Simple 3-state Markov model in R

The DARTH workgroup

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- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Alarid-Escudero F, Krijkamp EM, Enns EA, Yang A, Hunink MGM Pechlivanoglou P, Jalal H. Cohort State-Transition Models in R: A Tutorial. arXiv:200107824v2. 2020:1-48. http://arxiv.org/abs/2001.07824
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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Change eval to TRUE if you want to knit this document.

```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
# load (install if required) packages from CRAN
p_load("diagram")
# install_github("DARTH-git/darthtools", force = TRUE) Uncomment if there is a newer version
p_load_gh("DARTH-git/darthtools")
```

02 Load functions

```
# all functions are in the darthtools package
```

03 Input model parameters

```
# Strategy names
v_names_str <- c("Standard of Care")</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead") # state names</pre>
n_t <- 60
                                     # number of cycles
v_{init} \leftarrow c("Healthy" = 1,
           "Sick" = 0,
            "Dead" = 0)
                                    # initial cohort distribution (everyone allocated to the
                                    # "healthy" state)
# Transition probabilities
p_HD <- 0.02
                                     # probability of dying when healthy
p HS <- 0.05
                                     # probability of becoming sick when healthy, under standard of ca
p_SD <- 0.1
                                     # probability of dying when sick
# Costs and utilities
c_H <- 400
                                    # cost of one cycle in healthy state
c_S <- 1000
                                     # cost of one cycle in sick state
c_D <- 0
                                    # cost of one cycle in dead state
u_H <- 0.8
                                    # utility when healthy
u_S <- 0.5
                                    # utility when sick
u_D <- 0
                                     # utility when dead
d_e < d_c < 0.03
                                     # discount rate per cycle equal discount of costs and QALYs by 3%
```

n_str <- length(v_names_str) # Number of strategies</pre>

```
n_states <- length(v_n)  # number of states

# Discount weights for costs and effects
v_dwc <- 1 / (1 + d_c) ^ (0:n_t)
v_dwe <- 1 / (1 + d_e) ^ (0:n_t)</pre>
```

Draw the state-transition cohort model

04 Define and initialize matrices and vectors

04.1 Cohort trace

04.2 Transition probability matrix

Fill in the transition probability matrix:

```
# from Healthy
m_P["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS)
m_P["Healthy", "Sick"] <- (1 - p_HD) * p_HS
m_P["Healthy", "Dead"] <- p_HD

# from Sick
m_P["Sick", "Sick"] <- 1 - p_SD
m_P["Sick", "Dead"] <- p_SD

# from Dead
m_P["Dead", "Dead"] <- 1</pre>
```

04.3 Check if transition array and probabilities are valid

```
# Check that transition probabilities are in [0, 1]
check_transition_probability(m_P, verbose = TRUE)
# Check that all rows sum to 1
check_sum_of_transition_array(m_P, n_states = n_states, n_cycles = n_t, verbose = TRUE)
```

05 Run Markov model

06 Compute and Plot Epidemiological Outcomes

06.1 Cohort trace

06.2 Overall Survival (OS)

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2])  # alternative way of calculating the OS probability

plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os) # summing probablity of OS over time (i.e. life expectancy)
```

06.3 Disease prevalence

```
v_prev <- m_M[, "Sick"]/v_os

plot(v_prev,
    ylim = c(0, 1),
    ylab = "Prevalence",
    xlab = "Cycle",
    main = "Disease prevalence")</pre>
```

07 Compute Cost-Effectiveness Outcomes

07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
v_tc <- m_M %*% c(c_H, c_S, c_D)
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
v_tu <- m_M %*% c(u_H, u_S, u_D)</pre>
```

07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights (v_dw) v_tc_d <- t(v_tc) %*% v_dwc
```

```
# Discount QALYS by multiplying the QALYs vector with discount weights (v_dw) v_te_d <- t(v_tu) %*% v_dwe
```

07.3 Store Results