

Cohort state-transition model variations in R

**Using R for Decision Modeling in Health
Technology Assessment**

CE16

NIHES Erasmus Medical Center Rotterdam
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Time-dependency

- **Since start of the model**
- Transition probabilities often depend on age
 - Background mortality
 - Risk of developing disease or experiencing an event
- **Depending on state residency**
- Some transition probabilities depend on time since an event, not age
 - e.g., The risk of developing recurrence among newly diagnosed cancer patients declines with time
- In other words, matrix P is not the same every cycle

TIME DEPENDENCY SINCE START
OF THE MODEL

Time-dependency since model start

- Transition probabilities often depend on time since model start
 - Background mortality
 - Risk of developing disease or experiencing an event
- In other words, matrix P is not the same every cycle
- Replace matrix P with matrices P_t , where t is time since model start

Time-varying probabilities in R

- We create a 3D array, a_P , that stores a collection of time-varying transition matrices, P_t , in the third dimension
- For the Sick-Sicker Markov model:

$$a_P = \begin{matrix} & & \begin{matrix} \nearrow n_t \\ \nearrow n_s \end{matrix} & \begin{bmatrix} p[H,H,n_t] & p[H,S1,n_t] & p[H,S2,n_t] & p[H,D,n_t] \\ p[H,H,2] & p[H,S1,2] & p[H,S2,2] & p[H,D,2] \\ p[S1,H,1] & p[S1,S1,1] & p[S1,S2,1] & p[S1,D,1] \\ p[S2,H,1] & p[S2,S1,1] & p[S2,S2,1] & p[S2,D,1] \\ p[D,H,1] & p[D,S1,1] & p[D,S2,1] & p[D,D,1] \end{bmatrix} & \begin{bmatrix} p[S1,D,2] & p[S2,D,n_t] \\ p[S2,D,2] & p[D,D,n_t] \\ p[D,D,2] \end{bmatrix} \end{matrix}$$

R Session – 3 state example

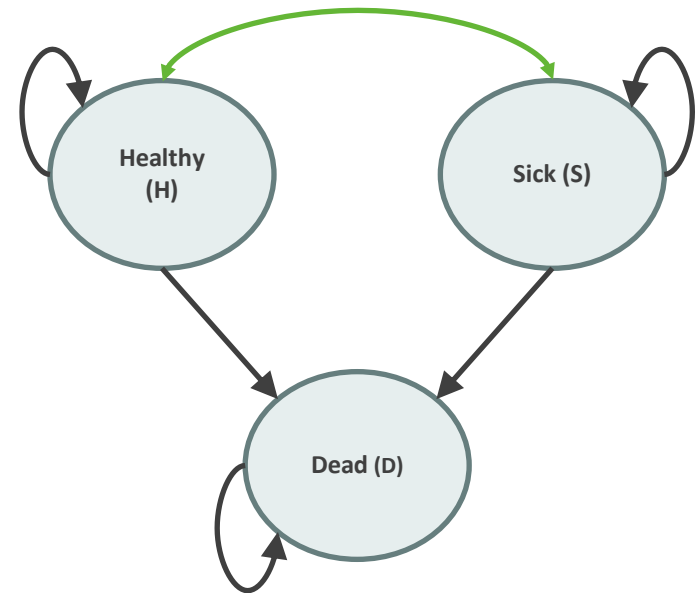
TIME-DEPENDENT BASED ON
STATE RESIDENCE

Other Types of Dependence

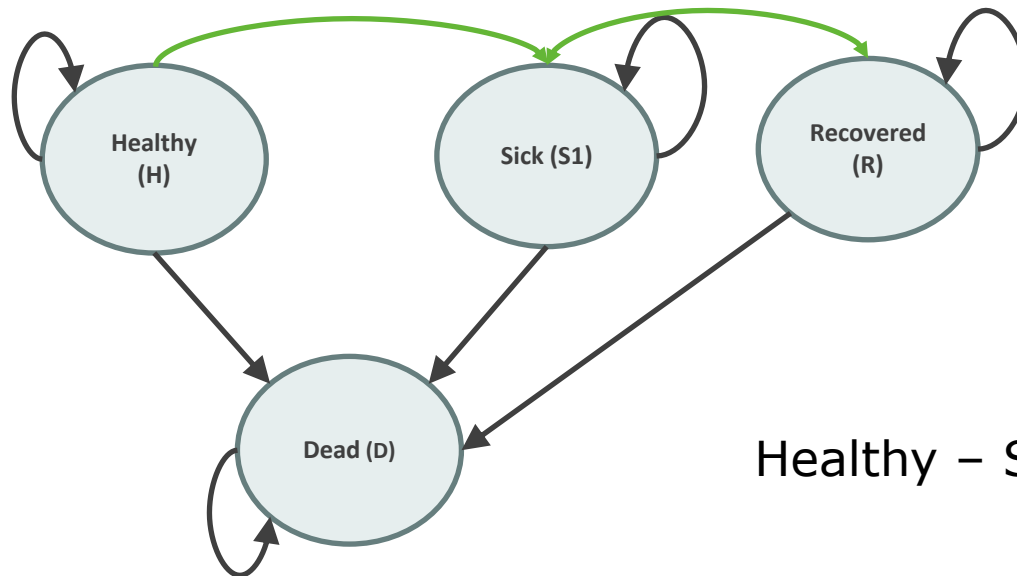
- “Memoryless” property of Markov models is a BIG assumption
 - Transition probabilities only depend on the current state and not on past states
- Many transition probabilities depend on model history, not time since model start
 - Risk of myocardial infarction (MI) greater for persons with prior MI
 - Effectiveness of a drug used as first-line therapy may be better than if used as second-line therapy

When history matters, create more states...

Healthy – Sick – Dead:



Once recovered, the risk of getting sick again or dying increases



Healthy – Sick – Recovered – Dead

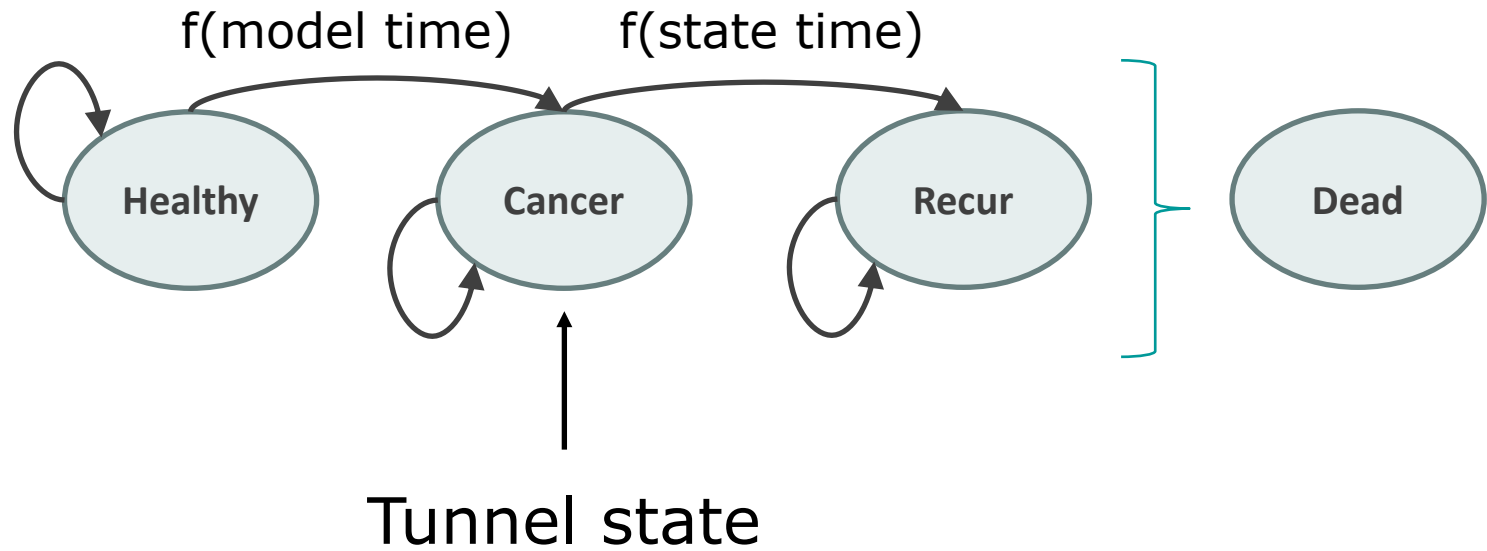
Tunnel states

If transition probabilities do not depend on the time since model start, replacing P with P_t does not work

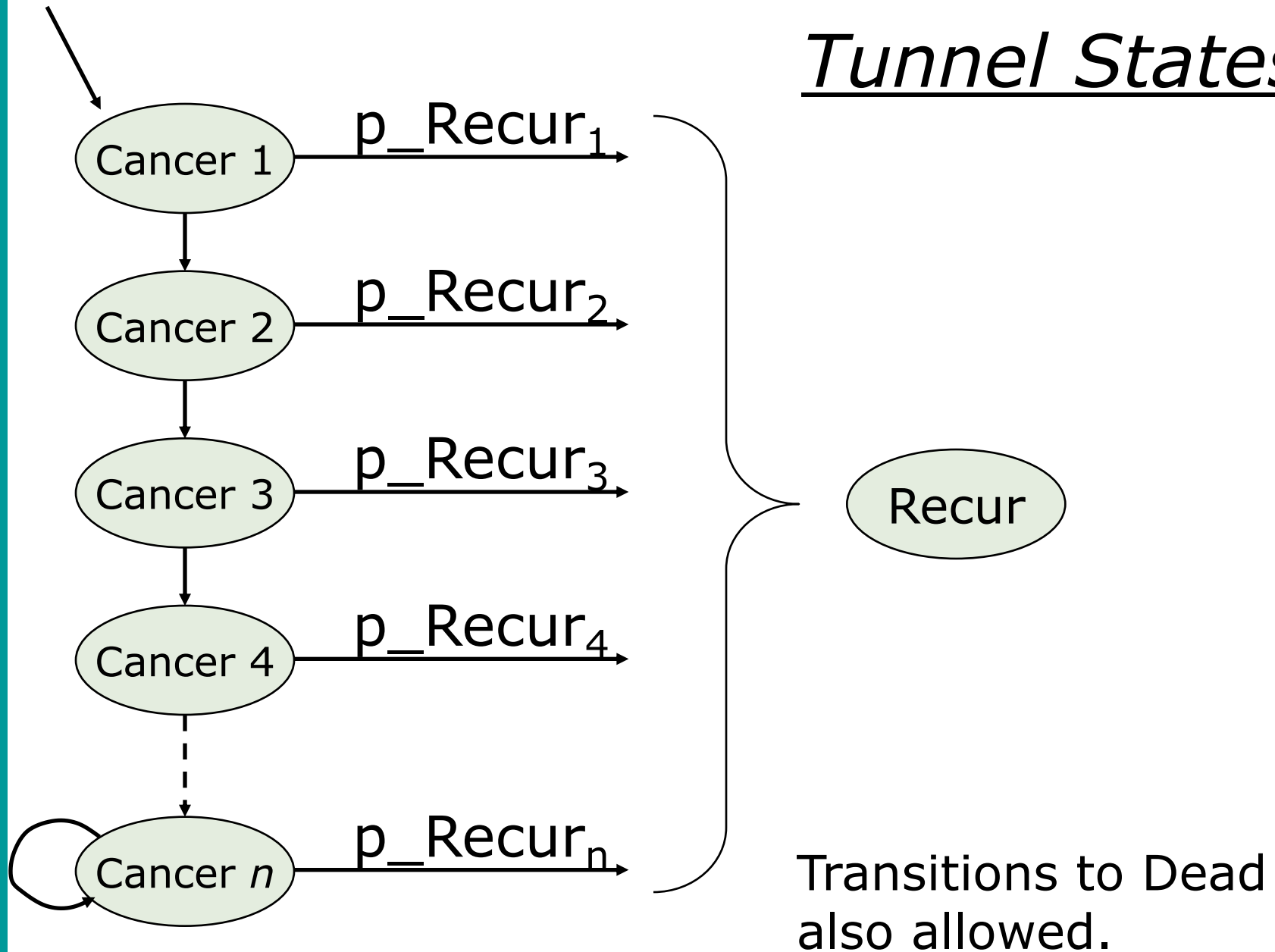
- E.g., Cohort of healthy patients at risk for cancer, but once cancer is diagnosed the risk of recurrence depends on time since diagnosis
- Solution?
 - Create “tunnel” states



State Time

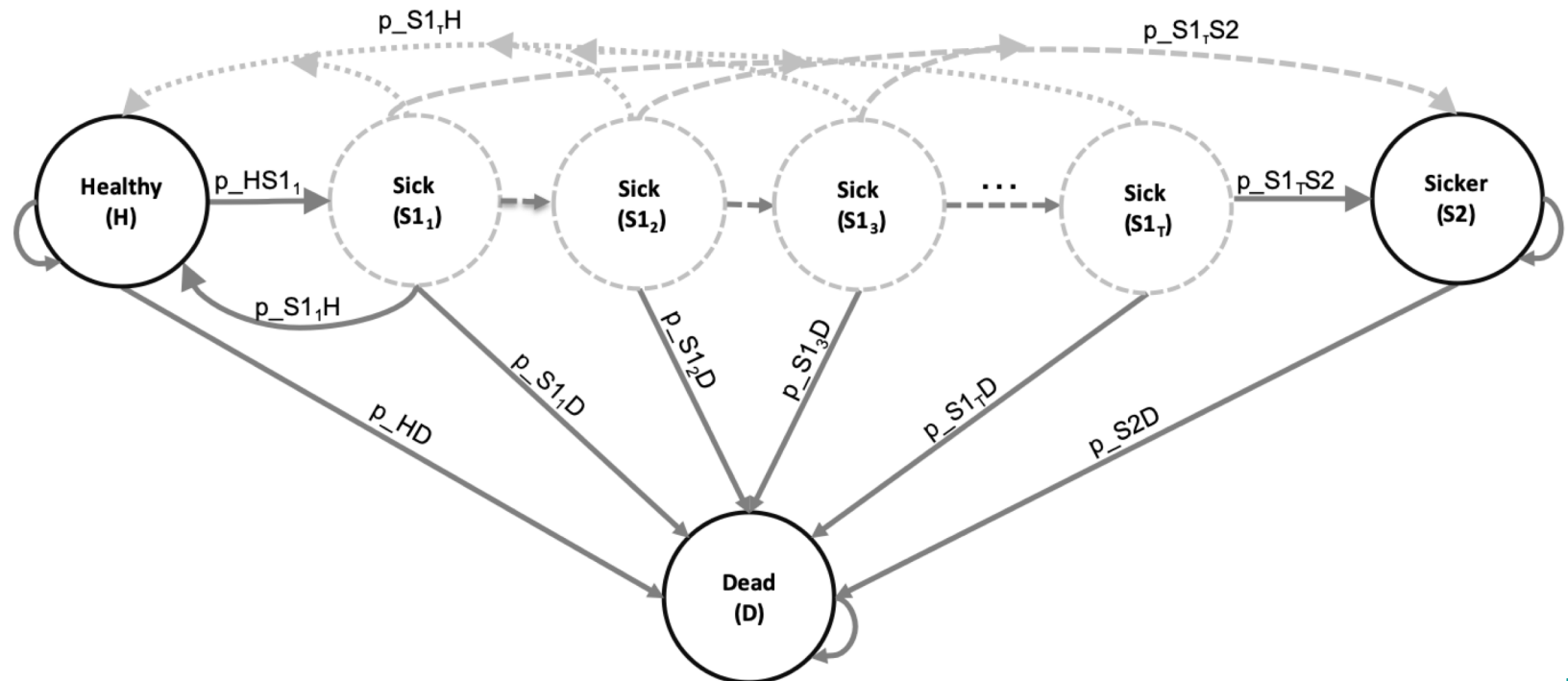


Tunnel States



Time-dependent probabilities

- Expand the states of the 3D array by the number of cycles considered in the time-dependency variable(s)
- For the Sick-Sicker Markov model:



R Session

R Exercise

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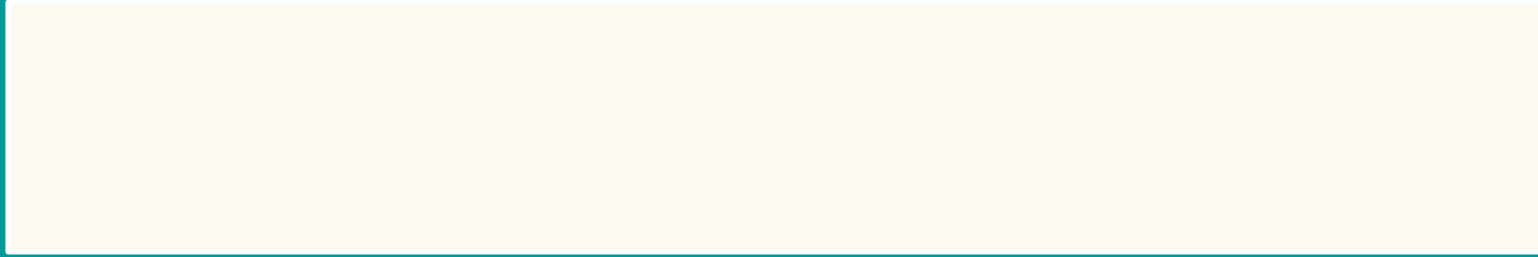


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<https://github.com/organizations/DARTH-git>



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