

Module 4F

Supervised Machine Learning

Different flavors of REGRESSION and General Linear Models

Blocking

Results in an additional variable, a block, that must be included in analysis
Can no longer use simple one-factor ANOVA

Randomized block design

Paired design for > 2 treatments

Example:

Every treatment is replicated **once** within each block

Minimize “noise”

Accounting for any variation caused by blocking **can improve our treatment effect detection** (i.e., increase the power of our test)

Treatment effects are assessed by different treatments within each block so there is no interaction term

Goals of experiments:

determine how explanatory variable (treatment) affects response variable

- Eliminate Bias
- Reduce Sampling Error
 - Blocking:



C = Control
T = Treated

Variance among hospitals
will not contribute to SE.

Only variance within hospitals
will contribute to "noise"

Main Principle of Blocking

$$\text{Response} = \text{Constant} + \text{Treatment} + \text{Block}$$

$$H_0: \text{Response} = \text{Constant} + \text{Block}$$

$$H_A: \text{Response} = \text{Constant} + \text{Block} + \text{Treatment}$$

- Determine significance via ANOVA table which includes a row for the **block**
- Calculates a F value for block - examines how much better fit is with the block versus without the block

Example of Blocking:

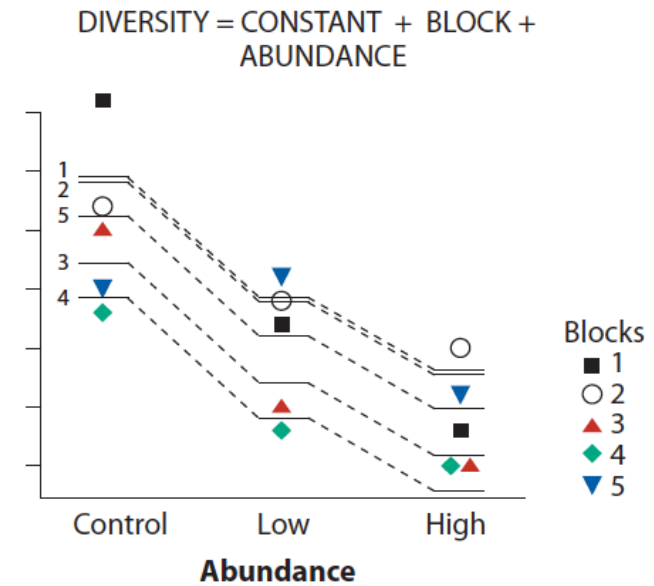
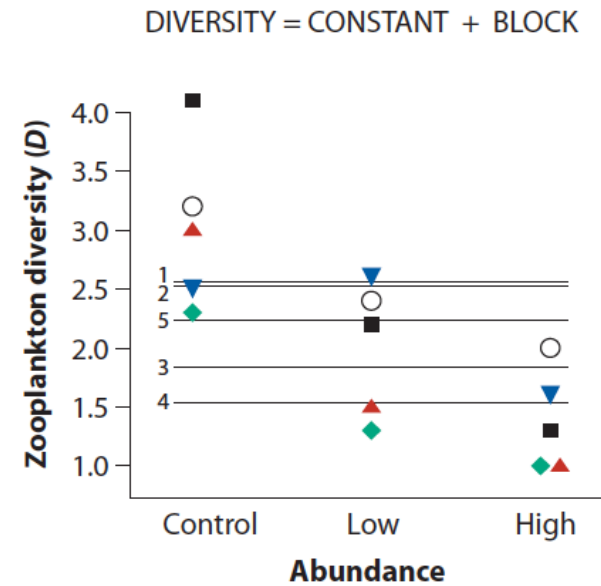
Response = Constant + Treatment + Block

H_0 : Response = Constant + Block

H_A : Response = Constant + Block + Treatment

$$F = \frac{H_A}{H_0} = \frac{\text{Constant} + \text{Block} + \text{Treatment}}{\text{Constant} + \text{Block}}$$

$$= \frac{\text{residual} + \text{location} + \text{fish Abundance}}{\text{residual} + \text{location}}$$



Source of variation	Sum of Squares	df	Mean Square	F	P
BLOCK	2.340	4	0.5850		
Treatment	6.8573	2	3.4287	16.37	0.001
Residual	1.6760	8	0.2095		
Total	10.8733	14			

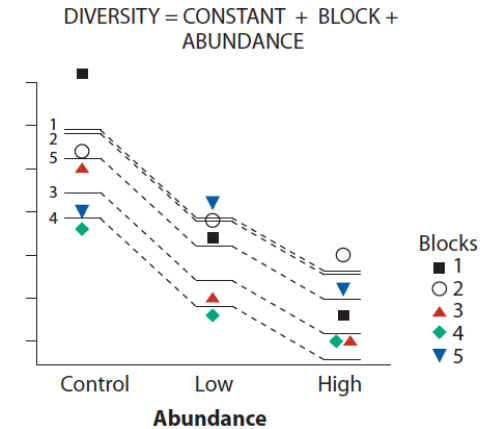
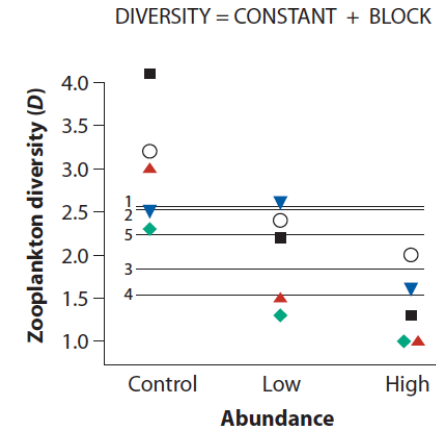
Example of Blocking:

Response Full = Constant + Treatment + Block

Treatment:

H_0 : Response = Constant + Block

H_A : Response = Constant + Block + Treatment



$$F = \frac{H_A}{H_0} = \frac{\text{Constant} + \text{Block} + \text{Treatment}}{\text{Constant} + \text{Block}}$$

$$= \frac{\text{residual} + \text{location} + \text{fish Abundance}}{\text{residual} + \text{location}}$$

$$= \frac{MS_{\text{treatment}}}{MS_{\text{block}}} = \frac{3.43}{0.59} = \mathbf{16.37}$$

$F_{0.05(1),2,14} = 3.74$ so we reject the H_0

Source of variation	Sum of Squares	df	Mean Square	F	P
BLOCK	2.340	4	0.5850		
Treatment	6.8573	2	3.4287	16.37	0.001
Residual	1.6760	8	0.2095		
Total	10.8733	14			

Example of Blocking:

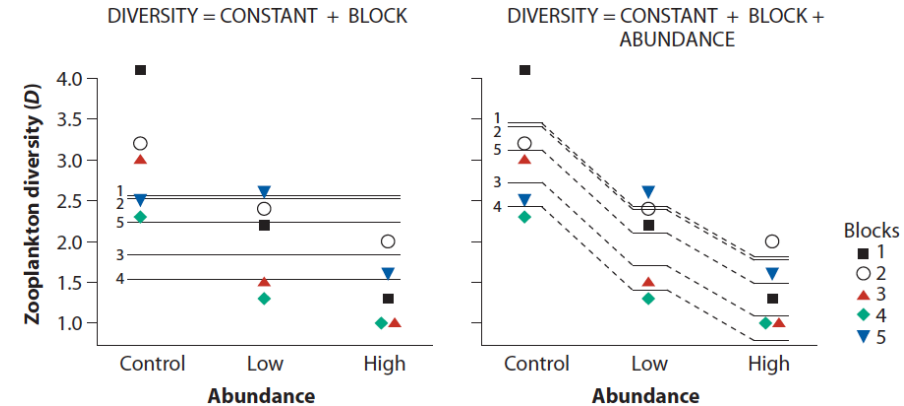
Treatment:

H_0 : Response = Constant + Block

H_A : Response = Constant + Block + Treatment

$$F = \frac{H_A}{H_0} = \frac{\text{Constant} + \text{Block} + \text{Treatment}}{\text{Constant} + \text{Block}}$$

$$= \frac{\text{residual} + \text{location} + \text{fish Abundance}}{\text{residual} + \text{location}} = \frac{MS_{\text{treatment}}}{MS_{\text{block}}} = \frac{3.43}{0.59} = \mathbf{16.37}$$



$F_{0.05(1),2,14} = \mathbf{3.74}$ so we reject the H_0

Block:

$$F_{\text{Block}} = \frac{H_A}{H_0} = \frac{\text{Residual} + \text{treatment} + \text{Block}}{\text{Residual} + \text{treatment}} = \frac{MS_{\text{block}}}{MS_{\text{residual}}} = \frac{0.5850}{0.2095} = 2.79$$

$F_{0.05(1),4,8} = \mathbf{3.84}$ so we fail to reject the H_0

Source of variation	Sum of Squares	df	Mean Square	F	P
BLOCK	2.340	4	0.5850		
Treatment	6.8573	2	3.4287	16.37	0.001
Residual	1.6760	8	0.2095		
Total	10.8733	14			