darthpack: An R package with DARTH's decision modeling coding framework

Supplementary Material to "A need for change! A coding framework for improving transparency in decision modeling"

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The Sick-Sicker model

In this case-study, we perform a cost-effectiveness analysis (CEA) using a previously published 4-state model called the Sick-Sicker model (Enns et al., 2015). In the Sick-Sicker model, a hypothetical disease affects individuals with an average age of 25 years and results in increased mortality, increased treatment costs and reduced quality of life (QoL). We simulate this hypothetical cohort of 25-year-old individuals over a lifetime (i.e., reaching an age of 100 years old) using 75 annual cycles, represented with n t. The cohort starts in the "Healthy" health state (denoted "H"). Healthy individuals are at risk of developing the illness, at which point they would transition to the first stage of the disease (the "Sick" health state, denoted "S1"). Sick individuals are at risk of further progressing to a more severe stage (the "Sicker" health state, denoted "S2"), which is a constant probability in this case-study. There is a chance that individuals in the Sick state eventually recover and return back to the Healthy state. However, once an individual reaches the Sicker state, they cannot recover; that is, the probability of transitioning to the Sick or Healthy states from the Sicker state is zero. Individuals in the Healthy state face background mortality that is age-specific (i.e., time-dependent). Sick and Sicker individuals face an increased mortality expressed as a hazard rate ratio (HR) of 3 and 10, respectively, on the background mortality rate. Sick and Sicker individuals also experience increased health care costs and reduced QoL compared to healthy individuals. Once simulated individuals die, they transition to the "Dead" state (denoted "D"), where they remain. Figure 1 shows the state-transition diagram of the Sick-Sicker model. The evolution of the cohort is simulated in one-year discrete-time cycles. Both costs and quality-adjusted life years (QALYs) are discounted at an annual rate of 0.03%.

Two alternative strategies exist for this hypothetical disease: a no-treatment and a treatment strategy. Under the treatment strategy, Sick and Sicker individuals receive treatment and continue doing so until they recover or die. The cost of the treatment is additional to the cost of being Sick or Sicker for one year. The treatment improves QoL for those individuals who are Sick but has no effect on the QoL of those who are sicker. To evaluate these two alternative strategies, we perform a CEA.

We assume that most of the parameters of the Sick-Sicker model and their uncertainty have been previously estimated and are known to the analyst. However, while we can identify those who are afflicted with the illness through obvious symptoms, we can not easily distinguish those in the Sick state from the those in the Sicker state. Thus, we can not directly estimate state-specific mortality hazard rate ratios, nor do we know the transition probability of progressing from Sick to Sicker. Therefore, we calibrate the model to different epidemiological data. We internally validated the calibrated model by comparing the predicted outputs from the model evaluated at the calibrated parameters against the calibration targets (Eddy et al., 2012, Goldhaber-Fiebert et al. (2010)).

As part of the CEA, we conducted different deterministic sensitivity analysis (SA), including one-way and

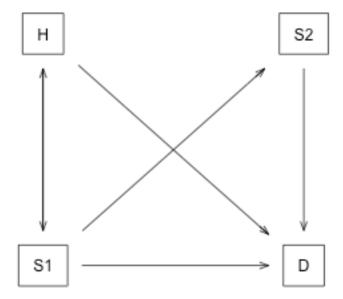


Figure 1: State-transition diagram of the Sick-Sicker model. Healthy individuals can get Sick, die or stay healthy. Sick individuals can recover, transitioning back to healthy, can die, or stay sick. Once individuals are Sicker, they stay Sicker until they die.

two-way SA, and tornado plots. To quantify the effect of parameter uncertainty on decision uncertainty, we conducted a probabilistic sensitivity analysis (PSA) and reported our uncertainty analysis results with a cost-effectiveness acceptability curve (CEAC), cost-effectiveness acceptability frontier (CEAF) and expected loss curves (ELC) (Alarid-Escudero et al., 2019). We also conducted a value of information (VOI) analysis to determine whether potential future research is needed to reduce parameter uncertainty. All steps of the CEA will be described using the different components of the framework.

Set-up

This report is a supplementary material meant to guide you through the R code of a fully functional decision model to showcase the framework described by the Decision Analysis in R for Technologies in Health (DARTH) workgroup in the manuscript A need for change! A coding framework for improving transparency in decision modeling. The code of this analysis can be downloaded from GitHub (https://github.com/DARTH-git/Decision-Modeling-Framework). We recommend downloading the case-study files as a single .zip file containing all directories. Unzip the folder and save to your desired directory. The framework is divided into different directories, described in Table 1, that could be accessed from the RStudio project Decision-Modeling-Framework.Rproj. In this framework, you will find multiple directories as described in Table 1 of the main manuscript. We refer to the directory names of this framework and scripts stored in these directories using italic style. This report is created with Markdown and is located in the reports directory of the framework. The figures for the case-study can be found in the figs directory, data required to conduct some of the analyses of the different components are in the data directory and the R scripts with functions, are located in the R directory. The main R scripts that conduct the analyses of the different components of the framework are stored in the R directory. In this document we do not show all the R code we refer to. Therefore, it is important to follow along while reading this document.

Chapter 1

Define model inputs

As described in the main manuscript, in this first component we declare all model input variables and set their values. The R script running the analysis of this component is the $01_model-inputs.R$ file in the analysis directory.

The input to inform the values is divided in three categories: external, estimated, and calibrated. The majority of the Sick-Sicker model parameters are informed by external data. Only three parameter values need to be estimated using model calibration.

In this component, we start with the general setup of the model, specifying among others the time horizon, name and number of health states, proportion of the cohort in each of the different health states at the start of the simulation and discount rates. The next step is to specify the external parameters. The initial model parameter values and R variable names are presented in Table 1.1.

Table 1.1: Description of the initial parameters with their R name and value of the Sick-Sicker model.

Parameter	R name	Value
Time horizon (n_t)	n_t	75 years
Names of health states (n)		H, S1, S2, D
Annual discount rate (costs/QALYs)	d_c/d_e	3%
Annual transition probabilities		
- Disease onset (H to S1)	p_HS1	0.15
- Recovery (S1 to H)	p_S1H	0.5
- Disease progression (S1 to S2) in the time-homogenous model		0.105
Annual mortality		
- All-cause mortality (H to D)	p_HD	age-specific
- Hazard rate ratio of death in S1 vs ${\rm H}$	hr_S1	3
- Hazard rate ratio of death in S2 vs H $$	hr_S2	3
Annual costs		
- Healthy individuals	c_H	\$2,000
- Sick individuals in S1	c_S1	\$4,000

Parameter	R name	Value
- Sick individuals in S2	c_S2	\$15,000
- Dead individuals	c_D	\$0
- Additional costs of sick individuals treated in S1 or S2 $$	c_Trt	\$12,000
Utility weights		
- Healthy individuals	u_H	1.00
- Sick individuals in S1	u_S1	0.75
- Sick individuals in S2	u_S2	0.50
- Dead individuals	u_D	0.00
Intervention effect		
- Utility for treated individuals in S1	u_Trt	0.95

Age-specific background mortality for healthy individuals is represented by the US population in 2015 and obtained from the Human Mortality database. This information is stored in the 01_all -cause-mortality.csv file in the data directory. Based on this .csv file a vector with mortality rates by age is created using the load_mort_data function in the 01_model -inputs_functions.R script. This function gives us the flexibility to easily import data from other countries or years.

print.function(load_mort_data) # print the function

```
## function(file = NULL){
##
     # Load mortality data from file
     if(!is.null(file)) {
##
##
       df_r_mort_by_age <- read.csv(file = file)}</pre>
##
     else{
##
       df_r_mort_by_age <- all_cause_mortality
##
     }
##
     # Vector with mortality rates
##
     v_r_mort_by_age <- as.matrix(dplyr::select(df_r_mort_by_age, Total))</pre>
##
##
     return(v_r_mort_by_age)
## }
## <bytecode: 0x10d1d43f8>
## <environment: namespace:darthpack>
```

Another function in the 01_model -inputs_functions.R script, is the load_all_parms function. This function, which is actually using the load_mort_data function, loads all parameters for the decision model from multiple sources and creates a list that contains all parameters and their values.

```
print.function(load_all_params) # print the function
## function(file.init = NULL,
```

```
## function(file.init = NULL,
## file.mort = NULL){ # User defined
## ### Load initial set of initial parameters form .csv file ###
## if(!is.null(file.init)) {
```

```
##
       df_params_init <- read.csv(file = file)</pre>
##
     } else{
##
       df_params_init <- df_params_init</pre>
##
     }
##
##
     #### All-cause age-specific mortality from .csv file ####
     v_r_mort_by_age <- load_mort_data(file = file.mort)</pre>
##
##
##
     l_params_all <- with(as.list(df_params_init), {</pre>
##
       #### General setup ####
##
       v_names_str <- c("No Treatment", "Treatment") # CEA strategies</pre>
##
                    <- length(v_names_str) # Number of strategies
##
       v_age_names <- n_age_init:(n_age_init + n_t - 1) # vector with age names
##
       v_n \leftarrow c("H", "S1", "S2", "D") # vector with the 4 health states of the model:
##
                                          # Healthy (H), Sick (S1), Sicker (S2), Dead (D)
##
       n_states <- length(v_n)</pre>
                                          # number of health states
##
       v_s_{init} \leftarrow c(H = 1, S1 = 0, S2 = 0, D = 0) # initial state vector
##
       #### Create list with all parameters ####
##
       l params all <- list(</pre>
##
         v_names_str = v_names_str,
##
         n str
                      = n_str
##
         n_age_init = n_age_init,
##
         n_t
                      = n_t
##
         v_age_names = v_age_names,
##
         v_n = v_n
##
         n_states = n_states,
         v_s_{init} = c(H = 1, S1 = 0, S2 = 0, D = 0),
##
##
         v_r_mort_by_age = v_r_mort_by_age
##
       )
##
       return(l_params_all)
     }
##
     )
##
##
##
     l_params_all <- c(l_params_all,</pre>
##
                         df_params_init) # Add initial set of parameters
## }
## <bytecode: 0x10d1c3118>
## <environment: namespace:darthpack>
```

The load_all_params function is informed by the arguments file.init and file.mort. The file.init argument is a string with the location and name of the file with initial set of parameters. The initial parameter values for our case-study are stored in the 01_init-params.csv file located in the data directory. The load_all_params function read this .csv file into the function environment as a dataframe called, df_params_init.

The file.mort argument is a string with the location and name of the file with mortality data. As described before, in our case-study this is the 01_all -cause-mortality.csv file. Within the load_all_parms function, the load mort data function is used to create a vector with mortality rates from the .csv data.

After loading all the information, the load_all_params generates a list called,l_params_all, including all parameters for the model including the general setup parameters and the vector of mortality rates. The function also stores the dataframe df_params_init with the initial set of parameters in the list. This is all executed in the in the 01_model-inputs.R script by running the code below.

```
l_params_all <- load_all_params()</pre>
```

For the Sick-Sicker model we do not have to estimate parameters, but we do have three parameters that need to be estimated via model calibration. In this stage of the framework, we simply set these parameters to valid "dummy" values that are compatible with the next phase of the analysis, model implementation, but are ultimately just placeholder values until we conduct the calibration phase. This means that these values will be replaced by the best-fitted calibrated values after we performed the calibration in component 3.

Using a function to create a list of base-case parameters to have all model parameters in a single object is very useful, because this object will have to be updated for the calibration and the different sensitivity analyses in components 3 and 5 of the framework, respectively. Below, we guide you through the components of the function.

Chapter 2

Decision model

In this second component, we build the backbone of the decision analysis: the implementation of the model. This component is performed by the $02_simulation_model.R$ script. This file itself is not very large. It simply loads some packages and sources the input from component 01 and in addition it runs the decision_model function that is used to caputre the dynamic process of the Sick-Sicker example and stores the output. The output of the model is the traditional cohort trace. The trace describes how the cohort is distributed among the different health states over time and is plotted at the end of this script.

The function decision_model is defined in the 02_simulation_model_functions.R file in the R folder. As described in the paper, constructing a model as a function at this stage facilitates subsequent stages of the model development and analysis. This since these processes will all call the same model function, but pass different parameter values and/or calculate different final outcomes based on the model outputs. In the next part, we will describe the code within the function.

```
print.function(decision_model) # print the code of the function
```

```
## function(l_params_all, err_stop = FALSE, verbose = FALSE){ # User defined
##
     ### Definition:
##
     ##
          Decision model implementation function
     ### Arguments:
##
##
          l_params_all: List with all parameters of decision model
     ##
##
     ##
          verbose: Logical variable to indicate print out of messages
##
     ### Returns:
##
     ##
          a_P: Transition probability array
##
     ##
          m_M: Matrix cohort trace
##
##
     with(as.list(l_params_all), {
       #### Error checking ####
##
       if ((n_t + n_age_init) > nrow(v_r_mort_by_age)) {
##
##
         stop("Not all the age in the age range have a corresponding mortality rate")
       }
##
##
```

```
if ((sum(v_s_init) != 1) | !all(v_s_init >= 0)) {
##
##
         stop("vector of initial states (v_s_init) is not valid")
##
       }
##
       #### Age-specific transition probabilities ####
##
##
       # Mortality for healthy individuals
       p_HDage <-1 - exp(-v_r_mort_by_age[(n_age_init + 1) + 0:(n_t - 1)])
##
##
       # Mortality for sick individuals
##
       p_S1Dage \leftarrow 1 - exp(-v_r_mort_by_age[(n_age_init + 1) + 0:(n_t - 1)] * hr_S1)
##
       # Mortality for sicker individuals
##
       p_S2Dage \leftarrow 1 - exp(-v_r_mort_by_age[(n_age_init + 1) + 0:(n_t - 1)] * hr_S2)
##
##
       #### Create age-specific transition probability matrices in an array ####
##
       # Initialize array
##
       a_P <- array(0, dim = c(n_states, n_states, n_t),</pre>
                    dimnames = list(v_n, v_n, 0:(n_t-1))
##
##
       # Fill in array
##
       # From H
##
       a_P["H", "H", ] <- (1-p_HDage) * (1 - p_HS1)
       a_P["H", "S1", ] <- (1-p_HDage) * p_HS1
##
##
       a_P["H", "D", ] <- p_HDage
       # From S1
##
##
       a_P["S1", "H", ] <- (1-p_S1Dage) * p_S1H
##
       a_P["S1", "S1", ] \leftarrow (1-p_S1Dage) * (1 - (p_S1S2 + p_S1H))
       a_P["S1", "S2", ] <- (1-p_S1Dage) * p_S1S2
##
##
       a_P["S1", "D", ] <- p_S1Dage
##
       # From S2
       a_P["S2", "S2", ] <- 1 - p_S2Dage
##
##
       a_P["S2", "D", ] <- p_S2Dage
##
       # From D
       a_P["D", "D", ] <- 1
##
##
##
       #### Check if transition array is valid ####
       check_transition_probability(a_P, err_stop = err_stop, verbose = verbose)
##
##
       check_sum_of_transition_array(a_P, n_states, n_t, err_stop = err_stop, verbose = verbose)
##
##
       #### Compute cohort trace matrix and transition array for age-dependent STM ####
##
       # Initialize cohort trace matrix
##
       m_M <- matrix(0,</pre>
##
                     nrow = (n_t + 1), ncol = n_states,
##
                     dimnames = list(0:n_t, v_n))
##
       # Set first row of m.M with the initial state vector
       m_M[1, ] <- v_s_init
##
```

```
##
##
       # Iterate STM over time
##
       for(t in 1:n t){
         m_M[t + 1, ] \leftarrow m_M[t, ] %*% a_P[, , t]
##
##
##
       return(list(a_P = a_P,
##
                    m M = m M)
     }
##
##
     )
## }
## <bytecode: 0x109a97998>
## <environment: namespace:darthpack>
```

The decision_model function is informed by the argument 1_params_all. Via this argument we give the function a list with all parameters of the decision model. For the Sick-Sicker model, these parameters are stored in the list 1_params_all, which we passed into the function as shown below.

```
1_out_stm <- decision_model(1_params_all = 1_params_all) # run the function</pre>
```

This function itself has all the mathematical equations of the decision models coded inside. It starts by calculating the age-specific transition probabilities from all non-dead states based on the vector of age-specific mortality rates v_r_mort_by_age. These parameters will become vectors of length n_t, describing the probability to die for all ages from all non-dead states.

The next part of the function, creates an array that stores age-specific transition probability matrices in each of the third dimension. The transition probability matrix is a core component of a state-transition cohort model (Iskandar, 2018). This matrix contains the probabilities of transitioning from the current health state, indicated by the rows, to the other health states, specified by the columns. Since we have age-specific transition probabilities, the transition probability matrix is different each cycle. These probabilities are only depending on the age of the cohort, and not on other events; therefore, we can generate all matrices at the start of the model. This results in n_t different age-specific matrices that are stored in an array, called a_P, of dimensions n_states x n_states x n_t. After initializing the array, it is filled with the transition probability stored in the list. When running the model, we can index the correct transition probability matrix corresponding with the current age of the cohort. We then added some sanity checks to make sure that the transition matrices and the transition probabilities are valid. The first three and last cycles of the transition probability matrices stored in the array a.P are shown below.

```
1_out_stm$a_P[, , 1:3] # show the first three time-points of a_P
```

```
##
##
      1
##
##
            Η
                    S1
                             S2
                                         D
## H 0.8491513 0.1498502 0.0000000 0.0009985012
## S1 0.4985037 0.3938180 0.1046858 0.0029925135
  S2 0.0000000 0.0000000 0.9900597 0.0099402657
##
##
  , , 2
##
##
            Η
                    S1
                             S2
                                        D
## H 0.8490910 0.1498396 0.0000000 0.001069428
## S1 0.4983976 0.3937341 0.1046635 0.003204853
## S2 0.0000000 0.0000000 0.9893570 0.010642959
1_out_stm$a_P[, , 1_params_all$n_t] # show it for the last cycle
##
            Н
                    S1
                              S2
## H 0.6055199 0.1068564 0.00000000 0.2876237
## S1 0.1807584 0.1427991 0.03795926 0.6384833
## S2 0.0000000 0.0000000 0.03365849 0.9663415
## D 0.0000000 0.0000000 0.00000000 1.0000000
```

By comparing these probability matrices, we observe an increase in the probabilities of transitioning to death from all health states.

After the array is filled, the cohort trace matrix, m_M, of dimensions n_t x n_states is initialized. This matrix will store the state occupation at each point in time. The first row of the matrix is informed by the initial state vector v_s_init. For the remaining points in time, we iteratively multiply the cohort trace with the age-specific transition probability matrix corresponding to the specific cycle obtained by indexing the array a_P appropriately. All the outputs and relevant elements of the decision model are stored in a list, called 1_out_stm. This list contains the array of the transition probability matrix for all cycles t and the cohort trace m_M.

5 0.7306193 0.1873106 0.07413838 0.007931783

```
## H S1 S2 D

## 70 0.009928317 0.0022433565 2.035951e-04 0.9876247

## 71 0.007153415 0.0015935925 1.311619e-04 0.9911218

## 72 0.005058845 0.0011174473 8.674540e-05 0.9937370

## 73 0.003460336 0.0007552206 5.436484e-05 0.9957301

## 74 0.002289594 0.0004937081 3.298632e-05 0.9971837

## 75 0.001475636 0.0003151589 1.985106e-05 0.9981894
```

Using the code below, we can graphically show the model dynamics by plotting the cohort trace. Figure 2.1 shows the distribution of the cohort among the different health states at each time point.

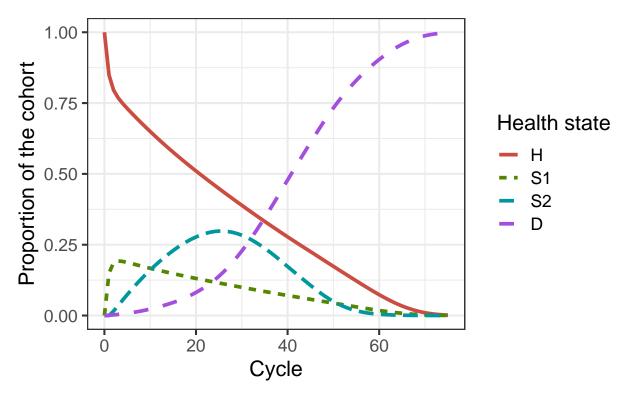


Figure 2.1: Cohort trace of the Sick-Sicker cohort model

Chapter 3

Model calibration

In this third component, we calibrate unknown model parameters by matching model outputs to specified calibration targets. Specifically, we calibrate the Sick-Sicker model to match survival, prevalence and the proportion who are Sicker, among all those afflicted (Sick+Sicker). We used a Bayesian calibration approach using the incremental mixture importance sampling (IMIS) algorithm (Steele et al., 2006), which has been used to calibrate health policy models (Raftery and Bao, 2010, Menzies et al. (2017), Rutter et al. (2018)). Bayesian methods allow us to quantify the uncertainty in the calibrated parameters even in the presence of non-identifiability (Alarid-Escudero et al., 2018). This analysis is coded in the $03_calibration.R$ file in the analysis folder. The target data is stored in the $03_calibration_targets.RData$ file. Similar to component 02 2, in the section 03.1 Load packages, we start by loading inputs and functions. In addition, we load the calibration targets data into the R workspace. In the next section, 03.2 Visualize targets, we plot each of the calibration targets with their confidence intervals.

In section 03.3 Run calibration algorithms, we set the parameters we need to calibrate to fixed values and test if the function calibration_out that produces model outputs corresponding to the calibration targets works. This function takes a vector of parameters that need to be calibrated and a list with all parameters of decision model and computes model outputs to be used for calibration routines.

```
print.function(calibration_out) # print the functions
```

```
## function(v_params_calib, l_params_all){  # User defined
    # Substitute values of calibrated parameters in base-case with
##
##
    # calibrated values
##
    l_params_all <- update_param_list(l_params_all = l_params_all, params_updated = v_params_calib)</pre>
##
    # Run model with updated calibrated parameters
##
##
    l_out_stm <- decision_model(l_params_all = l_params_all)</pre>
##
    ##
    #### Overall Survival (OS) ####
##
    v_os <- 1 - l_out_stm$m_M[, "D"]</pre>
##
##
```

```
##
    #### Disease prevalence #####
##
    v_prev <- rowSums(l_out_stm$m_M[, c("S1", "S2")])/v_os</pre>
##
##
    #### Proportion of sick in S1 state #####
    v prop S2 <- 1 out stm$m M[, "S2"] / rowSums(1 out stm$m M[, c("S1", "S2")])
##
##
    ##
    l_{out} \leftarrow list(Surv = v_{os}[c(11, 21, 31)],
##
##
                 Prev = v_prev[c(11, 21, 31)],
##
                 PropSicker = v_prop_S2[c(11, 21, 31)])
##
    return(l_out)
## }
## <bytecode: 0x10d3bb690>
## <environment: namespace:darthpack>
```

This function is informed by two argument v_params_calib and l_params_all. The vector v_params_calib contains the values of the three parameters of interest. The list l_params_all contains all parameters of the decision model. The placeholder values are replaced by v_params_calib and with these values the model is evaluated. Model evaluation takes place by running the decision_model function, described in component 02. The result in a new list with output of the model corresponding to the parameter values in the v_params_calib. With this new decision model output, the overall survival, disease prevalence and the proportion of Sicker in the Sick and Sicker states are calculated. The estimated values for these epidemiological outcomes at different timepoints are combined in a list called l_out produced but the calibration_out.

Once we make sure this code works, we specify the calibration parameters in section 03.3.1 Specify calibration parameters. These include setting the seed for the random number generation, specifying the number of random samples to obtain from the calibrated posterior distribution, the name of the input parameters and the range of these parameters that will inform the prior distributions of the calibrated parameters, and the name of the calibration targets: Surv, Prev, PropSick.

In the next section, 03.3.2 Run IMIS algorithm, we calibrate the Sick-Sicker model with the IMIS algorithm. For this case-study, we assume a normal likelihood and uniform priors. For a more detailed description of IMIS for Bayesian calibration, different likelihood functions and prior distributions, we refer the reader to the tutorial for Bayesian calibration by Menzies et al. (Menzies et al., 2017). We use the IMIS function from the IMIS package that calls the functions likelihood, sample.prior and prior, to draw samples from the posterior distribution (Raftery and Le Bao, 2012). The functions are specified in the 03_calibration_functions.R file in the R folder. For the IMIS function, we specify the incremental sample size at each iteration of IMIS, the desired posterior sample size at the resample stage, the maximum number of iterations in IMIS and the number of optimizers which could be 0. The function returns a list, which we call l_fit_imis, with the posterior samples, the diagnostic statistics at each IMIS iteration and the centers of Gaussian components (Raftery and Le Bao, 2012). We store the posterior samples in the matrix m_calib_post.

We then explore these posterior distributions in section 03.4 Exploring posterior distribution. We start by estimating the posterior mean, median and 95% credible interval, the mode and the maximum-a-posteriori (MAP). All for these summary statistics are combined in a dataframe called df_posterior_summ. Table 3.1

Table 3.1: Summary statistics of the posterior distribution

	Mean	2.5%	50%	97.5%	Mode	MAP
S1S2	0.1076687	0.0964559	0.1073187	0.1196543	0.1067639	0.107841
hr_S1	2.7261594	1.1010910	2.6790446	4.4020812	2.2857230	2.297053
hr_S2	9.6232710	7.3427361	9.6461532	11.9533402	9.4629634	9.886776

shows the summary statistics of the posterior distribution.

In section 03.4.2 Visualization of posterior distribution, we generate a pairwise scatter plot of the calibrated parameters (Figure 3.2) and a 3D scatter plot of the joint posterior distribution (Figure 3.1). These figures are saved in the figs directory.

Finally, the posterior distribution and MAP estimate from the IMIS calibration are stored in the file $03_imis_output.RData$. Storing this data as an .Rdata file allows to import the data in following sections without needing to re-run the calibration component.

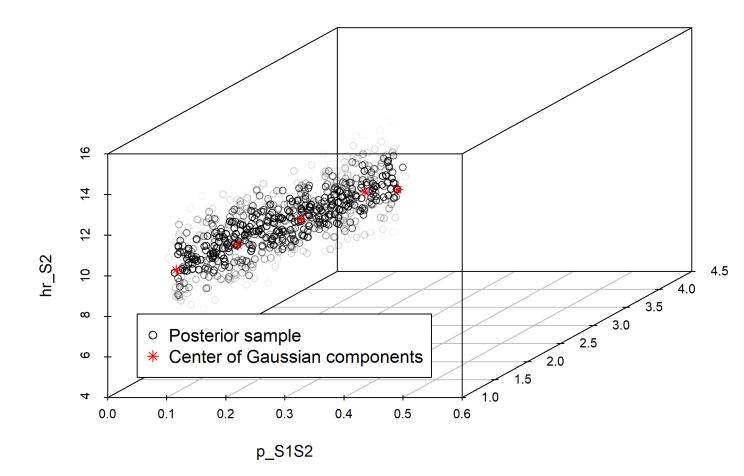


Figure 3.1: Joint posterior distribution

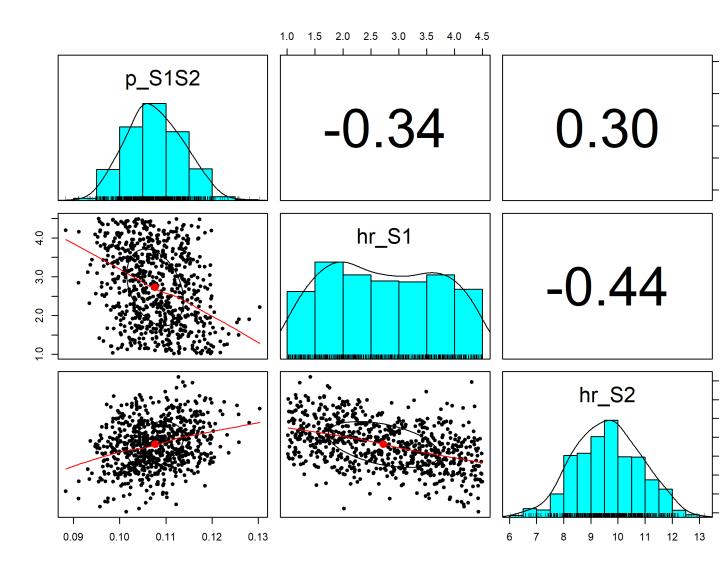


Figure 3.2: Pairwise posterior distribution of calibrated parameters

Chapter 4

Validation

In this forth component, we check the internal validity of our Sick-Sicker model before we move on to the analysis components. To internally validate the Sick-Sicker model, we compare the model-predicted output evaluated at posterior parameters against the calibration targets. This is all done in the 04_validation.R script in the analysis folder.

In section 04.2 Compute model-predicted outputs, we compute the model-predicted outputs for each sample of posterior distribution as well as for the MAP estimate. We then use the function data_summary to summarize the model-predicted posterior outputs into different summary statistics.

print.function(data_summary)

```
## function(data, varname, groupnames){
##
     summary_func <- function(x, col){</pre>
##
       c(mean = mean(x[[col]], na.rm = TRUE),
##
         median = quantile(x[[col]], probs = 0.5, names = FALSE),
         sd = sd(x[[col]], na.rm=TRUE),
##
##
         lb = quantile(x[[col]], probs = 0.025, names = FALSE),
         ub = quantile(x[[col]], probs = 0.975, names = FALSE))
##
     }
##
##
     data_sum <- plyr::ddply(data, groupnames, .fun = summary_func,</pre>
##
                        varname)
     data_sum <- plyr::rename(data_sum, c("mean" = varname))</pre>
##
##
     return(data_sum)
## }
## <bytecode: 0x10d41ca58>
## <environment: namespace:darthpack>
```

This function is informed by three arguments, data, varname and groupnames.

The computation of the model-predicted outputs using the MAP estimate is done by inserting the v_calib_post_map data into the previously described calibration_out function. This function creates a list including the estimated values for survival, prevalence and the proportion of sicker individuals at cycles

10, 20 and 30.

In sections 04.6 Internal validation: Model-predicted outputs vs. targets, we check the internal validation by plotting the model-predicted outputs against the calibration targets (Figures 4.1-4.3). The generated plots are saved as .png files in the fig folder. These files can be used in reports without the need of re-running the code.

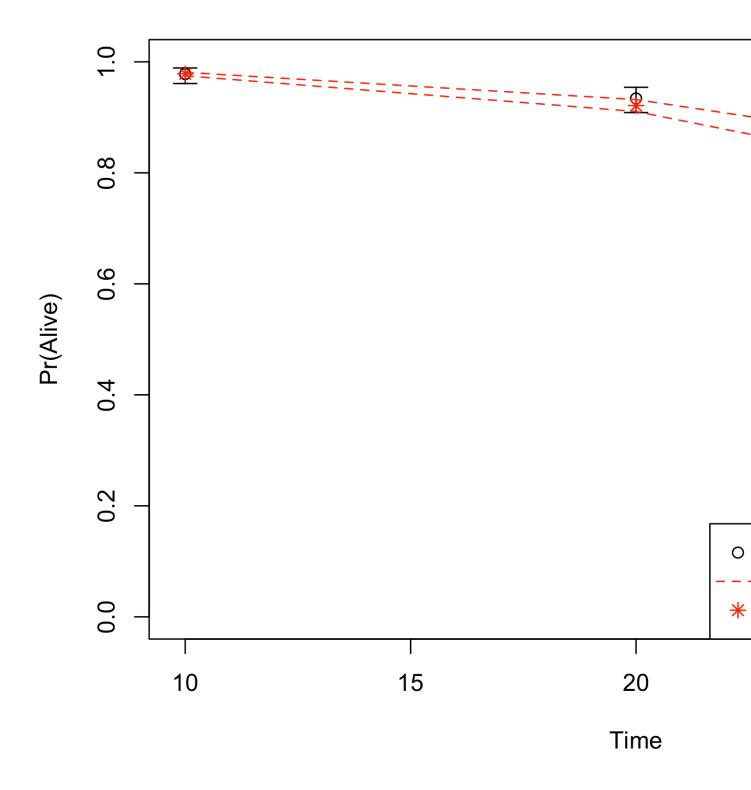


Figure 4.1: Survival data: Model-predicted outputs vs targets.

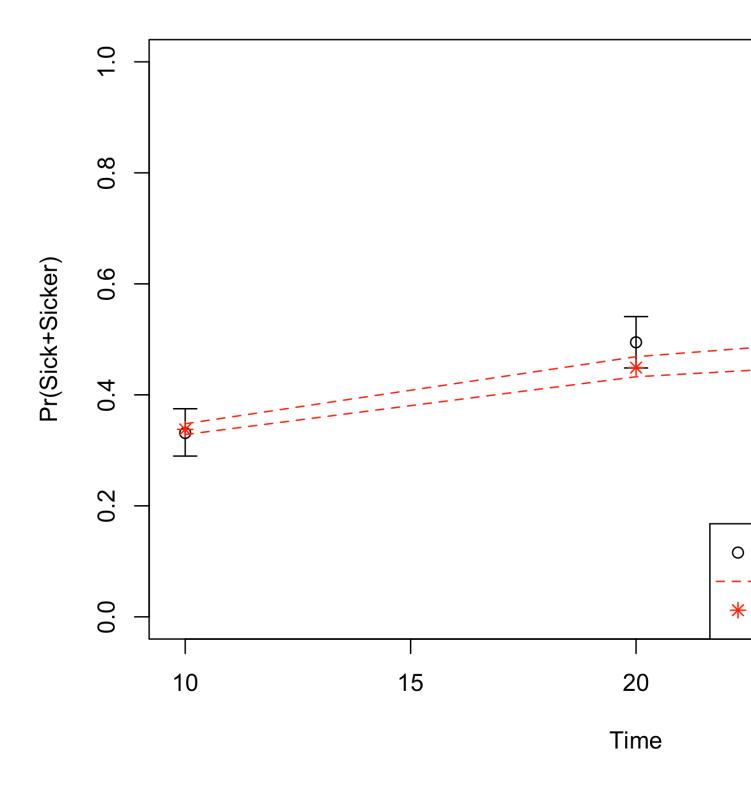


Figure 4.2: Prevalence data of sick individuals: Model-predicted output vs targets.

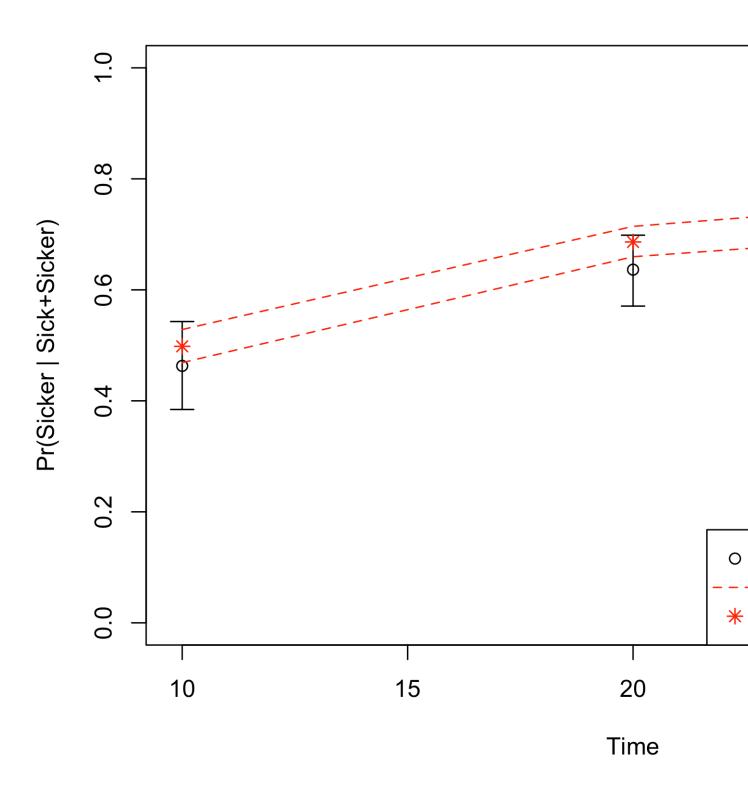


Figure 4.3: Proportion who are Sicker, among all those afflicted (Sick + Sicker): Model-predicted output.

Chapter 5

Analysis

The analysis component is where the elements in components 1-4 are combined to answer the question(s) of interest given current information and to quantify the value of potential further research. Our framework separates the analysis in three subcomponents: 05a Deterministic analysis, 05b Uncertainty analysis and 05c Value of information analysis. For the Sick-Sicker case-study, we use all three subcomponents to conduct the CEA and to quantify the uncertainty of our decision. For procedures in the CEA, we rely on the R package dampack, which is available here: https://github.com/DARTH-git/dampack. Instructions for installing dampack are described in Appendix 0 provided in the $app0_packages_setup.R$ script of the analysis folder.

5.1 05a Deterministic analysis

In this subcomponent, we perform a deterministic CEA, followed by some deterministic sensitivity analysis, including one-way, two-way and tornado sensitivity analyses. The function script of this subcomponent, $05a_deterministic_analysis_function.R$, contains the function calculate_ce_out. This function calculates costs and effects for a given vector of parameters using a simulation model. We need to run our simulation model using the calibrated parameter values, but the list we created in component 01 1 still contain the placeholder values for the calibrated parameters. This means we need to update these values by the calibrated values stored in the vector v_calib_post_map. The function update_param_list updates the list of parameters with new values for some specific parameters.

```
print.function(update_param_list)
```

```
## function(l_params_all, params_updated){
##

## if (typeof(params_updated)!="list"){
## params_updated <- split(unname(params_updated),names(params_updated)) #converte the named vector
## }

## l_params_all <- modifyList(l_params_all, params_updated) #update the values
## return(l_params_all)
## }</pre>
```

```
## <bytecode: 0x112beee78>
## <environment: namespace:darthpack>
```

The first argument of the function, called 1_params_all, is a list with all the parameters of decision model. The second argument, params_updated, is an object with parameters for which values need to be updated. The function returns the list 1_params_all with updated values.

In the 05a_deterministic_analysis.R script we execute the update_param_list function for our case-study, resulting in the list 1_params_basecase where the placeholder values for p_S1S2, hr_S1 and hr_S2 are replaced by the calibration estimates.

```
1_params_basecase <- update_param_list(l_params_all, v_calib_post_map)</pre>
```

We use this new list as an argument in the calculate_ce_out function. In addition, we specify the willingness-to-pay (WTP) threshold value using the n_wtp argument of this function. This WTP value is used to compute a net monetary benefit (NMB) value. If the user does not specify the WTP, a default value of \$100,000/QALY will be used by the function.

```
## function(l_params_all = load_all_params(),
##
                                  n_{wtp} = 100000){ # User defined
     with(as.list(l_params_all), {
##
##
       ## Create discounting vectors
##
       v_dwc \leftarrow 1 / ((1 + d_e) \hat{} (0:(n_t))) # vector with discount weights for costs
       v_dwe \leftarrow 1 / ((1 + d_c) \hat{} (0:(n_t))) # vector with discount weights for QALYs
##
##
##
       ## Run STM model at a parameter set for each intervention
##
       l_model_out_no_trt <- decision_model(l_params_all = l_params_all)</pre>
                          <- decision_model(l_params_all = l_params_all)</pre>
##
       l model out trt
##
       ## Cohort trace by treatment
##
       m_M_no_trt <- l_model_out_no_trt$m_M # No treatment</pre>
##
##
       m_M_{trt}
                   <- l_model_out_trt$m_M
                                               # Treatment
##
##
       ## Vectors with costs and utilities by treatment
       v_u_no_trt <- c(u_H, u_S1, u_S2, u_D)</pre>
##
                   <- c(u_H, u_Trt, u_S2, u_D)
       v_u_trt
##
##
       v_c_{no}trt <- c(c_H, c_S1, c_S2, c_D)
##
                   <- c(c_H, c_S1 + c_Trt, c_S2 + c_Trt, c_D)
##
       v_c_trt
##
##
       ## Mean Costs and QALYs for Treatment and NO Treatment
       v_tu_no_trt <- m_M_no_trt %*% v_u_no_trt
##
```

```
##
                    <- m_M_trt %*% v_u_trt
       v_tu_trt
##
##
       v_tc_no_trt <- m_M_no_trt %*% v_c_no_trt</pre>
##
       v tc trt
                    <- m_M_trt %*% v_c_trt
##
##
       ## Total discounted mean Costs and QALYs
       tu d no trt <- t(v tu no trt) %*% v dwe
##
                    <- t(v_tu_trt) %*% v_dwe
##
       tu d trt
##
##
       tc_d_no_trt <- t(v_tc_no_trt) %*% v_dwc
                    <- t(v_tc_trt)
                                       %*% v_dwc
##
       tc_d_trt
##
##
       ## Vector with total discounted mean Costs and QALYs
##
       v_tc_d <- c(tc_d_no_trt, tc_d_trt)</pre>
##
       v_tu_d <- c(tu_d_no_trt, tu_d_trt)</pre>
##
##
       ## Vector with discounted net monetary benefits (NMB)
##
       v_nmb_d <- v_tu_d * n_wtp - v_tc_d</pre>
##
##
       ## Dataframe with discounted costs, effectiveness and NMB
##
       df_ce <- data.frame(Strategy = v_names_str,</pre>
##
                             Cost
                                       = v_tc_d
##
                             Effect
                                       = v_tu_d,
##
                             NMB
                                       = v_nmb_d)
##
##
       return(df_ce)
     }
##
     )
##
## }
## <bytecode: 0x11b382670>
## <environment: namespace:darthpack>
```

After calculating the discount weights, this function runs the simulation model using the previously described function decision_model in the $02_simulatiomn_model_function.R$ script. Inside the function calculate_ce_out, the simulation model is run for both the treatment, l_model_out_trt, and no treatment, l_model_out_no_trt, strategies of the Sick-Sicker model. Running it for both treatment strategies is done for illustration purposes. In this case-study, the resulting cohort traces are identical and we could have executed it only once.

In the second part of the function we create multiple vectors for both the cost and effects of both strategies. These vectors multiply the cohort trace to compute the cycle-specific rewards. This results in vectors of total costs (v_tc) and total effects (v_tu) per cycle. By multiplying these vectors with the vectors with the discount weights for costs (v_dwc) and effects (v_dwe) we get the total discounted mean costs (tc_d_no_trt and tc_d_trt) and QALYs (tu_d_no_trt and tu_d_trt) for both strategies. These values are used in the

Table 5.1: Deterministic cost-effectiveness analysis results of the Sick-Sicker model comparing no treatment with treatment.

Strategy	Cost	Effect	Inc_Cost	Inc_Effect	ICER
No Treatment	115239.8	20.02366	NA	NA	NA
Treatment	214157.6	20.72299	98917.83	0.6993333	141445.9

calculation of the NMB. Finally, the total discounted costs, effectiveness and NMB are combined in the dataframe df_ce. The results for our case-study are shown below.

```
df_out_ce # print the dataframe

## Strategy Cost Effect NMB

## 1 No Treatment 115239.8 20.02366 2888309

## 2 Treatment 214157.6 20.72299 2894291
```

This dataframe of CE results can be used as an argument in the calculate_icers function from the dampack package to calculate the incremental cost-effectiveness ratios (ICERs) and noting which strategies are weakly and strongly dominated. Table 5.1 shows the result of the deterministic CEA.

Finally, Figure 5.1 shows the cost-effectiveness frontier of the CEA.

We then conduct a series of deterministic sensitivity analysis. First, we conduct a one-way sensitivity analysis (OWSA) on the variables c_Trt, p_HS1, u_S1 and u_Trt and a two-way sensitivity analysis (TWSA) using the owsa_det and twsa_det functions. We use the output of these functions to produce different SA plots, such as OWSA tornado, one-way optimal strategy and TWSA plots (Figures 5.2 - 5.5).

5.2 05b Probabilistic analysis

In this subcomponent, we evaluate decision uncertainty by propagating the uncertainty through the CEA using probabilistic sensitivity analysis (PSA). Until now we used the parameter values as described in Table 1.1. However, we are uncertain about these values. Most of these input parameters are defined by probability distribution as described in Table 5.2.

Table 5.2: Description of parameters with their R name and distribution.

Parameter	R name	Distribution	
Annual transition probabilities			
- Disease onset (H to S1)	p_HS1	beta(30, 170)	
- Recovery (S1 to H)	p_S1H	beta(60, 60)	
Annual costs			

Parameter	R name	Distribution
- Healthy individuals	c_H	gamma(shape =
		100, scale = 20)
- Sick individuals in S1	c_S1	<pre>gamma(shape =</pre>
		177.8, scale =
		22.5)
- Sick individuals in S2	c_S2	<pre>gamma(shape =</pre>
		225, scale =
		66.7)
- Additional costs of sick individuals treated	c.Trt	gamma(shape =
in S1 or S2		73.5, scale =
		163.3)
Utility weights		
- Healthy individuals	u_H	truncnorm(mean =
		1, sd = 0.01, b =
		1)
- Sick individuals in S1	u_S1	truncnorm(mean =
		0.75, sd = 0.02 ,
		b = 1
- Sick individuals in S2	u_S2	truncnorm(mean =
		0.50, sd = 0.03 ,
		b = 1
Intervention effect		
- Utility for treated individuals in S1	u_Trt	truncnorm(mean =
		0.95, sd = 0.02 ,
		b = 1)

In a PSA we sample the input parameter values from these distributions and we then run the model at each sample. In the file 05b_uncertainty_analysis_functions.R we created a single function, called generate_psa_params. This function generates a PSA dataset for all the CEA input parameters. We specify the number of PSA samples via the n_sim argument. The function also accepts specifying a seed to allow reproducibility of the results.

```
print.function(generate_psa_params) # print the function
```

```
## function(n_sim = 1000, seed = 20190220){ # User defined
## ## Load calibrated parameters
## data("m_calib_post")
## n_sim <- nrow(m_calib_post)
## set_seed <- seed
## df_psa_params <- data.frame(
## ### Calibrated parameters
## m_calib_post,</pre>
```

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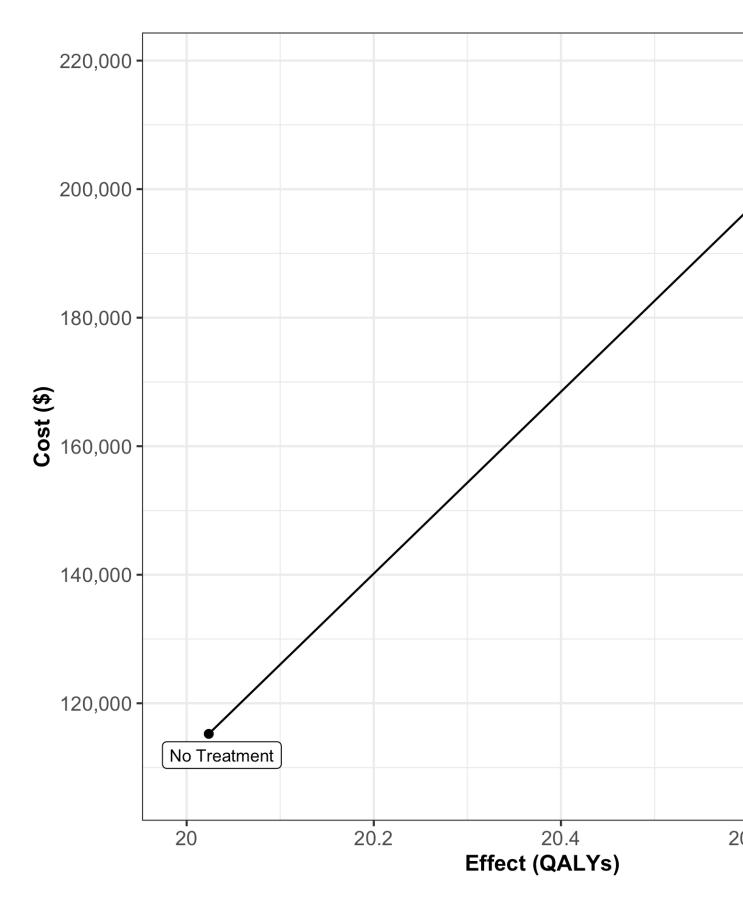
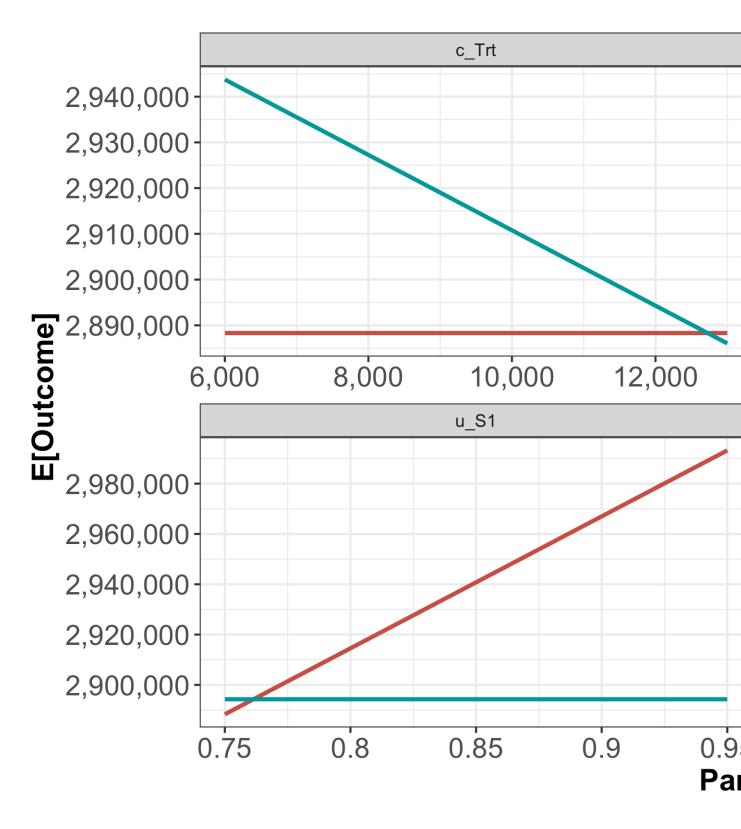


Figure 5.1: Cost-effectiveness frontier.



Strategy -

Figure 5.2: One-way sensitivity analysis results

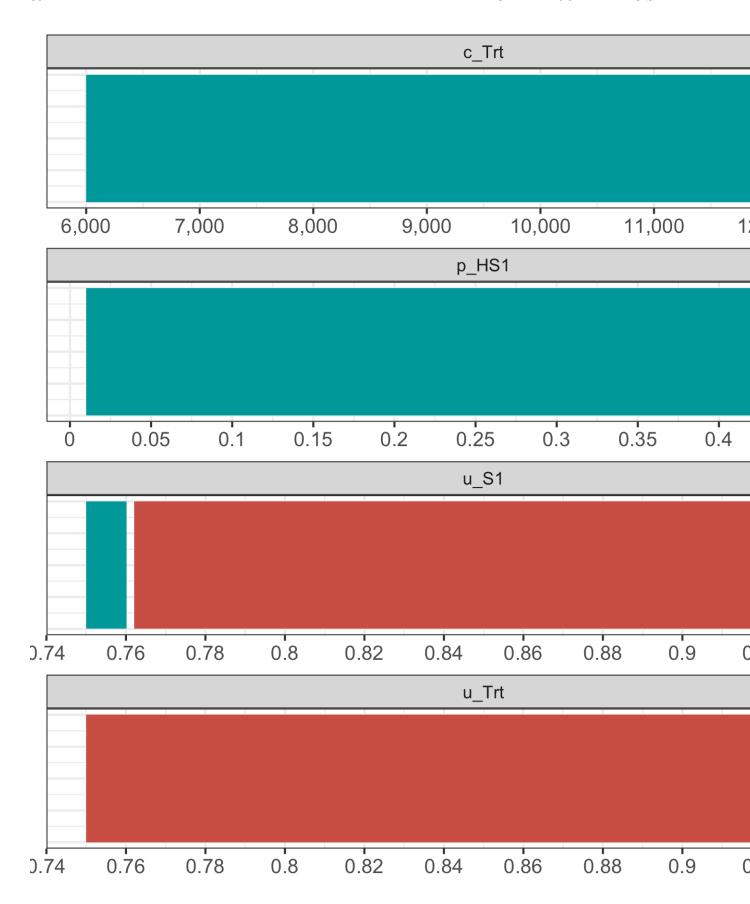


Figure 5.3: The optimal strategy with OWSA

Strategy: Treatment

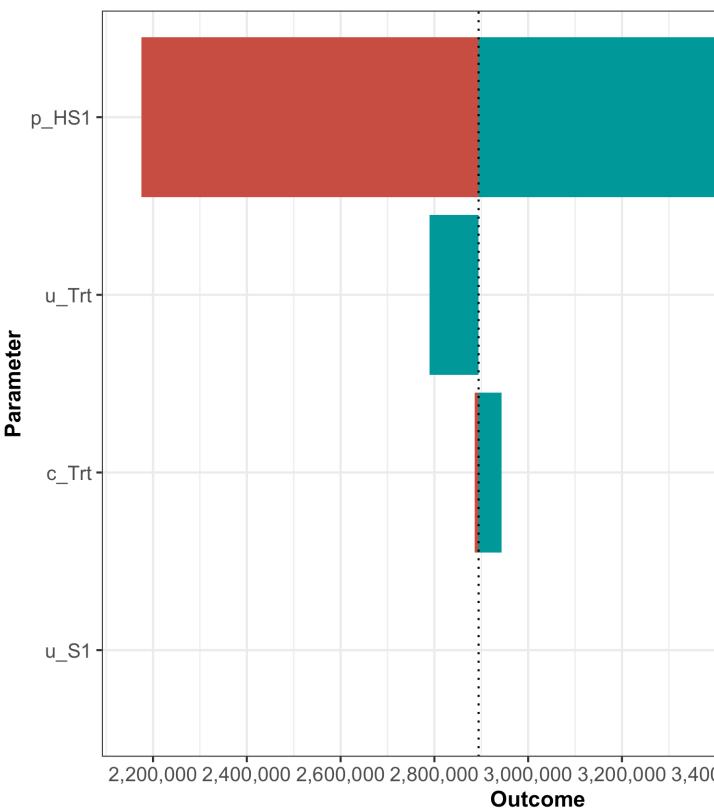


Figure 5.4: The tornado plot

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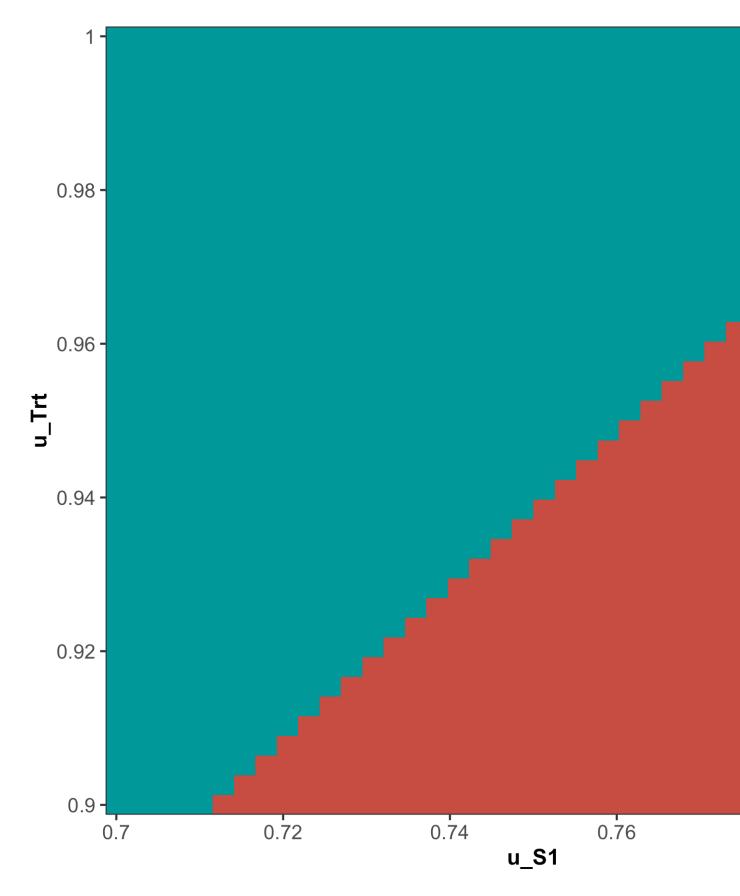


Figure 5.5: Two-way sensitivity results.

```
##
       ### Transition probabilities (per cycle)
##
##
       p HS1
               = rbeta(n_sim, 30, 170),
                                               # probability to become sick when healthy
##
       p S1H
               = rbeta(n sim, 60, 60),
                                               # probability to become healthy when sick
##
##
       ### State rewards
##
       ## Costs
            = rgamma(n_sim, shape = 100, scale = 20) , # cost of remaining one cycle in state H
##
       сН
##
       c_S1 = rgamma(n_sim, shape = 177.8, scale = 22.5), # cost of remaining one cycle in state S1
##
       c_S2 = rgamma(n_sim, shape = 225, scale = 66.7) , # cost of remaining one cycle in state S2
       c_Trt = rgamma(n_sim, shape = 73.5, scale = 163.3), # cost of treatment (per cycle)
##
##
       c_D
           = 0
                                                          , # cost of being in the death state
##
       ## Utilities
##
       u_H
            = truncnorm::rtruncnorm(n_sim, mean =
                                                      1, sd = 0.01, b = 1), # utility when healthy
##
       u S1 = truncnorm::rtruncnorm(n sim, mean = 0.75, sd = 0.02, b = 1), # utility when sick
       u_S2 = truncnorm::rtruncnorm(n_sim, mean = 0.50, sd = 0.03, b = 1), # utility when sicker
##
##
      u_D
           = 0
                                                                , # utility when dead
##
       u_Trt = truncnorm::rtruncnorm(n_sim, mean = 0.95, sd = 0.02, b = 1) # utility when being treate
##
     )
##
     return(df_psa_params)
## }
## <bytecode: 0x1177ccb20>
## <environment: namespace:darthpack>
```

The function returns the df_psa_input dataframe with a PSA dataset of the input parameters. With this dataframe we can run the PSA to produce distributions of costs, effectiveness and NMB. The PSA is performed by the <code>05b_probabilistic_analysis.R</code> script. As shown in the code below, the df_psa_input dataframe is used by the update_param_list function to generate the corresponding list of parameters for the PSA. For each simulation, we perfrom three steps. First, the list of parameters is updated by the update_param_list function. Second, the model is executed by the calculate_ce_out function using the updated parameter list and third, the dataframes df_c and df_e store the estimated cost and effects, respectively. The final part of this loop is to satisfy the modeler when waiting on the results, by displaying the simulation progress.

```
for(i in 1:n_sim){
    l_psa_input <- update_param_list(l_params_all, df_psa_input[i, ])
    df_out_temp <- calculate_ce_out(l_psa_input)
    df_c[i, ] <- df_out_temp$Cost
    df_e[i, ] <- df_out_temp$Effect
    # Display simulation progress
    if(i/(n_sim/10) == round(i/(n_sim/10), 0)) {
        cat('\r', paste(i/n_sim * 100, "% done", sep = " "))
    }
}</pre>
```

Table 5.3: Probabilistic cost-effectiveness analysis results of the Sick-Sicker model comparing no treatment with treatment

Strategy	Cost	Effect	Inc_Cost	Inc_Effect	ICER
No.Treatment	115538.9	19.95305	NA	NA	NA
Treatment	213755.8	20.63891	98216.84	0.6858646	143201.5

We can plot the results using the plot function from dampack. Figure 5.6 shows the CE scatter plot with the joint distribution of costs and effects for each strategy and their corresponding 95% confidence ellipse.

Next, we perform a CEA using the previously used calculate_icers functions from dampack. Table 5.3 shows the results of the probabilistic CEA. In addition, we plot a cost-effectiveness plane with the frontier, the cost-effectiveness acceptability curves (CEACs) and frontier (CEAF), expected Loss curves (ELCs) (Figure @ref(fig:05b_cea_frontier_psa) - 5.9) (Alarid-Escudero et al., 2019). Followed by creating linear regression metamodeling sensitivity analysis graphs (Figure 5.10 - @ref(fig:05b-twsa-lrm-uS1-uTrt_nmb))(Jalal et al., 2013). All generated figures are shown below and stored to the figs folder.

5.3 05c Value of information

In the VOI component, the results from the PSA generated in the probabilistic analysis subcomponent are used to determine whether further potential research is needed. We use the calc_evpi function from the dampack package to calculate the expected value of perfect information (EVPI). Figure 5.14 shows the EVPI for the different WTP values.

```
evpi <- calc_evpi(wtp = v_wtp, psa = 1_psa)</pre>
```

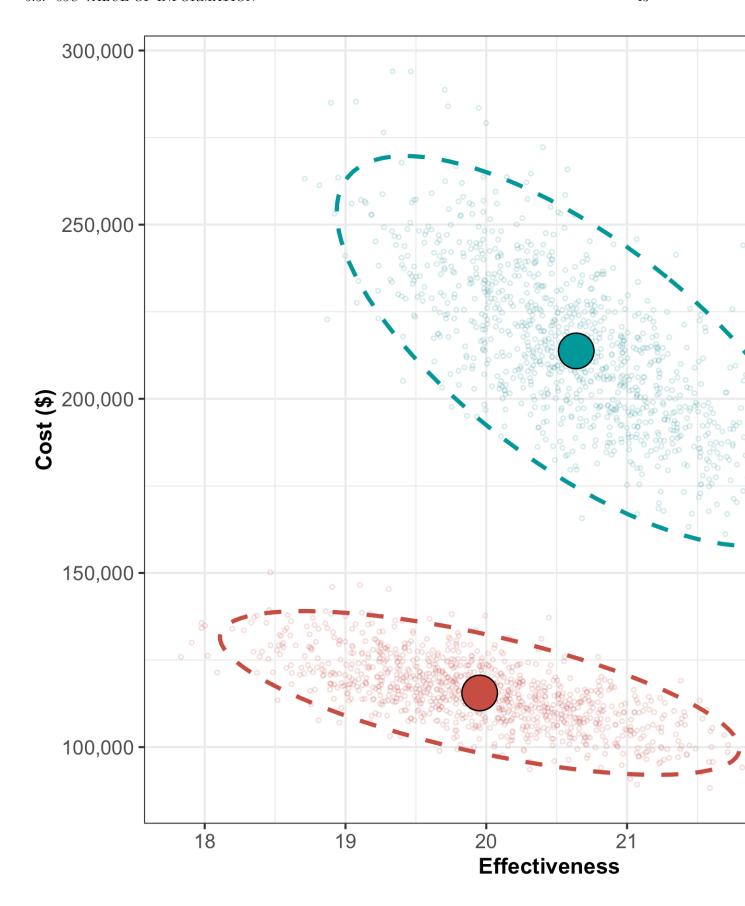


Figure 5.6: The cost-effectiveness plane graph showing the results of the probabilistic sensitivity analysis for the Sick-Sicker case-study.

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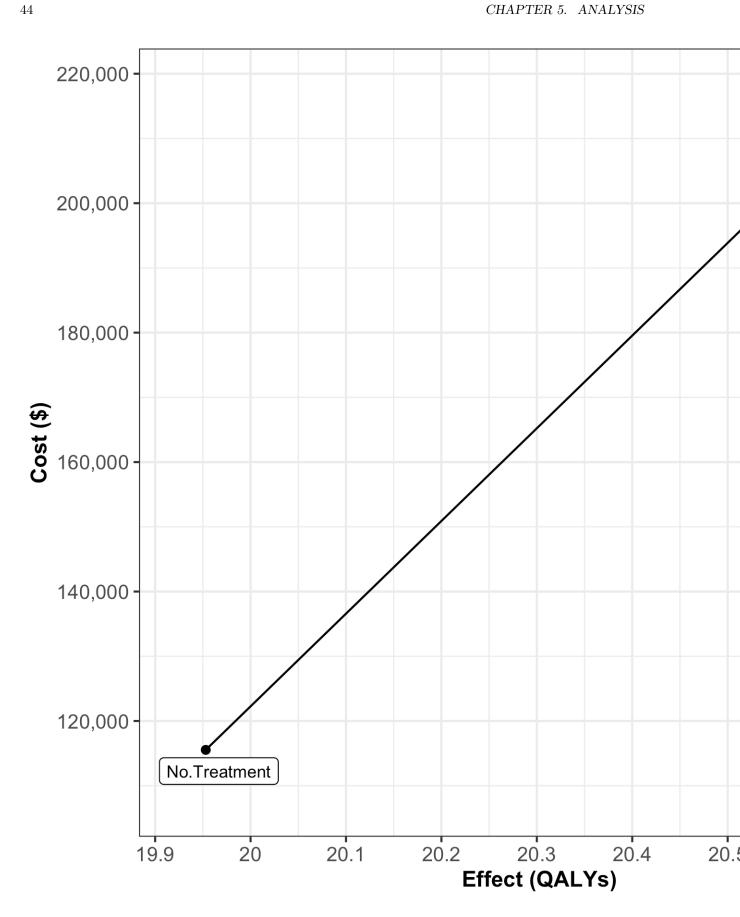


Figure 5.7: Cost-effectiveness frontier

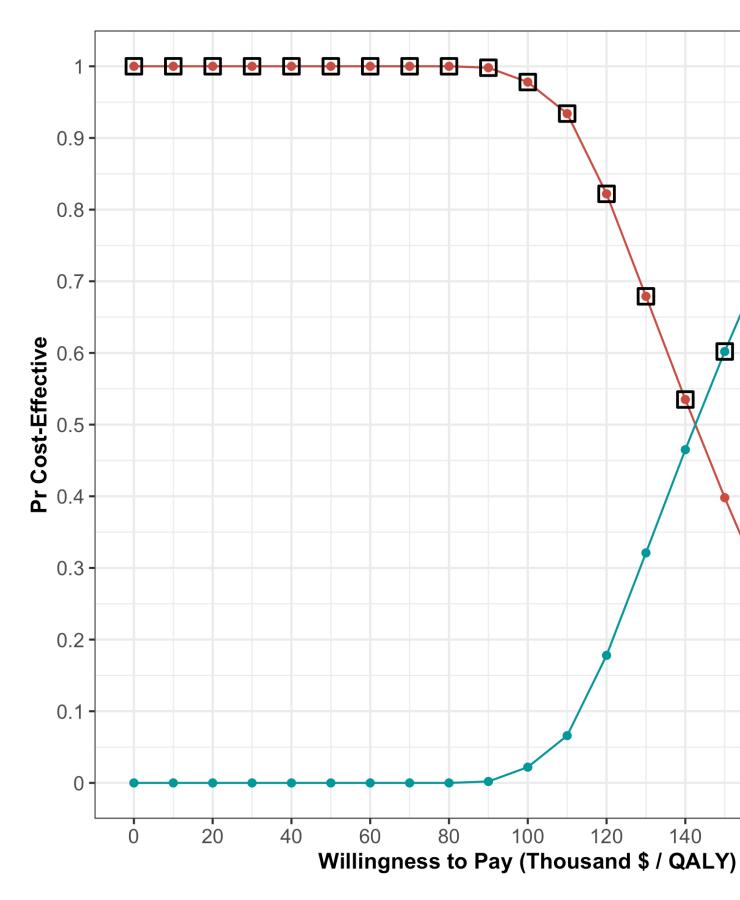


Figure 5.8: Cost-effectiveness acceptability curves (CEACs) and frontier (CEAF).

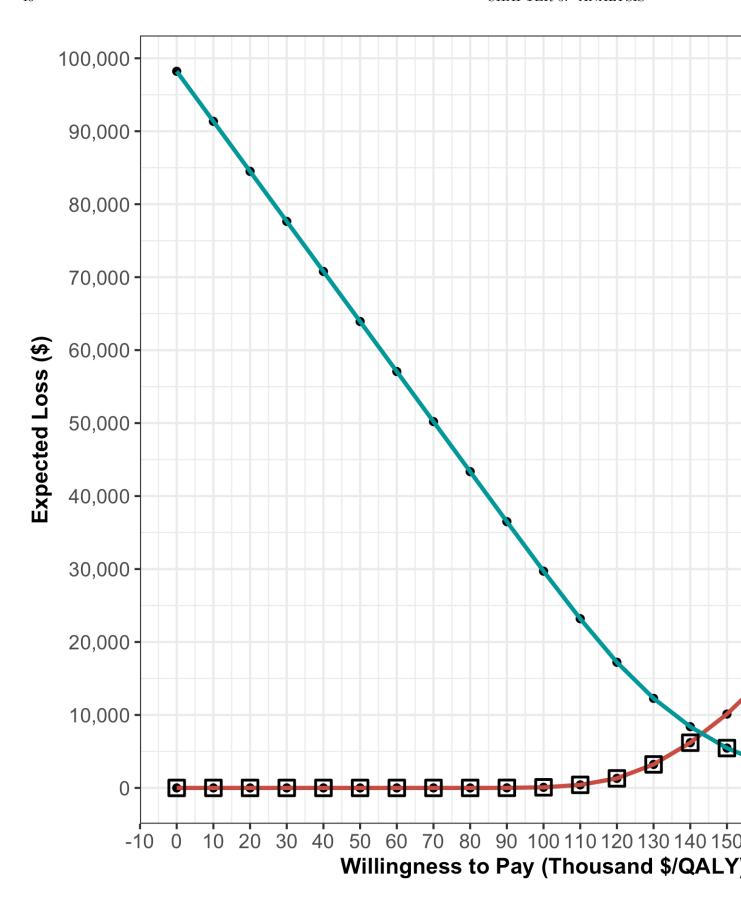
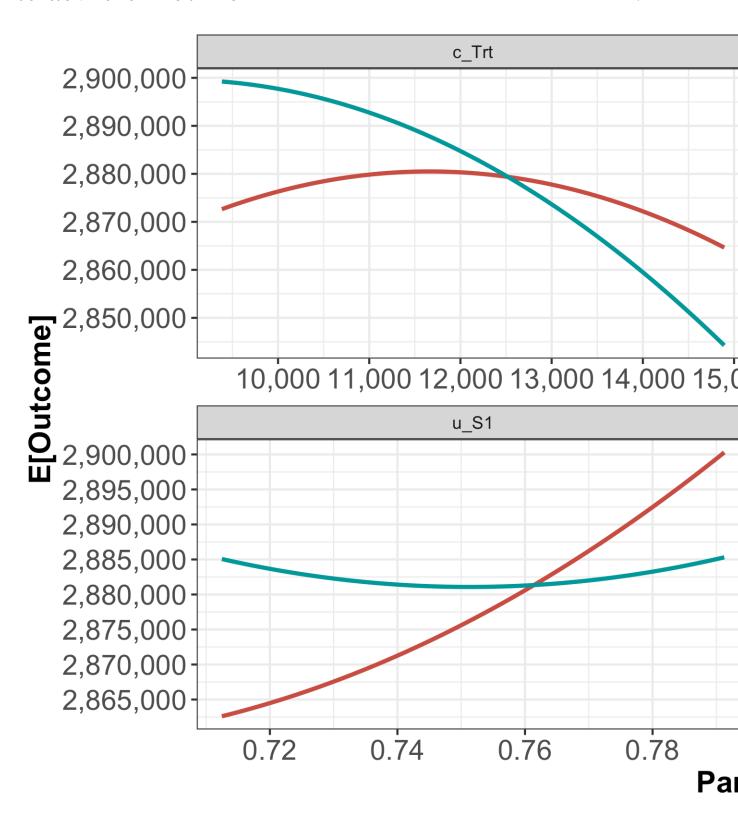


Figure 5.9: Expected Loss Curves.



Strategy -

Figure 5.10: One-way sensitivity analysis (OWSA).

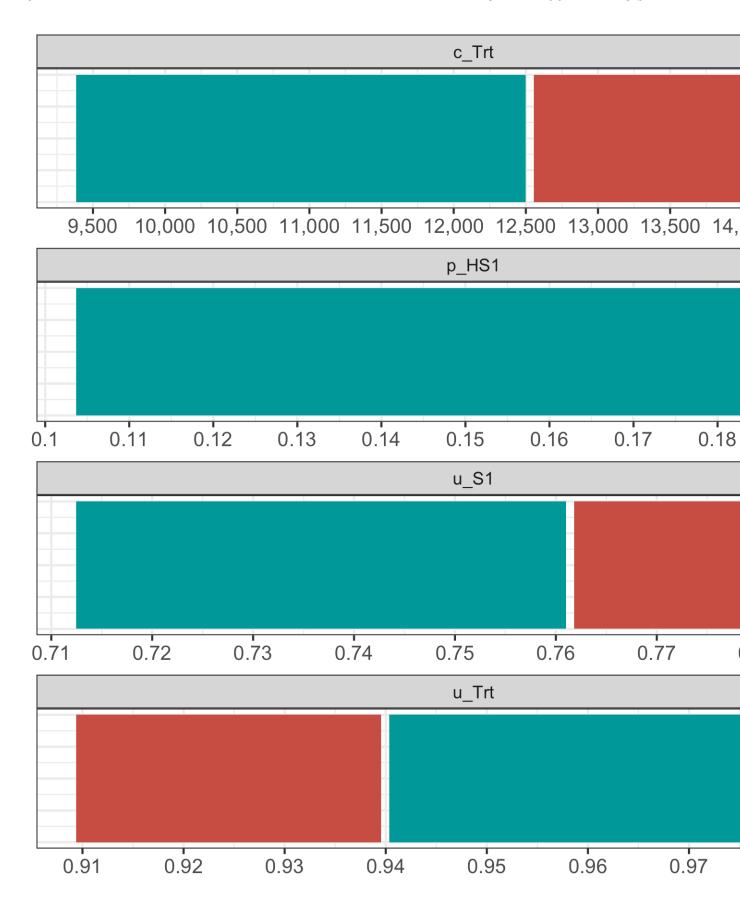


Figure 5.11: Optimal strategy with OWSA

Strategy: Treatment

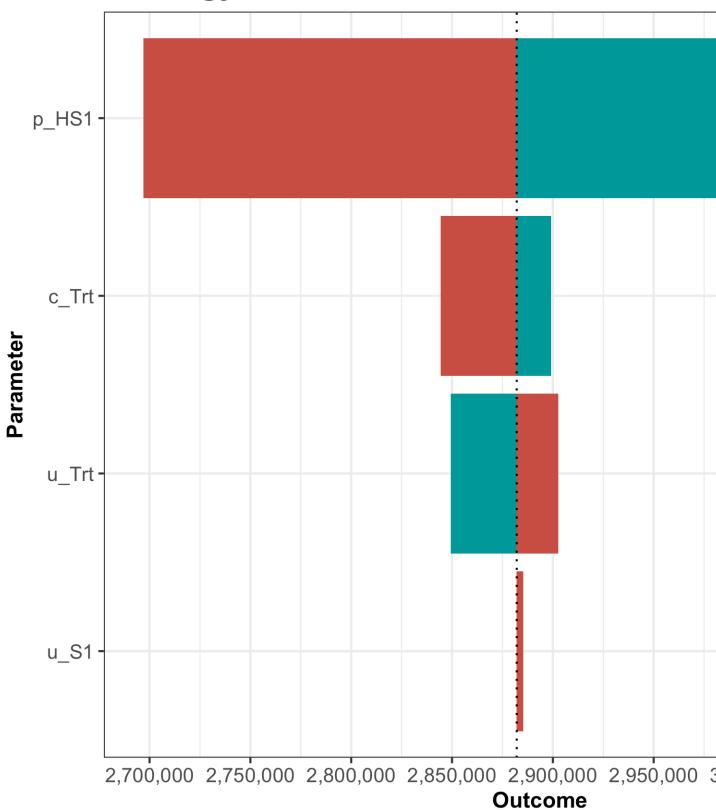


Figure 5.12: Tornado plot

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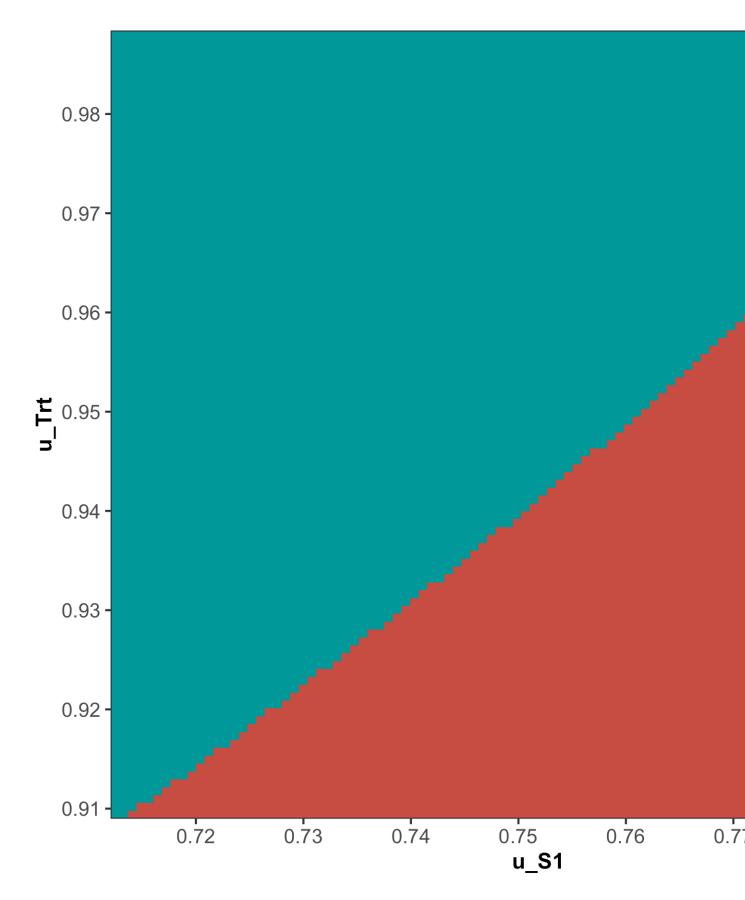


Figure 5.13: Two-way sensitivity analysis (TWSA).

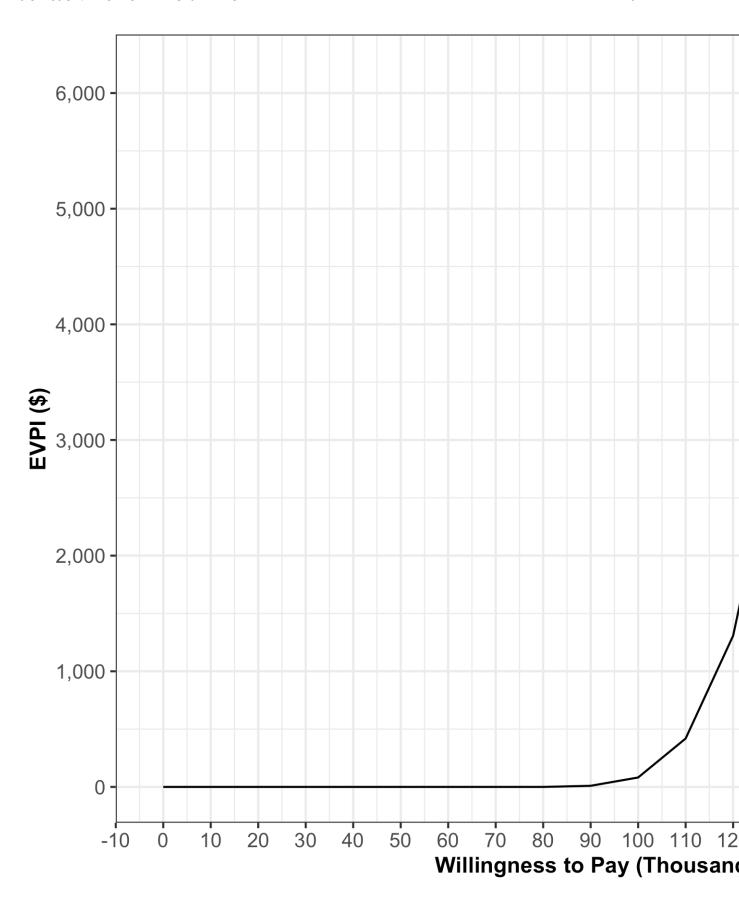


Figure 5.14: Expected value of perfect information

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