Simple 3-state Markov model in R

The DARTH workgroup

Developed by the Decision Analysis in R for Technologies in Health (DARTH) workgroup:

Fernando Alarid-Escudero, PhD (1)

Eva A. Enns, MS, PhD (2)

M.G. Myriam Hunink, MD, PhD (3,4)

Hawre J. Jalal, MD, PhD (5)

Eline M. Krijkamp, MSc (3)

Petros Pechlivanoglou, PhD (6,7)

Alan Yang, MSc (7)

In collaboration of:

- 1. Division of Public Administration, Center for Research and Teaching in Economics (CIDE), Aguas-calientes, Mexico
- 2. University of Minnesota School of Public Health, Minneapolis, MN, USA
- 3. Erasmus MC, Rotterdam, The Netherlands
- 4. Harvard T.H. Chan School of Public Health, Boston, USA
- 5. University of Pittsburgh Graduate School of Public Health, Pittsburgh, PA, USA
- 6. University of Toronto, Toronto ON, Canada
- 7. The Hospital for Sick Children, Toronto ON, Canada

Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001. 07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

Copyright 2017, THE HOSPITAL FOR SICK CHILDREN AND THE COLLABORATING INSTITUTIONS. All rights reserved in Canada, the United States and worldwide. Copyright, trademarks, trade names and any and all associated intellectual property are exclusively owned by THE HOSPITAL FOR Sick CHILDREN and the collaborating institutions. These materials may be used, reproduced, modified, distributed and adapted with proper attribution.

Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("diagram")
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/darthtools")
```

02 Load functions

```
# all functions are in the darthtools package
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("Standard of Care", "Treatment")</pre>
# Markov model parameters
v_names_states <- c("Healthy", "Sick", "Dead") # state names</pre>
n_t <- 60
                                                # number of cycles
v_{init} \leftarrow c("Healthy" = 1,
           "Sick" = 0,
            "Dead" = 0) # initial cohort distribution (everyone allocated to the "healthy" state)
# Transition probabilities
DH q
      <- 0.02
                                    # probability of dying when healthy
        <- 0.05
                                    # probability of becoming sick when healthy, under standard of car
p_HS
p_HS_trt <- 0.03
                                    # probability of becoming sick when healthy, under treatment
p_SD
                                    # probability of dying when sick
       <- 0.1
# Costs and utilities
c H <- 400
                                    # cost of one cycle in healthy state
c_S <- 1000
                                    # cost of one cycle in sick state
                                   # cost of one cycle in dead state
c_D <- 0
c_trt <- 800
                                   # cost of treatment (per cycle)
u_H <- 1
                                   # utility when healthy
u_S <- 0.5
                                    # utility when sick
                                    # utility when dead
u_D <- 0
d_e <- d_c <- 0.03
                                    # discount rate per cycle equal discount of costs and QALYs by 3%
```

```
n_str <- length(v_names_str)  # Number of strategies
n_states <- length(v_names_states)  # number of states

#discount weights for costs and effects
v_dwc <- 1 / (1 + d_c) ^ (0:n_t)
v_dwe <- 1 / (1 + d_e) ^ (0:n_t)</pre>
```

Draw the state-transition cohort model

04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability matrix

Fill in the transition probability matrix:

```
# from Healthy
m_P["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS)
m_P["Healthy", "Sick"] <- (1 - p_HD) * p_HS
m_P["Healthy", "Dead"] <- p_HD

# from Sick
m_P["Sick", "Sick"] <- 1 - p_SD
m_P["Sick", "Dead"] <- p_SD

# from Dead
m_P["Dead", "Dead"] <- 1

## Check if transition probability matrices are valid
# Check that transition probabilities are in [0, 1]
check_transition_probability(m_P, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(m_P, n_states = n_states, verbose = TRUE)</pre>
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

06.2 Overall Survival (OS)

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2])  # alternative way of calculating the OS probability

plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",</pre>
```

06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os) # summing probability of OS over time (i.e. life expectancy)
```

06.3 Disease prevalence

07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
v_tc <- m_M %*% c(c_H, c_S, c_D)
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
v_tu <- m_M %*% c(u_H, u_S, u_D)</pre>
```

07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights (v_dw)
v_tc_d <- t(v_tc) %*% v_dwc
# Discount QALYS by multiplying the QALYs vector with discount weights (v_dw)
v_te_d <- t(v_tu) %*% v_dwe</pre>
```

07.3 Store Results