

# SA: Simple 3-state Markov model in R

The DARTH workgroup

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Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. *Med Decis Making*. 2017; 37(3): 735-746. <https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559>
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM, Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. *arXiv:200107824v2*. 2020:1-48. <http://arxiv.org/abs/2001.07824>
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. *Med Decis Making*. 2018;38(3):400-22. <https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513>
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. *Med Decis Making*. Online First <https://doi.org/10.1177/0272989X19893973>

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Change `eval` to `TRUE` if you want to knit this document.

```
rm(list = ls())      # clear memory (removes all the variables from the workspace)
```

## 01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "ggraph", "reshape2")
# install_github("DARTH-git/dampack", force = TRUE) Uncomment if there is a newer version
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/dampack", "DARTH-git/darthtools")
```

## 02 Load functions

```
# all functions are in the darthtools package
```

## 03 Input model parameters

```
# Strategy names
v_names_str <- c("Standard of Care", "Treatment")

# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead") # state names
n_t <- 60                          # number of cycles

v_init <- c("Healthy" = 1,
            "Sick"    = 0,
            "Dead"    = 0)          # initial cohort distribution (everyone allocated to the
                                   # "healthy" state)

# Transition probabilities
p_HD <- 0.02                       # probability of dying when healthy
p_HS <- 0.05                       # probability of becoming sick when healthy, under standard of care
p_HS_trt <- 0.03                   # probability of becoming sick when healthy, under treatment
p_SD <- 0.1                        # probability of dying when sick

# Costs and utilities
c_H <- 400                         # cost of one cycle in healthy state
c_S <- 1000                        # cost of one cycle in sick state
c_D <- 0                           # cost of one cycle in dead state
c_trt <- 8000                      # cost of treatment (per cycle)
u_H <- 0.8                         # utility when healthy
u_S <- 0.5                         # utility when sick
u_D <- 0                           # utility when dead
```

```

d_e      <- d_c <- 0.03          # discount rate per cycle equal discount of costs and QALYs by 3%

n_str     <- length(v_names_str)  # Number of strategies
n_states  <- length(v_n)          # number of states

# Discount weights for costs and effects
v_dwc     <- 1 / (1 + d_c) ^ (0:n_t)
v_dwe     <- 1 / (1 + d_e) ^ (0:n_t)

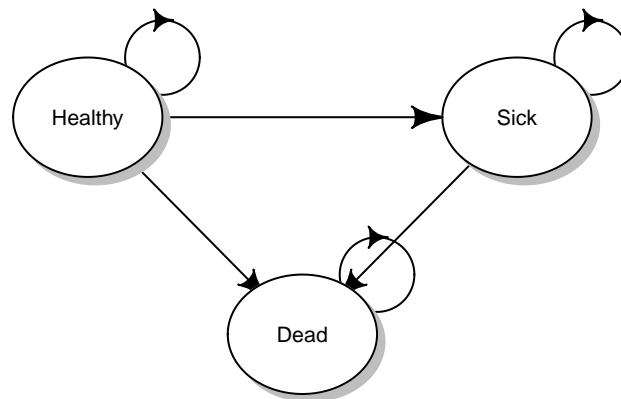
```

## Draw the state-transition cohort model

```

m_P_diag <- matrix(0, nrow = n_states, ncol = n_states, dimnames = list(v_n, v_n))
m_P_diag["Healthy", "Sick" ]      = ""
m_P_diag["Healthy", "Dead" ]      = ""
m_P_diag["Healthy", "Healthy" ]   = ""
m_P_diag["Sick" , "Dead" ]        = ""
m_P_diag["Sick" , "Sick" ]        = ""
m_P_diag["Dead" , "Dead" ]        = ""
layout.fig <- c(2, 1)
plotmat(t(m_P_diag), t(layout.fig), self.cex = 0.5, curve = 0, arr.pos = 0.8,
        latex = T, arr.type = "curved", relsize = 0.85, box.prop = 0.8,
        cex = 0.8, box.cex = 0.7, lwd = 1)

```



## 04 Define and initialize matrices and vectors

### 04.1 Cohort trace

```
# create the cohort trace
m_M_SoC <- m_M_trt <- matrix(NA,
                             nrow = n_t + 1, # create Markov trace (n_t + 1 because R doesn't
                             # understand Cycle 0)
                             ncol = n_states,
                             dimnames = list(0:n_t, v_n))

m_M_SoC[1, ] <- m_M_trt[1, ] <- v_init # initialize first cycle of Markov trace
```

### 04.2 Transition probability matrix

```
# create the transition probability matrices
m_P_SoC <- m_P_trt <- matrix(0,
                             nrow = n_states, ncol = n_states,
                             dimnames = list(v_n, v_n)) # name the columns and rows of the matrix

# print the probability matrices
m_P_SoC # for standard of care
```

```
##           Healthy Sick Dead
## Healthy      0      0      0
## Sick         0      0      0
## Dead         0      0      0
```

```
m_P_trt # treatment
```

```
##           Healthy Sick Dead
## Healthy      0      0      0
## Sick         0      0      0
## Dead         0      0      0
```

Fill in the transition probability matrix:

```
# For Standard of Care
# from Healthy
m_P_SoC["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS)
m_P_SoC["Healthy", "Sick"]    <- (1 - p_HD) * p_HS
m_P_SoC["Healthy", "Dead"]    <- p_HD

# from Sick
m_P_SoC["Sick", "Sick"] <- 1 - p_SD
m_P_SoC["Sick", "Dead"] <- p_SD

# from Dead
m_P_SoC["Dead", "Dead"] <- 1
```

```

# Under treatment
m_P_trt <- m_P_SoC # Assign the matrix for standard of care to the transition probability matrix for t
# replace values that are different under treatment
m_P_trt["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS_trt)
m_P_trt["Healthy", "Sick"] <- (1 - p_HD) * p_HS_trt

```

## 04.3 Check if transition probability structure and probabilities are valid

```

# Check that transition probabilities are in [0, 1]
check_transition_probability(m_P_SoC, verbose = TRUE)
check_transition_probability(m_P_trt, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(m_P_SoC, n_states = n_states, n_cycles = n_t, verbose = TRUE)
check_sum_of_transition_array(m_P_trt, n_states = n_states, n_cycles = n_t, verbose = TRUE)

```

## 05 Run Markov model

```

for (t in 1:n_t){ # loop through the number of cycles
  m_M_SoC[t + 1, ] <- m_M_SoC[t, ] %*% m_P_SoC # estimate the state vector for the next cycle (t + 1)
  m_M_trt[t + 1, ] <- m_M_trt[t, ] %*% m_P_trt # for treatment
}

```

## 06 Compute and Plot Epidemiological Outcomes

### 06.1 Cohort trace

Standard of Care:

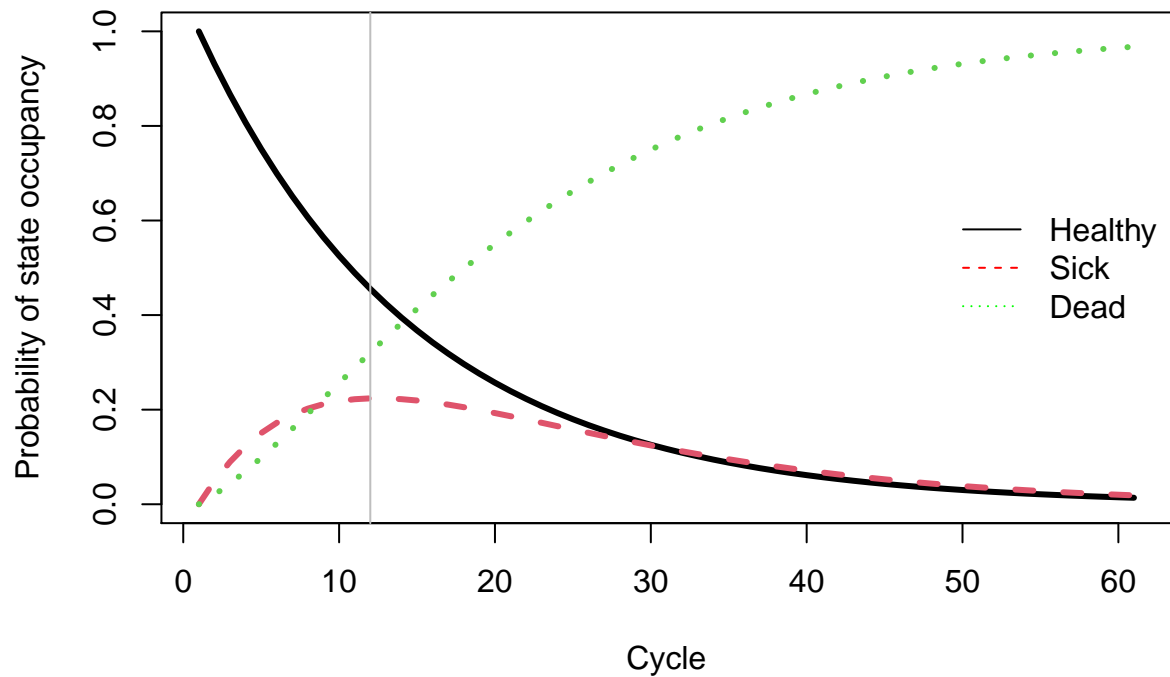
```

matplot(m_M_SoC, type = 'l',
        ylab = "Probability of state occupancy",
        xlab = "Cycle",
        main = "Cohort Trace - standard of care", lwd = 3) # create a plot of the data
legend("right", v_n, col = c("black", "red", "green"),
       lty = 1:3, bty = "n") # add a legend to the graph

abline(v = which.max(m_M_SoC[, "Sick"]), col = "gray") # plot a vertical line that helps identify

```

## Cohort Trace – standard of care

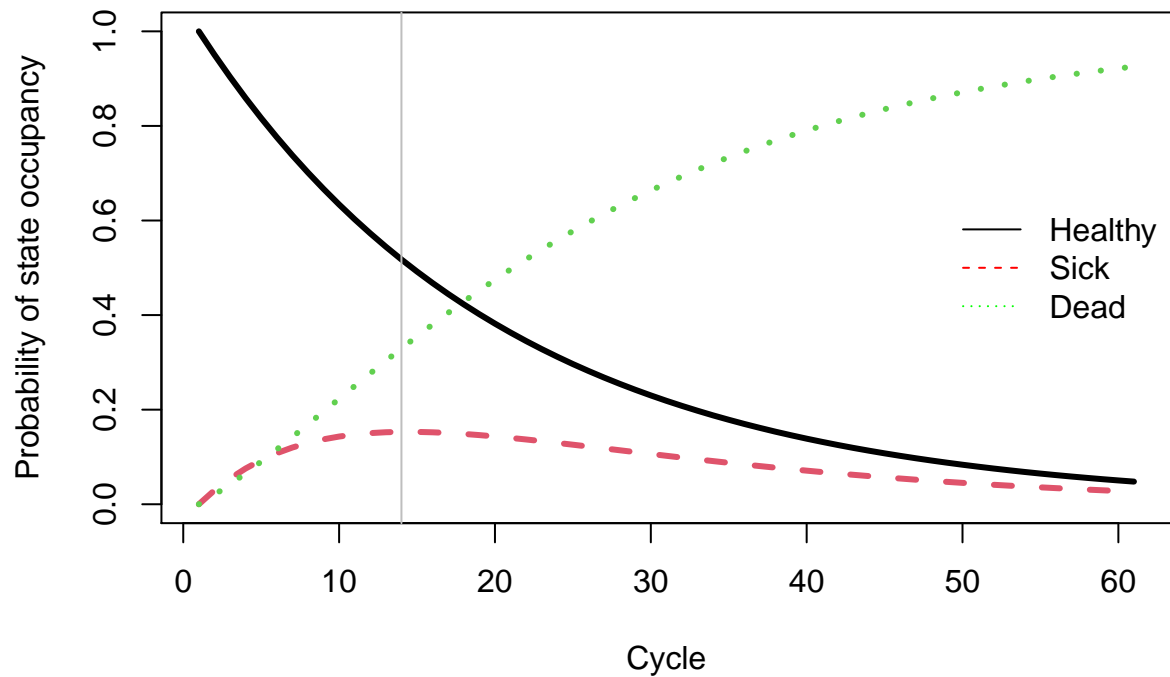


Treatment:

```
matplot(m_M_trt, type = 'l',
        ylab = "Probability of state occupancy",
        xlab = "Cycle",
        main = "Cohort Trace - treatment", lwd = 3)      # create a plot of the data
legend("right", v_n, col = c("black", "red", "green"),
        lty = 1:3, bty = "n")                          # add a legend to the graph

abline(v = which.max(m_M_trt[, "Sick"]), col = "gray") # plot a vertical line that helps identifying
```

## Cohort Trace – treatment



## 06.2 Overall Survival (OS)

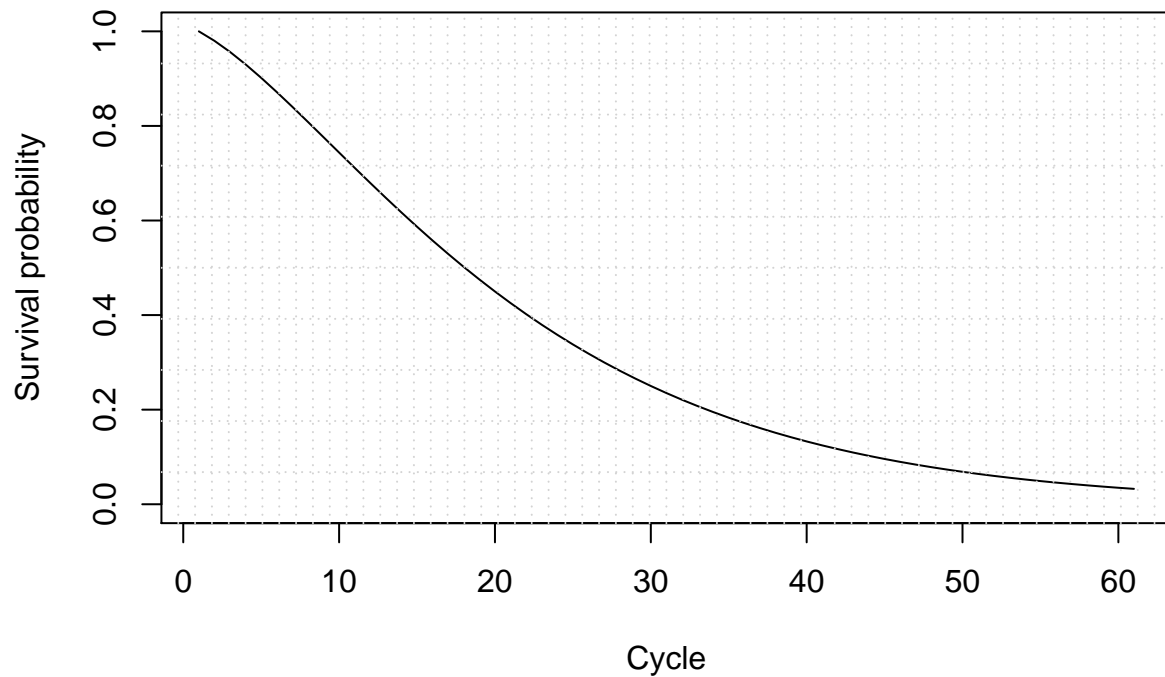
Standard of Care:

```
v_os_SoC <- 1 - m_M_SoC[, "Dead"] # calculate the overall survival (OS) probability
v_os_SoC <- rowSums(m_M_SoC[, 1:2]) # alternative way of calculating the OS probability

plot(v_os_SoC, type = 'l',
     ylim = c(0, 1),
     ylab = "Survival probability",
     xlab = "Cycle",
     main = "Overall Survival - Standard of Care") # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
     equilogs = TRUE)
```

## Overall Survival – Standard of Care



Treatment:

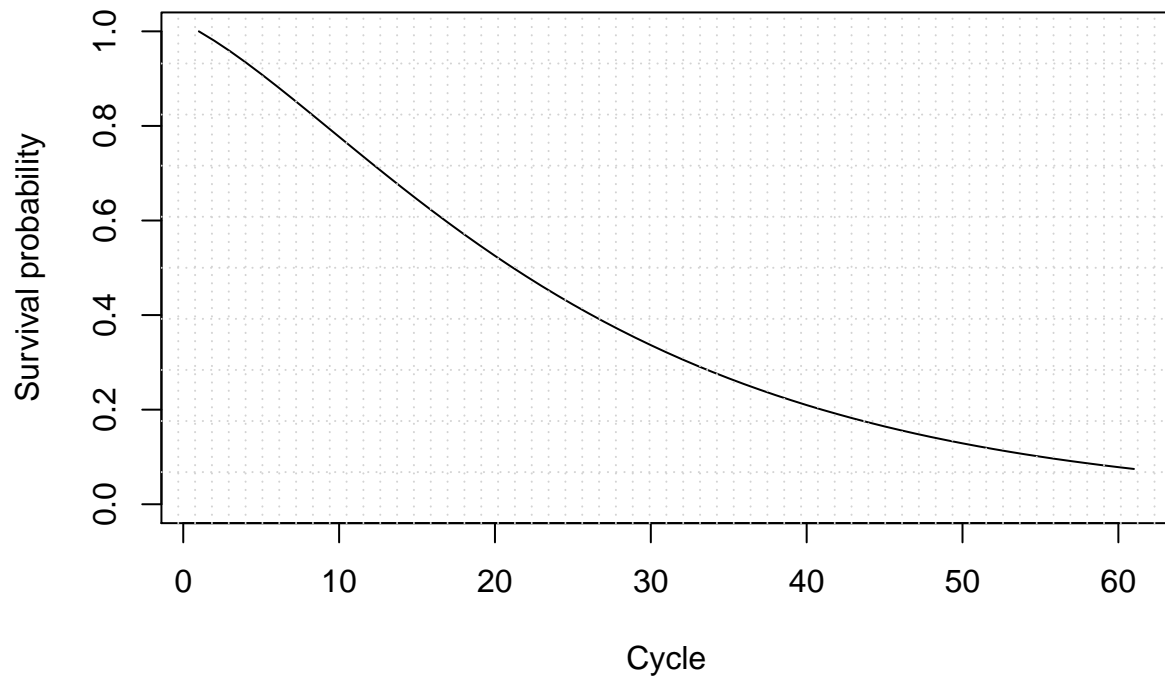
```
v_os_trt <- 1 - m_M_trt[, "Dead"]      # calculate the overall survival (OS) probability
v_os_trt <- rowSums(m_M_trt[, 1:2])    # alternative way of calculating the OS probability

plot(v_os_trt, type = 'l',
     ylim = c(0, 1),
     ylab = "Survival probability",
     xlab = "Cycle",
     main = "Overall Survival - Treatment") # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
     equilogs = TRUE)
```



## Overall Survival – Treatment



### 06.2.1 Life Expectancy (LE)

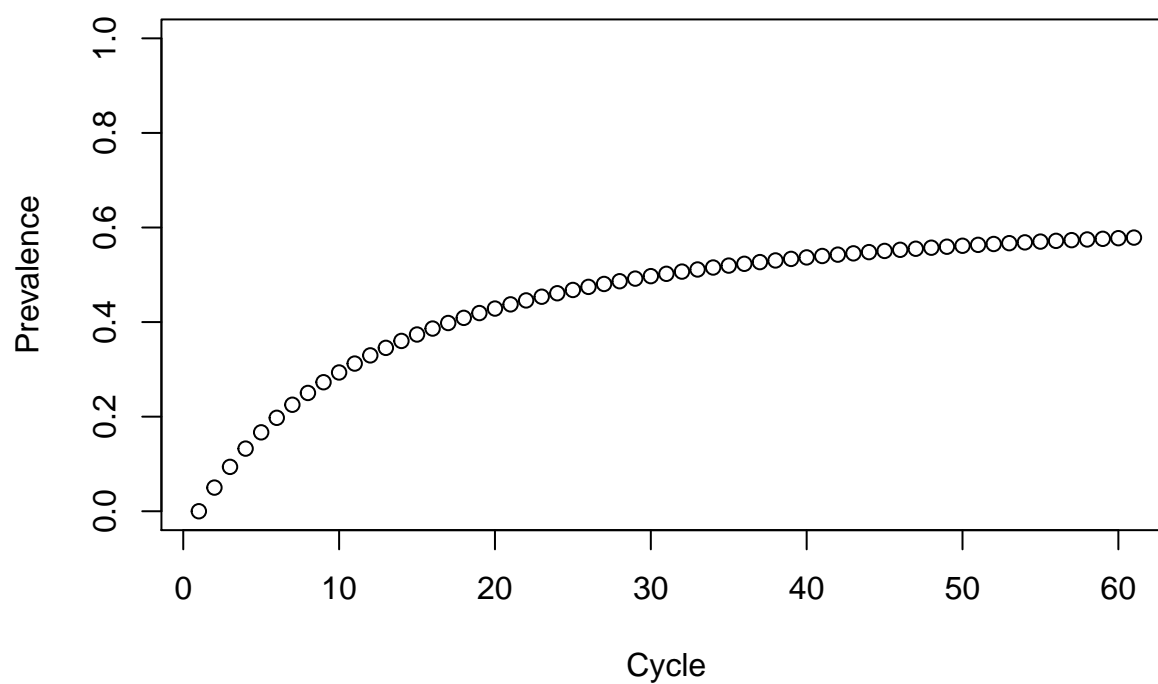
```
v_le_SoC <- sum(v_os_SoC) # summing probability of OS over time (i.e. life expectancy)
v_le_trt <- sum(v_os_trt) # summing probability of OS over time (i.e. life expectancy), treatment
```

### 06.3 Disease prevalence

Standard of Care:

```
v_prev_SoC <- m_M_SoC[, "Sick"]/v_os_SoC
plot(v_prev_SoC,
     ylim = c(0, 1),
     ylab = "Prevalence",
     xlab = "Cycle",
     main = "Disease prevalence - Standard of care")
```

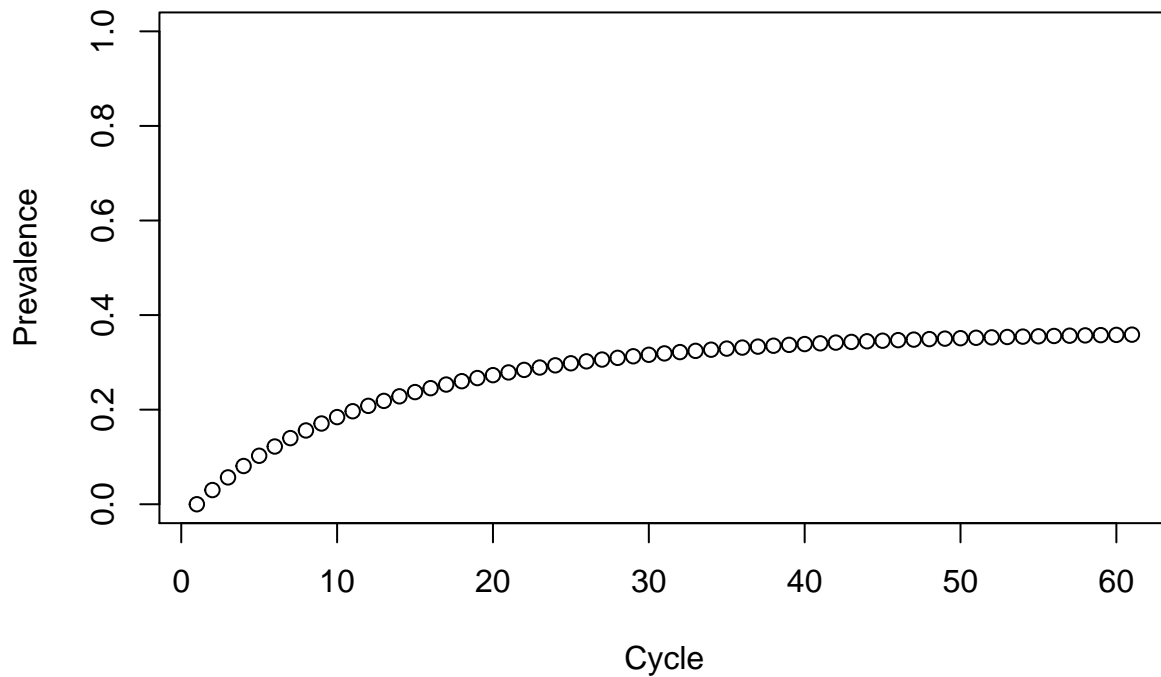
## Disease prevalence – Standard of care



Treatment:

```
v_prev_trt <- m_M_trt[, "Sick"]/v_os_trt
plot(v_prev_trt,
     ylim = c(0, 1),
     ylab = "Prevalence",
     xlab = "Cycle",
     main = "Disease prevalence - Treatment")
```

## Disease prevalence – Treatment



## 07 Compute Cost-Effectiveness Outcomes

### 07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
v_tc_SoC <- m_M_SoC %*% c(c_H, c_S, c_D) # Standard of Care
v_tc_trt <- m_M_trt %*% c(c_H, c_S, c_D) # Treatment
v_tc_trt[1] <- v_tc_trt[1] + c_trt
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
v_tu_SoC <- m_M_SoC %*% c(u_H, u_S, u_D) # Standard of Care
v_tu_trt <- m_M_trt %*% c(u_H, u_S, u_D) # Treatment
```

### 07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights
tc_d_SoC <- t(v_tc_SoC) %*% v_dwc # Standard of Care
tc_d_trt <- t(v_tc_trt) %*% v_dwc # Treatment
# Discount QALYs by multiplying the QALYs vector with discount weights
```

```

tu_d_SoC <- t(v_tu_SoC) %*% v_dwe # Standard of Care
tu_d_trt <- t(v_tu_trt) %*% v_dwe # Treatment

# store them into a vector
v_tc_d <- c(tc_d_SoC, tc_d_trt)
v_tu_d <- c(tu_d_SoC, tu_d_trt)

# Dataframe with discounted costs and effectiveness
df_ce <- data.frame(Strategy = v_names_str,
                    Cost      = v_tc_d,
                    Effect    = v_tu_d)

df_ce

```

```

##           Strategy      Cost    Effect
## 1 Standard of Care  8043.139  10.25087
## 2           Treatment 16028.490  11.73928

```

### 07.3 Compute ICERs of the Markov model

```

df_cea <- calculate_icers(cost      = df_ce$Cost,
                          effect    = df_ce$Effect,
                          strategies = df_ce$Strategy)

df_cea

```

```

##           Strategy      Cost    Effect Inc_Cost Inc_Effect      ICER Status
## 1 Standard of Care  8043.139  10.25087      NA      NA      NA      ND
## 2           Treatment 16028.490  11.73928 7985.351  1.488415 5365.002      ND

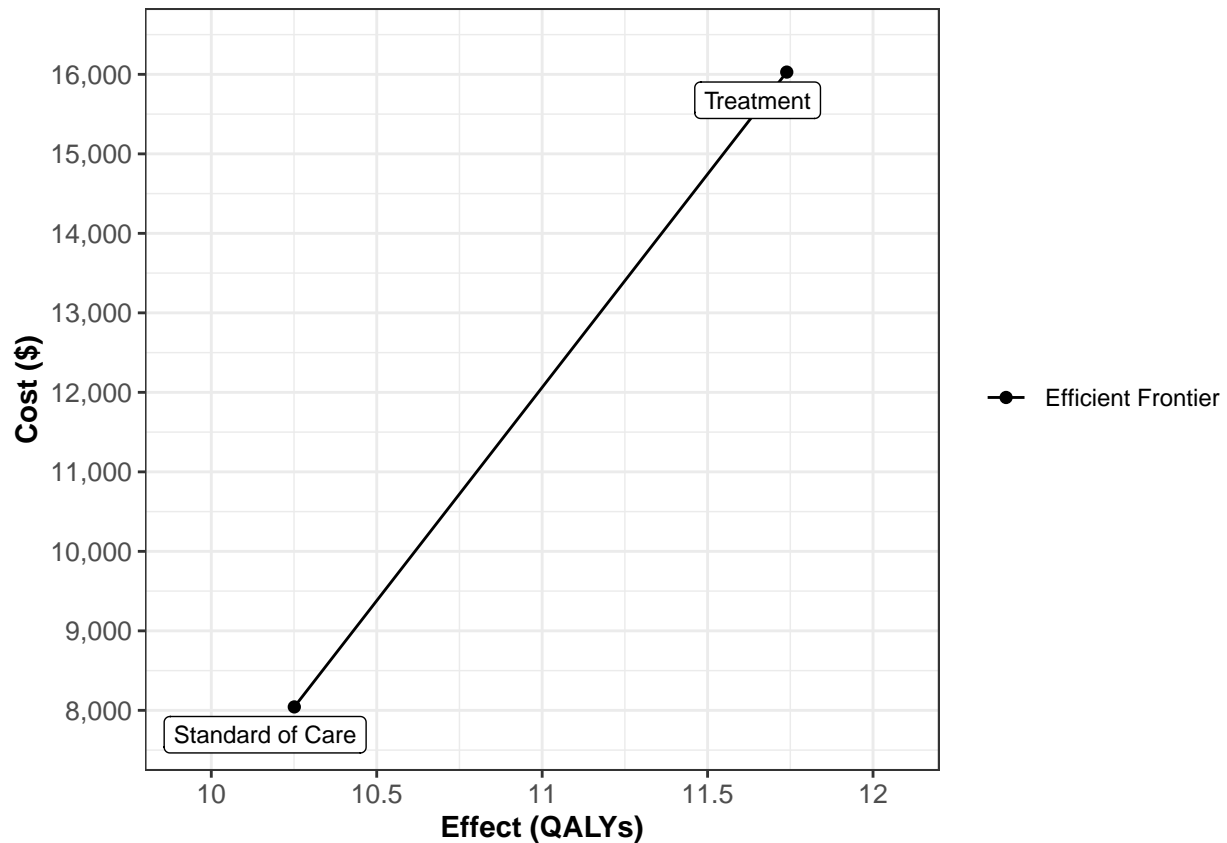
```

### 07.4 Plot frontier of the Markov model

```

plot(df_cea, effect_units = "QALYs", xlim = c(10, 12))

```



*# note: you need to adjust the xlim values to values that are covering the range of effect values in your analysis*

## 08 Probabilistic Sensitivity Analysis (PSA)

### 08.1 List of input parameters

Create list `l_params_all` with all input probabilities, cost and utilities.

```
l_params_all <- as.list(data.frame(
  p_HD = 0.02, # probability of dying when healthy
  p_HS = 0.05, # probability of becoming sick when healthy, conditioned on not dying
  p_HS_trt = 0.03, # probability of becoming sick when healthy, conditioned on not dying
  p_SD = 0.1, # probability of dying when sick
  c_H = 400, # cost of one cycle in healthy state
  c_S = 1000, # cost of one cycle in sick state
  c_D = 0, # cost of one cycle in dead state
  c_trt = 8000, # one-time cost of treatment (at first cycle)
  u_H = 0.8, # utility when healthy
  u_S = 0.5, # utility when sick
  u_D = 0, # utility when dead
  d_e = 0.03, # discount factor for effectiveness
  d_c = 0.03 # discount factor for costs
))
```

```
# store the parameter names into a vector
v_names_params <- names(l_params_all)
```

## 08.2 Load Sick-Sicker Markov model function

```
source("Functions_markov_3state.R")
# Test function
calculate_ce_out(l_params_all)
```

```
##           Strategy      Cost   Effect      NMB
## 1 Standard of Care 8043.139 10.25087 94465.51
## 2           Treatment 16028.490 11.73928 101364.32
```

## 08.3 Generate PSA datasets

```
# Function to generate PSA input dataset
gen_psa <- function(n_sim = 1000, seed = 071818){
  set.seed(seed) # set a seed to be able to reproduce the same results
  df_psa <- data.frame(
    # Transition probabilities (per cycle)
    # probability to become sick when healthy
    p_HS = rbeta(n_sim, shape1 = 24, shape2 = 450),
    p_HS_trt = rbeta(n_sim, shape1 = 9, shape2 = 281), # under treatment
    # probability of dying when healthy
    p_HD = rbeta(n_sim, shape1 = 16, shape2 = 767),
    # probability of dying when sick
    p_SD = rbeta(n_sim, shape1 = 22.4, shape2 = 201.6),

    # Cost vectors with length n_sim
    # cost of remaining one cycle in state H
    c_H = rgamma(n_sim, shape = 16, scale = 25),
    # cost of remaining one cycle in state S1
    c_S = rgamma(n_sim, shape = 100, scale = 10),
    # cost of being in the death state
    c_D = 0,
    # cost of treatment (per cycle)
    c_trt = rgamma(n_sim, shape = 64, scale = 125),

    # Utility vectors with length n_sim
    # utility when healthy
    u_H = rbeta(n_sim, shape1 = 50.4, shape2 = 12.6),
    # utility when sick
    u_S = rbeta(n_sim, shape1 = 49.5, shape2 = 49.5),
    # utility when dead
    u_D = 0
  )
  return(df_psa)
}
# Try it
gen_psa(10)
```

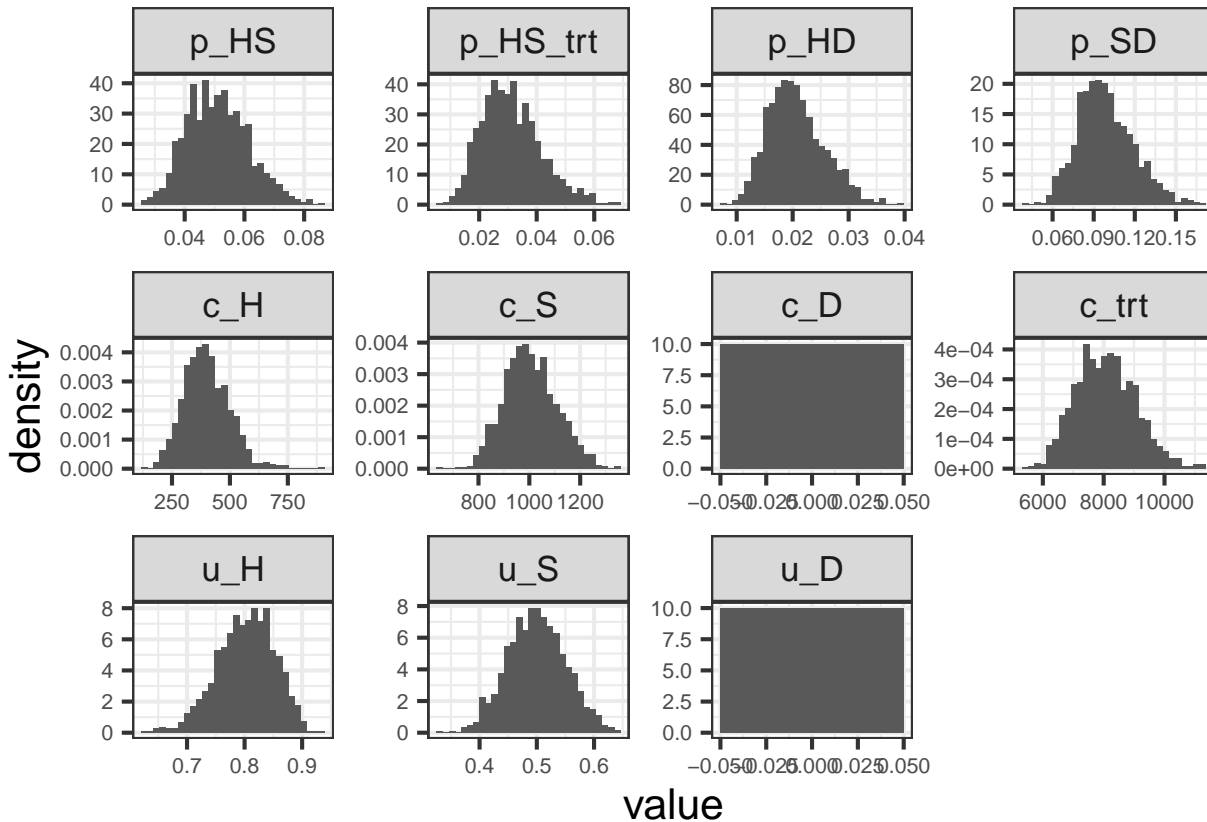
```
##      p_HS  p_HS_trt    p_HD    p_SD    c_H    c_S c_D    c_trt
## 1  0.05116365 0.02717469 0.02650780 0.09350365 331.7253 1001.3478 0 6217.035
## 2  0.04095451 0.01181545 0.02787410 0.15823599 535.2239 995.9279 0 9377.706
## 3  0.05334926 0.01972404 0.01561002 0.12357583 334.2034 955.0140 0 6591.331
## 4  0.03627100 0.03901602 0.02620191 0.08771020 352.7561 990.4764 0 8652.337
## 5  0.04782122 0.02128019 0.01998096 0.10799984 260.4642 943.7245 0 8555.065
## 6  0.07206924 0.02272066 0.01521342 0.12685251 291.1215 983.1453 0 8604.577
## 7  0.04803791 0.04457119 0.01499307 0.08911761 483.8274 1050.5295 0 9942.503
## 8  0.04335723 0.02882206 0.02131098 0.05814786 541.4731 864.3322 0 6018.085
## 9  0.05302297 0.03409499 0.01709267 0.15922549 551.1535 1080.4473 0 7571.225
## 10 0.03096171 0.01553948 0.01983932 0.10406523 315.7027 984.6521 0 7875.281
##      u_H    u_S u_D
## 1  0.8559721 0.4815761 0
## 2  0.7783084 0.5349337 0
## 3  0.8628224 0.5227023 0
## 4  0.8968823 0.4871518 0
## 5  0.8179546 0.5294793 0
## 6  0.6717953 0.5249675 0
## 7  0.8177386 0.5600215 0
## 8  0.8145828 0.5243320 0
## 9  0.8153981 0.5503887 0
## 10 0.8835447 0.5837644 0
```

```
# Number of simulations
n_sim <- 1000

# Generate PSA input dataset
df_psa_input <- gen_psa(n_sim = n_sim)
# First six observations
head(df_psa_input)
```

```
##      p_HS  p_HS_trt    p_HD    p_SD    c_H    c_S c_D    c_trt
## 1  0.05116365 0.01954245 0.02621456 0.13853135 307.8380 899.5153 0 6875.154
## 2  0.04095451 0.04346716 0.01760834 0.13075427 466.9600 1066.1617 0 8755.292
## 3  0.05334926 0.03357981 0.02404573 0.08454761 235.2890 955.0145 0 6582.810
## 4  0.03627100 0.03806155 0.02716409 0.10457346 306.5100 789.6969 0 7027.446
## 5  0.04782122 0.03737024 0.01716697 0.14474739 535.1188 868.0570 0 5661.605
## 6  0.07206924 0.04257367 0.01710648 0.12289879 353.6715 991.6205 0 10960.742
##      u_H    u_S u_D
## 1  0.7965014 0.4473598 0
## 2  0.7659582 0.4644020 0
## 3  0.7593770 0.4215045 0
## 4  0.8338376 0.5052819 0
## 5  0.8798517 0.5181703 0
## 6  0.7306958 0.5905503 0
```

```
# Histogram of parameters
ggplot(melt(df_psa_input, variable.name = "Parameter"), aes(x = value)) +
  facet_wrap(~Parameter, scales = "free") +
  geom_histogram(aes(y = ..density..)) +
  theme_bw(base_size = 16) +
  theme(axis.text = element_text(size=8))
```



```
# Initialize dataframes with PSA output
# Dataframe of costs
df_c <- as.data.frame(matrix(0,
                             nrow = n_sim,
                             ncol = n_str))
colnames(df_c) <- v_names_str
# Dataframe of effectiveness
df_e <- as.data.frame(matrix(0,
                             nrow = n_sim,
                             ncol = n_str))
colnames(df_e) <- v_names_str
```

## 08.4 Conduct probabilistic sensitivity analysis

```
# Run Markov model on each parameter set of PSA input dataset
for(i in 1:n_sim){
  l_out_temp <- calculate_ce_out(df_psa_input[i, ])
  df_c[i, ] <- l_out_temp$Cost
  df_e[i, ] <- l_out_temp$Effect
  # Display simulation progress
  if(i/(n_sim/10) == round(i/(n_sim/10), 0)) { # display progress every 10%
    cat('\r', paste(i/n_sim * 100, "% done", sep = " "))
  }
}
```



```
## 10 % done 20 % done 30 % done 40 % done 50 % done 60 % done 70 % done 80 % done 90 % done 100 % done
```

### 08.4.1 Create PSA object for dampack

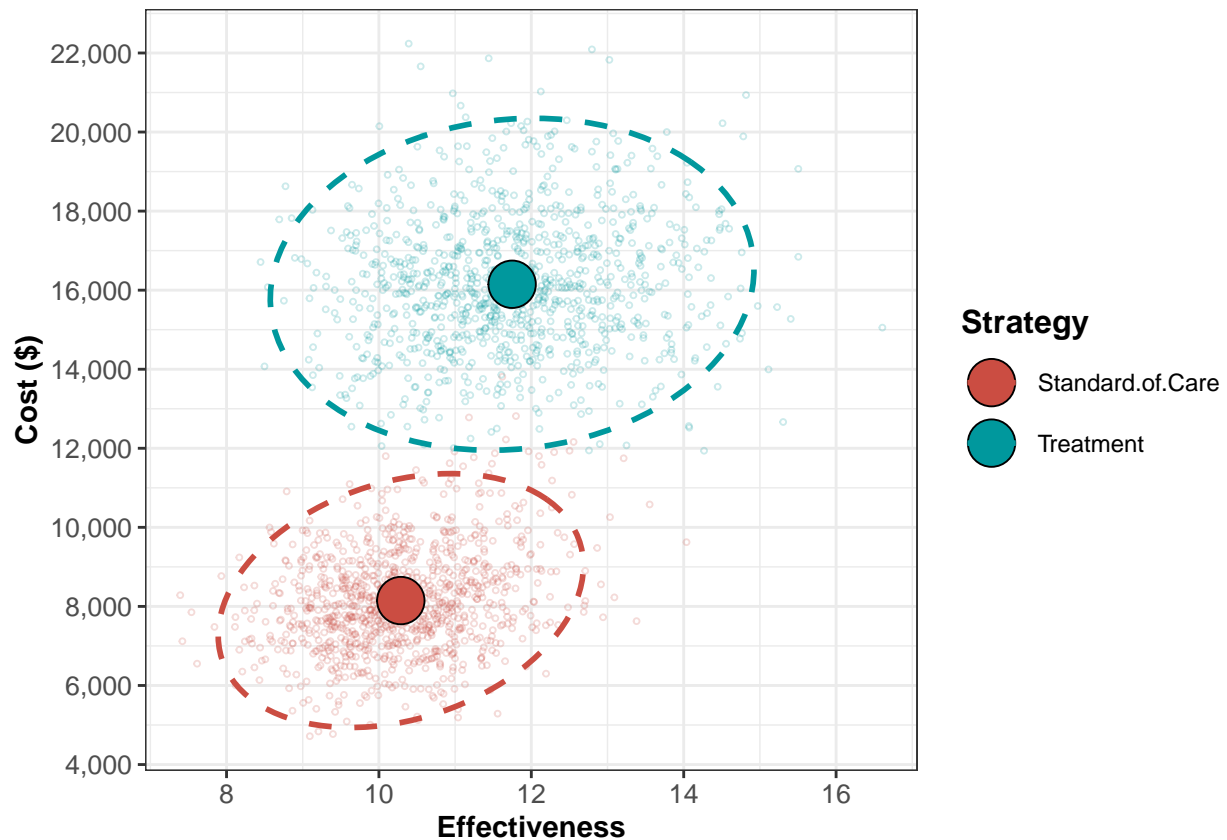
```
l_psa <- make_psa_obj(cost      = df_c,  
                      effectiveness = df_e,  
                      parameters  = df_psa_input,  
                      strategies  = v_names_str)
```

Vector with willingness-to-pay (WTP) thresholds.

```
v_wtp <- seq(0, 5000, by = 1000)
```

### 08.4.2 Cost-Effectiveness Scatter plot

```
plot(l_psa)
```



### 08.4.3 Conduct CEA with probabilistic output

```
# Compute expected costs and effects for each strategy from the PSA
df_out_ce_psa <- summary(l_psa)
```

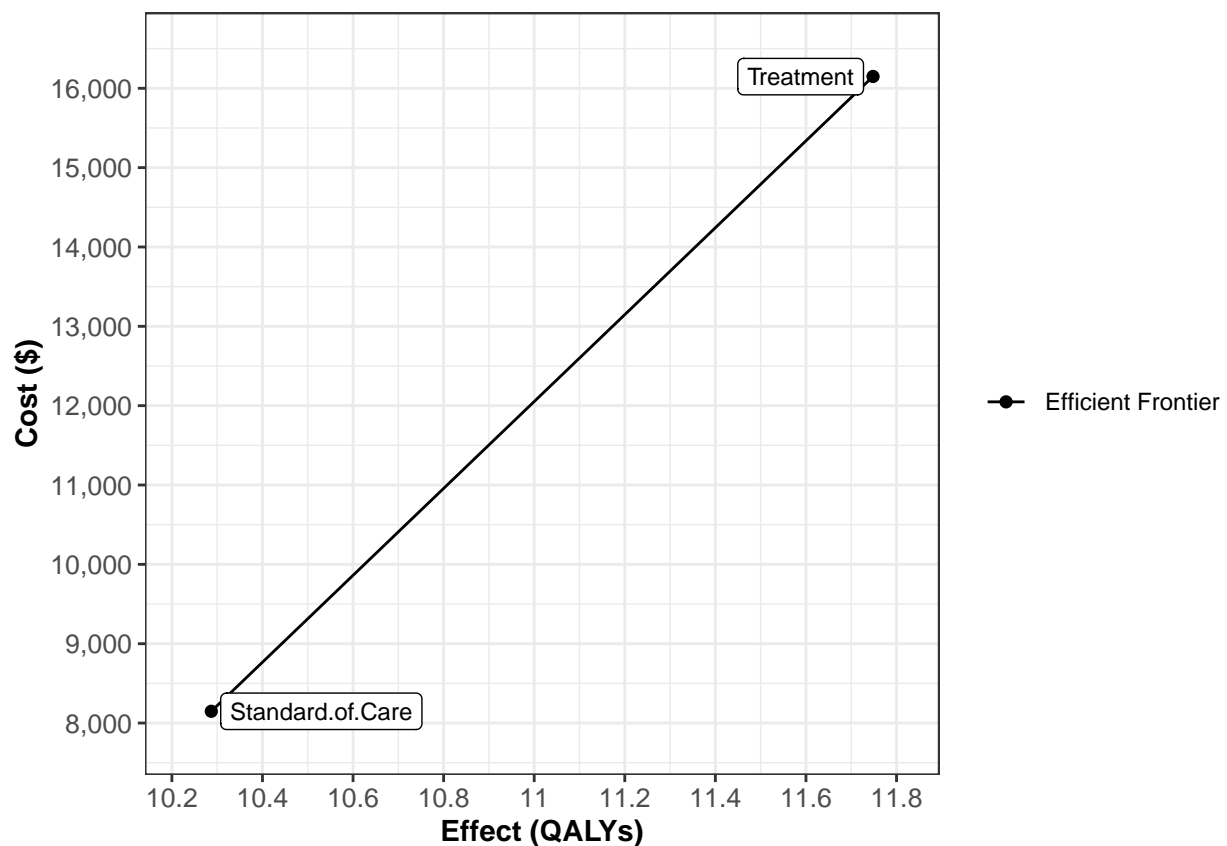
```
# Calculate incremental cost-effectiveness ratios (ICERs)
df_cea_psa <- calculate_icers(cost      = df_out_ce_psa$meanCost,
                             effect    = df_out_ce_psa$meanEffect,
                             strategies = df_out_ce_psa$Strategy)

df_cea_psa
```

##	Strategy	Cost	Effect	Inc_Cost	Inc_Effect	ICER	Status
## 1	Standard.of.Care	8148.004	10.28706	NA	NA	NA	ND
## 2	Treatment	16149.044	11.74808	8001.04	1.461028	5476.307	ND

#### 08.4.4 Plot cost-effectiveness frontier

```
plot(df_cea_psa)
```

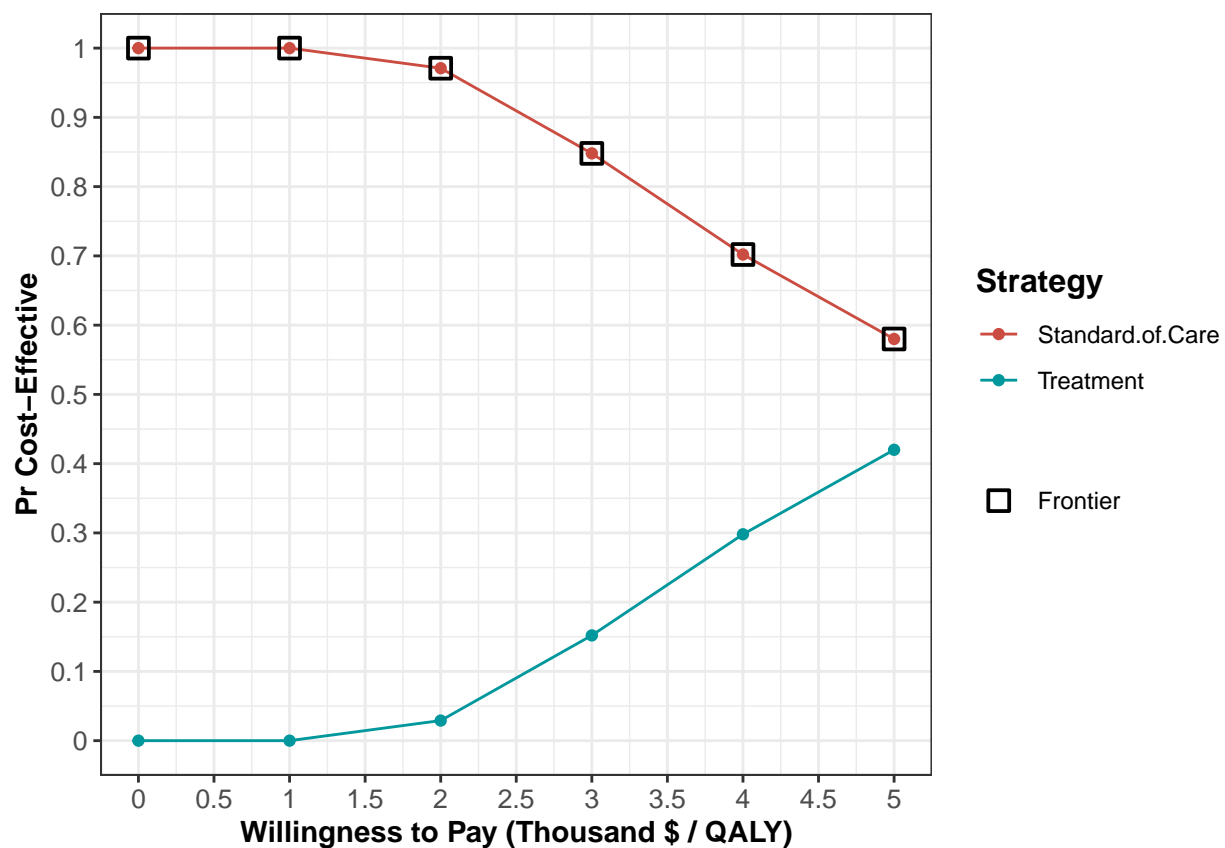


#### 08.4.5 Cost-effectiveness acceptability curves (CEACs) and frontier (CEAF)

```
ceac_obj <- ceac(wtp = v_wtp, psa = l_psa)
# Regions of highest probability of cost-effectiveness for each strategy
summary(ceac_obj)
```

```
##   range_min range_max cost_eff_strat
## 1         0      5000 Standard.of.Care
```

```
# CEAC & CEAF plot
plot(ceac_obj)
```



#### 08.4.6 Expected Loss Curves (ELCs)

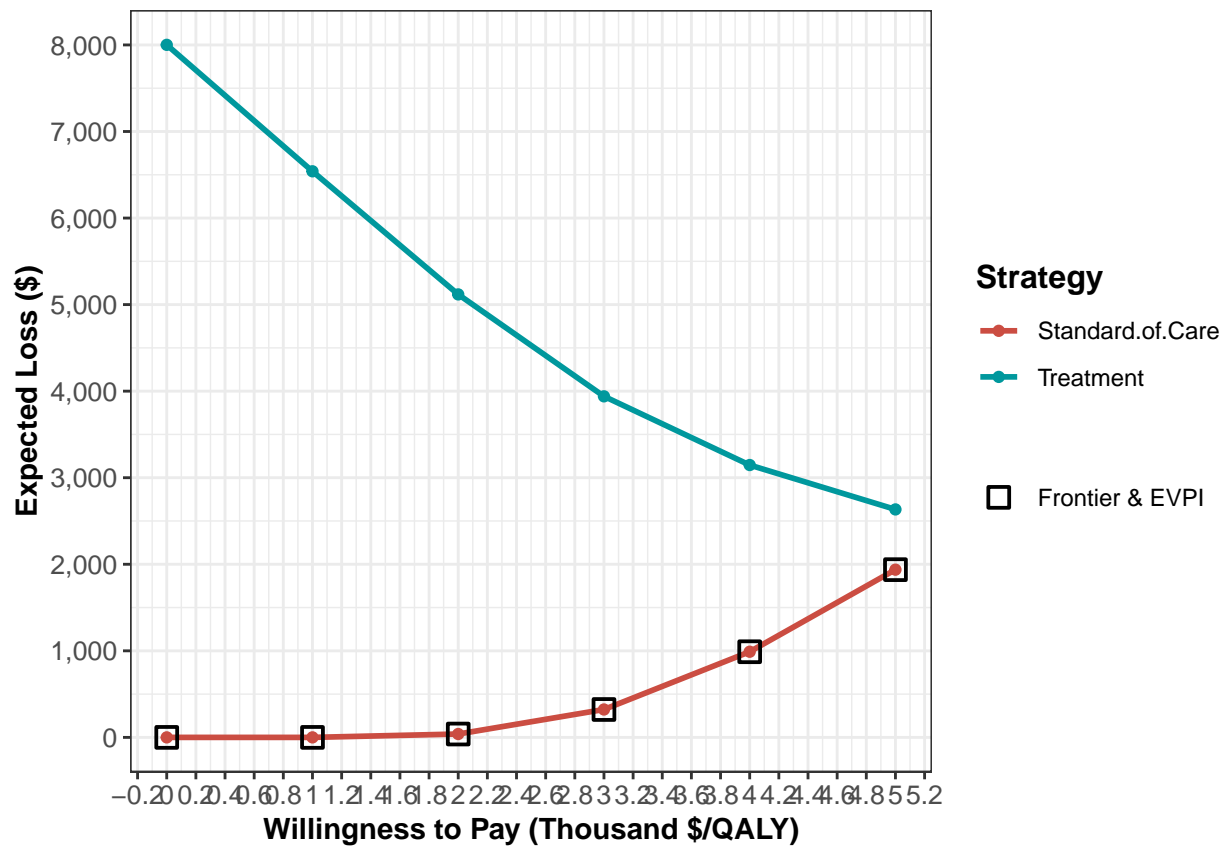
The expected loss is the the quantification of the foregone benefits when choosing a suboptimal strategy given current evidence.

```
elc_obj <- calc_exp_loss(wtp = v_wtp, psa = l_psa)
elc_obj
```

```
##   WTP      Strategy Expected_Loss On_Frontier
## 1    0 Standard.of.Care    0.00000      TRUE
## 2    0      Treatment    8001.03979     FALSE
## 3 1000 Standard.of.Care    0.00000      TRUE
```

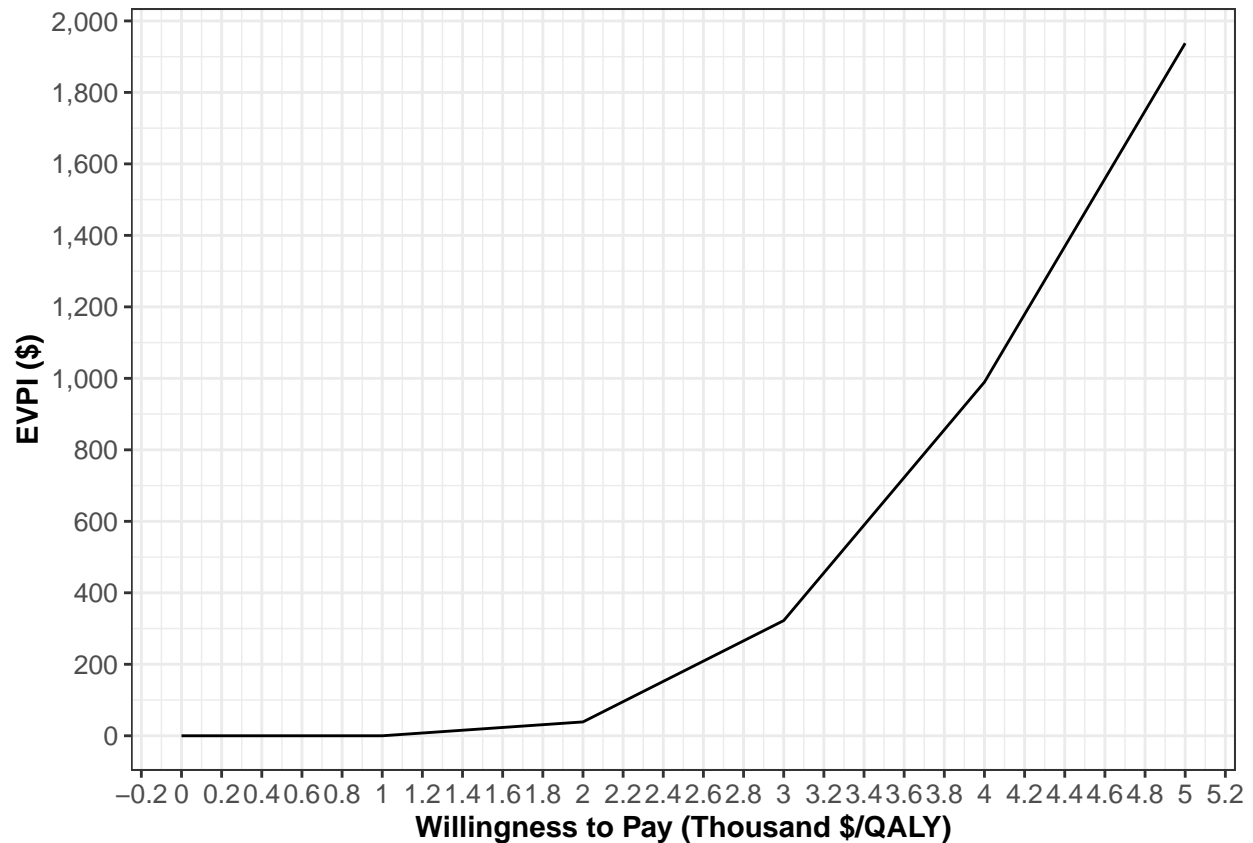
```
## 4 1000 Treatment 6540.01147 FALSE
## 5 2000 Standard.of.Care 38.76766 TRUE
## 6 2000 Treatment 5117.75081 FALSE
## 7 3000 Standard.of.Care 322.26595 TRUE
## 8 3000 Treatment 3940.22079 FALSE
## 9 4000 Standard.of.Care 989.52884 TRUE
## 10 4000 Treatment 3146.45536 FALSE
## 11 5000 Standard.of.Care 1937.60524 TRUE
## 12 5000 Treatment 2633.50344 FALSE
```

```
# ELC plot
plot(elc_obj, log_y = FALSE)
```



#### 08.4.7 Expected value of perfect information (EVPI)

```
evpi <- calc_evpi(wtp = v_wtp, psa = l_psa)
# EVPI plot
plot(evpi, effect_units = "QALY")
```



## 09 Using R package hesim

```
p_load("hesim")
```

### 09.1 Model setup

Here we define target population and intervention strategies.

We have one representative patient here of age 25, we can think of this as a cohort of homogenous patients instead of one individual patient.

```
# define strategies
strategies <- data.frame(
  strategy_id = 1:n_str,
  strategy_name = v_names_str
)
# define patient cohort
patients <- data.frame(
  patient_id = 1,
  age = 25
)
# create dataset with
```

```
hesim_dat <- hesim_data(
  strategies = strategies,
  patients   = patients
)
hesim_dat
```

```
## $strategies
##   strategy_id  strategy_name
## 1           1 Standard of Care
## 2           2      Treatment
##
## $patients
##   patient_id age
## 1           1  25
##
## attr("class")
## [1] "hesim_data"
```

## 09.2 parameters

```
params <- list(
  # medical costs
  c_medical = c(Healthy = c_H, Sick = c_S),
  c_medical_se = c(Healthy = 100, Sick = 100),
  # treatment costs (embedded in medical costs since only those who are sick get treated)
  c_trt = c_trt,
  # state utilities
  u_mean = c(Healthy = u_H, Sick = u_S),
  u_se = c(Healthy = 0.05, Sick = 0.05)
)
```

## 09.3 PSA setup

```
rng_def()
```

```
rng_def <- define_rng({
  list( # Parameters to return
    # medical costs
    c_medical = gamma_rng(mean = c_medical, sd = c_medical_se),
    c_trt      = gamma_rng(mean = c_trt,    sd = 1000),
    # state utilities
    u = beta_rng(mean = u_mean, sd = u_se)
  )
}, n = 1000)
```

## 09.4 Transform parameters

```
input_data <- hesim::expand(hesim_dat, by = c("strategies", "patients"))
head(input_data)
```

```
##      strategy_id patient_id    strategy_name age
## 1:              1           1 Standard of Care  25
## 2:              2           1      Treatment  25
```

The function `define_tparams()` returns:

- `tpmatrix`: The transition probability matrix
- `utility`: Utility assigned to each health state
- `costs`: Costs assigned to each health state or each cost category

Your task: write mathematical expressions

The function: automatically loops over PSA iterations (running the model on each sampled parameter set)

```
tparams_def <- define_tparams({
  # treatment reduces the risk of getting sick
  rr <- ifelse(strategy_name == "Standard of Care", 1, p_HS_trt / p_HS) # relative risk

  list(
    tpmatrix = tpmatrix(
      (1 - p_HD) * (1 - p_HS * rr), (1 - p_HD) * (p_HS * rr), p_HD,
      0, C, p_SD,
      0, 0, 1
    ),

    utility = u,
    costs = list(
      treatment = ifelse(strategy_name == "Standard of Care", 0, c_trt),
      medical    = c_medical
    )
  )
})
```

## 09.5 Simulation

Construct model:

```
mod_def <- define_model(tparams_def = tparams_def,
                        rng_def      = rng_def,
                        params       = params)
```

Initialize-model:

```
cost_args <- list(
  treatment = list(method = "starting"),
  medical    = list(method = "wlos")
)
econmod <- create_CohortDtstm(mod_def, input_data, cost_args = cost_args)
```

Simulate outcomes:

```
econmod$sim_stateprobs(n_cycles = n_t)
head(econmod$stateprobs_)
```

```
##      sample strategy_id patient_id grp_id state_id t      prob
## 1:      1           1           1      1      1 0 1.0000000
## 2:      1           1           1      1      1 1 0.9310000
## 3:      1           1           1      1      1 2 0.8667610
## 4:      1           1           1      1      1 3 0.8069545
## 5:      1           1           1      1      1 4 0.7512746
## 6:      1           1           1      1      1 5 0.6994367
```

```
econmod$sim_qalys(dr = d_e, lys = TRUE, integrate_method = "riemann_right")
head(econmod$qalys_)
```

```
##      sample strategy_id patient_id grp_id state_id  dr    qalys      lys
## 1:      1           1           1      1      1 0.03 6.484607  9.339850
## 2:      1           1           1      1      2 0.03 1.841271  3.861427
## 3:      1           2           1      1      1 0.03 8.199613 11.809992
## 4:      1           2           1      1      2 0.03 1.361197  2.854639
## 5:      2           1           1      1      1 0.03 8.063655  9.339850
## 6:      2           1           1      1      2 0.03 1.849052  3.861427
```

```
econmod$sim_costs(dr = d_c, integrate_method = "riemann_right")
head(econmod$costs_)
```

```
##      sample strategy_id patient_id grp_id state_id  dr category    costs
## 1:      1           1           1      1      1 0.03 treatment    0.000
## 2:      1           1           1      1      2 0.03 treatment    0.000
## 3:      1           2           1      1      1 0.03 treatment 7819.843
## 4:      1           2           1      1      2 0.03 treatment    0.000
## 5:      2           1           1      1      1 0.03 treatment    0.000
## 6:      2           1           1      1      2 0.03 treatment    0.000
```

## 09.6 Cost-effectiveness analysis

```
ce_sim <- econmod$summarize()
cea_pw_out <- cea_pw(ce_sim,
  comparator = 1,
  dr_qalys = 0.03, dr_costs = 0.03,
  k = seq(0, 5000, 1000))

## @knitr icer
icer_tbl(cea_pw_out, colnames = strategies$strategy_name)
```

```
##      Standard of Care Treatment
## Incremental QALYs  "-"          "1.47 (1.21, 1.72)"
## Incremental costs  "-"          "7,990 (6,070, 10,233)"
## Incremental NMB    "-"          "65,685 (52,214, 77,821)"
## ICER              "-"          "5,422"
## Conclusion         "-"          "Cost-effective"
```



## 10 Overview of **hesim**

### Advantages:

- Easy to build models without having to program the complete model structure (easier for novice modelers).
- A lot of the modeling code are implemented for you in the back end.
- Suitable for modelers who are not familiar with R programming and functionality.
- Code written in C++ in the back end, which offers enhanced computational speed.

### Disadvantages:

- Its rigid function structure inhibits its ability tweak models or incorporate more complex model components (e.g. tunnel states, transition rewards).
- Does not provide the option for running deterministic analysis or one-way and two-way sensitivity analyses.
- Does not provide the ability to capture information about the specific transitions among health states (transition dynamics).
- Does not provide the ability to easily compute epidemiological outcomes.
- Does not allow costs to be applied to certain health states (at least not easily).

## References

```
citation("hesim")
```

```
##
## To cite package 'hesim' in publications use:
##
##   Devin Incerti and Jeroen P. Jansen (2020). hesim: Health-Economic
##   Simulation Modeling and Decision Analysis. R package version 0.4.1.
##   https://CRAN.R-project.org/package=hesim
##
## A BibTeX entry for LaTeX users is
##
##   @Manual{,
##     title = {hesim: Health-Economic Simulation Modeling and Decision Analysis},
##     author = {Devin Incerti and Jeroen P. Jansen},
##     year = {2020},
##     note = {R package version 0.4.1},
##     url = {https://CRAN.R-project.org/package=hesim},
##   }
```