Simple 3-state Markov model in R

The DARTH workgroup

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Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001. 07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. 2020 Feb;40(2):242-248. https://journals.sagepub.com/doi/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load( "dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "ggraph", "reshape2"
# install_github("DARTH-git/dampack", force = TRUE) Uncomment if there is a newer version
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/dampack", "DARTH-git/darthtools")
```

02 Load functions

```
# all functions are in the darthtools package
```

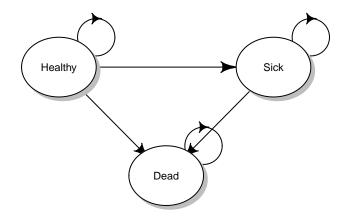
03 Input model parameters

```
# Strategy names
v_names_str <- c("Standard of Care", "Treatment")</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead") # state names</pre>
n_t <- 60
                                      # number of cycles
v_{init} \leftarrow c("Healthy" = 1,
            "Sick" = 0,
            "Dead" = 0)
                                     # initial cohort distribution (everyone allocated to the
                                      # "healthy" state)
\# Transition probabilities
        <- 0.02
                                      # probability of dying when healthy
p_HD
         <- 0.05
                                      # probability of becoming sick when healthy, under standard of ca
p_{HS}
p_HS_trt <- 0.03
                                      # probability of becoming sick when healthy, under treatment
p_SD
         <- 0.1
                                      # probability of dying when sick
# Costs and utilities
         <- 400
c_H
                                      # cost of one cycle in healthy state
         <- 1000
c_S
                                     # cost of one cycle in sick state
        <- 0
                                     # cost of one cycle in dead state
c_D
c_trt
         <- 800
                                      # cost of treatment (per cycle)
         <- 0.8
                                      # utility when healthy
u_H
                                      # utility when sick
        <- 0.5
u_S
u_D
         <- 0
                                      # utility when dead
```

```
d_e <- d_c <- 0.03  # discount rate per cycle equal discount of costs and QALYs by 3%
n_str <- length(v_names_str)  # Number of strategies
n_states <- length(v_n)  # number of states

# Discount weights for costs and effects
v_dwc <- 1 / (1 + d_c) ^ (0:n_t)
v_dwe <- 1 / (1 + d_e) ^ (0:n_t)</pre>
```

Draw the state-transition cohort model



04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability matrix

```
# create the transition probability matrices
m_P <- m_P_trt <- matrix(0,</pre>
                   nrow = n_states, ncol = n_states,
                   dimnames = list(v_n, v_n)) # name the columns and rows of the transition
# print the probability matrices
m_P # for standard of care
          Healthy Sick Dead
                0
## Healthy
                    0
## Sick
                     0
                0
                         0
                0
## Dead
m_P_trt # treatment
          Healthy Sick Dead
## Healthy
             0 0
## Sick
                     0
                         0
## Dead
                0
                         0
```

Fill in the transition probability matrix:

```
# For Standard of Care
# from Healthy
m_P["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS)
m_P["Healthy", "Sick"] <- (1 - p_HD) * p_HS
m_P["Healthy", "Dead"] <- p_HD

# from Sick
m_P["Sick", "Sick"] <- 1 - p_SD
m_P["Sick", "Dead"] <- p_SD

# from Dead
m_P["Dead", "Dead"] <- 1</pre>
```

```
# Under treatment
m_P_trt <- m_P # Assign the matrix for standard of care to the transition probability matrix for treat
# replace values that are different under treatment
m_P_trt["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS_trt)
m_P_trt["Healthy", "Sick"] <- (1 - p_HD) * p_HS_trt</pre>
```

04.3 Check if transition probability structure and probabilities are valid

```
# Check that transition probabilities are in [0, 1]
check_transition_probability(m_P, verbose = TRUE)
check_transition_probability(m_P_trt, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(m_P, n_states = n_states, n_cycles = n_t, verbose = TRUE)
check_sum_of_transition_array(m_P_trt, n_states = n_states, n_cycles = n_t, verbose = TRUE)
```

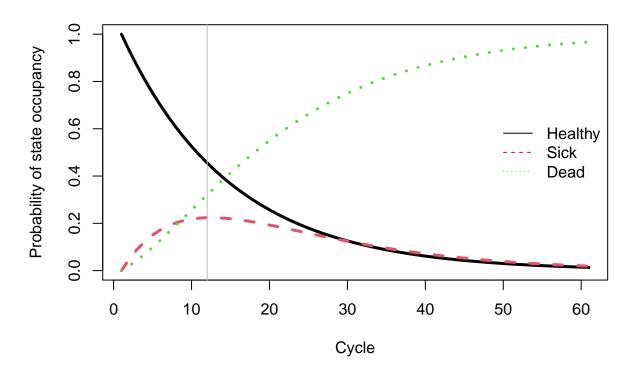
05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

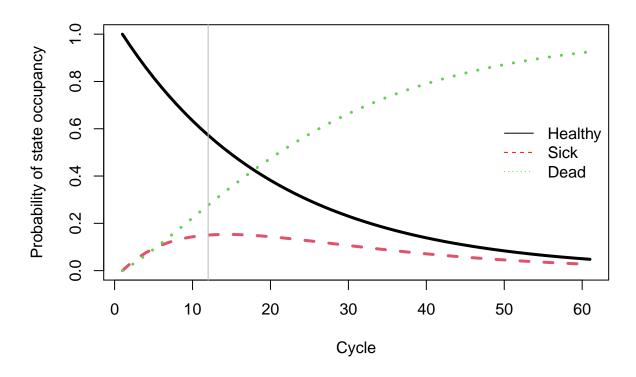
Standard of Care:

Cohort Trace – standard of care



Treatment:

Cohort Trace – treatment



06.2 Overall Survival (OS)

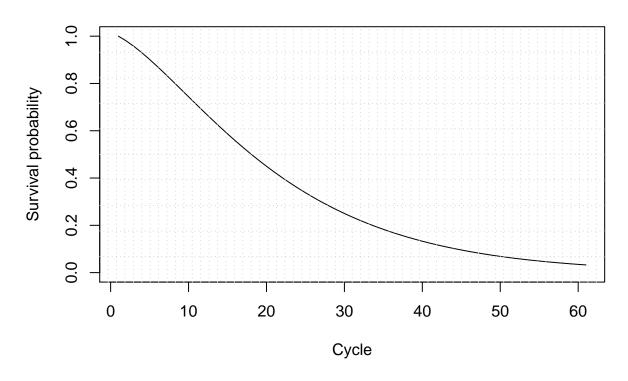
Standard of Care:

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2])  # alternative way of calculating the OS probability

plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival - Standard of Care")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

Overall Survival - Standard of Care



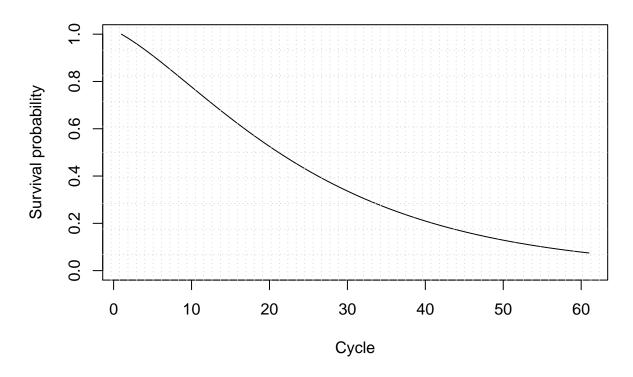
Treatment:

```
v_os_trt <- 1 - m_M_trt[, "Dead"]  # calculate the overall survival (OS) probability
v_os_trt <- rowSums(m_M_trt[, 1:2])  # alternative way of calculating the OS probability

plot(v_os_trt, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival - Treatment")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

Overall Survival - Treatment



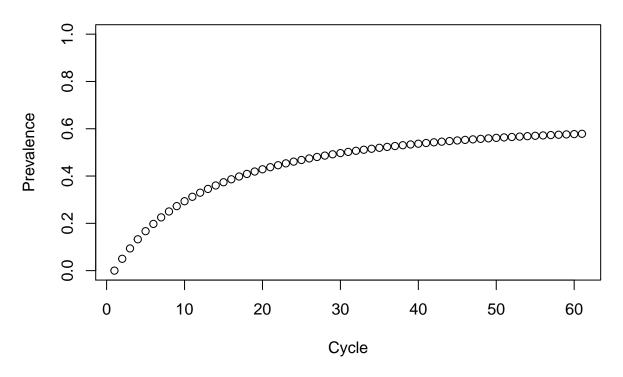
06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os)  # summing probability of OS over time (i.e. life expectancy)
v_le_trt <- sum(v_os_trt)  # summing probability of OS over time (i.e. life expectancy), treatment</pre>
```

06.3 Disease prevalence

Standard of Care:

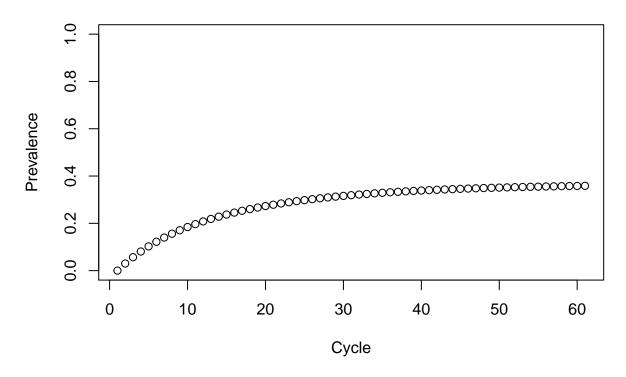
Disease prevalence - Standard of care



Treatment:

```
v_prev_trt <- m_M_trt[, "Sick"]/v_os_trt
plot(v_prev_trt,
    ylim = c(0, 1),
    ylab = "Prevalence",
    xlab = "Cycle",
    main = "Disease prevalence - Treatment")</pre>
```

Disease prevalence - Treatment



07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
                    %*% c(c_H, c_S,
v_tc
        <- m_M
                                             c_D) # Standard of Care
v_tc_trt <- m_M_trt %*% c(c_H, c_S + c_trt, c_D) # Treatment</pre>
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
        <-m_M
                    %*% c(u_H, u_S, u_D)
                                                   # Standard of Care
v_tu
v_tu_trt <- m_M_trt %*% c(u_H, u_S, u_D)</pre>
                                                   # Treatment
```

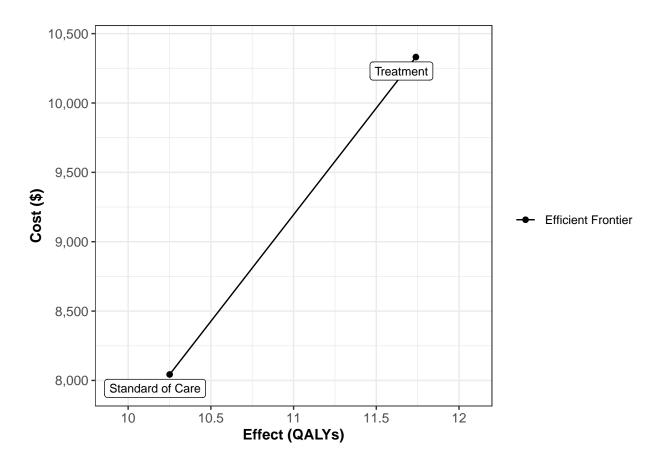
07.2 Discounted Mean Costs and QALYs

Strategy Cost Effect ## 1 Standard of Care 8043.139 10.25087 ## 2 Treatment 10331.262 11.73928

07.3 Compute ICERs of the Markov model

07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "QALYs", xlim = c(10, 12))
```



note: you need to adjust the xlim values to values that are covering the range of effect values in yo