Markov Sick-Sicker model in R

The DARTH workgroup

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Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("here", "dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "truncnorm",
# load (install if required) packages from GitHub
# install_github("DARTH-git/dampack", force = TRUE) Uncomment if there is a newer version
# install_github("DARTH-git/dectree", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/dampack", "DARTH-git/dectree")
```

02 Load functions

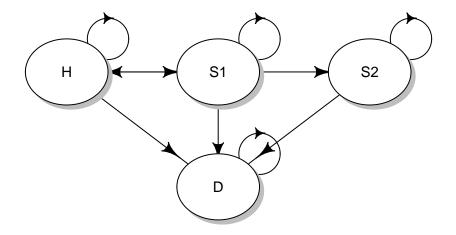
```
# no functions needed
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("No Treatment", "Treatment")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
      <- 25
age
                                    # age at baseline
max_age <- 55
                                    # maximum age of follow up
n_t <- max_age - age
                                    # time horizon, number of cycles
      <- c("H", "S1", "S2", "D") # the 4 states of the model: Healthy (H), Sick (S1),</pre>
v n
                                    # Sicker (S2), Dead (D)
             <- length(v n)
                                    # number of health states
n states
# Transition probabilities (per cycle)
       <- 0.005
                                    # probability to die when healthy
p_HD
       <- 0.15
                                      # probability to become sick when healthy
p_HS1
p_S1H <- 0.5
                                      # probability to become healthy when sick
p_S1S2 <- 0.105
                                      # probability to become sicker when sick
hr_S1
       <- 3
                                      # hazard ratio of death in sick vs healthy
hr_S2 <- 10
                                      # hazard ratio of death in sicker vs healthy
r_{HD} < - \log(1 - p_{HD})
                                   # rate of death in healthy
r_S1D \leftarrow hr_S1 * r_HD
                                     # rate of death in sick
r_S2D <- hr_S2 * r_HD
                                      # rate of death in sicker
p_S1D \leftarrow 1 - exp(-r_S1D)
                                    # probability to die in sick
p_S2D \leftarrow 1 - exp(-r_S2D)
                                    # probability to die in sicker
# Cost and utility inputs
c_H <- 2000
                                    # cost of remaining one cycle in the healthy state
c_S1 <- 4000
                                    # cost of remaining one cycle in the sick state
c_S2 <- 15000
                                    # cost of remaining one cycle in the sicker state
c_trt <- 12000
                                    # cost of treatment(per cycle)
```

```
c_D
        <- 0
                                      # cost of being in the death state
        <- 1
                                      # utility when healthy
u_H
u S1
        <- 0.75
                                      # utility when sick
                                      # utility when sicker
        <- 0.5
u S2
        <- 0
                                      # utility when dead
u_D
u_trt
        <- 0.95
                                      # utility when being treated
# Discounting factor
d_e < d_c < 0.03
                                          # equal discount of costs and QALYs by 3%
\# calculate discount weights for costs for each cycle based on discount rate d\_c
v_dwc \leftarrow 1 / (1 + d_e) ^ (0:n_t)
 \hbox{\it\# calculate discount weights for effectiveness for each cycle based on discount rate $d\_e$ }
v_dwe \leftarrow 1 / (1 + d_c) ^ (0:n_t)
```

Create a state-transition diagram of the cohort model



04 Define and initialize matrices and vectors

04.1 Cohort trace

```
\# create the markov trace matrix M capturing the proportion of the cohort in each state
# at each cycle
m_M_notrt <- m_M_trt <- matrix(NA,</pre>
                                           = n_t + 1, ncol = n_states,
                                 nrow
                                 dimnames = list(paste("cycle", 0:n_t, sep = " "), v_n))
head(m_M_notrt) # show first 6 rows of the matrix
            H S1 S2 D
## cycle O NA NA NA NA
## cycle 1 NA NA NA NA
## cycle 2 NA NA NA NA
## cycle 3 NA NA NA NA
## cycle 4 NA NA NA NA
## cycle 5 NA NA NA NA
# The cohort starts as healthy
m_M_{notrt[1, ]} \leftarrow m_M_{trt[1, ]} \leftarrow c(1, 0, 0, 0) # initiate first cycle of cohort trace
```

04.2 Transition probability matrix

```
# create the transition probability matrix for NO treatment
m_P_notrt <- matrix(0,</pre>
                      nrow = n_states,
                      ncol = n_states,
                      dimnames = list(v_n, v_n)) # name the columns and rows of the matrix
m_P_notrt
      H S1 S2 D
## H O O O O
## S1 0 0 0 0
## S2 0 0 0 0
## D O O O O
Fill in the transition probability matrix:
# from Healthy
m_P_notrt["H", "H" ] <- 1 - (p_HS1 + p_HD)</pre>
m P notrt["H", "S1" ] <- p HS1</pre>
m_P_notrt["H", "D" ] <- p_HD</pre>
# from Sick
m_P_notrt["S1", "H"] <- p_S1H</pre>
m_P_notrt["S1", "S1"] <- 1 - (p_S1H + p_S1S2 + p_S1D)</pre>
m_P_notrt["S1", "S2"] <- p_S1S2</pre>
m_P_notrt["S1", "D" ] <- p_S1D
# from Sicker
m_P_notrt["S2", "S2"] <- 1 - p_S2D
m_P_notrt["S2", "D"] <- p_S2D
# from Dead
m_P_notrt["D", "D" ] <- 1</pre>
# check rows add up to 1
rowSums(m_P_notrt)
## H S1 S2 D
## 1 1 1 1
# create transition probability matrix for treatment same as no treatment
m_P_trt <- m_P_notrt</pre>
```

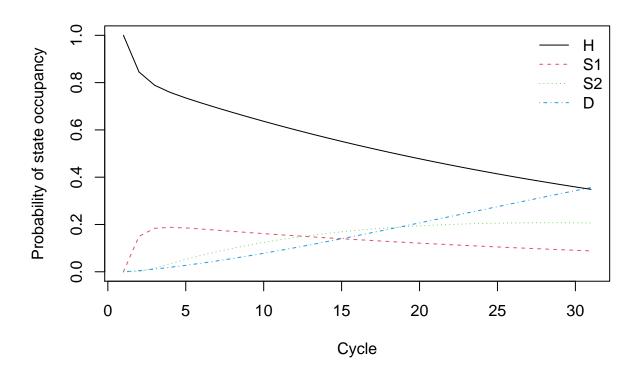
05 Run Markov model

```
## cycle 2 0.7890250 0.1837612 0.01575000 0.01146377
## cycle 3 0.7586067 0.1881968 0.03427491 0.01892157
## cycle 4 0.7351211 0.1853199 0.05235988 0.02719916
## cycle 5 0.7138373 0.1807036 0.06925860 0.03620055
```

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

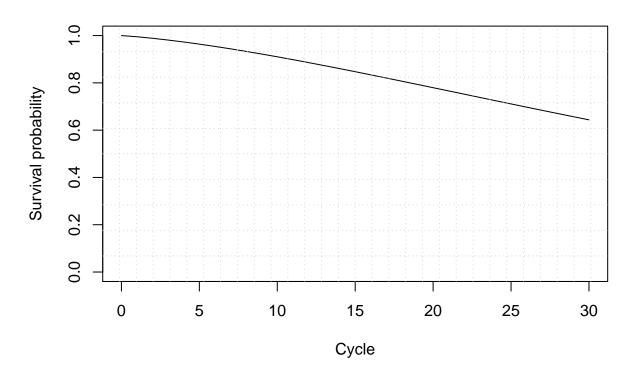
Cohort Trace



06.2 Overall Survival (OS)

```
# calculate the overall survival (OS) probability for no treatment
v_os_notrt <- 1 - m_M_notrt[, "D"]
# alternative way of calculating the OS probability
v_os_notrt <- rowSums(m_M_notrt[, 1:3])
# create a simple plot showing the OS
plot(0:n_t, v_os_notrt, type = 'l',</pre>
```

Overall Survival

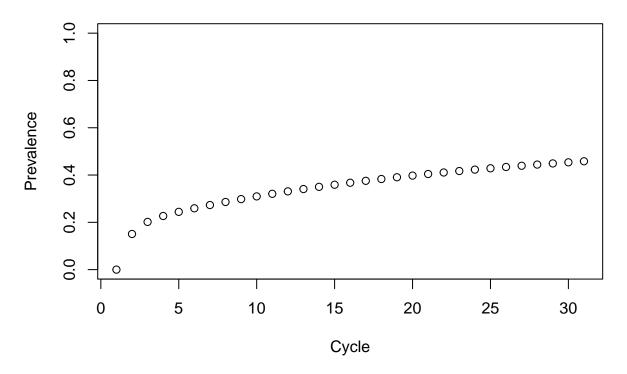


06.2.1 Life Expectancy (LE)

06.3 Disease prevalence

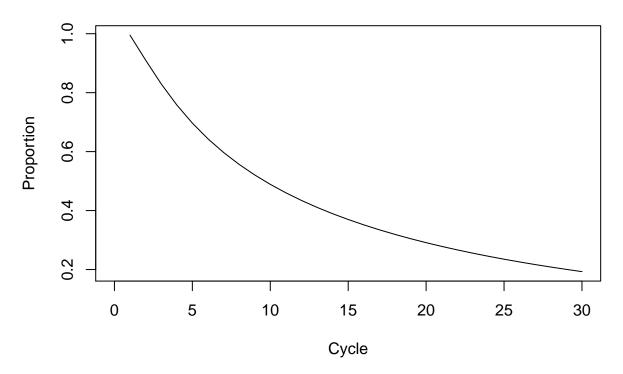
```
v_prev <- rowSums(m_M_notrt[, c("S1", "S2")]) / v_os_notrt
plot(v_prev,
    ylim = c(0, 1),
    ylab = "Prevalence",
    xlab = "Cycle",
    main = "Disease prevalence")</pre>
```

Disease prevalence



06.4 Proportion of sick in S1 state

Proportion of sick in S1 state



07 Compute Cost-Effectiveness Outcomes

```
# Vectors with costs and utilities by treatment

v_u_notrt <- c(u_H, u_S1, u_S2, u_D)

v_u_trt <- c(u_H, u_trt, u_S2, u_D)

v_c_notrt <- c(c_H, c_S1, c_S2, c_D)

v_c_trt <- c(c_H, c_S1 + c_trt, c_S2 + c_trt, c_D)
```

07.1 Mean Costs and QALYs for Treatment and NO Treatment

07.2 Discounted Mean Costs and QALYs

07.3 Compute ICERs of the Markov model

```
## Strategy Cost Effect Inc_Cost Inc_Effect ICER Status
## 1 No Treatment 75976.15 15.83885 NA NA NA NA
## 2 Treatment 141623.03 16.40041 65646.88 0.5615578 116901.4 ND
```

07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "Quality of Life", xlim = c(15.6, 16.6))
```

