## SA: Markov Sick-Sicker model in R

#### The DARTH workgroup

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- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

## 01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "truncnorm", "ggraph"
# load (install if required) packages from GitHub
# install_github("DARTH-git/dampack", force = TRUE) Uncomment if there is a newer version
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/dampack", "DARTH-git/darthtools")
```

#### 02 Load functions

```
# No function needed
```

## 03 Input model parameters

```
# Strategy names
v_names_str <- c("No Treatment", "Treatment")</pre>
# Markov model parameters
age <- 25
                                    # age at baseline
max_age <- 55
                                   # maximum age of follow up
n_t <- max_age - age
                                    # time horizon, number of cycles
       <- c("H", "S1", "S2", "D") # the 4 states of the model: Healthy (H), Sick (S1),
v n
                                   # Sicker (S2), Dead (D)
v_{init} \leftarrow c(1, 0, 0, 0)
                                   # initial cohort distribution
# Transition probabilities (per cycle)
       <- 0.005
                                    # probability to die when healthy
p HD
p_HS1 <- 0.15
                                    # probability to become sick when healthy, conditional on survivin
p_S1H <- 0.5
                                    # probability to become healthy when sick, conditional on survivin
p_S1S2 <- 0.105
                                    # probability to become sicker when sick, conditional on surviving
        <- 3
                                    # hazard ratio of death in sick vs healthy
hr_S1
hr_S2
       <- 10
                                    # hazard ratio of death in sicker vs healthy
{	t r}_{	t HD}
       \leftarrow - log(1 - p_HD)
                                   # rate of death in healthy
r_S1D <- hr_S1 * r_HD
                                   # rate of death in sick
r_S2D <- hr_S2 * r_HD
                                   # rate of death in sicker
                                # probability to die in sick
p_S1D \leftarrow 1 - exp(-r_S1D)
p_S2D \leftarrow 1 - exp(-r_S2D)
                                    # probability to die in sicker
# Cost and utility inputs
```

```
c_H <- 2000
                                    # cost of remaining one cycle in the healthy state
c_S1
       <- 4000
                                    # cost of remaining one cycle in the sick state
c S2
        <- 15000
                                    # cost of remaining one cycle in the sicker state
c_trt <- 12000
                                   # cost of treatment(per cycle)
       <- 0
                                    # cost of being in the death state
c D
       <- 1
uН
                                    # utility when healthy
u_S1 <- 0.75
                                    # utility when sick
u_S2
       <- 0.5
                                   # utility when sicker
       <- 0
u_D
                                   # utility when dead
u_trt <- 0.95
                                    # utility when being treated
\mathtt{d}_{-}\mathsf{e}
       <- d_c <- 0.03
                                    # discount rate per cycle equal discount of costs and QALYs by 3%
n_str <- length(v_names_str) # Number of strategies</pre>
n_states <- length(v_n)
                                    # number of states
# Discount weights for costs and effects
v_dwc \leftarrow 1 / (1 + d_c) ^ (0:n_t)
v_dwe \leftarrow 1 / (1 + d_e) ^ (0:n_t)
```

#### 04 Define and initialize matrices and vectors

#### 04.1 Cohort trace

#### 04.2 Transition probability matrix

Fill in the transition probability matrix:

```
# from Healthy
m_P_notrt["H", "H" ] <- (1 - p_HD) * (1 - p_HS1)
m_P_notrt["H", "S1" ] <- (1 - p_HD) * p_HS1</pre>
```

```
m_P_notrt["H", "D" ] <- p_HD</pre>
# from Sick
m_P_notrt["S1", "H"] <- (1 - p_S1D) * p_S1H
m_P_notrt["S1", "S1"] \leftarrow (1 - p_S1D) * (1 - (p_S1H + p_S1S2))
m_P_notrt["S1", "S2"] <- (1 - p_S1D) * p_S1S2
m_P_notrt["S1", "D" ] <- p_S1D</pre>
# from Sicker
m_P_notrt["S2", "S2"] <- 1 - p_S2D</pre>
m_P_notrt["S2", "D" ] <- p_S2D</pre>
# from Dead
m_P_notrt["D", "D" ] <- 1</pre>
# Check that transition probabilities are in [0, 1]
check_transition_probability(m_P_notrt, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(m_P_notrt, n_states = n_states, n_cycles = n_t, verbose = TRUE)
# create transition probability matrix for treatment same as no treatment
m_P_trt <- m_P_notrt</pre>
```

#### 05 Run Markov model

# 06 Compute and Plot Epidemiological Outcomes

#### 06.1 Cohort trace

#### 06.2 Overall Survival (OS)

```
# calculate the overall survival (OS) probability for no treatment
v_os_notrt <- 1 - m_M_notrt[, "D"]
# alternative way of calculating the OS probability
v_os_notrt <- rowSums(m_M_notrt[, 1:3])
# create a simple plot showing the OS
plot(0:n_t, v_os_notrt, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")
# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

#### 06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os_notrt)  # summing probablity of OS over time (i.e. life expectancy)</pre>
```

#### 06.3 Disease prevalence

#### 06.4 Proportion of sick in S1 state

# 07 Compute Cost-Effectiveness Outcomes

## 07.1 Mean Costs and QALYs for Treatment and NO Treatment

### 07.2 Discounted Mean Costs and QALYs

#### 07.3 Compute ICERs of the Markov model

#### 07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "Quality of Life", xlim = c(15.6, 16.6))
```

# 08 Deterministic Sensitivity Analysis

#### 08.1 List of input parameters

Create list 1\_params\_all with all input probabilities, cost and utilities.

```
l_params_all <- as.list(data.frame(</pre>
  p_HD = 0.005, # probability to die when healthy
  p_HS1 = 0.15, # probability to become sick when healthy
  p_S1H = 0.5, # probability to become healthy when sick
  p_S1S2 = 0.105, # probability to become sicker when sick
 hr_S1 = 3,  # hazard ratio of death in sick vs healthy
hr_S2 = 10,  # hazard ratio of death in sicker vs healthy
  c_H = 2000, # cost of remaining one cycle in the healthy state
 c_S1 = 4000, # cost of remaining one cycle in the sick state
c_S2 = 15000, # cost of remaining one cycle in the sicker state
  c_trt = 12000, # cost of treatment(per cycle)
 c_D = 0,  # cost of being in the death state
u_H = 1,  # utility when healthy
 u_S1 = 0.75, # utility when sick
 u_S2 = 0.5, # utility when sicker
  u_D = 0,
                   # utility when dead
 u_trt = 0.95, # utility when treated
 d_e = 0.03, # discount factor for effectiveness
 d_c = 0.03 # discount factor for costs
))
# store the parameter names into a vector
v_names_params <- names(l_params_all)</pre>
```

#### 08.2 Load Sick-Sicker Markov model function

```
source("Functions_markov_sick-sicker.R")
# Test function
calculate_ce_out(l_params_all)
```

#### 08.3 One-way sensitivity analysis (OWSA)

```
# your turn
```

#### 08.3.1 Plot OWSA

```
# your turn
```

## 08.3.2 Optimal strategy with OWSA

```
# your turn
```

## 08.3.3 Tornado plot

# your turn

## 08.4 Two-way sensitivity analysis (TWSA)

# your turn

#### 08.4.1 Plot TWSA

# your turn

# 09 Probabilistic Sensitivity Analysis (PSA)

# Function to generate PSA input dataset
gen\_psa <-</pre>

## 09.1 Conduct probabilistic sensitivity analysis

# your turn

## 09.2 Create PSA object for dampack

# your turn

### 09.2.1 Save PSA objects

# your turn

### 09.3 Create probabilistic analysis graphs

# your turn

Vector with willingness-to-pay (WTP) thresholds.

# your turn 09.3.1 Cost-Effectiveness Scatter plot # your turn 09.4 Conduct CEA with probabilistic output # your turn 09.4.1 Plot cost-effectiveness frontier # your turn 09.4.2 Cost-effectiveness acceptability curves (CEACs) and frontier (CEAF) # your turn 09.4.3 Expected Loss Curves (ELCs) # your turn

# your turn