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Q Given three integers n , a and b return n^{th} magical no.
Answer may be very large return $(10^9 + 7)$ mod.

=> Brute Force Approach :-

- i) Get the min of the given two elements.
- ii) Keep two counters for both numbers starting with 1.
- iii) Multiply both number with their respective counter and pick the minimum number increment the counter of respective number.
- iv) Repeat step 3 for n times
- v) return the last number
- vi) The last number will be the required magical no.

=> Optimal Binary Search approach :-

- i) Find the LCM of the given two numbers.

$$\text{LCM} = (a * b) / \text{gcd}(a, b)$$

- ii) Set the range of binary searching :-

$$\text{low} = \min(a, b)$$

$$\text{high} = n * \min(a, b)$$

- iii) Get the midpoint :

$$\text{midpoint} = (\text{low} + \text{high}) / 2$$

- iv) For each midpoint count magic :

$$\text{magic} = \text{midpoint}/a + \text{midpoint}/b - \text{midpoint}/\text{LCM}$$

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v) If $\text{magic} < n$:
 move low to midpoint
 else
 move high to midpoint

vii) return $(\text{high}) \% (10^9 + 7)$