Simple 3-state Markov model in R

with age dependency

The DARTH workgroup

Developed by the Decision Analysis in R for Technologies in Health (DARTH) workgroup:

Fernando Alarid-Escudero, PhD (1)

Eva A. Enns, MS, PhD (2)

M.G. Myriam Hunink, MD, PhD (3,4)

Hawre J. Jalal, MD, PhD (5)

Eline M. Krijkamp, MSc (3)

Petros Pechlivanoglou, PhD (6,7)

Alan Yang, MSc (7)

In collaboration of:

- 1. Division of Public Administration, Center for Research and Teaching in Economics (CIDE), Aguas-calientes, Mexico
- 2. University of Minnesota School of Public Health, Minneapolis, MN, USA
- 3. Erasmus MC, Rotterdam, The Netherlands
- 4. Harvard T.H. Chan School of Public Health, Boston, USA
- 5. University of Pittsburgh Graduate School of Public Health, Pittsburgh, PA, USA
- 6. University of Toronto, Toronto ON, Canada
- 7. The Hospital for Sick Children, Toronto ON, Canada

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- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001. 07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. 2020 Online first. https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("diagram")
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/darthtools")
```

02 Load functions

```
# No functions needed
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("Standard of Care")</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead") # state names</pre>
n_t <- 60
                                      # number of cycles
v_{init} \leftarrow c("Healthy" = 1,
            "Sick" = 0,
            "Dead" = 0)
                                    # initial cohort distribution (everyone allocated to the
                                     # "healthy" state)
# Transition probabilities
p_HD_min <- 0.003</pre>
                                      # probability of dying when healthy at t = 0
p_HD_max <- 0.01
                                    # probability of dying when health at t = n.t
p_HS
       <- 0.05
                                     # probability of becoming sick when healthy, under standard of ca
p_SD
        <- 0.1
                                      # probability of dying when sick
# Costs and utilities
       <- 400
c_H
                                     # cost of one cycle in healthy state
        <- 1000
                                     # cost of one cycle in sick state
c_S
       <- 0
c_D
                                    # cost of one cycle in dead state
u_H
       <- 0.8
                                    # utility when healthy
       <- 0.5
                                     # utility when sick
u_S
u_D
        <- 0
                                     # utility when dead
       <- d_c <- 0.03
                                      # discount rate per cycle equal discount of costs and QALYs by 3%
d_e
```

04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability array

```
# create the transition probability array
a_P <- array(0,  # Create 3-D array
dim = c(n_states, n_states, n_t),
dimnames = list(v_n, v_n, 0:(n_t - 1))) # name the dimensions of the array</pre>
```

Fill in the transition probability array:

```
# from Healthy
a_P["Healthy", "Healthy", ] <- (1 - p_HD) * (1 - p_HS)
a_P["Healthy", "Sick", ] <- (1 - p_HD) * p_HS
a_P["Healthy", "Dead", ] <- p_HD

# from Sick
a_P["Sick", "Sick", ] <- 1 - p_SD
a_P["Sick", "Dead", ] <- p_SD

# from Dead
a_P["Dead", "Dead", ] <- 1</pre>
```

04.3 Check if transition array and probabilities are valid

```
# Check that transition probabilities are in [0, 1]
check_transition_probability(a_P, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(a_P, n_states = n_states, n_cycles = n_t, verbose = TRUE)
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

06.2 Overall Survival (OS)

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2]) # alternative way of calculating the OS probability

# create a simple plot showing the OS
plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")

# add grid
grid(nx = n_t, ny = 10,
    col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os) # summing probablity of OS over time (i.e. life expectancy)
```

06.3 Disease prevalence

07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
v_tc <- m_M %*% c(c_H, c_S, c_D)
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
v_tu <- m_M %*% c(u_H, u_S, u_D)</pre>
```

07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights (v_dw)
v_tc_d <- t(v_tc) %*% v_dwc
# Discount QALYS by multiplying the QALYs vector with discount weights (v_dw)
v_te_d <- t(v_tu) %*% v_dwe</pre>
```

07.3 Store Results