# Simple 3-state Markov model in R

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Please cite our publications when using this code:

- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. Online First https://doi.org/10.1177/0272989X19893973

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```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

# 01 Load packages

```
if (!require('pacman')) install.packages('pacman'); library(pacman) # use this package to conveniently
## Loading required package: pacman
# load (install if required) packages from CRAN
p_load("diagram")
```

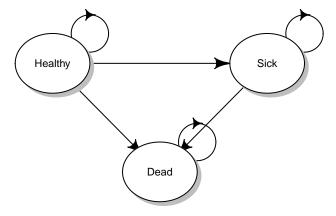
#### 02 Load functions

```
# no functions required
```

# 03 Input model parameters

```
# Strategy names
v_names_str <- c("Base Case")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead")  # state names
n_states <- length(v_n)</pre>
                                         # number of states
n t <- 60
                                         # number of cycles
                                         # initial cohort distribution
v_{init} \leftarrow c(1, 0, 0)
p_{HD} < -0.02
                                         # probability of dying when healthy
p_{HS} < -0.05
                                          # probability of becoming sick when healthy, conditioned on not
p_SD <- 0.1
                                          # probability of dying when sick
# Costs and utilities
c H <- 400
                                         # cost of one cycle in healthy state
c_S <- 1000
                                         # cost of one cycle in sick state
c_D <- 0
                                         # cost of one cycle in dead state
u_H <- 0.8
                                         # utility when healthy
u_S <- 0.5
                                         # utility when sick
u_D <- 0
                                         # utility when dead
d_e < -d_c < -0.03
                                         # discount rate per cycle equal discount of costs and QALYs by
\# calculate discount weights for costs for each cycle based on discount rate d_{\_}c
v_dwc \leftarrow 1 / (1 + d_e) ^ (0:n_t)
\# calculate discount weights for effectiveness for each cycle based on discount rate d_e
v_dwe \leftarrow 1 / (1 + d_c) ^ (0:n_t)
```

#### Draw the state-transition cohort model



#### 04 Define and initialize matrices and vectors

#### 04.1 Cohort trace

#### 04.2 Transition probability matrix

## Healthy Sick Dead

```
## Healthy
                0
                             0
## Sick
                       0
                             0
                  0
## Dead
Fill in the transition probability matrix:
# from Healthy
m_P["Healthy", "Healthy"] <- (1 - p_HD) * (1 - p_HS)</pre>
m_P["Healthy", "Sick"] <- (1 - p_HD) * p_HS</pre>
m_P["Healthy", "Dead"] <- p_HD</pre>
# from Sick
m_P["Sick", "Sick"] <- 1 - p_SD</pre>
m_P["Sick", "Dead"] <- p_SD</pre>
# from Dead
m_P["Dead", "Dead"] <- 1</pre>
# print matrix
m_P
           Healthy Sick Dead
## Healthy 0.931 0.049 0.02
```

# 05 Run Markov model

Sick

1

# check rows add up to 1

## Sick ## Dead

rowSums(m\_P)

## Healthy

1

0.000 0.900 0.10

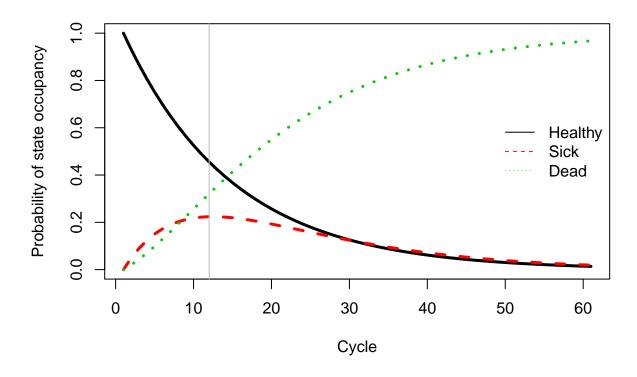
0.000 0.000 1.00

Dead

# 06 Compute and Plot Epidemiological Outcomes

#### 06.1 Cohort trace

## **Cohort Trace**



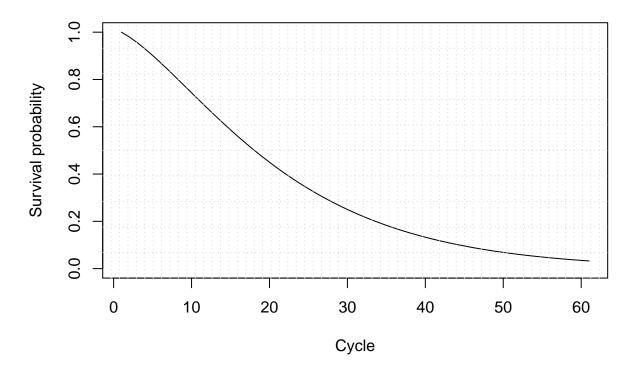
### 06.2 Overall Survival (OS)

```
v_os <- 1 - m_M[, "Dead"]  # calculate the overall survival (OS) probability
v_os <- rowSums(m_M[, 1:2])  # alternative way of calculating the OS probability

plot(v_os, type = 'l',
    ylim = c(0, 1),
    ylab = "Survival probability",
    xlab = "Cycle",
    main = "Overall Survival")  # create a simple plot showing the OS

# add grid
grid(nx = n_t, ny = 10, col = "lightgray", lty = "dotted", lwd = par("lwd"),
    equilogs = TRUE)</pre>
```

# **Overall Survival**

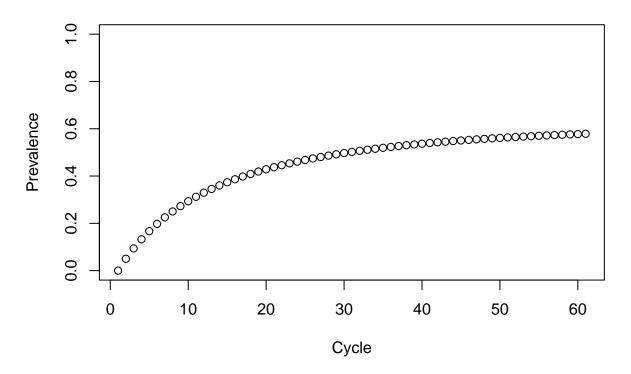


# 06.2.1 Life Expectancy (LE)

```
v_le <- sum(v_os) # summing probablity of OS over time (i.e. life expectancy)
```

## 06.3 Disease prevalence

## Disease prevalence



# 07 Compute Cost-Effectiveness Outcomes

#### 07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
v_tc <- m_M %*% c(c_H, c_S, c_D)
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
v_tu <- m_M %*% c(u_H, u_S, u_D)</pre>
```

#### 07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights (v_dw)
v_tc_d <- t(v_tc) %*% v_dwc
# Discount QALYS by multiplying the QALYs vector with discount weights (v_dw)
v_te_d <- t(v_tu) %*% v_dwe</pre>
```

#### 07.3 Results

# check.names = F)

results