# Simple 3-state Markov model in R

### with age dependency

#### The DARTH workgroup

Developed by the Decision Analysis in R for Technologies in Health (DARTH) workgroup:

Fernando Alarid-Escudero, PhD (1)

Eva A. Enns, MS, PhD (2)

M.G. Myriam Hunink, MD, PhD (3,4)

Hawre J. Jalal, MD, PhD (5)

Eline M. Krijkamp, MSc (3)

Petros Pechlivanoglou, PhD (6,7)

Alan Yang, MSc (7)

In collaboration of:

- 1. Drug Policy Program, Center for Research and Teaching in Economics (CIDE) CONACyT, Aguas-calientes, Mexico
- 2. University of Minnesota School of Public Health, Minneapolis, MN, USA
- 3. Erasmus MC, Rotterdam, The Netherlands
- 4. Harvard T.H. Chan School of Public Health, Boston, USA
- 5. University of Pittsburgh Graduate School of Public Health, Pittsburgh, PA, USA
- 6. University of Toronto, Toronto ON, Canada
- 7. The Hospital for Sick Children, Toronto ON, Canada

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- Jalal H, Pechlivanoglou P, Krijkamp E, Alarid-Escudero F, Enns E, Hunink MG. An Overview of R in Health Decision Sciences. Med Decis Making. 2017; 37(3): 735-746. https://journals.sagepub.com/doi/abs/10.1177/0272989X16686559
- Krijkamp EM, Alarid-Escudero F, Enns EA, Jalal HJ, Hunink MGM, Pechlivanoglou P. Microsimulation modeling for health decision sciences using R: A tutorial. Med Decis Making. 2018;38(3):400–22. https://journals.sagepub.com/doi/abs/10.1177/0272989X18754513
- Krijkamp EM, Alarid-Escudero F, Enns E, Pechlivanoglou P, Hunink MM, Jalal H. A Multidimensional Array Representation of State-Transition Model Dynamics. Med Decis Making. 2020 Online first. https://doi.org/10.1177/0272989X19893973

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```
rm(list = ls())  # clear memory (removes all the variables from the workspace)
```

### 01 Load packages

```
# no packages required
```

#### 02 Load functions

```
# no functions required
```

# 03 Input model parameters

```
# Strategy names
v_names_str <- c("Base Case")</pre>
# Number of strategies
n_str <- length(v_names_str)</pre>
# Markov model parameters
v_n <- c("Healthy", "Sick", "Dead") # state names</pre>
n_states <- length(v_n)
                                        # number of states
n_t <- 60
                                         # number of cycles
p_HD <- seq(0.003, 0.01, length.out = n_t) # probabilities of dying when sick (age-dependent) - this i
p_{HS} < -0.05
                                             # probability of becoming sick when healthy, conditioned on
p_SD <- 0.1
                                             # probability of dying when sick
# Costs and utilities
c H <- 400
                                        # cost of one cycle in healthy state
c_S <- 1000
                                         # cost of one cycle in sick state
c_D <- 0
                                        # cost of one cycle in dead state
                                        # utility when healthy
u H <- 0.8
u S <- 0.5
                                        # utility when sick
u_D <- 0
                                        # utility when dead
d_e <- d_c <- 0.03
                                         # equal discount of costs and QALYs by 3%
\# calculate discount weights for costs for each cycle based on discount rate d\_c
v_dwc \leftarrow 1 / (1 + d_e) ^ (0:n_t)
\# calculate discount weights for effectiveness for each cycle based on discount rate d_{\_}e
v_dwe \leftarrow 1 / (1 + d_c) ^ (0:n_t)
```

#### 04 Define and initialize matrices and vectors

#### 04.1 Cohort trace

#### 04.2 Transition probability array

```
# create the transition probability array
a_P <- array(0,  # Create 3-D array
dim = c(n_states, n_states, n_t),
dimnames = list(v_n, v_n, 0:(n_t - 1))) # name the dimensions of the array</pre>
```

Fill in the transition probability array:

```
# from Healthy
a_P["Healthy", "Healthy", ] <- (1 - p_HD) * (1 - p_HS)
a_P["Healthy", "Sick", ] <- (1-p_HD) * p_HS
a_P["Healthy", "Dead", ] <- p_HD

# from Sick
a_P["Sick", "Sick", ] <- 1 - p_SD
a_P["Sick", "Dead", ] <- p_SD

# from Dead
a_P["Dead", "Dead", ] <- 1</pre>
```

#### 04.3 Check if transition array and probabilities are valid

```
check.names = FALSE)
if(verbose){
    message("Not valid transition probabilities")
    stop(print(df_notvalid), call. = FALSE)
}
}

# Check if transition probability array is valid
valid <- apply(a_P, 3, function(x) all.equal(sum(rowSums(x)), n_states))
if (!isTRUE(all.equal(as.numeric(sum(valid)), as.numeric(n_t)))) {
    if(verbose){
        stop("This is not a valid transition Matrix")
    }
}</pre>
```

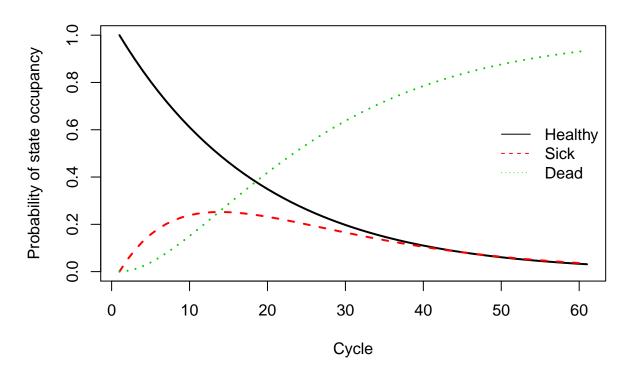
#### 05 Run Markov model

```
for (t in 1:n t){ # t<-1
                                           # loop through the number of cycles
 m_M[t + 1, ] \leftarrow m_M[t, ] **% a_P[, , t] # estimate the Markov trace for cycle t + 1
                                           # using the t-th matrix from the
                                           # probability array
}
head(m_M) # print the first lines of the matrix
       Healthy
                                Dead
##
                     Sick
## 0 1.0000000 0.00000000 0.00000000
## 1 0.9471500 0.04985000 0.00300000
## 2 0.8969864 0.09207481 0.01093882
## 3 0.8493784 0.12757146 0.02305011
## 4 0.8042016 0.15714071 0.03865771
## 5 0.7613370 0.18149700 0.05716604
```

# 06 Compute and Plot Epidemiological Outcomes

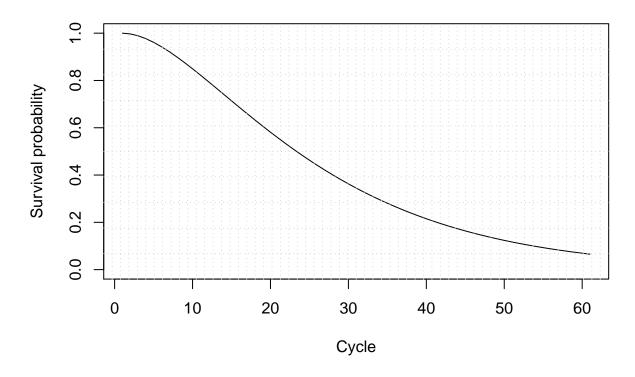
#### 06.1 Cohort trace

# **Cohort Trace**



### 06.2 Overall Survival (OS)

# **Overall Survival**

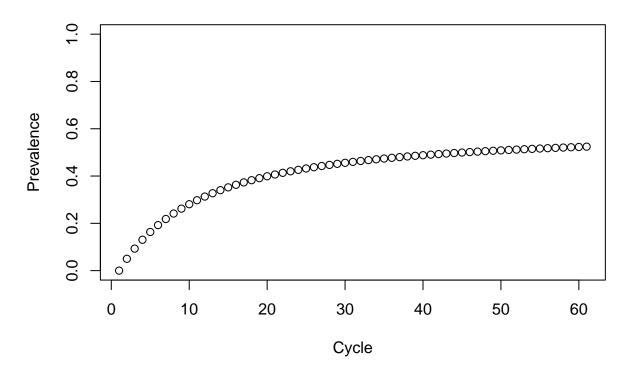


# 06.2.1 Life Expectancy (LE)

```
v_{e} = sum(v_{o}) # summing probablity of OS over time (i.e. life expectancy)
```

# 06.3 Disease prevalence

# Disease prevalence



# 07 Compute Cost-Effectiveness Outcomes

#### 07.1 Mean Costs and QALYs

```
# per cycle
# calculate expected costs by multiplying m_M with the cost vector for the different
# health states
v_tc <- m_M %*% c(c_H, c_S, c_D)
# calculate expected QALYs by multiplying m_M with the utilities for the different
# health states
v_tu <- m_M %*% c(u_H, u_S, u_D)</pre>
```

#### 07.2 Discounted Mean Costs and QALYs

```
# Discount costs by multiplying the cost vector with discount weights (v_dw)
v_tc_d <- t(v_tc) %*% v_dwc
# Discount QALYS by multiplying the QALYs vector with discount weights (v_dw)
v_te_d <- t(v_tu) %*% v_dwe</pre>
```

#### 07.3 Results

# check.names = F)

results

## Total Discounted Cost Life Expectancy Total Discounted QALYs
## 1 9504.301 26.32364 12.06788