Simple 3-state Markov model in R

With a probabilistic sensitivty analysis (PSA)

The DARTH workgroup

Developed by the Decision Analysis in R for Technologies in Health (DARTH) workgroup:

Fernando Alarid-Escudero, PhD (1)

Eva A. Enns, MS, PhD (2)

M.G. Myriam Hunink, MD, PhD (3,4)

Hawre J. Jalal, MD, PhD (5)

Eline M. Krijkamp, MSc (3)

Petros Pechlivanoglou, PhD (6,7)

Alan Yang, MSc (7)

In collaboration of:

- 1. Division of Public Administration, Center for Research and Teaching in Economics (CIDE), Aguas-calientes, Mexico
- 2. University of Minnesota School of Public Health, Minneapolis, MN, USA
- 3. Erasmus MC, Rotterdam, The Netherlands
- 4. Harvard T.H. Chan School of Public Health, Boston, USA
- 5. University of Pittsburgh Graduate School of Public Health, Pittsburgh, PA, USA
- 6. University of Toronto, Toronto ON, Canada
- 7. The Hospital for Sick Children, Toronto ON, Canada

Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001. 07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

Copyright 2017, THE HOSPITAL FOR SICK CHILDREN AND THE COLLABORATING INSTITUTIONS. All rights reserved in Canada, the United States and worldwide. Copyright, trademarks, trade names and any and all associated intellectual property are exclusively owned by THE HOSPITAL FOR Sick CHILDREN and the collaborating institutions. These materials may be used, reproduced, modified, distributed and adapted with proper attribution.

Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load( "dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "ggraph", "reshape2"
# load (install if required) packages from GitHub
p_load_gh("DARTH-git/dampack", "DARTH-git/darthtools")
```

02 Load functions

 $d_e < -d_c < -0.03$

```
# all functions are in the darthtools package
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("Standard of Care", "Treatment")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead") # state names</pre>
n_states <- length(v_n)
                                     # number of states
n_t <- 60
                                     # number of cycles
v_{init} \leftarrow c(1, 0, 0)
                                      # initial cohort distribution (everyone allocated to the "healthy
# Transition probabilities
p_{HD} < -0.02
                                      # probability of dying when healthy
p_{HS} < -0.05
                                      # probability of becoming sick when healthy, under standard of ca
                                      # probability of becoming sick when healthy, under treatment
p_HS_trt <- 0.03
p_SD <- 0.1
                                      # probability of dying when sick
# Costs and utilities
c_H <- 400
                                      # cost of one cycle in healthy state
c_S <- 1000
                                      # cost of one cycle in sick state
                                     # cost of one cycle in dead state
c_D <- 0
c_trt <- 800
                                      # cost of treatment (per cycle)
u H <- 0.8
                                      # utility when healthy
u_S <- 0.5
                                      # utility when sick
u_D <- 0
                                      # utility when dead
```

discount rate per cycle equal discount of costs and QALYs by 3%

```
# calculate discount weights for costs for each cycle based on discount rate d_c
v_dwc <- 1 / (1 + d_e) ^ (0:n_t)
# calculate discount weights for effectiveness for each cycle based on discount rate d_e
v_dwe <- 1 / (1 + d_c) ^ (0:n_t)</pre>
```

Draw the state-transition cohort model

04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability matrix

Fill in the transition probability matrix:

```
# from Healthy
m_P["Healthy", "Healthy"] <- 1 - p_HS - p_HD
m_P["Healthy", "Sick"] <- p_HS
m_P["Healthy", "Dead"] <- p_HD

# from Sick
m_P["Sick", "Sick"] <- 1 - p_SD
m_P["Sick", "Dead"] <- p_SD

# from Dead
m_P["Dead", "Dead"] <- 1

# Under treatment
m_P_trt <- m_P
m_P_trt["Healthy", "Healthy"] <- 1 - p_HS_trt - p_HD
m_P_trt["Healthy", "Sick"] <- p_HS_trt</pre>
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

Standard of Care:

Treatment:

06.2 Overall Survival (OS)

Standard of Care:

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2])  # alternative way of calculating the OS probability

plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

Treatment:

```
v_os_trt <- 1 - m_M_trt[, "Dead"]  # calculate the overall survival (OS) probability
v_os_trt <- rowSums(m_M_trt[, 1:2])  # alternative way of calculating the OS probability

plot(v_os_trt, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os)  # summing probability of OS over time (i.e. life expectancy)
v_le_trt <- sum(v_os_trt)  # summing probability of OS over time (i.e. life expectancy), treatment</pre>
```

06.3 Disease prevalence

Standard of Care:

```
v_prev <- m_M[, "Sick"]/v_os
plot(v_prev,
    ylim = c(0, 1),
    ylab = "Prevalence",
    xlab = "Cycle",
    main = "Disease prevalence")</pre>
```

Treatment:

07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

07.2 Discounted Mean Costs and QALYs

07.3 Compute ICERs of the Markov model

```
df_cea
```

07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "QALYs", xlim = c(10, 12))
```

08 Probabilistic Sensitivity Analysis

08.1 List of input parameters

Create list 1_params_all with all input probabilities, cost and utilities.

```
l_params_all <- as.list(data.frame(</pre>
 p_HD
          = 0.02, # probability of dying when healthy
 p_HS
          = 0.05, # probability of becoming sick when healthy, conditioned on not dying
 p_HS_trt = 0.03, # probability of becoming sick when healthy, conditioned on not dying
                  # probability of dying when sick
 p_SD
          = 0.1,
          = 400,
 c_H
                 # cost of one cycle in healthy state
 c_S
          = 1000, # cost of one cycle in sick state
 c_D
          = 0,
                 # cost of one cycle in dead state
          = 800, # cost of treatment (per cycle)
 c_trt
 u_H
          = 0.8, # utility when healthy
          = 0.5, # utility when sick
 u S
          = 0,
                  # utility when dead
 u_D
          = 0.03, # discount factor for effectiveness
 d e
          = 0.03 # discount factor for costs
 d_c
# store the parameter names into a vector
v_names_params <- names(l_params_all)</pre>
```

08.2 Load Sick-Sicker Markov model function

```
source("Functions_markov_3state.R")
# Test function
calculate_ce_out(l_params_all)
```

08.3 Generate PSA datasets

```
# Function to generate PSA input dataset
gen_psa <- function(n_sim = 1000, seed = 071818){
   set.seed(seed) # set a seed to be able to reproduce the same results
   df_psa <- data.frame(
        # Transition probabilities (per cycle)</pre>
```

```
# probability to become sick when healthy
   p_{HS} = rbeta(n_{sim}, shape1 = 24, shape2 = 450),
   p_HS_trt = rbeta(n_sim, shape1 = 9, shape2 = 281), # under treatment
    # probability of dying when healthy
           = rbeta(n_sim, shape1 = 16, shape2 = 767),
    # probability of dying when sick
   p_SD
           = rbeta(n_sim, shape1 = 22.4, shape2 = 201.6),
   # Cost vectors with length n_sim
    # cost of remaining one cycle in state H
            = rgamma(n_sim, shape = 16, scale = 25),
    # cost of remaining one cycle in state S1
           = rgamma(n_sim, shape = 100, scale = 10),
    # cost of being in the death state
   c_D
            = 0,
    # cost of treatment (per cycle)
   c_{trt} = rgamma(n_{sim}, shape = 64, scale = 12.5),
   # Utility vectors with length n_sim
   # utility when healthy
            = rbeta(n sim, shape1 = 50.4, shape2 = 12.6),
   u H
   # utility when sick
            = rbeta(n_sim, shape1 = 49.5, shape2 = 49.5),
   # utility when dead
            = 0
   u_D
 return(df_psa)
}
# Try it
gen_psa(10)
# Number of simulations
n_sim <- 1000
# Generate PSA input dataset
df_psa_input <- gen_psa(n_sim = n_sim)</pre>
# First six observations
head(df_psa_input)
# Histogram of parameters
ggplot(melt(df_psa_input, variable.name = "Parameter"), aes(x = value)) +
       facet_wrap(~Parameter, scales = "free") +
       geom_histogram(aes(y = ..density..)) +
       theme_bw(base_size = 16) +
       theme(axis.text = element_text(size=8))
# Initialize dataframes with PSA output
# Dataframe of costs
df_c <- as.data.frame(matrix(0,</pre>
                      nrow = n_sim,
                      ncol = n_str))
colnames(df_c) <- v_names_str</pre>
# Dataframe of effectiveness
```

08.4 Conduct probabilistic sensitivity analysis

```
# Run Markov model on each parameter set of PSA input dataset
for(i in 1:n_sim){
   l_out_temp <- calculate_ce_out(df_psa_input[i, ])
   df_c[i, ] <- l_out_temp$Cost
   df_e[i, ] <- l_out_temp$Effect
   # Display simulation progress
   if(i/(n_sim/10) == round(i/(n_sim/10), 0)) { # display progress every 10%
      cat('\r', paste(i/n_sim * 100, "% done", sep = " "))
   }
}</pre>
```

08.5 Analyze and visualize PSA results using R package: dampack

Create PSA object for dampack

08.5.1 Save PSA objects

```
save(df_psa_input, df_c, df_e, v_names_str, n_str, l_psa,
    file = "markov_3state_PSA_dataset.RData")
```

Vector with willingness-to-pay (WTP) thresholds.

```
v_{wtp} \leftarrow seq(0, 5000, by = 1000)
```

08.5.2 Cost-Effectiveness Scatter plot

```
plot(l_psa)
```

08.5.3 Conduct CEA with probabilistic output

08.5.4 Plot cost-effectiveness frontier

```
plot(df_cea_psa)
```

08.5.6 Cost-effectiveness acceptability curves (CEACs) and frontier (CEAF)

```
ceac_obj <- ceac(wtp = v_wtp, psa = l_psa)
# Regions of highest probability of cost-effectiveness for each strategy
summary(ceac_obj)
# CEAC & CEAF plot
plot(ceac_obj)</pre>
```

08.5.7 Expected Loss Curves (ELCs)

The expected loss is the the quantification of the foregone benefits when choosing a suboptimal strategy given current evidence.

```
elc_obj <- calc_exp_loss(wtp = v_wtp, psa = 1_psa)
elc_obj
# ELC plot
plot(elc_obj, log_y = FALSE)</pre>
```

08.5.8 Expected value of perfect information (EVPI)

```
evpi <- calc_evpi(wtp = v_wtp, psa = l_psa)
# EVPI plot
plot(evpi, effect_units = "QALY")</pre>
```