SA: Markov Sick-Sicker model in R

The DARTH workgroup

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- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to
# load (install if required) packages from CRAN
p_load("here", "dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "truncnorm",
# load (install if required) packages from GitHub
# install_github("DARTH-git/dampack", force = TRUE) Uncomment if there is a newer version
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/dampack", "DARTH-git/darthtools")
```

02 Load functions

```
# No function needed
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("No Treatment", "Treatment")</pre>
# Markov model parameters
       <- 25
                                    # age at baseline
age
max_age <- 55
                                   # maximum age of follow up
    <- max_age - age
                                    # time horizon, number of cycles
       <- c("H", "S1", "S2", "D") # the 4 states of the model: Healthy (H), Sick (S1),
v n
                                   # Sicker (S2), Dead (D)
v_{init} <- c(1, 0, 0, 0)
                                   # initial cohort distribution
# Transition probabilities (per cycle)
       <- 0.005
                                    # probability to die when healthy
p HD
p_HS1 <- 0.15
                                    # probability to become sick when healthy, conditional on survivin
p_S1H
        <- 0.5
                                    # probability to become healthy when sick, conditional on survivin
p_S1S2 <- 0.105
                                    # probability to become sicker when sick, conditional on surviving
        <- 3
                                    # hazard ratio of death in sick vs healthy
hr_S1
hr_S2
        <- 10
                                    # hazard ratio of death in sicker vs healthy
{	t r}_{	t HD}
       \leftarrow - \log(1 - p_HD)
                                   # rate of death in healthy
r_S1D <- hr_S1 * r_HD
                                   # rate of death in sick
r_S2D <- hr_S2 * r_HD
                                   # rate of death in sicker
                                # probability to die in sick
p_S1D \leftarrow 1 - exp(-r_S1D)
p_S2D \leftarrow 1 - exp(-r_S2D)
                                    # probability to die in sicker
# Cost and utility inputs
```

```
c_H <- 2000
                                    # cost of remaining one cycle in the healthy state
c_S1
        <- 4000
                                    # cost of remaining one cycle in the sick state
c S2
        <- 15000
                                    # cost of remaining one cycle in the sicker state
c_trt <- 12000
                                   # cost of treatment(per cycle)
       <- 0
                                   # cost of being in the death state
c D
       <- 1
uН
                                   # utility when healthy
u_S1
       <- 0.75
                                   # utility when sick
       <- 0.5
u_S2
                                   # utility when sicker
u_D
       <- 0
                                   # utility when dead
u_trt <- 0.95
                                   # utility when being treated
d_e
       <- d_c <- 0.03
                                   # discount rate per cycle equal discount of costs and QALYs by 3%
n_str <- length(v_names_str) # Number of strategies</pre>
n_states <- length(v_n)
                                    # number of states
# Discount weights for costs and effects
v_dwc \leftarrow 1 / (1 + d_c) ^ (0:n_t)
v_dwe \leftarrow 1 / (1 + d_e) ^ (0:n_t)
```

04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability matrix

Fill in the transition probability matrix:

```
# from Healthy
m_P_notrt["H", "H" ] <- (1 - p_HD) * (1 - p_HS1)
m_P_notrt["H", "S1" ] <- (1 - p_HD) * p_HS1</pre>
```

```
m_P_notrt["H", "D" ] <- p_HD
# from Sick
m_P_notrt["S1", "H" ] <- (1 - p_S1D) * p_S1H
m_P_notrt["S1", "S1"] <- (1 - p_S1D) * (1 - (p_S1H + p_S1S2))
m_P_notrt["S1", "S2"] <- (1 - p_S1D) * p_S1S2
m_P_notrt["S1", "D" ] <- p_S1D
# from Sicker
m_P_notrt["S2", "S2"] <- 1 - p_S2D
m_P_notrt["S2", "D" ] <- p_S2D
# from Dead
m_P_notrt["D", "D" ] <- 1
# create transition probability matrix for treatment same as no treatment
m_P_trt <- m_P_notrt</pre>
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

06.2 Overall Survival (OS)

```
# calculate the overall survival (OS) probability for no treatment
v_os_notrt <- 1 - m_M_notrt[, "D"]
# alternative way of calculating the OS probability
v_os_notrt <- rowSums(m_M_notrt[, 1:3])
# create a simple plot showing the OS</pre>
```

```
plot(0:n_t, v_os_notrt, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")
# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)
```

06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os_notrt)  # summing probablity of OS over time (i.e. life expectancy)
```

06.3 Disease prevalence

06.4 Proportion of sick in S1 state

07 Compute Cost-Effectiveness Outcomes

```
# Vectors with costs and utilities by treatment

v_u_notrt <- c(u_H, u_S1, u_S2, u_D)

v_u_trt <- c(u_H, u_trt, u_S2, u_D)

v_c_notrt <- c(c_H, c_S1, c_S2, c_D)

v_c_trt <- c(c_H, c_S1 + c_trt, c_S2 + c_trt, c_D)
```

07.1 Mean Costs and QALYs for Treatment and NO Treatment

07.2 Discounted Mean Costs and QALYs

07.3 Compute ICERs of the Markov model

07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "Quality of Life", xlim = c(15.6, 16.6))
```

08 Deterministic Sensitivity Analysis

08.1 List of input parameters

Create list 1_params_all with all input probabilities, cost and utilities.

```
l_params_all <- as.list(data.frame(
    p_HD = 0.005,  # probability to die when healthy
    p_HS1 = 0.15,  # probability to become sick when healthy</pre>
```

```
p_S1H = 0.5, # probability to become healthy when sick
  p_S1S2 = 0.105, # probability to become sicker when sick
  hr_S1 = 3,  # hazard ratio of death in sick vs healthy
hr_S2 = 10,  # hazard ratio of death in sicker vs healthy
         = 2000, # cost of remaining one cycle in the healthy state
  с Н
           = 4000, # cost of remaining one cycle in the sick state
= 15000, # cost of remaining one cycle in the sicker state
  c_S1
  c_S2
  c_trt = 12000, # cost of treatment(per cycle)
  c_D = 0,  # cost of being in the death state
u_H = 1,  # utility when healthy
  u_S1 = 0.75, # utility when sick
  u_S2 = 0.5, # utility when sicker

u_D = 0, # utility when dead

u_{trt} = 0.95, # utility when treated
  d_e = 0.03, # discount factor for effectiveness
  d_c
          = 0.03 # discount factor for costs
))
# store the parameter names into a vector
v_names_params <- names(l_params_all)</pre>
```

08.2 Load Sick-Sicker Markov model function

```
source("Functions_markov_sick-sicker.R")
# Test function
calculate_ce_out(l_params_all)
```

08.3 One-way sensitivity analysis (OWSA)

```
# your turn
```

08.3.1 Plot OWSA

```
# your turn
```

08.3.2 Optimal strategy with OWSA

```
# your turn
```

08.3.3 Tornado plot

```
# your turn
```

08.4 Two-way sensitivity analysis (TWSA)

your turn

08.4.1 Plot TWSA

your turn

09 Probabilistic Sensitivity Analysis (PSA)

Function to generate PSA input dataset
gen_psa <-</pre>

09.1 Conduct probabilistic sensitivity analysis

your turn

09.2 Create PSA object for dampack

your turn

09.2.1 Save PSA objects

your turn

09.3 Create probabilistic analysis graphs

your turn

Vector with willingness-to-pay (WTP) thresholds.

your turn

09.3.1 Cost-Effectiveness Scatter plot

your turn

09.4 Conduct CEA with probabilistic output

your turn

09.4.1 Plot cost-effectiveness frontier

your turn

09.4.2 Cost-effectiveness acceptability curves (CEACs) and frontier (CEAF)

your turn

09.4.3 Expected Loss Curves (ELCs)

your turn

your turn