Simple 3-state Markov model in R

with dependency for time-since model start AND with state-residency dependency

The DARTH workgroup

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- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001. 07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Mak. 2020;40(2):242-248. https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("diagram")
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/darthtools")
```

02 Load functions

```
# No functions needed
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("Base Case")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
v_names_states <- c("Healthy", "Sick", "Dead") # state names</pre>
n_states <- length(v_names_states) # number of states
               <- 60
                                                 # number of cycles
n_t
# Tunnels
n tunnel size <- n t
# Sick state
v_Sick_tunnels <- paste("Sick_", seq(1, n_tunnel_size), "Yr", sep = "")</pre>
# Create variables for time-dependent model
v_names_states_tunnels <- c("Healthy", v_Sick_tunnels, "Dead") # state names</pre>
n_states_tunnels
                      <- length(v_names_states_tunnels)</pre>
                                                                # number of states
p_HD <- seq(0.003, 0.01, length.out = n_t) # probability of dying when sick (age-dependent) - this is
                                             # probability of becoming sick when healthy, conditioned on
p_HS <- 0.05
p_SD <- 0.1
                                             # probability of dying when sick
# Weibull parameters
1 <- 0.08
  <- 1.1
p_SD <- l*g*(1:n_tunnel_size)^{g-1}</pre>
                                            # probability of dying when sick (time-in-state dependent)
```

```
# Costs and utilities
c H <- 400
                                             # cost of one cycle in healthy state
                                             # cost of one cycle in sick state
c_S <- 1000
                                             # cost of one cycle in dead state
c D <- 0
u H <- 1
                                             # utility when healthy
u_S <- 0.5
                                             # utility when sick
u_D <- 0
                                             # utility when dead
d e < - d c < - 0.03
                                             # equal discount of costs and QALYs by 3%
\# calculate discount weights for costs for each cycle based on discount rate d_c
v_dwc < 1 / (1 + d_e) ^ (0:n_t)
\# calculate discount weights for effectiveness for each cycle based on discount rate d_{\_}e
v_dwe \leftarrow 1 / (1 + d_c) ^ (0:n_t)
```

04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability array

Fill in the transition probability array:

```
# from Healthy
a_P["Healthy", "Healthy", ] <- (1 - p_HD)* (1 - p_HS)
a_P["Healthy", "Sick_1Yr", ] <- (1 - p_HD) * p_HS
a_P["Healthy", "Dead", ] <- p_HD

# from Sick
for(i in 1:(n_tunnel_size - 1)){
    a_P[v_Sick_tunnels[i], v_Sick_tunnels[i + 1], ] <- 1 - p_SD[i]
    a_P[v_Sick_tunnels[i], "Dead", ] <- p_SD[i]
}</pre>
```

```
a_P[v_Sick_tunnels[n_tunnel_size], v_Sick_tunnels[n_tunnel_size], ] <- 1 - p_SD[n_tunnel_size]
a_P[v_Sick_tunnels[n_tunnel_size], "Dead", ] <- p_SD[n_tunnel_size]

# from Dead
a_P["Dead", "Dead", ] <- 1</pre>
```

04.3 Check if transition array and probabilities are valid

```
# Check that transition probabilities are in [0, 1]
check_transition_probability(a_P, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(a_P, n_states = n_states_tunnels, n_cycles = n_t, verbose = TRUE)
```

05 Run Markov model

```
for (t in 1:n_t) {
    m_M[t + 1, ] <- m_M[t, ] %*% a_P[, , t] # loop through the number of cycles
    # estimate the Markov trace for cycle t + 1
    # using the t-th matrix from the
    # probability array
}
head(m_M)</pre>
```

Create aggregated trace.

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

06.2 Overall Survival (OS)

06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os) # summing probablity of OS over time (i.e. life expectancy)
```

06.3 Disease prevalence

07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
v_tc <- m_M_tunnels %*% c(c_H, c_S, c_D)
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
v_tu <- m_M_tunnels %*% c(u_H, u_S, u_D)</pre>
```

07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights (v_dw)
v_tc_d <- t(v_tc) %*% v_dwc
# Discount QALYS by multiplying the QALYs vector with discount weights (v_dw)
v_te_d <- t(v_tu) %*% v_dwe</pre>
```

07.3 Store Results