Simple 3-state Markov model in R

The DARTH workgroup

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- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001. 07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. 2020 Feb;40(2):242-248. https://journals.sagepub.com/doi/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls()) # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load( "dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "ggraph", "reshape2"
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/darthtools")
```

02 Load functions

d_e

```
# all functions are in the darthtools package
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("Standard of Care", "Treatment")</pre>
# Markov model parameters
v_names_states <- c("Healthy", "Sick", "Dead") # state names</pre>
n_t <- 60
                              # number of cycles
v_{init} \leftarrow c("Healthy" = 1,
             "Sick" = 0,
             "Dead" = 0) # initial cohort distribution (everyone allocated to the
                              # "healthy" state)
# Transition probabilities
p_HD <- 0.02 # probability of dying when healthy
         <- 0.05
                            # probability of becoming sick when healthy, conditional on surviving, unde
p HS
                            # probability of becoming sick when healthy, under treatment
p_HS_trt <- 0.03
p_SD
         <- 0.1
                              # probability of dying when sick
                        # cost of one cycle in healthy state
# cost of one cycle in sick state
# cost of one cycle in dead state
# cost of treatment (per cycle)
# utility when health.
# Costs and utilities
         <- 400
c_H
c_S
          <- 1000
c_D
         <- 0
c_trt <- 800
         <- 1
                            # utility when healthy
u_H
        <- 0.5 # utility when sick
<- 0 # utility when dead
u_S
u_D
```

<- d_c <- 0.03 # discount rate per cycle equal discount of costs and QALYs by 3%, separate

```
n_str <- length(v_names_str) # Number of strategies
n_states <- length(v_names_states) # number of states

# Discount weights for costs and effects
v_dwc <- 1 / (1 + d_c) ^ (0:n_t)
v_dwe <- 1 / (1 + d_e) ^ (0:n_t)</pre>
```

03.1 Draw the state-transition cohort model

04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability matrix

Fill in the transition probability matrix:

```
# For Standard of Care
# from Healthy
m_P_SoC["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS)
m_P_SoC["Healthy", "Sick"] <- (1 - p_HD) * p_HS
m_P_SoC["Healthy", "Dead"] <- p_HD

# from Sick
m_P_SoC["Sick", "Sick"] <- 1 - p_SD
m_P_SoC["Sick", "Dead"] <- p_SD

# from Dead
m_P_SoC["Dead", "Dead"] <- 1

# Under treatment
m_P_trt <- m_P_SoC # Assign the matrix for standard of care to the transition probability matrix for t
# replace values that are different under treatment
m_P_trt["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS_trt)
m_P_trt["Healthy", "Sick"] <- (1 - p_HD) * p_HS_trt</pre>
```

04.3 Check if transition probability structure and probabilities are valid

```
# Check that transition probabilities are in [0, 1]
check_transition_probability(m_P_SoC, verbose = TRUE)
check_transition_probability(m_P_trt, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(m_P_SoC, n_states = n_states, n_cycles = n_t, verbose = TRUE)
check_sum_of_transition_array(m_P_trt, n_states = n_states, n_cycles = n_t, verbose = TRUE)
```

05 Run Markov model

```
for (t in 1:n_t){  # loop through the number of cycles
  m_M_SoC[t + 1, ] <- m_M_SoC[t, ] %*% m_P_SoC  # estimate the state vector for the next cycle (t + 1)
  m_M_trt[t + 1, ] <- m_M_trt[t, ] %*% m_P_trt  # for treatment
}</pre>
```

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

Standard of Care:

```
lty = 1:3, bty = "n")  # add a legend to the graph

abline(v = which.max(m_M_SoC[, "Sick"]), col = "gray")  # plot a vertical line that helps identifyi
```

Treatment:

06.2 Overall Survival (OS)

Standard of Care:

```
v_os_SoC <- 1 - m_M_SoC[, "Dead"]  # calculate the overall survival (OS) probability
v_os_SoC <- rowSums(m_M_SoC[, 1:2])  # alternative way of calculating the OS probability

plot(v_os_SoC, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival - Standard of Care")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

Treatment:

```
v_os_trt <- 1 - m_M_trt[, "Dead"]  # calculate the overall survival (OS) probability
v_os_trt <- rowSums(m_M_trt[, 1:2])  # alternative way of calculating the OS probability

plot(v_os_trt, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival - Treatment")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

06.2.1 Life Expectancy (LE)

```
v_le_SoC <- sum(v_os_SoC) # summing probability of OS over time (i.e. life expectancy)
v_le_trt <- sum(v_os_trt) # summing probability of OS over time (i.e. life expectancy), treatment</pre>
```

06.3 Disease prevalence

Standard of Care:

```
v_prev_SoC <- m_M_SoC[, "Sick"]/v_os_SoC
plot(v_prev_SoC,
    ylim = c(0, 1),
    ylab = "Prevalence",
    xlab = "Cycle",
    main = "Disease prevalence - Standard of care")</pre>
```

Treatment:

```
v_prev_trt <- m_M_trt[, "Sick"]/v_os_trt
plot(v_prev_trt,
    ylim = c(0, 1),
    ylab = "Prevalence",
    xlab = "Cycle",
    main = "Disease prevalence - Treatment")</pre>
```

07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights
tc_d_SoC <- t(v_tc_SoC) %*% v_dwc # Standard of Care
tc_d_trt <- t(v_tc_trt) %*% v_dwc # Treatment
# Discount QALYS by multiplying the QALYs vector with discount weights
tu_d_SoC <- t(v_tu_SoC) %*% v_dwe # Standard of Care
tu_d_trt <- t(v_tu_trt) %*% v_dwe # Treatment</pre>
```

07.3 Compute ICERs of the Markov model

07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "QALYs", xlim = c(10, 12))
# note: you need to adjust the xlim values to values that are covering the range of effect values in yo
```