# Simple 3-state Markov model in R

#### with age dependency

#### The DARTH workgroup

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- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001. 07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. 2020 Online first. https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

## 01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("diagram")
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/darthtools")
```

#### 02 Load functions

```
# No functions needed
```

### 03 Input model parameters

```
# Strategy names
v_names_str <- c("Base Case")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead") # state names</pre>
n_states <- length(v_n)
                                         # number of states
n t <- 60
                                         # number of cycles
p_HD <- seq(0.003, 0.01, length.out = n_t) # probabilities of dying when healthy (age-dependent) - thi
p_HS <- 0.05
                                             # probability of becoming sick when healthy, conditioned on
                                             # probability of dying when sick
p_SD <- 0.1
# Costs and utilities
c H <- 400
                                         # cost of one cycle in healthy state
c_S <- 1000
                                         # cost of one cycle in sick state
c_D <- 0
                                         # cost of one cycle in dead state
u_H <- 0.8
                                         # utility when healthy
u_S <- 0.5
                                         # utility when sick
u D <- 0
                                         # utility when dead
d_e <- d_c <- 0.03
                                         # equal discount of costs and QALYs by 3%
\# calculate discount weights for costs for each cycle based on discount rate d\_c
v_dwc \leftarrow 1 / (1 + d_e) ^ (0:n_t)
\# calculate discount weights for effectiveness for each cycle based on discount rate d_e
v_{dwe} \leftarrow 1 / (1 + d_c) ^ (0:n_t)
```

### 04 Define and initialize matrices and vectors

#### 04.1 Cohort trace

#### 04.2 Transition probability array

```
# create the transition probability array
a_P <- array(0,  # Create 3-D array
dim = c(n_states, n_states, n_t),
dimnames = list(v_n, v_n, 0:(n_t - 1))) # name the dimensions of the array</pre>
```

Fill in the transition probability array:

```
# from Healthy
a_P["Healthy", "Healthy", ] <- (1 - p_HD) * (1 - p_HS)
a_P["Healthy", "Sick", ] <- (1-p_HD) * p_HS
a_P["Healthy", "Dead", ] <- p_HD

# from Sick
a_P["Sick", "Sick", ] <- 1 - p_SD
a_P["Sick", "Dead", ] <- p_SD

# from Dead
a_P["Dead", "Dead", ] <- 1</pre>
```

#### 04.3 Check if transition array and probabilities are valid

```
# Check that transition probabilities are in [0, 1]
check_transition_probability(a_P, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(a_P, n_states = n_states, n_t = n_t, verbose = TRUE)
```

#### 05 Run Markov model

## 06 Compute and Plot Epidemiological Outcomes

#### 06.1 Cohort trace

#### 06.2 Overall Survival (OS)

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2]) # alternative way of calculating the OS probability

# create a simple plot showing the OS
plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")

# add grid
grid(nx = n_t, ny = 10,
    col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

#### 06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os) # summing probablity of OS over time (i.e. life expectancy)
```

#### 06.3 Disease prevalence

```
ylab = "Prevalence",
xlab = "Cycle",
main = "Disease prevalence")
```

## 07 Compute Cost-Effectiveness Outcomes

### 07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
v_tc <- m_M %*% c(c_H, c_S, c_D)
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
v_tu <- m_M %*% c(u_H, u_S, u_D)</pre>
```

#### 07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights (v_dw)
v_tc_d <- t(v_tc) %*% v_dwc
# Discount QALYS by multiplying the QALYs vector with discount weights (v_dw)
v_te_d <- t(v_tu) %*% v_dwe</pre>
```

#### 07.3 Store Results