Markov Sick-Sicker model in R

The DARTH workgroup

Developed by the Decision Analysis in R for Technologies in Health (DARTH) workgroup:

Fernando Alarid-Escudero, PhD (1)

Eva A. Enns, MS, PhD (2)

M.G. Myriam Hunink, MD, PhD (3,4)

Hawre J. Jalal, MD, PhD (5)

Eline M. Krijkamp, MSc (3)

Petros Pechlivanoglou, PhD (6,7)

Alan Yang, MSc (7)

In collaboration of:

- 1. Drug Policy Program, Center for Research and Teaching in Economics (CIDE) CONACyT, Aguas-calientes, Mexico
- 2. University of Minnesota School of Public Health, Minneapolis, MN, USA
- 3. Erasmus MC, Rotterdam, The Netherlands
- 4. Harvard T.H. Chan School of Public Health, Boston, USA
- 5. University of Pittsburgh Graduate School of Public Health, Pittsburgh, PA, USA
- 6. University of Toronto, Toronto ON, Canada
- 7. The Hospital for Sick Children, Toronto ON, Canada

Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("dplyr", "devtools", "scales", "ellipse", "ggplot2", "lazyeval", "igraph", "truncnorm", "ggraph"
# load (install if required) packages from GitHub
# install_github("DARTH-git/dampack", force = TRUE) Uncomment if there is a newer version
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/dampack", "DARTH-git/darthtools")
```

02 Load functions

```
# all functions are in the darthtools package
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("No Treatment", "Treatment")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
age <- 25
                                    # age at baseline
max_age <- 55
                                   # maximum age of follow up
n_t
    <- max_age - age
                                  # time horizon, number of cycles
       <- c("H", "S1", "S2", "D") # the 4 states of the model: Healthy (H), Sick (S1),
                                   # Sicker (S2), Dead (D)
n states <- length(v n)
                                   # number of health states
                                   # initial cohort distribution
v_{init} \leftarrow c(1, 0, 0, 0)
# Transition probabilities (per cycle)
      <- 0.005
                                    # probability to die when healthy
p_HD
      <- 0.15
                                      # probability to become sick when healthy
p_HS1
                                      # probability to become healthy when sick
p_S1H <- 0.5
p_S1S2 <- 0.105
                                      # probability to become sicker when sick
hr_S1 <- 3
                                     # hazard ratio of death in sick vs healthy
hr S2
      <- 10
                                      # hazard ratio of death in sicker vs healthy
r_{HD} < -llog(1 - p_{HD})
                                   # rate of death in healthy
r_S1D <- hr_S1 * r_HD
                                    # rate of death in sick
r_S2D \leftarrow hr_S2 * r_HD
                                      # rate of death in sicker
```

```
\leftarrow 1 - \exp(-r_S1D)
                                    # probability to die in sick
p_S1D
p_S2D
        \leftarrow 1 - \exp(-r_S2D)
                                     # probability to die in sicker
# Cost and utility inputs
       <- 2000
c_H
                                    # cost of remaining one cycle in the healthy state
c S1
       <- 4000
                                    # cost of remaining one cycle in the sick state
       <- 15000
c_S2
                                   # cost of remaining one cycle in the sicker state
c_trt <- 12000
                                   # cost of treatment(per cycle)
       <- 0
                                   # cost of being in the death state
c D
uН
       <- <u>1</u>
                                    # utility when healthy
u_S1 <- 0.75
                                    # utility when sick
      <- 0.5
                                   # utility when sicker
u S2
       <- 0
u_D
                                    # utility when dead
u_trt <- 0.95
                                    # utility when being treated
# Discounting factor
d_e <- d_c <- 0.03
                                    # equal discount of costs and QALYs by 3%
\# calculate discount weights for costs for each cycle based on discount rate d_c
v_dwc \leftarrow 1 / (1 + d_e) ^ (0:n_t)
# calculate discount weights for effectiveness for each cycle based on discount rate d_e
v_{dwe} \leftarrow 1 / (1 + d_c) ^ (0:n_t)
```

Create a state-transition diagram of the cohort model

04 Define and initialize matrices and vectors

04.1 Cohort trace

```
\# create the markov trace matrix M capturing the proportion of the cohort in each state \# at each cycle
```

04.2 Transition probability matrix

Fill in the transition probability matrix:

```
# from Healthy
m_P_notrt["H", "H" ] <- 1 - (p_HS1 + p_HD)</pre>
m_P_notrt["H", "S1" ] <- p_HS1</pre>
m_P_notrt["H", "D" ] <- p_HD</pre>
# from Sick
m_P_notrt["S1", "H"] <- p_S1H</pre>
m_P_notrt["S1", "S1"] <- 1 - (p_S1H + p_S1S2 + p_S1D)</pre>
m_P_notrt["S1", "S2"] <- p_S1S2</pre>
m_P_notrt["S1", "D" ] <- p_S1D</pre>
# from Sicker
m_P_notrt["S2", "S2"] <- 1 - p_S2D</pre>
m_P_notrt["S2", "D" ] <- p_S2D
# from Dead
m_P_notrt["D", "D" ] <- 1</pre>
# create transition probability matrix for treatment same as no treatment
m_P_trt <- m_P_notrt</pre>
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

06.2 Overall Survival (OS)

06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os_notrt) # summing probability of OS over time (i.e. life expectancy)
```

06.3 Disease prevalence

06.4 Proportion of sick in S1 state

07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs for Treatment and NO Treatment

07.2 Discounted Mean Costs and QALYs

07.3 Compute ICERs of the Markov model

07.4 Plot frontier of the Markov model

```
plot(df_cea, effect_units = "QALYs", xlim = c(15.6, 16.6))
```