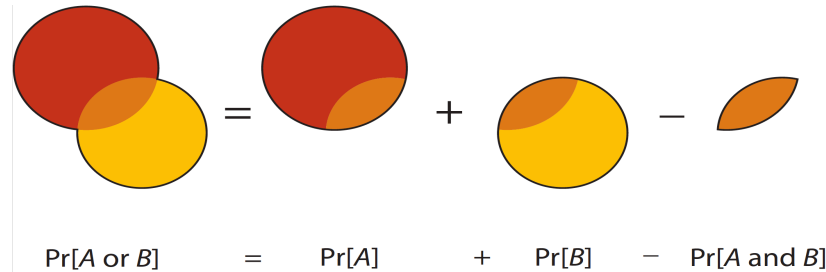


## Two other probability fundamentals are:

- Addition:  $P[A \text{ or } B] = P[A] + P[B] - P[A \text{ AND } B]$

$$P[A \cup B] = P[A] + P[B] - P[A \cap B]$$



- Multiplication:

$$P[A \text{ AND } B] = P[A | B] * P[B] = P[B | A] * P[A] \rightarrow P[A]P[B]$$

$$P[A \cap B] = P[A | B]P[B] = P[B | A]P[A] \xrightarrow{\text{If Independent}} P[A]P[B]$$

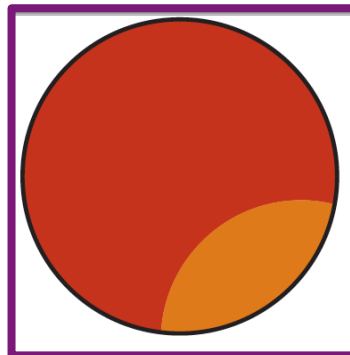
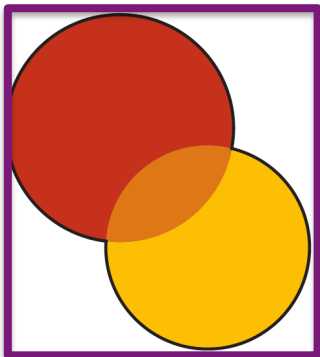
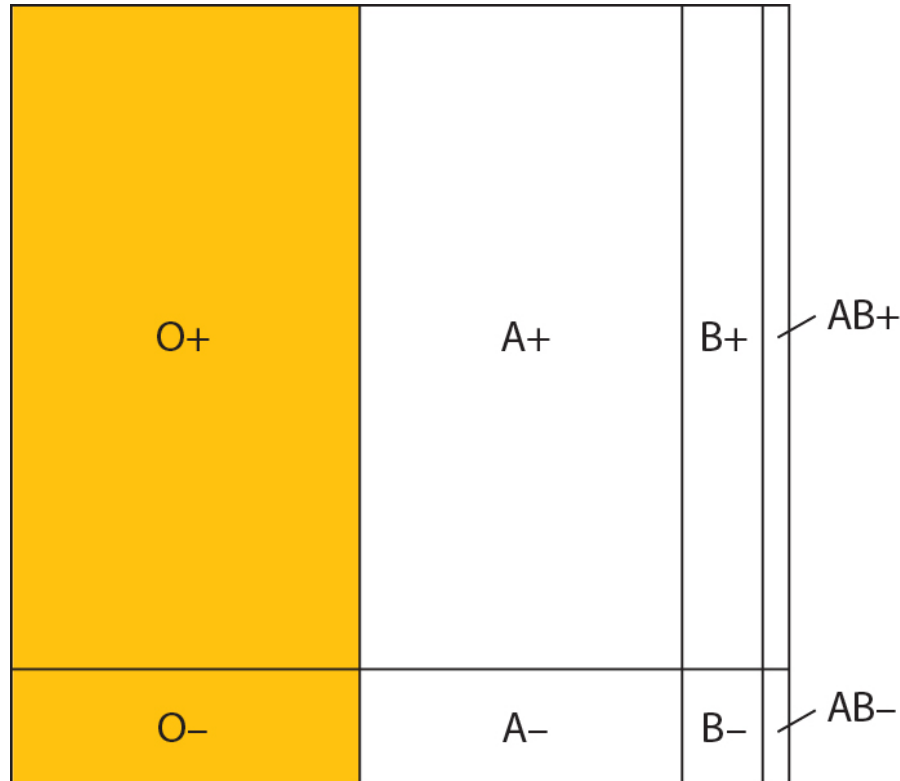


Table 5.5-1: Additional rule (mutually exclusive)

<b>Blood Type</b>	<b>Probability</b>
<b>O+</b>	<b>0.374</b>
<b>O-</b>	<b>0.066</b>
<b>A+</b>	<b>0.357</b>
<b>A-</b>	<b>0.063</b>
<b>B+</b>	<b>0.085</b>
<b>B-</b>	<b>0.015</b>
<b>AB+</b>	<b>0.034</b>
<b>AB-</b>	<b>0.006</b>

# Manipulating Probabilities

Sometimes easier to visualize using Venn:



Blood Type	Probability
O+	0.374
O-	0.066
A+	0.357
A-	0.063
B+	0.085
B-	0.015
AB+	0.034
AB-	0.006

$$\Pr[\text{O- or O+}] =$$

## 2. Multiplication

- Independence

*Two events are independent if the occurrence of one gives no information about whether or not the second will occur*

- Dependence

*The probability or outcome of one event changes because of the outcome of a second event*