

习题 6.2 判断下列文法是不是 LL(1)文法, 若不是, 转换之。

(1)  $\check{A} \rightarrow \varepsilon | \check{A}\check{A}$ ;  $A \rightarrow Td | Td[\check{I}]$   $T \rightarrow \text{int} | \text{float}$   $\check{I} \rightarrow i | \check{I}, i$

(2)  $S \rightarrow Ab$   $A \rightarrow a | B | \varepsilon$   $B \rightarrow b | \varepsilon$

(3)  $S \rightarrow aSe | B$   $B \rightarrow bBe | C$   $C \rightarrow cCe | d$

(1)  $\text{first}(\check{A}) = \{\varepsilon, \text{int}, \text{float}\}$ ,  $\text{first}(A) = \{\text{int}, \text{float}\}$ ,  
 $\text{first}(T) = \{\text{int}, \text{float}\}$ ,  $\text{first}(\check{I}) = i$   
 $\text{follow}(\check{A}) = \{\text{int}, \text{float}\}$ ,  $\text{follow}(A) = \{;$   
 $\text{follow}(T) = \{d\}$ ,  $\text{follow}(\check{I}) = \{, , ]\}$   
 $\therefore \check{A} \rightarrow \varepsilon$  且  $\text{first}(\check{A}) \cap \text{follow}(\check{A}) \neq \emptyset$

$\therefore$  不是 LL(1)文法, 同样 A 的两个子式 first 集也重叠, 这是左递归

$\therefore$  修改如下:  $\check{A} \rightarrow \check{A}\check{A}' | \varepsilon$   
 $\check{A}' \rightarrow ; \check{A} \check{A}'' | \varepsilon$   
 $A \rightarrow T d \check{A}''$   
 $\check{A}'' \rightarrow [ \check{I} ] | \varepsilon$   
 $T \rightarrow \text{int} | \text{float}$   
 $\check{I} \rightarrow i \check{I}'$   
 $\check{I}' \rightarrow , i \check{I}' | \varepsilon$

(2)

	first	follow
S	{a, b}	{#}
A	{a, b, $\varepsilon$ }	{b}
B	{b, $\varepsilon$ }	{b}

$\therefore \varepsilon \in \text{first}(B)$ , 且  $\text{follow}(A) \cap \text{first}(A) \neq \emptyset$

$\therefore$  不是 LL(1), 修改如下

$S \rightarrow Ab$   
 $A \rightarrow a | b | \varepsilon$

	first	follow
S	$\{a, b, c, d\}$	$\{e\}$
B	$\{b, c, d\}$	$\{e\}$
C	$\{c, d\}$	$\{e\}$

∴  $\text{first}(aSe) = \{a\}, \text{first}(B) = \{b, c, d\}$

$\text{first}(bBe) = \{b\}, \text{first}(C) = \{c, d\}$

$\text{first}(c[e) = \{c\}, \text{first}(d) = \{d\}$

∴ is LL(1)

习题6.2; 大作业(二): 对下列文法分别计算每个变元的FIRST集和FOLLOW集, 然后从该文法中找出不满足LL(1)文法条件的各个原因。

$$P \rightarrow \check{D} \check{S}$$

$$\check{D} \rightarrow \varepsilon \mid \check{D} D;$$

$$D \rightarrow T d \mid T d[i] \mid T d(\check{A}) \{ \check{D} \check{S} \}$$

$$T \rightarrow \text{int} \mid \text{void}$$

$$\check{A} \rightarrow \varepsilon \mid \check{A} A;$$

$$A \rightarrow T d \mid d[] \mid T d()$$

$$\check{S} \rightarrow S \mid \check{S}; S$$

$$S \rightarrow d = E \mid \text{if} (B) S \mid \text{if} (B) S \text{ else } S \mid \text{while} (B) S \mid \text{return } E \mid \{ \check{S} \} \mid d(\check{R})$$

$$B \rightarrow B \wedge B \mid B \vee B \mid E r E \mid E$$

$$E \rightarrow d = E \mid i \mid d \mid d(\check{R}) \mid E + E \mid E * E \mid (E)$$

$$\check{R} \rightarrow \varepsilon \mid \check{R} R,$$

$$R \rightarrow E \mid d[] \mid d()$$

可看出  $\text{FIRST}(T) = \{\text{int}, \text{void}\} \therefore \text{FIRST}(\check{D}) = \text{FIRST}(T)$

$$\text{FIRST}(\check{D}) = \text{FIRST}(D) \cup \{\varepsilon\} = \{\text{int}, \text{void}, \varepsilon\}$$

$$\text{FIRST}(A) = \text{FIRST}(D) \cup \{d\} = \{\text{int}, \text{void}, d\}$$

$$\text{FIRST}(\check{A}) = \text{FIRST}(A) \cup \{\varepsilon\} = \{\text{int}, \text{void}, d, \varepsilon\}$$

$$\text{FIRST}(S) = \{d, \text{if}, \text{while}, \text{return}, \{ \}$$

$$\text{FIRST}(\check{S}) = \text{FIRST}(S)$$

$$\text{FIRST}(E) = \{d, i, ( \}, \text{FIRST}(R) = \text{FIRST}(E) \cup \{d\}$$

$$\text{FIRST}(\check{R}) = \{\varepsilon\} \cup \text{FIRST}(R) = \{\varepsilon, d, i, ( \}$$

$$\text{FIRST}(B) = \text{FIRST}(E) = \{d, i, ( \}$$

$$\text{FIRST}(P) = \text{FIRST}(\check{D}) \cup \text{FIRST}(\check{S})$$

综上所述可得 FIRST 集如下

## FIRST 集

P:	int, void, ε, d, if, while, return, {
Y:	int, void, ε
D:	int, void
T:	int, void
X:	int, void, d, ε
A:	int, void, d
S:	d, if, while, return, {
S:	d, if, while, return, {
B:	d, i, (
E:	d, i, (
R:	ε, d, i, (
R:	d, i, (

首先  $FOLLOW(P) = \{\#\}$  ①

根据  $D \rightarrow TD(Y)/\{Y S\}$ ,  $S \rightarrow S ; S$ , 得  $FOLLOW(S) = \{ \#, \}, \{ ; \}$  ②

$\therefore Y \rightarrow Y D$ ;  $\therefore FOLLOW(D) = \{ ; \}$  ③

$\therefore Y \rightarrow \epsilon | Y D$ ;  $\therefore FOLLOW(Y) = FIRST(D)$

$\therefore P \rightarrow Y S$   $\therefore FOLLOW(Y) = FIRST(D) \cup FIRST(S) = \{ \text{int, void, d, if, while, return, } \}$  ④

$\therefore X \rightarrow X A$ ;  $\therefore FOLLOW(A) = \{ ; \}$  ⑤, 同理  $FOLLOW(R) = \{ , \}$

$\therefore R \rightarrow \epsilon | R R$ ,  $\therefore FOLLOW(R) \supseteq FOLLOW(R)$

而  $FOLLOW(R) = \{ , \}$  ⑥  $\therefore FOLLOW(R) = \{ , \}$  ⑦

$\therefore A \rightarrow T d$   $\therefore FOLLOW(T) = \{ d \}$  ⑧

$\therefore D \rightarrow T d (Y)$   $\therefore FOLLOW(X) = \{ , \}$  ⑨

$\therefore E \rightarrow E + E | E * E | (E)$   $\therefore FOLLOW(E) = \{ +, *, , \}$

$\therefore R \rightarrow E$   $\therefore FOLLOW(E) \supseteq FOLLOW(R) = \{ , \}$

$\therefore B \rightarrow E \mid E \quad \therefore \text{FOLLOW}(E) \supseteq \{ +, *, ), , , r \}$

$\therefore S \rightarrow \text{if}(B) S \quad \therefore \text{FOLLOW}(B) = \{ ) \}$  (10)

$\therefore S \rightarrow S \quad \therefore \text{FOLLOW}(S) \supseteq \text{FOLLOW}(S)$

$\therefore S \rightarrow \text{if}(B) S \text{ else } S \quad \therefore \text{FOLLOW}(S) = \{ \}, ;, \text{else} \}$  (11)

$\therefore S \rightarrow d = E \quad \therefore \text{FOLLOW}(E) \supseteq \text{FOLLOW}(S)$

$\therefore \text{FOLLOW}(E) = \{ +, *, ), , , r, \}, ;, \text{else} \}$  (12)

综上, FOLLOW集如下:

FOLLOW 集	
P	#
$\check{D}$	int, void, d, if, while, return, {
D	;
T	d
$\check{A}$	)
A	;
$\check{S}$	;, }, #
S	;, else, }
B	)
E	+, *, ), , , r, }, ;, else
$\check{R}$	)
R	), ,

不满足的原因:

① 对  $\check{D} \rightarrow \epsilon \mid \check{D} D$ ;  $\therefore \text{FIRST}(\check{D}) \cap \text{FOLLOW}(\check{D}) \neq \emptyset$   
 $\therefore$  不满足 LL(1)

② 对  $D \rightarrow T d \mid T d [ T d ]$   $\therefore \text{FIRST}(T d) \cap \text{FIRST}(T d [ T d ] ) \neq \emptyset$   
 $\therefore$  不满足 LL(1)

③ 对  $\check{A} \rightarrow \epsilon \mid \check{A} A$ , 属于左递归  $\therefore$  不满足 LL(1)

④ 对  $A \rightarrow Td \mid Td()$ , 同②, 不满足 LL(1)

⑤  $\check{S} \rightarrow S \mid \check{S}$ ;  $S$  仍是左递归

⑥  $S \rightarrow d = E \mid d(\check{R})$ , 同②, 不满足 LL(1)

⑦  $B \rightarrow B \wedge B \mid B \vee B$ , 同②, 不满足 LL(1)

⑧  $F \rightarrow d = E \mid d \mid d(\check{R})$ , 同②, 不满足 LL(1)

⑨  $\check{R} \rightarrow \epsilon \mid \check{R} R$  仍是左递归  $\therefore$  不满足 LL(1)

⑩  $R \rightarrow d[] \mid d()$ , 同②, 不满足 LL(1)