## Rule R: Atomic post-agglomerable producer

Rule R is similar to a post agglomeration rule and a formal description of Rule R is in Figure 1. In Rule R we look for a place  $p_0$  with a producer  $t_0$  such that  $t_0$  can always be followed by a firing of any consumer of  $p_0$  without inhibiting other transitions or affecting places in  $places(\varphi)$ . The producer  $t_0$  is then replaced with new transitions, one for each consumer, and these new transitions combine the effect of firing  $t_0$  and the given consumer. Similarly to an agglomeration rule, Rule R removes interleavings despite potentially increasing the size of the Petri net. However, Rule R is more general, since it only operates on one producer at a time and leaves  $p_0$  untouched, allowing tokens in  $p_0$  in the initial marking, which a post agglomeration does not. Additionally, Rule R does not require the weights of the arcs to and from the agglomerated place to be equal, making R usable in many cases.

**Theorem 1** Rule R in Figure 1 is correct for  $LTL \setminus X$ .



Precondition	Update
Fix place $p_0$ and transition $t_0$ s.t.:	
R1) $t_0 \in {}^{\bullet}p_0 \wedge p_0^{\bullet} \neq \emptyset$	UR1) For each transition $t \in p_0^{\bullet}$ create a transition $\langle t_0 t \rangle$ with the following arcs:
$R2)  ^{\bullet}p_0 \cap p_0^{\bullet} = \emptyset$	$oxed{\Box(\langle t_0 t \rangle) = \Box(t_0)}$
R3) $p_0^{\circ} = {}^{\circ}(p_0^{\bullet}) = ((p_0^{\bullet})^{\bullet})^{\circ} = \emptyset$	$\boxplus(\langle t_0 t \rangle) = \boxplus(t_0) + \boxplus(t) - \boxminus(t)$
R4) $(\{p_0\} \cup (p_0^{\bullet})^{\bullet}) \cap places(\varphi) = \emptyset$	$I(\langle t_0 t \rangle) = I(t_0)$
R5) $\bullet(p_0^{\bullet}) = \{p_0\}$	UR2) Remove $t_0$
R6) $\boxplus (t_0, p_0) \ge \boxminus (p_0, t)$ for all $t \in p_0^{\bullet}$	

Figure 1: Rule R: Atomic post-agglomerable producer