Markov Sick-Sicker model in R

The DARTH workgroup

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- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "truncnorm", "ggraph"
# load (install if required) packages from GitHub
# install_github("DARTH-git/dampack", force = TRUE) Uncomment if there is a newer version
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/dampack", "DARTH-git/darthtools")
```

02 Load functions

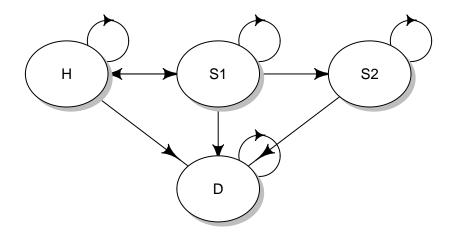
```
# all functions are in the darthtools package
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("No Treatment", "Treatment")</pre>
# Markov model parameters
       <- 25
                                    # age at baseline
age
max_age <- 55
                                   # maximum age of follow up
    <- max_age - age
                                    # time horizon, number of cycles
       <- c("H", "S1", "S2", "D") # the 4 states of the model: Healthy (H), Sick (S1),
v n
                                   # Sicker (S2), Dead (D)
v_{init} <- c(1, 0, 0, 0)
                                   # initial cohort distribution
# Transition probabilities (per cycle)
       <- 0.005
                                    # probability to die when healthy
p HD
p_HS1 <- 0.15
                                    # probability to become sick when healthy, conditional on survivin
p_S1H
        <- 0.5
                                    # probability to become healthy when sick, conditional on survivin
p_S1S2 <- 0.105
                                    # probability to become sicker when sick, conditional on surviving
        <- 3
                                    # hazard ratio of death in sick vs healthy
hr_S1
        <- 10
hr_S2
                                    # hazard ratio of death in sicker vs healthy
{	t r}_{	t HD}
       \leftarrow - \log(1 - p_HD)
                                   # rate of death in healthy
r_S1D <- hr_S1 * r_HD
                                   # rate of death in sick
r_S2D <- hr_S2 * r_HD
                                   # rate of death in sicker
                                # probability to die in sick
p_S1D \leftarrow 1 - exp(-r_S1D)
p_S2D \leftarrow 1 - exp(-r_S2D)
                                    # probability to die in sicker
# Cost and utility inputs
```

```
c_H <- 2000
                                     # cost of remaining one cycle in the healthy state
c_S1
         <- 4000
                                     # cost of remaining one cycle in the sick state
c_S2
         <- 15000
                                     # cost of remaining one cycle in the sicker state
                                     # cost of treatment(per cycle)
        <- 12000
c_trt
        <- 0
                                     # cost of being in the death state
c_D
        <- 1
                                     # utility when healthy
u_H
u_S1
        <- 0.75
                                     # utility when sick
        <- 0.5
                                     # utility when sicker
u_S2
       <- 0
u_D
                                     # utility when dead
u_trt
        <- 0.95
                                     # utility when being treated
d_e
        <- d_c <- 0.03
                                     # discount rate per cycle equal discount of costs and QALYs by 3%
        <- length(v_names_str)</pre>
                                     # Number of strategies
n_str
                                     # number of states
n_states <- length(v_n)</pre>
# Discount weights for costs and effects
v_dwc \leftarrow 1 / (1 + d_c) ^ (0:n_t)
v_{dwe} \leftarrow 1 / (1 + d_e) ^ (0:n_t)
```

Create a state-transition diagram of the cohort model



04 Define and initialize matrices and vectors

04.1 Cohort trace

```
# create the markov trace matrix M capturing the proportion of the cohort in each state
# at each cycle
m_M_notrt <- m_M_trt <- matrix(NA,</pre>
                                         = n_t + 1, ncol = n_states,
                               dimnames = list(paste("cycle", 0:n_t, sep = " "), v_n))
head(m_M_notrt) # show first 6 rows of the matrix
            H S1 S2 D
##
## cycle O NA NA NA NA
## cycle 1 NA NA NA NA
## cycle 2 NA NA NA NA
## cycle 3 NA NA NA NA
## cycle 4 NA NA NA NA
## cycle 5 NA NA NA NA
# The cohort starts as healthy
m_M_notrt[1, ] <- m_M_trt[1, ] <- v_init # initiate first cycle of cohort trace</pre>
```

04.2 Transition probability matrix

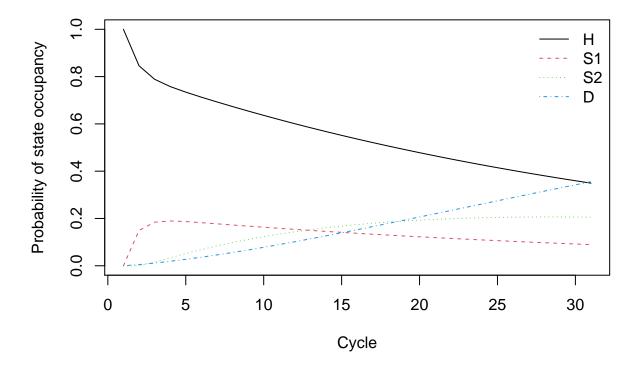
```
# from Healthy
m_P_notrt["H", "H" ] <- (1 - p_HD) * (1 - p_HS1)
m_P_notrt["H", "S1" ] <- (1 - p_HD) * p_HS1</pre>
m_P_notrt["H", "D" ] <- p_HD</pre>
# from Sick
m_P_notrt["S1", "H"] <- (1 - p_S1D) * p_S1H</pre>
m_P_notrt["S1", "S1"] <- (1 - p_S1D) * (1 - (p_S1H + p_S1S2))
m_P_notrt["S1", "S2"] <- (1 - p_S1D) * p_S1S2
m_P_notrt["S1", "D" ] <- p_S1D</pre>
# from Sicker
m_P_notrt["S2", "S2"] <- 1 - p_S2D
m_P_notrt["S2", "D" ] <- p_S2D</pre>
# from Dead
m_P_notrt["D", "D" ] <- 1</pre>
# Check that transition probabilities are in [0, 1]
check_transition_probability(m_P_notrt, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(m_P_notrt, n_states = n_states, n_cycles = n_t, verbose = TRUE)
# create transition probability matrix for treatment same as no treatment
m_P_trt <- m_P_notrt</pre>
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

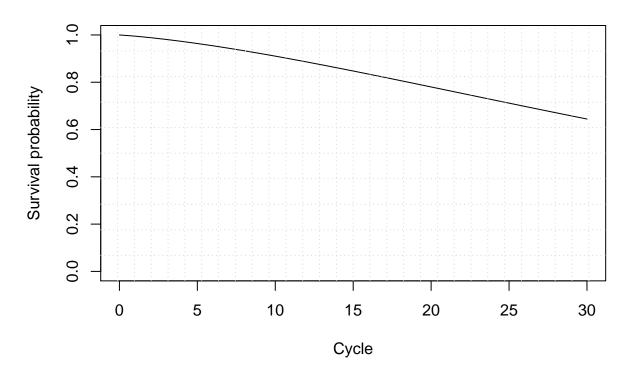
Cohort Trace



06.2 Overall Survival (OS)

```
# calculate the overall survival (OS) probability for no treatment
v_os_notrt <- 1 - m_M_notrt[, "D"]
# alternative way of calculating the OS probability
v_os_notrt <- rowSums(m_M_notrt[, 1:3])
# create a simple plot showing the OS
plot(O:n_t, v_os_notrt, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")
# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

Overall Survival

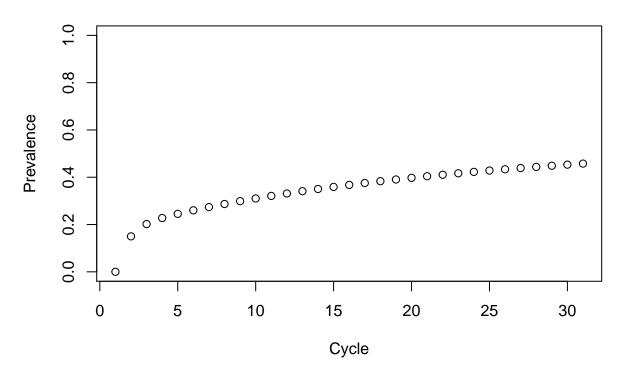


06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os_notrt) # summing probability of OS over time (i.e. life expectancy)
```

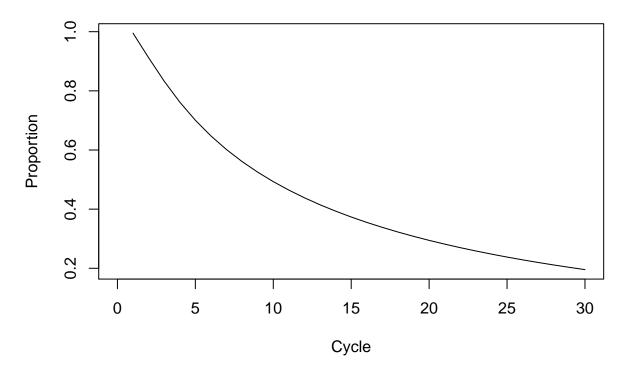
06.3 Disease prevalence

Disease prevalence



06.4 Proportion of sick in S1 state

Proportion of sick in S1 state



07 Compute Cost-Effectiveness Outcomes

```
# Vectors with costs and utilities by treatment

v_u_notrt <- c(u_H, u_S1, u_S2, u_D)

v_u_trt <- c(u_H, u_trt, u_S2, u_D)

v_c_notrt <- c(c_H, c_S1, c_S2, c_D)

v_c_trt <- c(c_H, c_S1 + c_trt, c_S2 + c_trt, c_D)
```

07.1 Mean Costs and QALYs for Treatment and NO Treatment

07.2 Discounted Mean Costs and QALYs

```
tu_d_notrt <- t(v_tu_notrt)</pre>
                             %*% v_dwe
tu_d_trt <- t(v_tu_trt)</pre>
                             %*% v_dwe
tc_d_notrt <- t(v_tc_notrt) %*% v_dwc
tc_d_trt <- t(v_tc_trt)
                             %*% v_dwc
# store them into a vector
v_tc_d <- c(tc_d_notrt, tc_d_trt)
v_tu_d
          <- c(tu_d_notrt, tu_d_trt)
# Dataframe with discounted costs and effectiveness
df_ce
          <- data.frame(Strategy = v_names_str,
                         Cost
                               = v_tc_d,
                        Effect = v_tu_d
df_ce
##
        Strategy
                      Cost
                           Effect
## 1 No Treatment 75795.04 15.84802
       Treatment 141511.41 16.41446
```

07.3 Compute ICERs of the Markov model

07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "QALYs", xlim = c(15.6, 16.6))
```

