

DYNAMIC PROGRAMMING

Playing with Numbers:

Ram and Sita are playing with numbers by giving puzzles to each other. Now it was Ram's turn, so he gave Sita a positive integer 'n' and two numbers 1 and 3. He asked her to find the possible ways by which the number n can be represented using 1 and 3. Write an efficient algorithm to find the possible ways.

Example 1:

Input: 6

Output: 6

Explanation: There are 6 ways to represent the number with 1 and 3.

1+1+1+1+1+1

3+3

1+1+1+3

1+1+3+1

1+3+1+1

3+1+1+1

Input Format

First Line contains the number n

Output Format

Print: The number of possible ways 'n' can be represented using 1 and 3

Sample Input

6

Sample Output

6

Answer: (penalty regime: 0 %)

```
1 | #include <stdio.h>
2 |
3 |
4. long long countWays(int n) {
5     long long dp[n + 1];
6     dp[0] = 1;
7     for (int i = 1; i <= n; i++) {
8         dp[i] = 0;
9         if (i >= 1) dp[i] += dp[i - 1];
10        if (i >= 3) dp[i] += dp[i - 3];
11    }
12    return dp[n];
13 }
14
15 int main() {
16     int n;
17     scanf("%d", &n);
18     printf("%llu\n", countWays(n));
19     return 0;
20 }
```

	Input	Expected	Got	
✓	6	6	6	✓
✓	25	8641	8641	✓
✓	100	24382819596721629	24382819596721629	✓

Passed all tests! ✓

Correct

Marks for this submission: 10.00/10.00.

Playing with Chessboard:

Ram is given with an $n \times n$ chessboard with each cell with a monetary value. Ram stands at the (0,0), that the position of the top left white rook. He is been given a task to reach the bottom right black rook position ($n-1, n-1$) constrained that he needs to reach the position by traveling the maximum monetary path under the condition that he can only travel one step right or one step down the board. Help ram to achieve it by providing an efficient DP algorithm.

Example:**Input**

```
3  
1 2 4  
2 3 4  
8 7 1
```

Output:

```
19
```

Explanation:

Totally there will be 6 paths among that the optimal is

Optimal path value: $1+2+8+7+1=19$

Input Format

First Line contains the integer n

The next n lines contain the $n \times n$ chessboard values

Output Format

Print Maximum monetary value of the path

Answer: (penalty regime: 0 %)

```
1 #include <stdio.h>  
2  
3 int main() {  
4     int n;  
5     scanf("%d", &n);  
6     int board[n][n];  
7     int dp[n][n];  
8     for (int i = 0; i < n; i++) {  
9         for (int j = 0; j < n; j++) {  
10            scanf("%d", &board[i][j]);  
11        }  
12    }  
13  
14    dp[0][0] = board[0][0];  
15    for (int i = 1; i < n; i++) {  
16        dp[0][i] = dp[0][i - 1] + board[0][i];  
17    }  
18    for (int i = 1; i < n; i++) {  
19        dp[i][0] = dp[i - 1][0] + board[i][0];  
20    }  
21  
22    for (int i = 1; i < n; i++) {  
23        for (int j = 1; j < n; j++) {  
24            int fromTop = dp[i - 1][j];  
25            int fromLeft = dp[i][j - 1];  
26            dp[i][j] = board[i][j] + (fromTop > fromLeft ? fromTop : fromLeft);  
27        }  
28    }  
29  
30    printf("%d\n", dp[n - 1][n - 1]);  
31    return 0;  
32}  
33  
34
```

	Input	Expected	Got	
✓	3 1 2 4 2 3 4 8 7 1	19	19	✓
✓	3 1 3 1 1 5 1	12	12	✓

✓	3 1 3 1 1 5 1 4 2 1	12	12	✓
✓	4 1 1 3 4 1 5 7 8 2 3 4 6 1 6 9 0	28	28	✓

Passed all tests! ✓

Correct

Marks for this submission: 10.00/10.00.

Given two strings find the length of the common longest subsequence(need not be contiguous) between the two.

Example:

s1: ggtabe

s2: tgatasb

s1	a	g	g	t	a	b
s2	g	x	t	x	a	y

The length is 4

Solving it using Dynamic Programming

For example:

Input	Result
aab	2
azb	

Answer: (penalty regime: 0 %)

```
1 #include <stdio.h>
2 #include <string.h>
3
4 int LCS(char s1[], char s2[]) {
5     int n = strlen(s1);
6     int m = strlen(s2);
7     int dp[n+1][m+1];
8
9     for (int i = 0; i <= n; i++) {
10        for (int j = 0; j <= m; j++) {
11            if (i == 0 || j == 0) {
12                dp[i][j] = 0;
13            } else if (s1[i-1] == s2[j-1]) {
14                dp[i][j] = dp[i-1][j-1] + 1;
15            } else {
16                dp[i][j] = (dp[i-1][j] > dp[i][j-1]) ? dp[i-1][j] : dp[i][j-1];
17            }
18        }
19    }
20
21    return dp[n][m];
22 }
23
24 int main() {
25     char s1[100], s2[100];
26     scanf("%s %s", s1, s2);
27     printf("%d\n", LCS(s1, s2));
28     return 0;
29 }
```

	Input	Expected	Got	
✓	aab azb	2	2	✓
✓	ABCD ABCD	4	4	✓

Passed all tests! ✓

Correct

Marks for this submission: 1.00/1.00.

Problem statement:

Find the length of the Longest Non-decreasing Subsequence in a given Sequence.

Eg:

Input:9

Sequence:[-1,3,4,5,2,2,2,2,3]

the subsequence is [-1,2,2,2,2,3]

Output:6

Answer: (penalty regime: 0 %)

```
1 #include <stdio.h>
2 #include <stdlib.h>
3
4 int find(int arr[], int n) {
5     int dp[n];
6     for (int i = 0; i < n; i++) {
7         dp[i] = 1;
8     }
9
10    int maxlen = 1;
11    for (int i = 1; i < n; i++) {
12        for (int j = 0; j < i; j++) {
13            if (arr[i] >= arr[j] && dp[i] < dp[j] + 1) {
14                dp[i] = dp[j] + 1;
15            }
16        }
17        if (dp[i] > maxlen) {
18            maxlen = dp[i];
19        }
20    }
21    return maxlen;
22 }
23
24 int main() {
25     int n;
26     scanf("%d", &n);
27     int arr[n];
28     for (int i = 0; i < n; i++) {
29         scanf("%d", &arr[i]);
30     }
31     int res = find(arr, n);
32     printf("%d\n", res);
33     return 0;
34 }
```

	Input	Expected	Got	
✓	9 -1 3 4 5 2 2 2 2 3	6	6	✓
✓	7 1 2 2 4 5 7 6	6	6	✓

Passed all tests! ✓