Simple 3-state Markov model in R

The DARTH workgroup

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Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
## Loading required package: pacman
# load (install if required) packages from CRAN
p_load("diagram")
```

02 Load functions

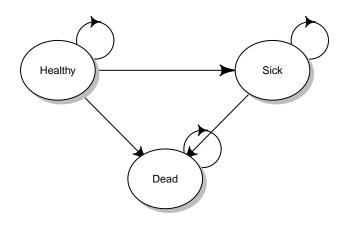
```
# no functions required
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("Base Case")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead")</pre>
                                         # state names
n_states <- length(v_n)
                                          # number of states
n_t <- 60
                                          # number of cycles
p_{HD} < -0.02
                                          # probability to die when healthy
p_HS <- 0.05
                                          # probability to become sick when healthy
p_SD \leftarrow 0.1
                                          # probability to die when sick
# Costs and utilities
c H <- 400
                                         # cost of remaining one cycle healthy
c S <- 1000
                                         # cost of remaining one cycle sick
c D <- 0
                                         # cost of remaining one cycle dead
u H <- 0.8
                                         # utility when healthy
u_S < 0.5
                                         # utility when sick
u D <- 0
                                         # utility when dead
                                          # equal discount of costs and QALYs by 3%
d = < - d < < - 0.03
\# calculate discount weights for costs for each cycle based on discount rate d_{\_}c
v_dwc \leftarrow 1 / (1 + d_e) ^ (0:n_t)
# calculate discount weights for effectiveness for each cycle based on discount rate d_e
v_dwe \leftarrow 1 / (1 + d_c) ^ (0:n_t)
```

Draw the state-transition cohort model

```
m_P_diag <- matrix(0, nrow = n_states, ncol = n_states, dimnames = list(v_n, v_n))
m_P_diag["Healthy", "Sick"] = ""</pre>
```



04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability matrix

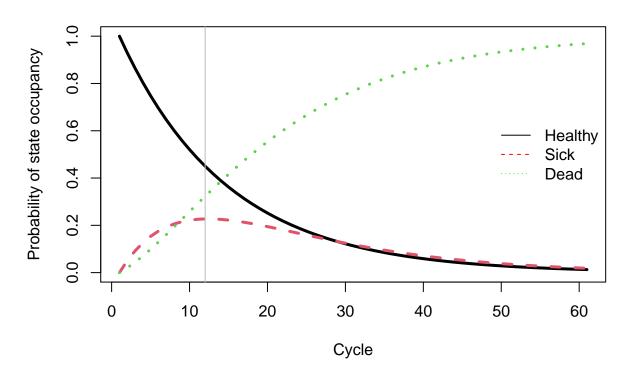
```
# create the transition probability matrix
m_P <- matrix(0,</pre>
                nrow = n_states, ncol = n_states,
                dimnames = list(v_n, v_n)) # name the columns and rows of the transition
                                             # probability matrix
m_P
           Healthy Sick Dead
##
                  0
                       0
## Healthy
## Sick
                  0
                       0
                             0
## Dead
                       0
                             0
Fill in the transition probability matrix:
# from Healthy
m_P["Healthy", "Healthy"] <- 1 - p_HD - p_HS</pre>
m_P["Healthy", "Sick"] <- p_HS
m_P["Healthy", "Dead"]
                           <- p HD
# from Sick
m_P["Sick", "Sick"] <- 1 - p_SD</pre>
m_P["Sick", "Dead"] <- p_SD</pre>
# from Dead
m_P["Dead", "Dead"] <- 1</pre>
# check rows add up to 1
rowSums(m_P)
## Healthy
               Sick
                       Dead
        1
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

Cohort Trace



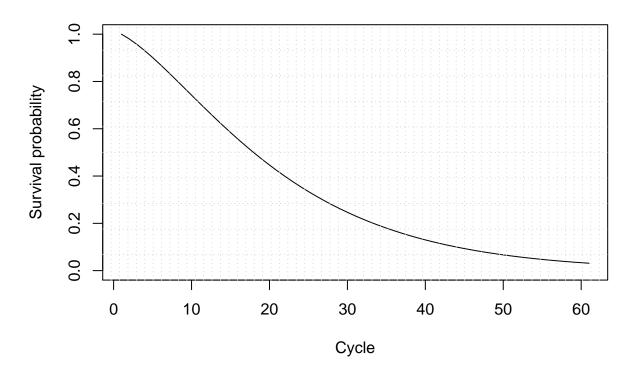
06.2 Overall Survival (OS)

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2])  # alternative way of calculating the OS probability

plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

Overall Survival

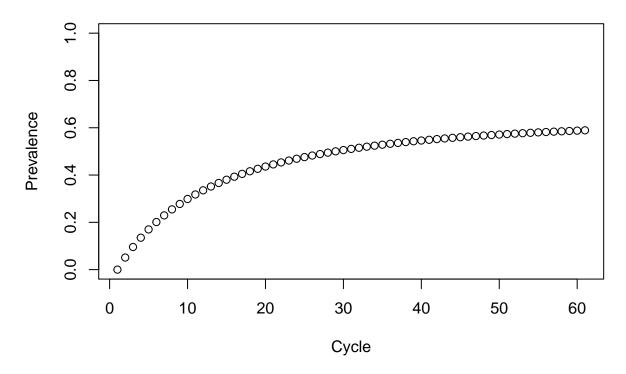


06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os) # summing probablity of OS over time (i.e. life expectancy)
```

06.3 Disease prevalence

Disease prevalence



07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
v_tc <- m_M %*% c(c_H, c_S, c_D)
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
v_tu <- m_M %*% c(u_H, u_S, u_D)</pre>
```

07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights (v_dw)
v_tc_d <- t(v_tc) %*% v_dwc
# Discount QALYS by multiplying the QALYs vector with discount weights (v_dw)
v_te_d <- t(v_tu) %*% v_dwe</pre>
```

07.3 Results

check.names = F)
results

Total Discounted Cost Life Expectancy Total Discounted QALYs
1 8043.131 21.00019 10.18939