SA: Simple 3-state Markov model in R

The DARTH workgroup

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Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001. 07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("here", "dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "truncnorm",
# install_github("DARTH-git/dampack", force = TRUE) Uncomment if there is a newer version
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/dampack", "DARTH-git/darthtools")
```

02 Load functions

u D <- 0

```
# No function needed
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("Standard of Care", "Treatment")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead") # state names</pre>
n_states <- length(v_n) # number of states
n t <- 60
                                     # number of cycles
v_{init} \leftarrow c(1, 0, 0)
                                     # initial cohort distribution
\# Transition probabilities
p HD < -0.02
                                      # probability of dying when healthy
                                      # probability of becoming sick when healthy, conditioned on not d
p_HS <- 0.05
p_HS_trt <- 0.03
                                      # probability of becoming sick when healthy, conditioned on not d
p_SD <- 0.1
                                      # probability of dying when sick
# Costs and utilities
c_H <- 400
                                      # cost of one cycle in healthy state
c_S <- 1000
                                     # cost of one cycle in sick state
c_D <- 0
                                      # cost of one cycle in dead state
c_trt <- 800
                                      # cost of treatment (per cycle)
                                      # utility when healthy
u_H <- 0.8
u_S <- 0.5
                                      # utility when sick
```

utility when dead

Draw the state-transition cohort model

04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability matrix

Fill in the transition probability matrix:

```
# from Healthy
m_P["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS)</pre>
m_P["Healthy", "Sick"] <- (1 - p_HD) * p_HS
m_P["Healthy", "Dead"] <- p_HD</pre>
# from Sick
m_P["Sick", "Sick"] <- 1 - p_SD</pre>
m_P["Sick", "Dead"] <- p_SD</pre>
# from Dead
m_P["Dead", "Dead"] <- 1</pre>
# Under treatment
m_P_trt <- m_P
m_P_trt["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS_trt)</pre>
m_P_trt["Healthy", "Sick"] <- (1 - p_HD) * p_HS_trt</pre>
# Check that transition probabilities are in [0, 1]
check_transition_probability(m_P, verbose = TRUE)
check_transition_probability(m_P_trt, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(m_P, n_states = n_states, n_cycles = n_t, verbose = TRUE)
check_transition_probability(m_P_trt, verbose = TRUE)
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

Standard of Care:

Treatment:

06.2 Overall Survival (OS)

Standard of Care:

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2])  # alternative way of calculating the OS probability

plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

Treatment:

```
v_os_trt <- 1 - m_M_trt[, "Dead"]  # calculate the overall survival (OS) probability
v_os_trt <- rowSums(m_M_trt[, 1:2])  # alternative way of calculating the OS probability

plot(v_os_trt, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os)  # summing probability of OS over time (i.e. life expectancy)
v_le_trt <- sum(v_os_trt)  # summing probability of OS over time (i.e. life expectancy), treatment</pre>
```

06.3 Disease prevalence

Standard of Care:

Treatment:

```
v_prev_trt <- m_M_trt[, "Sick"]/v_os_trt
plot(v_prev_trt,
    ylim = c(0, 1),
    ylab = "Prevalence",
    xlab = "Cycle",
    main = "Disease prevalence")</pre>
```

07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

07.2 Discounted Mean Costs and QALYs

07.3 Compute ICERs of the Markov model

07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "QALYs", xlim = c(10, 12))
```

08 Deterministic Sensitivity Analysis

08.1 List of input parameters

Create list 1_params_all with all input probabilities, cost and utilities.

```
l_params_all <- as.list(data.frame(</pre>
          = 0.02, # probability of dying when healthy
          = 0.05, # probability of becoming sick when healthy, conditioned on not dying
 p_HS
 p_HS_trt = 0.03, # probability of becoming sick when healthy, conditioned on not dying
          = 0.1, # probability of dying when sick
 p_SD
 c_H
          = 400, # cost of one cycle in healthy state
          = 1000, # cost of one cycle in sick state
 c_S
 c_D
          = 0.
                  # cost of one cycle in dead state
          = 800, # cost of treatment (per cycle)
 c_trt
          = 0.8, # utility when healthy
 u_H
          = 0.5, # utility when sick
 u_S
 u D
                  # utility when dead
          = 0,
 d_e
          = 0.03, # discount factor for effectiveness
          = 0.03 # discount factor for costs
 d_c
))
# store the parameter names into a vector
v_names_params <- names(l_params_all)</pre>
```

08.2 Load Sick-Sicker Markov model function

```
source("Functions_markov_3state.R")
# Test function
calculate_ce_out(1_params_all)
```

08.3 One-way sensitivity analysis (OWSA)

```
options(scipen = 999) # disabling scientific notation in R
# dataframe containing all parameters, their base case values, and the min and
# max values of the parameters of interest
df params owsa <- data.frame(pars = c("c trt", "c S", "u H"),</pre>
                            min = c(300, 500, 0.7), # min parameter values
                            \max = c(1200, 2000, 0.9)
                                                        # max parameter values
                                          = df_params_owsa,
                                                               # dataframe with parameters for OWSA
owsa nmb <- run owsa det(params range
                         params_basecase = l_params_all,
                                                               # list with all parameters
                         nsamp = 100,
                                                              # number of parameter values
                         FUN
                                         = calculate_ce_out, # function to compute outputs
                                      = c("NMB"), # output to do the OWSA on
= v_names_str, # names of the strategies
                         outcomes
                         strategies
                                        = 2000)
                                                              # extra argument to pass to FUN
                         n_wtp
```

08.3.1 Plot OWSA

```
plot(owsa_nmb, txtsize = 10, n_x_ticks = 4,
    facet_scales = "free") +
    theme(legend.position = "bottom")
```

08.3.2 Optimal strategy with OWSA

Only useful if we have more than one strategies to compare.

```
owsa_opt_strat(owsa = owsa_nmb, txtsize = 10)
```

08.3.3 Tornado plot

```
owsa_tornado(owsa = owsa_nmb, txtsize = 11)
```

08.4 Two-way sensitivity analysis (TWSA)

```
nsamp = 40, # number of parameter values

FUN = calculate_ce_out, # function to compute outputs

outcomes = "NMB", # output to do the TWSA on

strategies = v_names_str, # names of the strategies

n_wtp = 2000) # extra argument to pass to FUN
```

08.4.1 Plot TWSA

Only useful if we have more than one strategies to compare.

```
plot(twsa_nmb)
```

09 Probabilistic Sensitivity Analysis (PSA)

```
# Function to generate PSA input dataset
gen_psa <- function(n_sim = 1000, seed = 071818){</pre>
  set.seed(seed) # set a seed to be able to reproduce the same results
  df_psa <- data.frame(</pre>
    # Transition probabilities (per cycle)
    # probability to become sick when healthy
           = rbeta(n_sim, shape1 = 24, shape2 = 450),
   p_HS_trt = rbeta(n_sim, shape1 = 9, shape2 = 281), # under treatment
    # probability of dying when healthy
            = rbeta(n_sim, shape1 = 16, shape2 = 767),
    # probability of dying when sick
           = rbeta(n_sim, shape1 = 22.4, shape2 = 201.6),
   p_SD
    # Cost vectors with length n_sim
    # cost of remaining one cycle in state H
            = rgamma(n_sim, shape = 16, scale = 25),
    # cost of remaining one cycle in state S1
            = rgamma(n_sim, shape = 100, scale = 10),
    # cost of being in the death state
           = 0,
    c_D
    # cost of treatment (per cycle)
    c_{trt} = rgamma(n_{sim}, shape = 64, scale = 12.5),
   # Utility vectors with length n_sim
    # utility when healthy
            = rbeta(n_sim, shape1 = 50.4, shape2 = 12.6),
    # utility when sick
            = rbeta(n_sim, shape1 = 49.5, shape2 = 49.5),
    # utility when dead
   u D
  )
 return(df_psa)
# Try it
gen_psa(10)
```

```
# Number of simulations
n_sim <- 1000
# Generate PSA input dataset
df_psa_input <- gen_psa(n_sim = n_sim)</pre>
# First six observations
head(df_psa_input)
# Histogram of parameters
ggplot(melt(df_psa_input, variable.name = "Parameter"), aes(x = value)) +
       facet_wrap(~Parameter, scales = "free") +
       geom_histogram(aes(y = ..density..)) +
       theme_bw(base_size = 16) +
       theme(axis.text = element_text(size=8))
# Initialize dataframes with PSA output
# Dataframe of costs
df_c <- as.data.frame(matrix(0,</pre>
                      nrow = n_sim,
                      ncol = n_str))
colnames(df_c) <- v_names_str</pre>
# Dataframe of effectiveness
df_e <- as.data.frame(matrix(0,</pre>
                       nrow = n_sim,
                       ncol = n_str))
colnames(df_e) <- v_names_str</pre>
```

09.1 Conduct probabilistic sensitivity analysis

```
# Run Markov model on each parameter set of PSA input dataset
for(i in 1:n_sim){
    l_out_temp <- calculate_ce_out(df_psa_input[i, ])
    df_c[i, ] <- l_out_temp$Cost
    df_e[i, ] <- l_out_temp$Effect
    # Display simulation progress
    if(i/(n_sim/10) == round(i/(n_sim/10), 0)) { # display progress every 10%
        cat('\r', paste(i/n_sim * 100, "% done", sep = " "))
    }
}</pre>
```

09.2 Create PSA object for dampack

09.2.1 Save PSA objects

```
save(df_psa_input, df_c, df_e, v_names_str, n_str, l_psa,
    file = "markov_3state_PSA_dataset.RData")
```

Vector with willingness-to-pay (WTP) thresholds.

```
v_{wtp} \leftarrow seq(0, 5000, by = 1000)
```

09.3.1 Cost-Effectiveness Scatter plot

```
plot(l_psa)
```

09.4 Conduct CEA with probabilistic output

09.4.1 Plot cost-effectiveness frontier

```
plot(df_cea_psa)
```

09.4.2 Cost-effectiveness acceptability curves (CEACs) and frontier (CEAF)

```
ceac_obj <- ceac(wtp = v_wtp, psa = l_psa)
# Regions of highest probability of cost-effectiveness for each strategy
summary(ceac_obj)
# CEAC & CEAF plot
plot(ceac_obj)</pre>
```

09.4.3 Expected Loss Curves (ELCs)

The expected loss is the the quantification of the foregone benefits when choosing a suboptimal strategy given current evidence.

```
elc_obj <- calc_exp_loss(wtp = v_wtp, psa = l_psa)
elc_obj
# ELC plot
plot(elc_obj, log_y = FALSE)</pre>
```

09.4.4 Expected value of perfect information (EVPI)

```
evpi <- calc_evpi(wtp = v_wtp, psa = l_psa)
# EVPI plot
plot(evpi, effect_units = "QALY")</pre>
```