

# **A BFT protocol**

**Simplified HotStuff**

**Leander Jehl**

# BFT protocol

## Model

### Model:

- We assume a permissioned system with  $N = 3f + 1$  nodes.
- At most  $f$  of the nodes are byzantine faulty.
- Nodes have unique ids and unique, known cryptographic keys.

### Certificate:

- A block has a certificate, if it contains signatures of  $2f + 1$  nodes.

# BFT protocol

## Certificate vs. PoW

**PoW:** Requiring that blocks contains a proof of work gives the following:

- **Rate limit:** Limit at which rate new blocks are created.
- **Fork probability:** Reduce probability for forks
- **Prevent system split:** Small subsystem will not be able to create blocks at correct rate.

# BFT protocol

## Certificate vs. PoW

**Certificate:** If blocks require a certificate, we get similar properties.

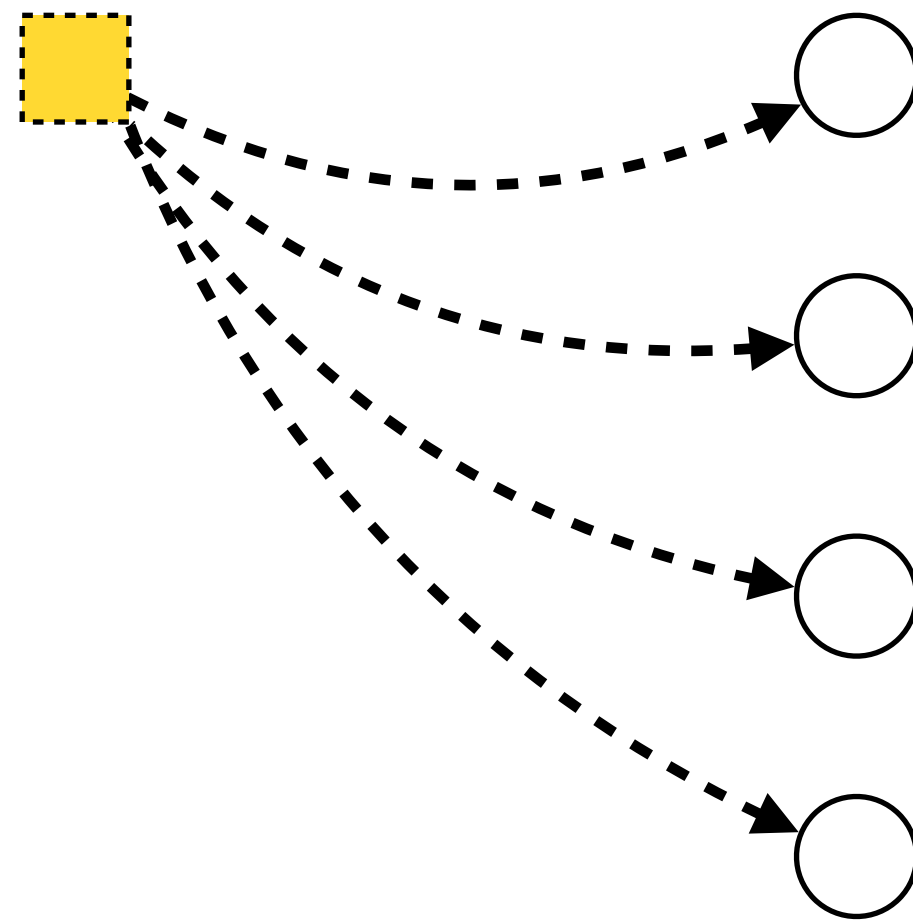
- **Rate limit:**
- **Fork probability:**
- **Prevent system split:**

# BFT protocol

## Certificate vs. PoW

**Idea:** Send new block to nodes for validation and signature.  
Then collect certificate.

new block

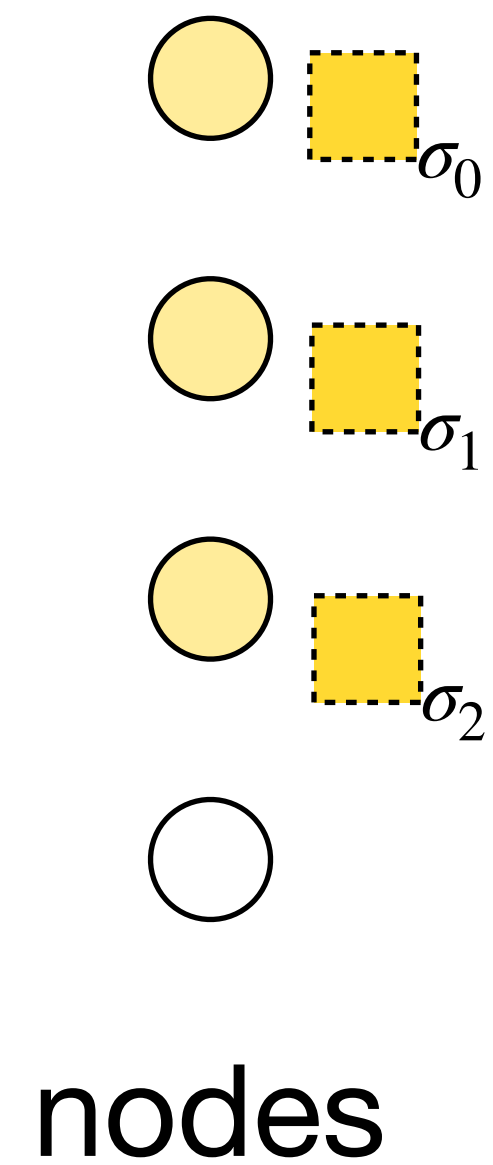


nodes

# BFT protocol

## Certificate vs. PoW

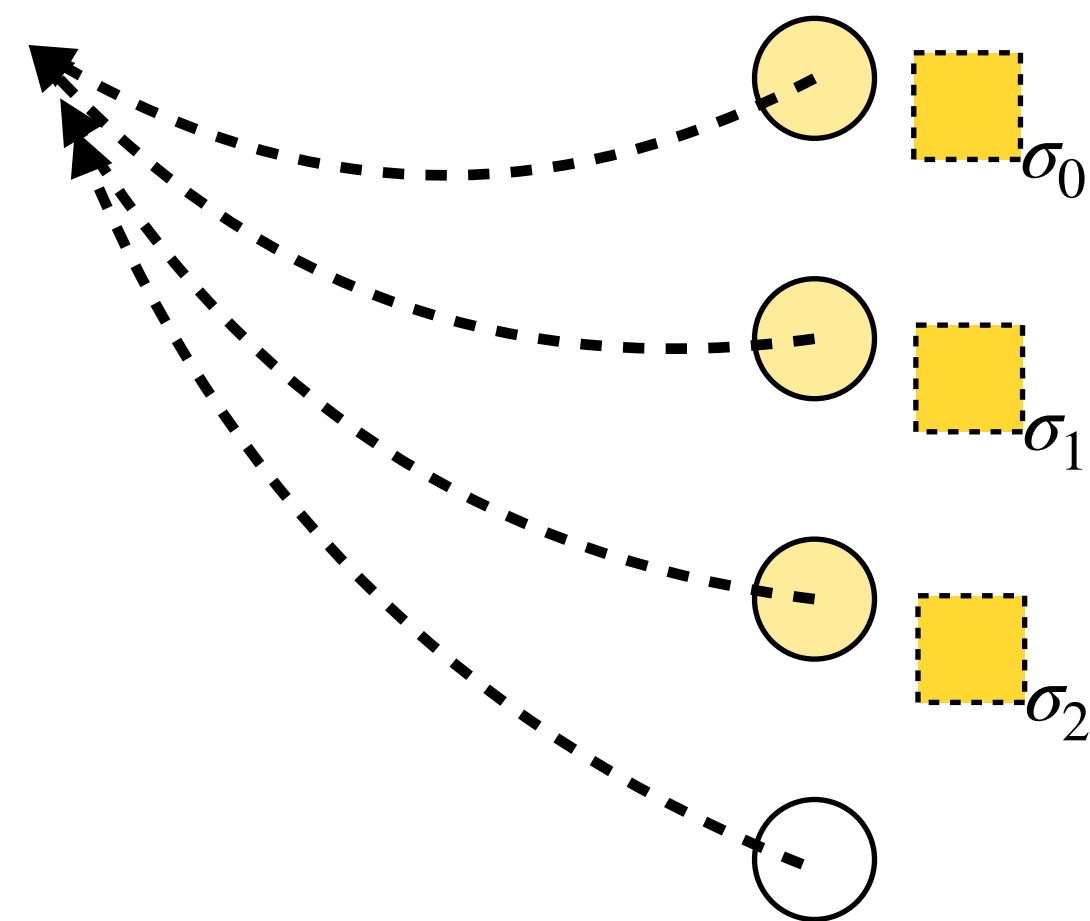
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## Certificate vs. PoW

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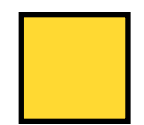


nodes

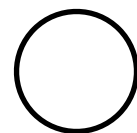
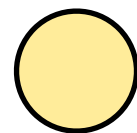
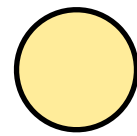
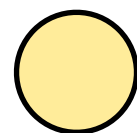
# BFT protocol

## Certificate vs. PoW

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$\langle \sigma_0, \sigma_1, \sigma_2 \rangle$



nodes



# BFT protocol

## Certificate vs. PoW

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**Certificate:** If blocks require a certificate, we get similar properties.

- **Rate limit:**
- **Fork probability:**
- **Prevent system split:**

# BFT protocol

## Certificate vs. PoW

**Idea:** Send new block to nodes for validation and signature.  
Then collect certificate.

**Certificate:** If blocks require a certificate, we get similar properties.

- **Rate limit:**  
Blocks need to be verified and signed by most of the nodes.  
Cannot create blocks faster than they are verified and signed.
- **Fork probability:**
- **Prevent system split:**

# BFT protocol

## Certificate vs. PoW

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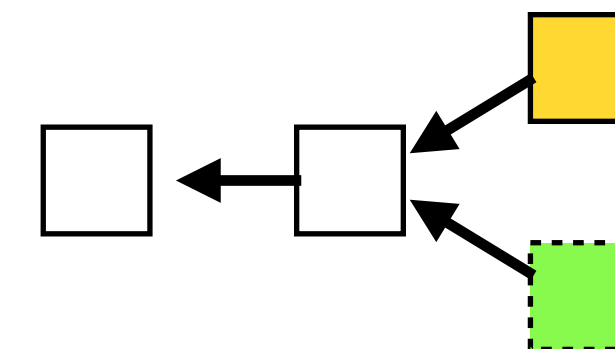
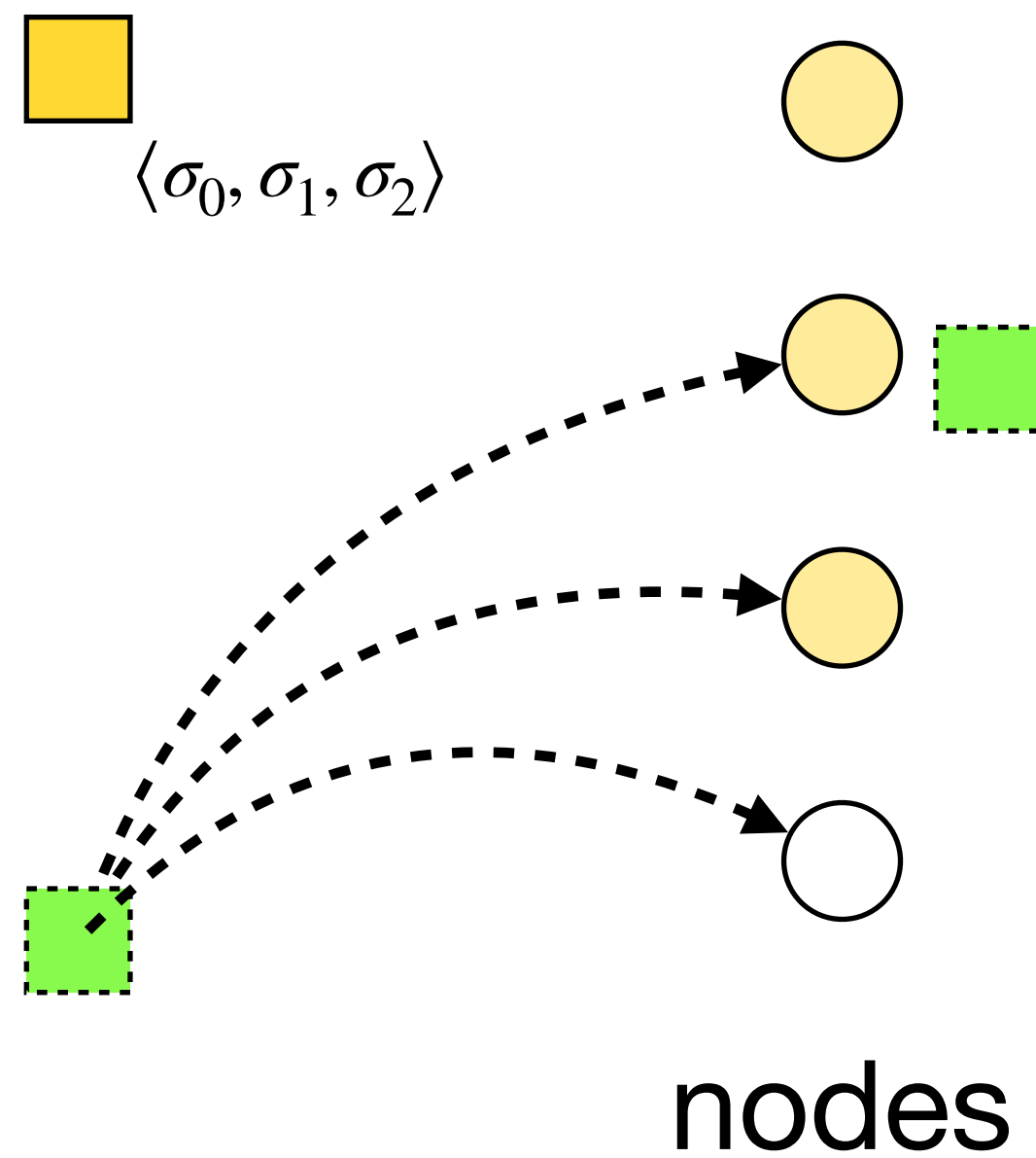
**Certificate:** If blocks require a certificate, we get similar properties.

- **Rate limit:**
- **Fork probability:**  
If nodes do not sign multiple blocks, at most one block at a given height can get a certificate.
- **Prevent system split:**

# BFT protocol

## Certificate vs. PoW

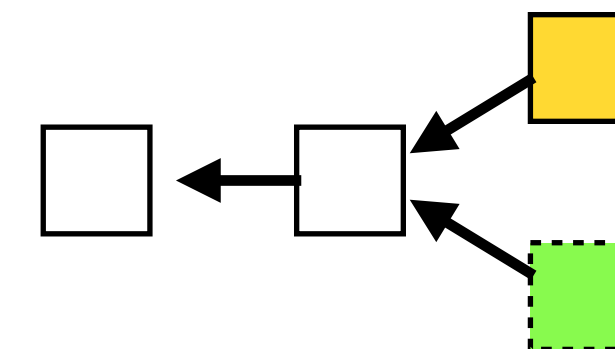
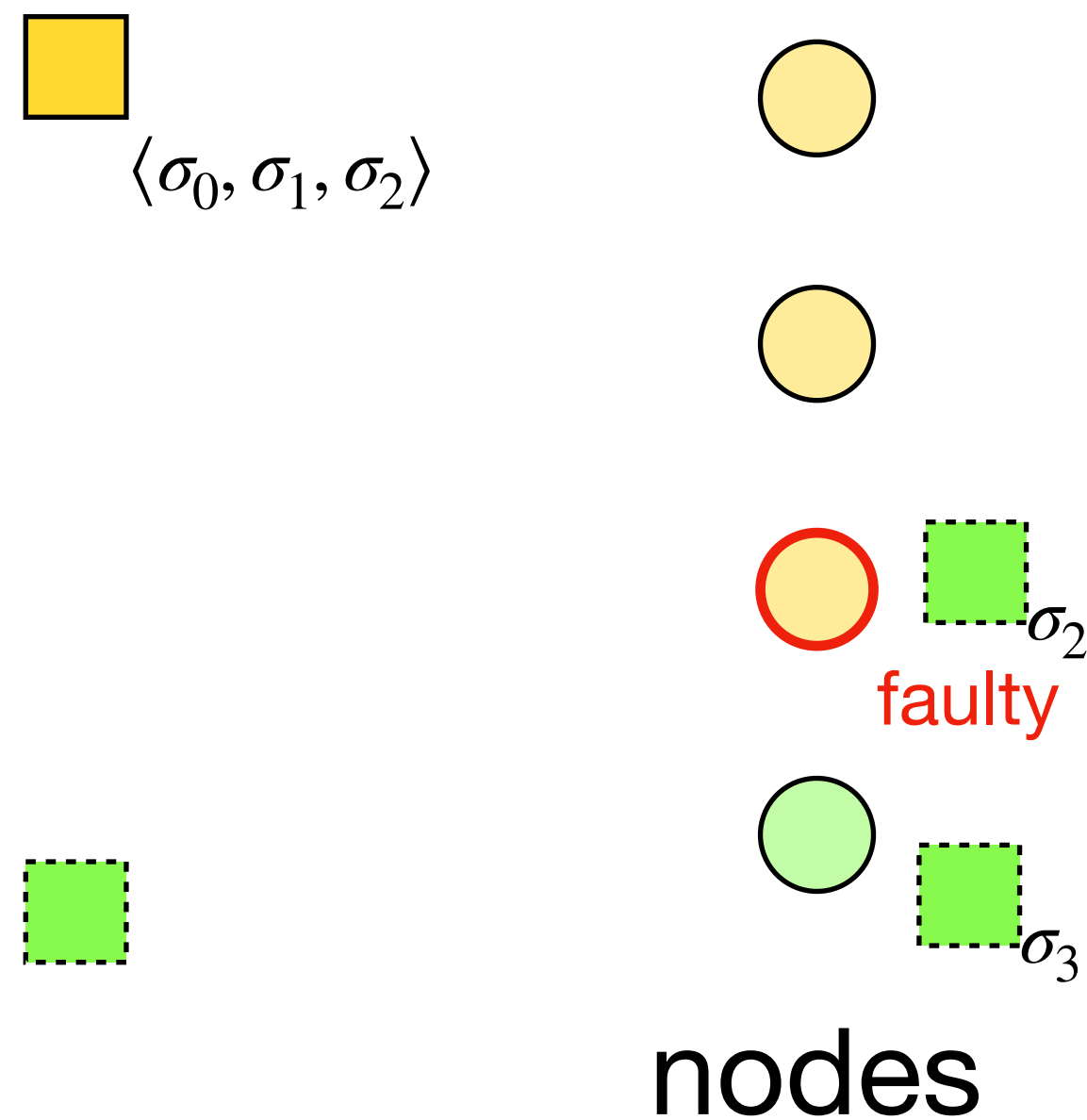
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# BFT protocol

## Certificate vs. PoW

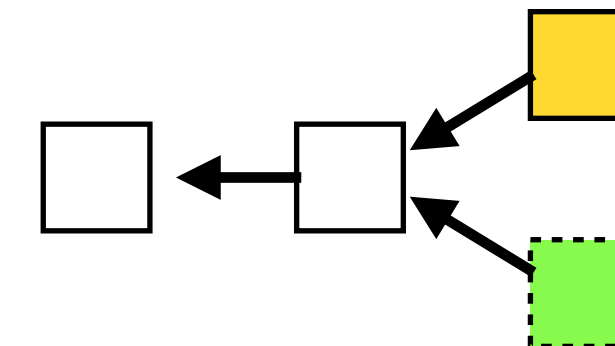
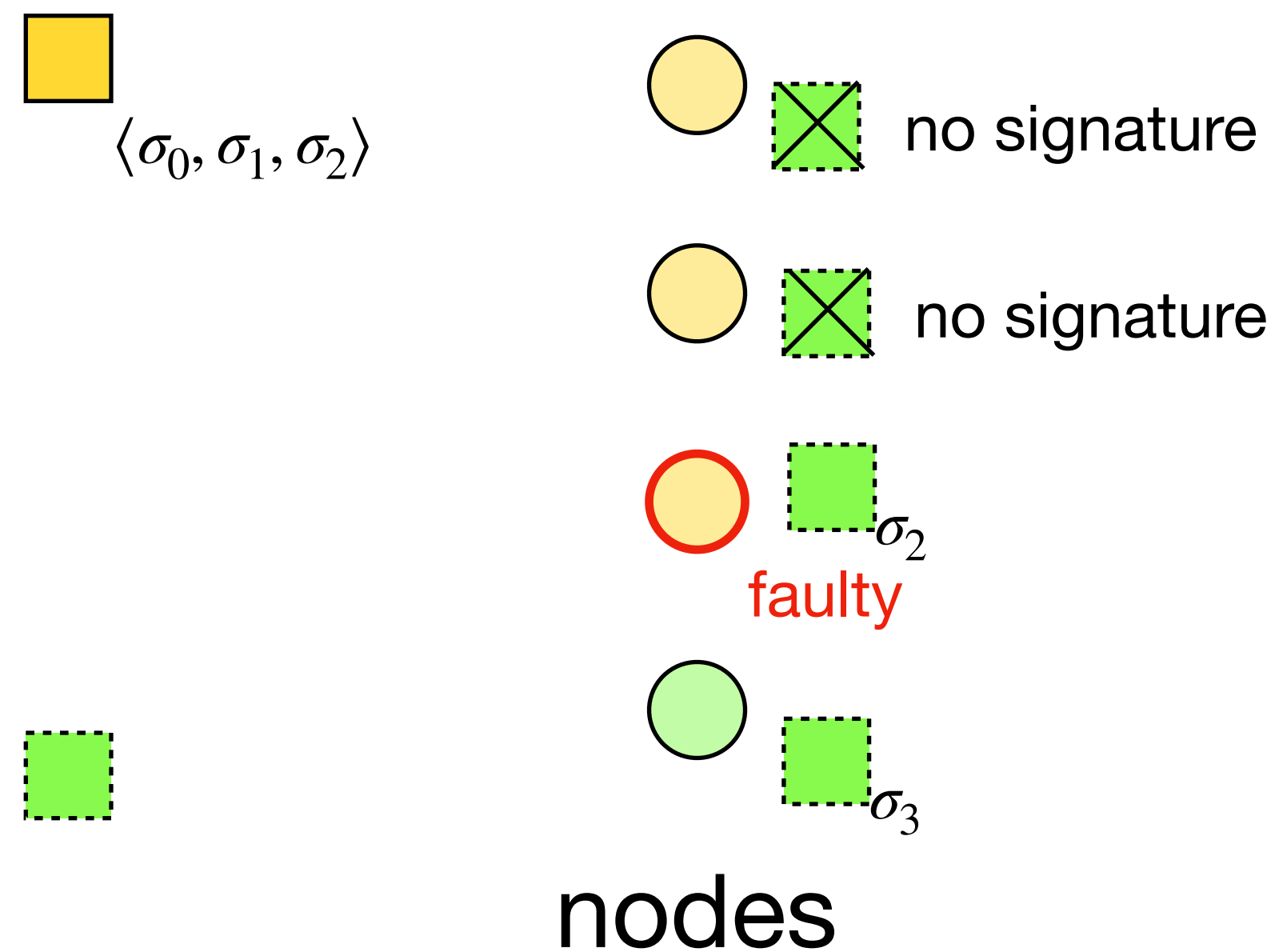
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# BFT protocol

## Certificate vs. PoW

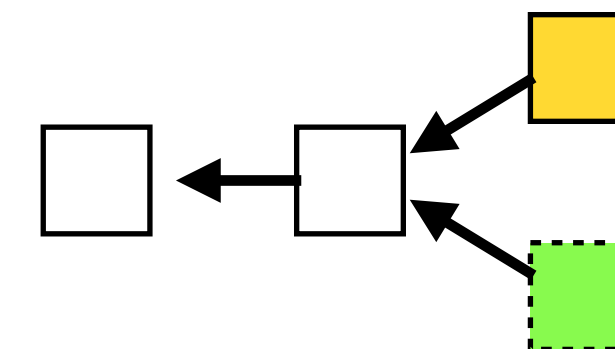
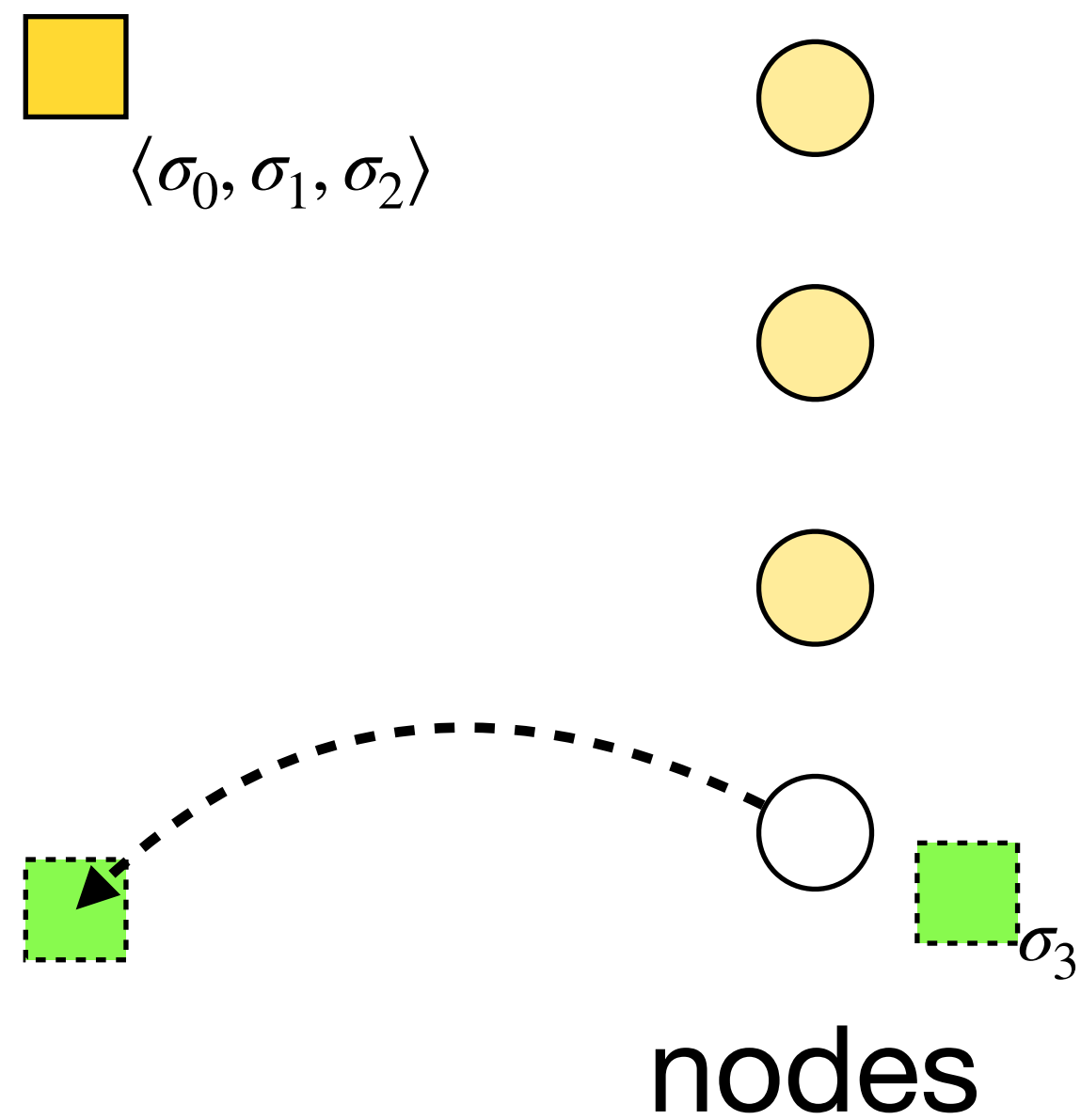
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## Certificate vs. PoW

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# BFT protocol

## Certificate vs. PoW

**Idea:** Send new block to nodes for validation and signature.

*Correct nodes sign only one block at given depth.*

Then collect certificate.

**Certificate:** If blocks require a certificate, we get similar properties.

- **Rate limit:**
- **Fork probability:**  
If nodes do not sign multiple blocks, at most one block at a given height can get a certificate.  
*Obs: Faulty nodes may sign multiple blocks!*
- **Prevent system split:**



# BFT protocol

## Certificate vs. PoW

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**Certificate:** If blocks require a certificate, we get similar properties.

- **Rate limit:**
- **Fork probability:**
- **Prevent system split:**  
A subsystem, with few nodes cannot create certificates.

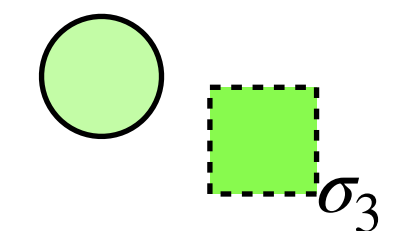
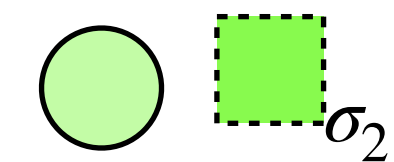
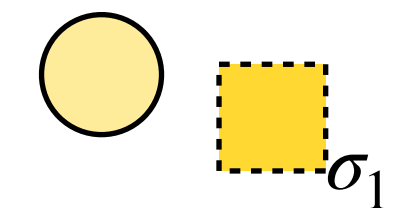
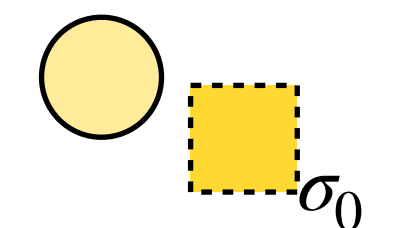
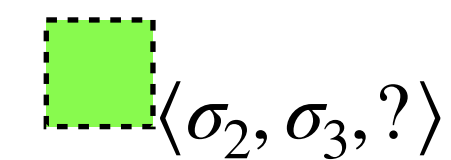
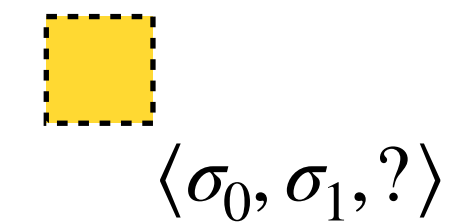
# BFT protocol

## Certificate vs. PoW problem

**Idea:** Send new block to nodes for validation and signature.  
*Correct nodes sign only one block at given depth.*  
Then collect certificate.

**Problem:** How to ensure that a certificate is created?

- Nodes may sign different blocks
- No block gets a certificate
- **Solution:**



nodes

# BFT protocol

## Certificate vs. PoW problem

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*Correct nodes sign only one block at given depth.*  
Then collect certificate.

**Problem:** How to ensure that a certificate is created?

- Nodes may sign different blocks
- No block gets a certificate
- **Solution:** Leader

# BFT protocol

## Certificate vs. PoW problem

**Idea:** Send new block to nodes for validation and signature.  
*Correct nodes sign only one block at given depth.*  
Then collect certificate.

**Problem:** How to know that a certificate was created?

- A certificate may be collected by a single node
- The node with the certificate may fail and come back later
- **Solution:**

# BFT protocol

## Certificate vs. PoW problem

**Idea:** Send new block to nodes for validation and signature.  
*Correct nodes sign only one block at given depth.*  
Then collect certificate.

**Problem:** How to know that a certificate was created?

- A certificate may be collected by a single node
- The node with the certificate may fail and come back later
- **Solution:** Require multiple certificates

# BFT protocol

## Simple HotStuff (2 chain)

### Preliminary:

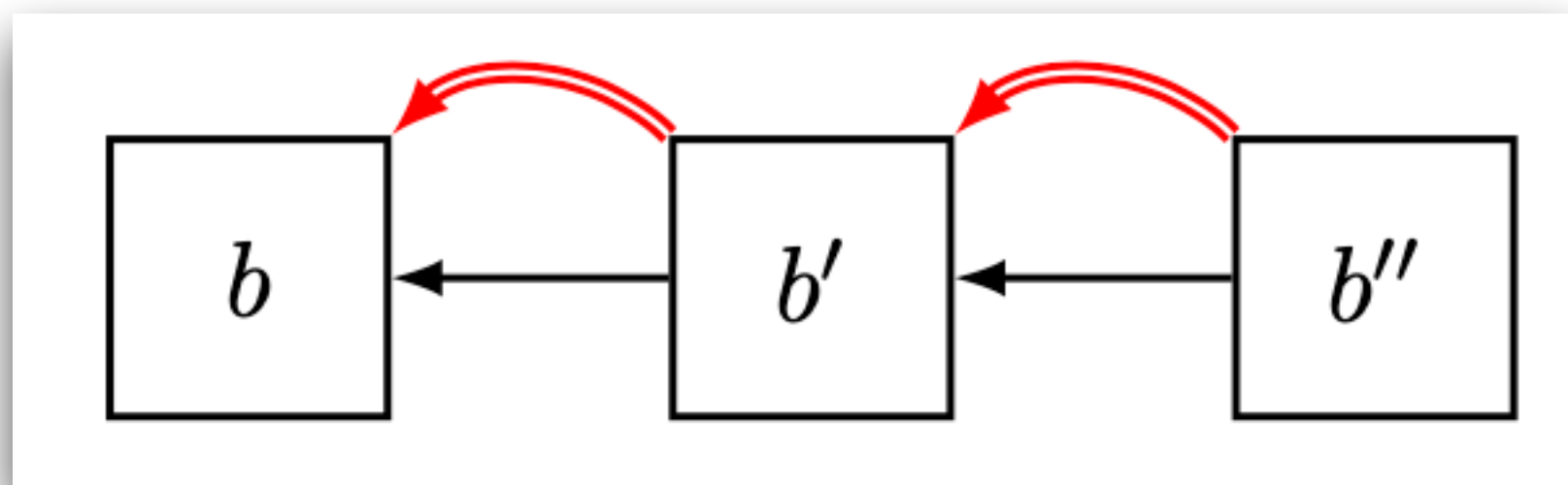
- Every block includes a parent link (*previous block*).  
=> Blocks form a **tree**.  
A blocks *depth* is the distance from the root (genesis block).
- Every block may includes a **certificate** for an ancestor.

# BFT protocol

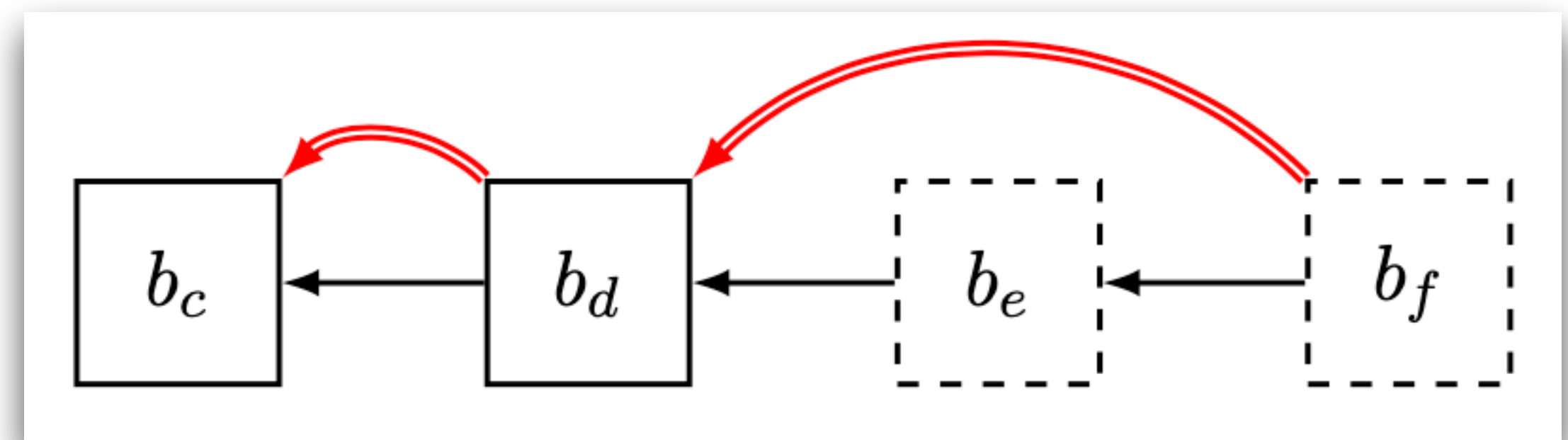
## Simple HotStuff (2 chain)

### Preliminary:

- Every block includes a parent link (*previous block*).  
=> Blocks form a **tree**.  
A blocks *depth* is the distance from the root (genesis block).
- Every block may includes a **certificate** for an ancestor.  
This is called **justification**.



Blocks with certificate for parent.



Blocks with certificates.

# BFT protocol

## Simple HotStuff (2 chain)

### Rules

- **Rule 1:** After signing a block as depth  $d$ , a node may only sign at depth  $d' > d$ .

Every node maintains the **locked block**, i.e. the block at largest height for which it has seen a certificate.

- **Rule 2:** A node only signs a block, if it is a descendant of the locked block.

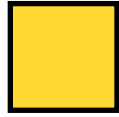
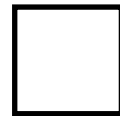
*Obs: a node may update the locked block, based on the certificate included in a block.*

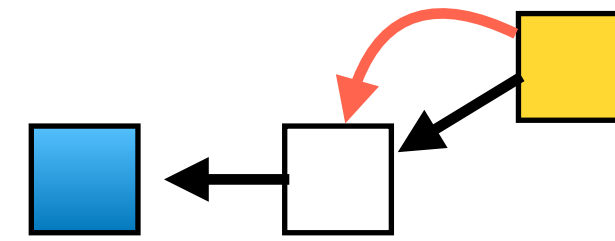


# BFT protocol

## Example

### Example



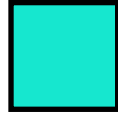
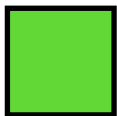
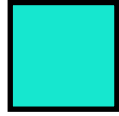
- Nodes  $n_0$ ,  $n_1$ , and  $n_2$  sign block 
- They set *lock* to 

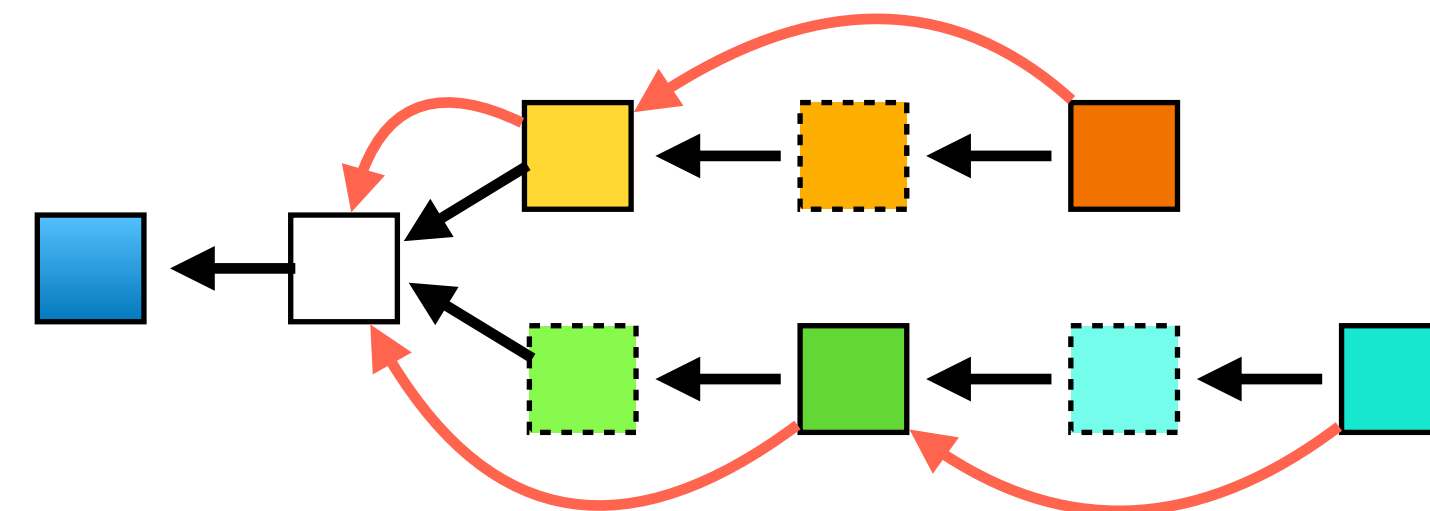


# BFT protocol

## Example

### Example (bad case)


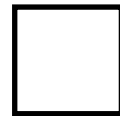
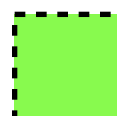

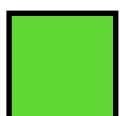
- $n_0$ ,  $n_1$ , and  $n_2$  sign block 
- $n_1$ , and  $n_2$  set *lock* to 
- $n_3$  creates 
- $n_1$ , and  $n_2$  set *lock* to 
- $n_3$ ,  $n_1$ , and  $n_2$  sign block 

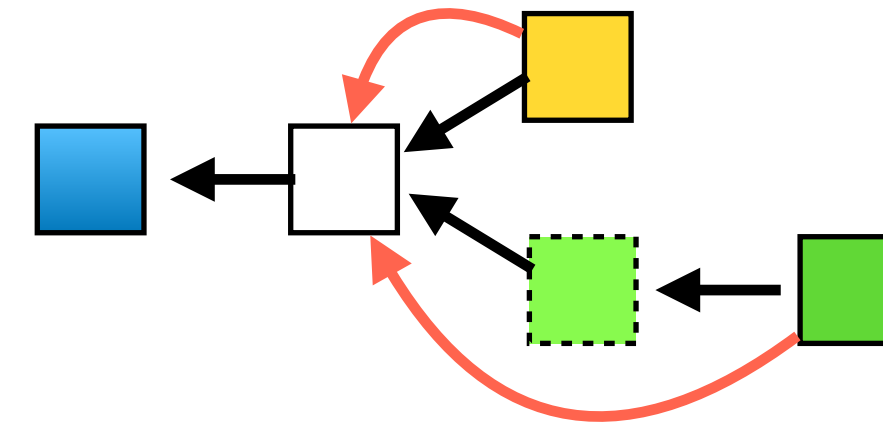


# BFT protocol

## Example

### Example (recall)



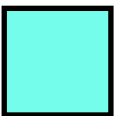


- Nodes  $n_0$ ,  $n_1$ , and  $n_2$  sign block 
- They set *lock* to 
- $n_3$  signs 
- $n_3$  creates 
- $n_3$ ,  $n_1$ , and  $n_2$  sign block 

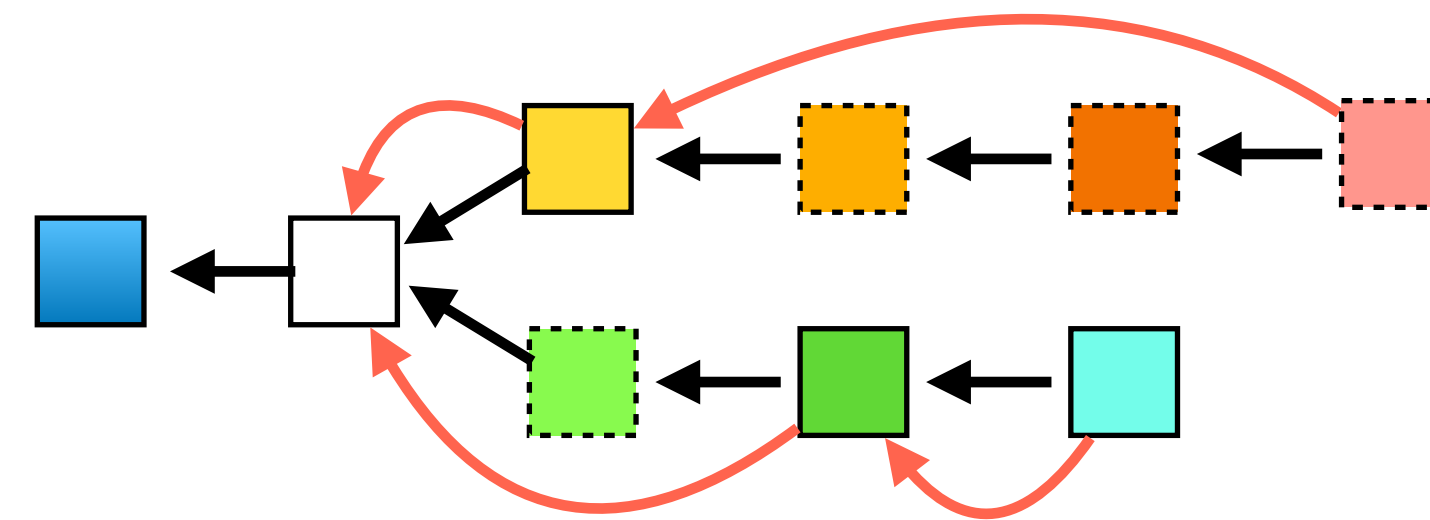


# BFT protocol

## Example

### Example (good case)



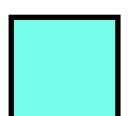


- $n_3$  creates 
- $n_1$ , and  $n_2$  set *lock* to 
- $n_3$ ,  $n_1$ , and  $n_2$  sign block 
- $n_0$  creates 
- $n_1$ , and  $n_2$  will not sign 

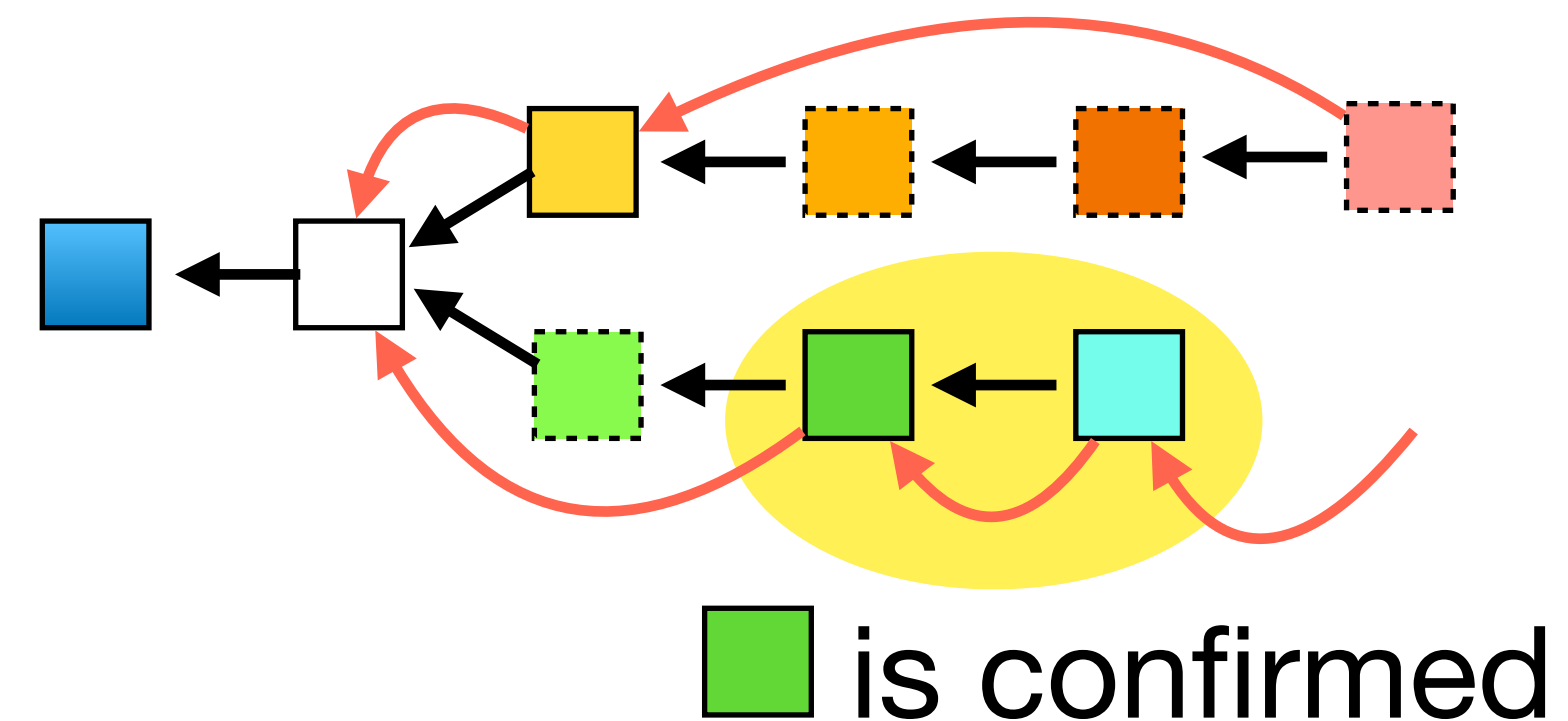


# BFT protocol

## Example

### Example (good case)

- $n_3$  creates 
- $n_1$ , and  $n_2$  set *lock* to 
- $n_3$ ,  $n_1$ , and  $n_2$  sign block 
- $n_0$  creates 
- $n_1$ , and  $n_2$  will not sign 



# BFT protocol

## Simple HotStuff

**Def.:** A block is **confirmed** if both the block and its successor have a certificate.

**Theorem:** *If a block is confirmed, only descendants of that block, can get a certificate.*

**Proof:** A majority of correct nodes have set their *lock* to the confirmed node.

# BFT protocol

## Simple HotStuff - Leader

**Idea 1:** Every depth has designated leader.

**Idea 2:** Nodes wait for  $\Delta$  time for a proposal in current depth, before accepting at next depth.

# BFT protocol

## Simple HotStuff - Leader

**Idea 1:** Every depth has designated leader.

**Idea 2:** Nodes wait for  $\Delta$  time for a proposal in current depth, before accepting at next depth.

*How can a leader avoid the situation from the example?*

Ask all nodes for most recent certificate.

Wait for  $\Delta$  time to receive proposal from all correct nodes.