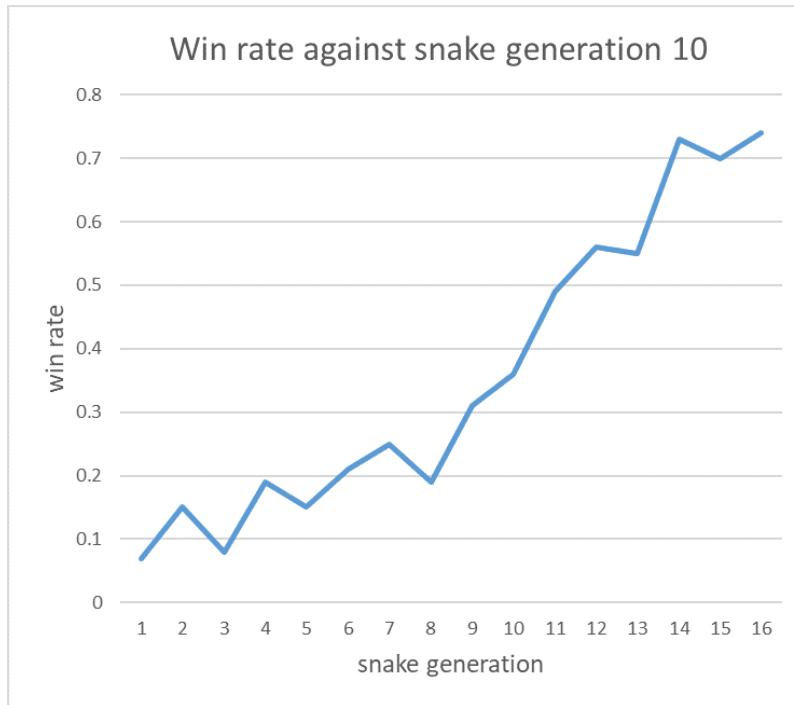


Figure 6: Winrate

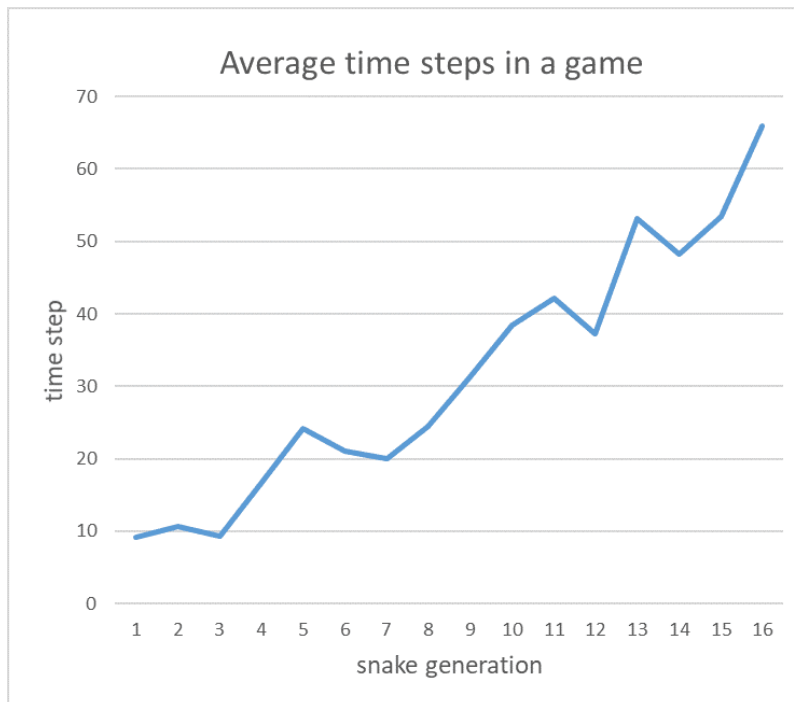


Figure 7: Average Number of Time Steps



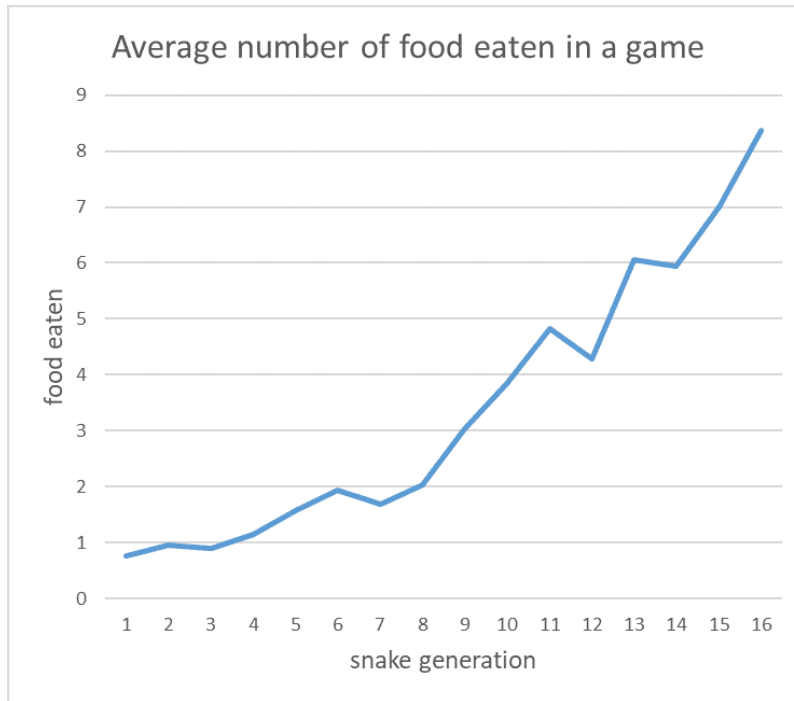


Figure 8: Average Number of Food Eaten

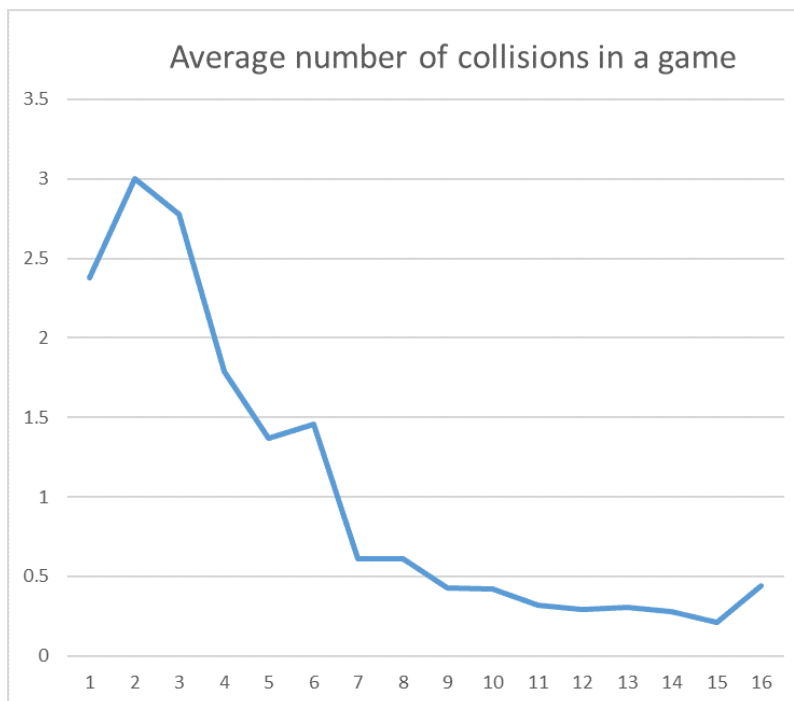


Figure 9: Average Number of Collisions

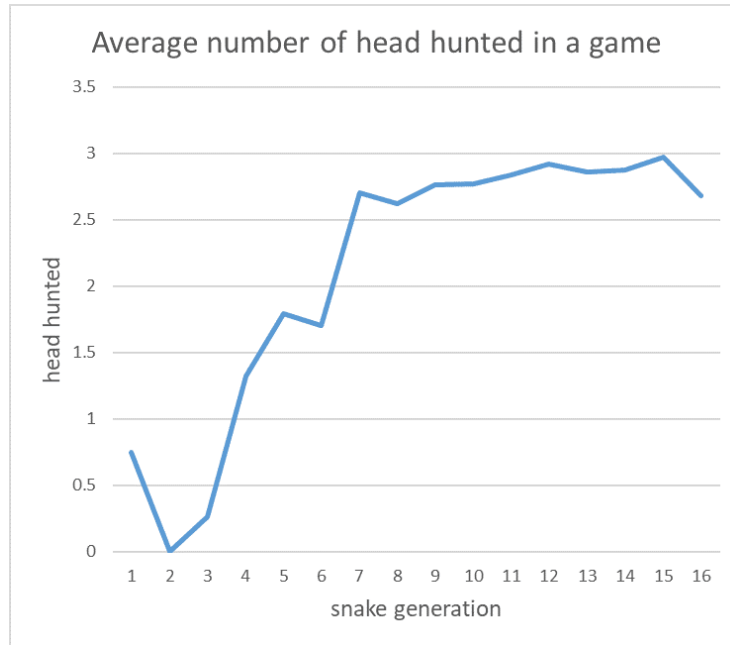


Figure 10: Average Number of Heads Hunted

For the final experiment, three different generations of the snakes were added to the Battlesnake arena to compete against other snake AIs. All performed quite well and currently in the top 150 of the leaderboard. The 10th and 15th generation AlphaSnake Zero currently sits at 147th and 135th position on the leaderboards respectively. The 145th generation is currently 100th in the world. This suggests that creating a top placing snake is possible given that there is still a lot of room for improvement and optimization for the AI.

The next steps for improving our algorithm include the following:

1. Further experimentation with the look-ahead algorithm and in particular using the Monte Carlo Tree search algorithm
2. Conduct further testing with varying input parameters for model training
3. See how our model performs as we continue to increase the number of training iterations and if it reaches more local optimums
4. Consider implementing better heuristics
5. Consider using a better computing device to increase training efficiency

## 5 Conclusion

We have presented our initial implementation of the AlphaGo version AI algorithm for battlesnake, which has proven to have a reasonable winrate. Furthermore, it seems to have potential due to several areas of improvement including look-ahead and a loss function implementation. Our AI has also proven to be a viable reinforcement learning solution as it has improved throughout each of its training iterations. We hope to explore our solution further by implementing the previous features, continuing training our model, and varying our training parameters. We'd also like to further explore how it compares against other solutions and how to more reliably compare them without bias.

## Acknowledgments

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## References

- [1] B. Inc, “Battlesnake documentation.” <https://docs.battlesnake.com/>, 2020. [Online; accessed 1-April-2020].
- [2] K. S. David Silver, Julian Schrittwieser, “Mastering the game of go without human knowledge.” <https://www.nature.com/articles/nature24270>, 2017. [Online; accessed 1-April-2020].
- [3] Klambauer, “Self-normalizing neural networks.” <https://arxiv.org/pdf/1706.02515.pdf>, 2017. [Online; accessed 1-April-2020].