Simple 3-state Markov model in R

The DARTH workgroup

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Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001. 07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load( "dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "ggraph", "reshape2"
# install_github("DARTH-git/dampack", force = TRUE) Uncomment if there is a newer version
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/dampack", "DARTH-git/darthtools")
```

02 Load functions

```
# all functions are in the darthtools package
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("Standard of Care", "Treatment")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead") # state names</pre>
n_states <- length(v_n)
                                    # number of states
n t <- 60
                                     # number of cycles
v_{init} \leftarrow c(1, 0, 0)
                                      # initial cohort distribution (everyone allocated to the "healthy
\# Transition probabilities
p HD < -0.02
                                      # probability of dying when healthy
                                      # probability of becoming sick when healthy, under standard of ca
p_{HS} < -0.05
p_HS_trt <- 0.03
                                      # probability of becoming sick when healthy, under treatment
p_SD <- 0.1
                                      # probability of dying when sick
# Costs and utilities
c_H <- 400
                                      # cost of one cycle in healthy state
c_S <- 1000
                                     # cost of one cycle in sick state
c_D <- 0
                                      # cost of one cycle in dead state
c_trt <- 800
                                      # cost of treatment (per cycle)
u_H <- 0.8
                                      # utility when healthy
u_S <- 0.5
                                      # utility when sick
u D <- 0
                                      # utility when dead
```

Draw the state-transition cohort model

04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability matrix

Fill in the transition probability matrix:

```
# from Healthy
m_P["Healthy", "Healthy"] <- 1 - p_HS - p_HD
m_P["Healthy", "Sick"] <- p_HS
m_P["Healthy", "Dead"] <- p_HD

# from Sick
m_P["Sick", "Sick"] <- 1 - p_SD
m_P["Sick", "Dead"] <- p_SD

# from Dead
m_P["Dead", "Dead"] <- 1

# Under treatment
m_P_trt <- m_P
m_P_trt["Healthy", "Healthy"] <- 1 - p_HS_trt - p_HD
m_P_trt["Healthy", "Sick"] <- p_HS_trt</pre>
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

Standard of Care:

Treatment:

06.2 Overall Survival (OS)

Standard of Care:

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2])  # alternative way of calculating the OS probability

plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

Treatment:

```
v_os_trt <- 1 - m_M_trt[, "Dead"]  # calculate the overall survival (OS) probability
v_os_trt <- rowSums(m_M_trt[, 1:2])  # alternative way of calculating the OS probability

plot(v_os_trt, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os)  # summing probability of OS over time (i.e. life expectancy)
v_le_trt <- sum(v_os_trt)  # summing probability of OS over time (i.e. life expectancy), treatment</pre>
```

06.3 Disease prevalence

Standard of Care:

```
v_prev <- m_M[, "Sick"]/v_os
plot(v_prev,
    ylim = c(0, 1),
    ylab = "Prevalence",
    xlab = "Cycle",
    main = "Disease prevalence")</pre>
```

Treatment:

07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

07.2 Discounted Mean Costs and QALYs

07.3 Compute ICERs of the Markov model

```
df_cea
```

07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "QALYs", xlim = c(10, 12))
```