Poverty and Inequality with Complex Survey Data

Guilherme Jacob, Anthony Damico, and Djalma Pessoa

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Contents

Chapter 1

Introduction

This is a *sample* book written in **Markdown**. You can use anything that Pandoc's Markdown supports, e.g., a math equation $a^2 + b^2 = c^2$.

For now, you have to install the development version of **bookdown** from Github:

```
devtools::install_github("rstudio/bookdown")
```

Remember each Rmd file contains one and only one chapter, and a chapter is defined by the first-level heading `#`.

To compile this example to PDF, you need to install XeLaTeX.

The library convey aims at estimating measures of poverty and income concentration. There are already at least two libraries covering this subject: vardpoor and Laeken. The main difference between the library convey and these two is that the convey strongly hinges on the survey library.

1.1 Installation

`convey` is free and open-source software that runs inside the R environment for statistical computing.

- the latest released version from CRAN with

  ```
  install.packages("convey")
  ```

- the latest development version from github with

  ```
  devtools::install_github("djalmapessoa/convey")
  ```

[This may present how to install R, RStudio and required packages. Providing brief information about `survey` and `MonetDBLite` may also be recommended.]

You can label chapter and section titles using `{#label}` after them, e.g., we can reference Chapter 1.1. If you do not manually label them, there will be automatic labels anyway, e.g., Chapter 3.

Figures and tables with captions will be placed in `figure` and `table` environments, respectively.

```
par(mar = c(4, 4, .1, .1))
plot(pressure, type = 'b', pch = 19)
```

Reference a figure by its code chunk label with the `fig:` prefix, e.g., see Figure 1.1. Similarly, you can reference tables generated from `knitr::kable()`, e.g., see Table 1.1.

Figure 1.1: Here is a nice figure!

```
knitr::kable(
  head(iris, 20), caption = 'Here is a nice table!',
  booktabs = TRUE
)
```

You can write citations, too. For example, we are using the **bookdown** package (Xie, 2016) in this sample book, which was built on top of R Markdown and **knitr** (Xie, 2015).

1.2   Complex surveys and statistical inference

In this book we estimate measures of poverty and income concentration in a populatiion, generaly of households or people, based on data colected from a complex survey sample from the population, involving

1- different units selection probabilities;

2- clustering of units;

3- stratification of clusters, and

4- reweighting to compensate missing values and other adjustments.

Items 1 and 4 imply that we should use different units weights to avoid biases when performing statistical analysis. Also, when estimating variances, we should consider, not only the design weights but all listed design characteristics 1-4.

In order to take into account the sample design characteristics it should be used a specialized software like the R library **survey**, adopted in this book.

Table 1.1: Here is a nice table!

Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
5.1	3.5	1.4	0.2	setosa
4.9	3.0	1.4	0.2	setosa
4.7	3.2	1.3	0.2	setosa
4.6	3.1	1.5	0.2	setosa
5.0	3.6	1.4	0.2	setosa
5.4	3.9	1.7	0.4	setosa
4.6	3.4	1.4	0.3	setosa
5.0	3.4	1.5	0.2	setosa
4.4	2.9	1.4	0.2	setosa
4.9	3.1	1.5	0.1	setosa
5.4	3.7	1.5	0.2	setosa
4.8	3.4	1.6	0.2	setosa
4.8	3.0	1.4	0.1	setosa
4.3	3.0	1.1	0.1	setosa
5.8	4.0	1.2	0.2	setosa
5.7	4.4	1.5	0.4	setosa
5.4	3.9	1.3	0.4	setosa
5.1	3.5	1.4	0.3	setosa
5.7	3.8	1.7	0.3	setosa
5.1	3.8	1.5	0.3	setosa

1.3 Linearization

Some measures of poverty and income concentration are defined by non-differentiable functions so that it is not possible to use Taylor linearization to estimate their variances. An alternative is to use **Influence functions** as described in (Deville, 1999) and (Osier, 2009). The library convey implements this methodology to work with `survey.design` objects and also with `svyrep.design` objects.

Some examples of these measures are:

- At-risk-of-poverty threshold: $arpt = .60q_{.50}$ where $q_{.50}$ is the income median;

- At-risk-of-poverty rate $arpr = \frac{\sum_U 1(y_i \leq arpt)}{N}.100$

- Quintile share ratio

$$qsr = \frac{\sum_U 1(y_i > q_{.80})}{\sum_U 1(y_i \leq q_{.20})}$$

- Gini coefficient $1 + G = \frac{2\sum_U (r_i - 1)y_i}{N \sum_U y_i}$ where r_i is the rank of y_i.

Note that it is not possible to use Taylor linearization for these measures because they depend on quantiles and the Gini is defined as a function of ranks. This could be done using the approach proposed by Deville (1999) based upon influence functions.

1.4   Influence function

Let U be a population of size N and M be a measure that allocates mass one to the set composed by one unit, that is $M(i) = M_i = 1$ if $i \in U$ and $M(i) = 0$ if $i \notin U$

Now, a population parameter θ can be expressed as a functional of M $\theta = T(M)$

Examples of such parameters are:

- Total: $Y = \sum_U y_i = \sum_U y_i M_i = \int y dM = T(M)$

- Ratio of two totals: $R = \frac{Y}{X} = \frac{\int y dM}{\int x dM} = T(M)$

- Cumulative distribution function: $F(x) = \frac{\sum_U 1(y_i \leq x)}{N} = \frac{\int 1(y \leq x) dM}{\int dM} = T(M)$

To estimate these parameters from the sample, we replace the measure M by the estimated measure $\hat{M}$ defined by: $\hat{M}(i) = \hat{M}_i = w_i$ if $i \in s$ and $\hat{M}(i) = 0$ if $i \notin s$.

The estimators of the population parameters can then be expressed as functional of the measure $\hat{M}$.

- Total: $\hat{Y} = T(\hat{M}) = \int y d\hat{M} = \sum_s w_i y_i$

- Ratio of totals: $\hat{R} = T(\hat{M}) = \frac{\int y d\hat{M}}{\int x d\hat{M}} = \frac{\sum_s w_i y_i}{\sum_s w_i x_i}$

- Cumulative distribution function: $\hat{F}(x) = T(\hat{M}) = \frac{\int 1(y \leq x) d\hat{M}}{\int d\hat{M}} = \frac{\sum_s w_i 1(y_i \leq x)}{\sum_s w_i}$

1.5   The variance estimator

The variance of the estimator $T(\hat{M})$ can approximated by:

$$Var\left[T(\hat{M})\right] \cong var\left[\sum_s w_i z_i\right]$$

The `linearized` variable z is given by the derivative of the functional:

$$z_k = lim_{t \to 0} \frac{T(M + t\delta_k) - T(M)}{t} = IT_k(M)$$

where, δ_k is the Dirac measure in k: $\delta_k(i) = 1$ if and only if $i = k$.

This **derivative** is called **Influence Function** and was introduced in the area of **Robust Statistics**.

1.6   Influence functions - Examples

- Total:

$$IT_k(M) = lim_{t \to 0} \frac{T(M + t\delta_k) - T(M)}{t}$$
$$= lim_{t \to 0} \frac{\int y.d(M + t\delta_k) - \int y.dM}{t}$$
$$= lim_{t \to 0} \frac{\int y d(t\delta_k)}{t} = y_k$$

- Ratio of two totals:

$$IR_k(M) = I\left(\frac{U}{V}\right)_k (M) = \frac{V(M) \times IU_k(M) - U(M) \times IV_k(M)}{V(M)^2}$$
$$= \frac{Xy_k - Yx_k}{X^2} = \frac{1}{X}(y_k - Rx_k)$$

1.7 Linearization by influence function - Examples

- At-risk-of-poverty threshold:

$$arpt = 0.6 \times m$$

where m is the median income.

$$z_k = -\frac{0.6}{f(m)} \times \frac{1}{N} \times [I(y_k \leq m - 0.5)]$$

- At-risk-of-poverty rate:

$$arpr = \frac{\sum_U I(y_i \leq t)}{\sum_U w_i}.100$$

$$z_k = \frac{1}{N}[I(y_k \leq t) - t] - \frac{0.6}{N} \times \frac{f(t)}{f(m)}[I(y_k \leq m) - 0.5]$$

where:

N - population size;

t - at-risk-of-poverty threshold;

y_k - income of person k;

m - median income;

f - income density function;

1.8 Structure of the library

In the library convey, there are some basic functions that produces the linearized variables of some estimates that often enter in the definition of measures of concentration and poverty. For example the `quantile` which is linearized by the function `svyiqalpha`. Other example is the function `svyisq` that linearizes the total below a quantile of the variable.

From the linearized variables of these basic estimates it is possible by using rules of composition, valid for influence functions, to derive the influence function of more complex estimates. By definition the influence function is a Gateaux derivative and the rules rules of composition valid for Gateaux derivatives also hold for Influence Functions.

The following property of Gateaux derivatives was often used in the library convey. Let g be a differentible function of m variables. Suppose we want to compute the influence function of the estimator $g(T_1, T_2, \ldots, T_m)$, knowing the Influence function of the estimators $T_i, i = 1, \ldots, m$. Then the following holds:

$$I(g(T_1, T_2, \ldots, T_m)) = \sum_{i=1}^m \frac{\partial g}{\partial T_i} I(T_i)$$

In the library convey this rule is implemented by the function `contrastinf` which uses the R function `deriv` to compute the formal partial derivatives $\frac{\partial g}{\partial T_i}$.

For example, suppose we want to linearize the `Relative median poverty gap`(rmpg), defined as the difference between the at-risk-of-poverty threshold (`arpt`) and the median of incomes less than the `arpt` relative to the `arprt`:

$$rmpg = \frac{arpt - medpoor}{arpt}$$

where `medpoor` is the median of incomes less than `arpt`.

Suppose we know how to linearize `arpt` and `medpoor`, then by applying the function `contrastinf` with

$$g(T_1, T_2) = \frac{(T_1 - T_2)}{T_1}$$

we linearize the `rmpg`.

1.8.1   Examples of use of the library convey

In the following examples we will use the data set `eusilc` contained in the libraries `vardpoor` and `Laeken`.

```
library(vardpoor)
data(eusilc)
```

Next, we create an object of class `survey.design` using the function `svydesign` of the library survey:

```
library(survey)
des_eusilc <- svydesign(ids = ~rb030, strata =~db040,  weights = ~rb050, data = eusilc)
```

Right after the creation of the design object `des_eusilc`, we should use the function `convey_prep` that adds an attribute to the survey design which saves information on the design object based upon the whole sample, needed to work with subset designs.

```
library(convey)
des_eusilc <- convey_prep( des_eusilc )
```

To estimate the `at-risk-of-poverty rate` we use the function `svyarpt`:

```
svyarpr(~eqIncome, design=des_eusilc)
```

```
              arpr     SE
eqIncome 0.14444 0.0028
```

To estimate the `at-risk-of-poverty rate` for domains defined by the variable `db040` we use

```
svyby(~eqIncome, by = ~db040, design = des_eusilc, FUN = svyarpr, deff = FALSE)
```

```
                       db040  eqIncome          se
Burgenland        Burgenland 0.1953984 0.017202243
Carinthia          Carinthia 0.1308627 0.010610622
Lower Austria Lower Austria 0.1384362 0.006517660
Salzburg            Salzburg 0.1378734 0.011579280
Styria                Styria 0.1437464 0.007452360
Tyrol                  Tyrol 0.1530819 0.009880430
Upper Austria Upper Austria 0.1088977 0.005928336
Vienna                Vienna 0.1723468 0.007682826
Vorarlberg        Vorarlberg 0.1653731 0.013754670
```

Using the same data set, we estimate the `quintile share ratio`:

```
# for the whole population
svyqsr(~eqIncome, design=des_eusilc, alpha= .20)
```

```
          qsr     SE
eqIncome 3.97 0.0426
```

```
# for domains
svyby(~eqIncome, by = ~db040, design = des_eusilc,
  FUN = svyqsr, alpha= .20, deff = FALSE)
```

```
                      db040 eqIncome         se
Burgenland       Burgenland 5.008486 0.32755685
Carinthia         Carinthia 3.562404 0.10909726
Lower Austria Lower Austria 3.824539 0.08783599
Salzburg           Salzburg 3.768393 0.17015086
Styria               Styria 3.464305 0.09364800
Tyrol                 Tyrol 3.586046 0.13629739
Upper Austria Upper Austria 3.668289 0.09310624
Vienna               Vienna 4.654743 0.13135731
Vorarlberg       Vorarlberg 4.366511 0.20532075
```

These functions can be used as S3 methods for the classes `survey.design` and `svyrep.design`.

Let's create a design object of class `svyrep.design` and run the function `convey_prep` on it:

```
des_eusilc_rep <- as.svrepdesign(des_eusilc, type = "bootstrap")
des_eusilc_rep <- convey_prep(des_eusilc_rep)
```

and then use the function svyarpr:

```
svyarpr(~eqIncome, design=des_eusilc_rep)
```

```
           arpr     SE
eqIncome 0.14444 0.0026
```

```
svyby(~eqIncome, by = ~db040, design = des_eusilc_rep, FUN = svyarpr, deff = FALSE)
```

```
                      db040  eqIncome se.eqIncome
Burgenland       Burgenland 0.1953984 0.018160170
Carinthia         Carinthia 0.1308627 0.012136183
Lower Austria Lower Austria 0.1384362 0.007689382
Salzburg           Salzburg 0.1378734 0.013658170
Styria               Styria 0.1437464 0.007331796
Tyrol                 Tyrol 0.1530819 0.010196732
Upper Austria Upper Austria 0.1088977 0.006773692
Vienna               Vienna 0.1723468 0.006875140
Vorarlberg       Vorarlberg 0.1653731 0.014161893
```

The functions of the library convey are called in a similar way to the functions in library survey.

It is also possible to deal with missing values by using the argument `na.rm`.

```
# survey.design using a variable with missings
svygini( ~ py010n , design = des_eusilc )
```

```
       gini SE
py010n   NA NA
```

```r
svygini( ~ py010n , design = des_eusilc , na.rm = TRUE )
```

```
         gini     SE
py010n 0.64606 0.0036
```

```r
# svyrep.design using a variable with missings
# svygini( ~ py010n , design = des_eusilc_rep ) get error
svygini( ~ py010n , design = des_eusilc_rep , na.rm = TRUE )
```

```
         gini     SE
py010n 0.64606 0.0031
```

djalma, where do these references go on this page? (Berger and Skinner, 2003) and (Osier, 2009) and (Deville, 1999)

Chapter 2

Poverty Indices

[I think this is a good start. I don't think that gender pay gap, quantiles and totals are measures of poverty. Consider another chapter on other wellbeing measures.] this is a test ## At Risk of Poverty Ratio and Threshold (svyarpr, svyarpt)

here are the references

(Osier, 2009) and (Deville, 1999)

2.1 The Gender Pay Gap (svygpg)

here are the references

(Osier, 2009) and (Deville, 1999)

2.2 Quintile Share Ratio (svyqsr)

here are the references

(Osier, 2009) and (Deville, 1999)

2.3 Relative Median Income Ratio (svyrmir)

here are the references

(Osier, 2009) and (Deville, 1999)

2.4 Relative Median Poverty Gap (svyrmpg)

here are the references

(Osier, 2009) and (Deville, 1999)

2.5   Median Income Below the At Risk of Poverty Threshold (svy-poormed)

here are the references

(Osier, 2009) and (Deville, 1999)

2.6   Foster-Greer-Thorbecke class (svyfgt)

here are the references

(Foster et al., 1984) and (Berger and Skinner, 2003)

(Foster et al., 1984) proposed a family of indicators to measure poverty.

The class of FGT measures, can be defined as

$$p = \frac{1}{N} \sum_{k \in U} h(y_k, \theta),$$

where

$$h(y_k, \theta) = \left[\frac{(\theta - y_k)}{\theta} \right]^\gamma \delta \left\{ y_k \leq \theta \right\},$$

where: θ is the poverty threshold; δ the indicator function that assigns value 1 if the condition $\{y_k \leq \theta\}$ is satisfied and 0 otherwise, and γ is a non-negative constant.

When $\gamma = 0$, p can be interpreted as the poverty headcount ratio, and for $\gamma \geq 1$, the weight of the income shortfall of the poor to a power γ, (Foster and all, 1984).

The poverty measure FGT is implemented in the library convey by the function `svyfgt`. The argument `thresh_type` of this function defines the type of poverty threshold adopted. There are three possible choices:

1. `abs` – fixed and given by the argument thresh_value
2. `relq` – a proportion of a quantile fixed by the argument `proportion` and the quantile is defined by the argument `order`.
3. `relm` – a proportion of the mean fixed the argument `proportion`

The quantile and the mean involved in the definition of the threshold are estimated for the whole population. When $\gamma = 0$ and $\theta = .6 * MED$ the measure is equal to the indicator `arpr` computed by the function `svyarpr`.

Next, we give some examples of the function `svyfgt` to estimate the values of the FGT poverty index.

Consider first the poverty threshold fixed ($\gamma = 0$) in the value 10000. The headcount ratio (FGT0) is

```
svyfgt(~eqIncome, des_eusilc, g=0, abs_thresh=10000)
```

```
          fgt0     SE
eqIncome 0.11444 0.0027
```

The poverty gap (FGT1) ($\gamma = 1$) index for the poverty threshold fixed at the same value is

```
svyfgt(~eqIncome, des_eusilc, g=1, abs_thresh=10000)
```

```
            fgt1     SE
eqIncome 0.032085 0.0011
```

To estimate the FGT0 with the poverty threshold fixed at $0.6*MED$ we fix the argument type_thresh="relq" and use the default values for `percent` and `order`:

```
svyfgt(~eqIncome, des_eusilc, g=0, type_thresh= "relq")
```

```
           fgt0     SE
eqIncome 0.14444 0.0028
```

that matches the estimate obtained by

```
svyarpr(~eqIncome, design=des_eusilc, .5, .6)
```

```
           arpr     SE
eqIncome 0.14444 0.0028
```

To estimate the poverty gap(FGT1) with the poverty threshold equal to $0.6 * MEAN$ we use:

```
svyfgt(~eqIncome, des_eusilc, g=1, type_thresh= "relm")
```

```
            fgt1     SE
eqIncome 0.051187 0.0011
```

Chapter 3

Inequality Measurement

3.1 Lorenz Curve (svylorenz)

Though not an inequality measure in itself, the Lorenz curve is a classic instrument of distribution analysis. Basically, it is a function that associates a cumulative share of the population and the share of the total income it owns. In mathematical terms,

$$L(p) = \frac{\int_{-\infty}^{Q_p} y f(y) dy}{\int_{-\infty}^{+\infty} y f(y) dy}$$

where Q_p is the quantile p of the population.

The two extreme distributive cases are

- Perfect equality:
    - Every individual has the same income;
    - Every share of the population has the same share of the income;
    - Therefore, the reference curve is
    $$L(p) = p \ \forall p \in [0, 1].$$

    .

- Perfect inequality:
    - One individual concentrates all of society's income, while the other individuals have zero income;
    - Therefore, the reference curve is

    $$L(p) = \begin{cases} 0, & \forall p < 1 \\ 1, & \text{if } p = 1. \end{cases}$$

In order to evaluate the degree of inequality in a society, the analyst looks at the distance between the real curve and those two reference curves.

The estimator of this function was derived by (Kovacevic and Binder, 1997):

$$L(p) = \frac{\sum_{i \in S} w_i \cdot y_i \cdot \delta\{y_i \leq \widehat{Q}_p\}}{\widehat{Y}}, \ 0 \leq p \leq 1.$$

Yet, this formula is used to calculate specific points of the curve and their respective SEs. The formula to plot an approximation of the continuous empirical curve comes from (Lerman and Yitzhaki, 1989).

3.2   Measures derived from the Lorenz Curve

3.2.1   Gini index (svygini)

The Gini index is an attempt to express the inequality presented in the Lorenz curve as a single number. In essence, the Gini index is twice the area between the equality curve and the real Lorenz curve. Put simply:

$$G = 2\left(\int_0^1 p\,dp - \int_0^1 L(p)\,dp \right)$$

$$\therefore G = 1 - 2\int_0^1 L(p)\,dp$$

where $G = 0$ in case of perfect equality and $G = 1$ in the case of perfect inequality.

The estimator proposed by (Osier, 2009) is defined as:

$$\widehat{G} = \frac{2\sum_{i\in S} w_i r_i y_i - \sum_{i\in S} w_i y_i}{\widehat{Y}}$$

The linearized formula of $\widehat{G}$ is used to calculate the SE.

3.2.2   Amato index (svyamato)

The Amato index is also based on the Lorenz curve, but instead of focusing on the area of the curve, it focuses on its length. (Arnold, 2012) proposes a formula not directly based in the Lorenz curve, which (Barabesi et al., 2016) uses to present the following estimator:

$$\widehat{A} = \sum_{i\in S} w_i \left[\frac{1}{\widehat{N}^2} + \frac{y_i^2}{\widehat{Y}^2} \right]^{\frac{1}{2}},$$

which also generates the linearized formula for SE estimation.

The minimum value A assumes is $\sqrt{2}$ and the maximum is 2. In order to get a measure in the interval $[0,1]$, the standardized Amato index $\widetilde{A}$ can be defined as:

$$\widetilde{A} = \frac{A - \sqrt{2}}{2 - \sqrt{2}} \ .$$

3.2.3   Zenga Index and Curve (svyzenga, svyzengacurve)

The Zenga index and its curve were proposed in (Zenga, 2007). As (Polisicchio and Porro, 2011) noticed, this curve derives directly from the Lorenz curve, and can be defined as:

$$Z(p) = 1 - \frac{L(p)}{p} \cdot \frac{1 - p}{1 - L(p)}.$$

In the `convey` library, an experimental estimator based on the Lorenz curve is used:

$$\widehat{Z(p)} = \frac{p\widehat{Y} - \widehat{\widetilde{Y}}(p)}{p\left[\widehat{Y} - \widehat{\widetilde{Y}}(p)\right]}.$$

In turn, the Zenga index derives from this curve and is defined as:

$$Z = \int_0^1 Z(p)dp.$$

However, its estimators were proposed by (Langel, 2012) and (Barabesi et al., 2016). In this library, the latter is used and is defined as:

$$\widehat{Z} = 1 - \sum_{i \in S} w_i \left[\frac{(\widehat{N} - \widehat{H}_{y_i})(\widehat{Y} - \widehat{K}_{y_i})}{\widehat{N} \cdot \widehat{H}_{y_i} \cdot \widehat{K}_{y_i}} \right]$$

where $\widehat{N}$ is the population total, $\widehat{Y}$ is the total income, $\widehat{H}_{y_i}$ is the sum of incomes below or equal to y_i and $\widehat{N}_{y_i}$ is the sum of incomes greater or equal to y_i.

3.3 Entropy-based Measures

3.3.1 Atkinson index (svyatk)

here are the references

(Langel, 2012) and (Biewen and Jenkins, 2003)

3.3.2 Generalized Entropy and Decomposition (svygei, svygeidec)

guilherme..this has three references? not just two?

here are the references

(Langel, 2012) and (Biewen and Jenkins, 2003) and (Shorrocks, 1984)

3.3.3 J-Divergence Entropy and Decomposition (svyjdiv, svyjdivdec)

here are the references

(Shorrocks, 1984) and (Rohde, 2016) and (Biewen and Jenkins, 2003)

3.3.4 Rényi Divergence (svyrenyi)

here are the references

(Langel, 2012)

Chapter 4

Multidimensional Indices

4.1 Alkire-Foster Class and Decomposition (svyafc, svyafcdec)

In November 2015, Christopher Jindra presented at the Oxford Poverty and Human Development Initiative on the Alkire-Foster multidimensional poverty measure. His presentation can be viewed here. The example below reproduces those statistics.

Load and prepare the same data set:

```r
# load the convey package
library(convey)

# load the survey library
library(survey)

# load the stata-style webuse library
library(webuse)

# load the same microdata set used by Jindra in his presentation
webuse("nlsw88")

# coerce that `tbl_df` to a standard R `data.frame`
nlsw88 <- data.frame( nlsw88 )

# create a `collgrad` column
nlsw88$collgrad <-
    factor(
        as.numeric( nlsw88$collgrad ) ,
        label = c( 'not college grad' , 'college grad' ) ,
        ordered = TRUE
    )

# initiate a linearized survey design object
des_nlsw88 <- svydesign( ids = ~1 , data = nlsw88 )

# immediately run the `convey_prep` function on the survey design
des_nlsw88 <- convey_prep(des_nlsw88)
```

Replicate PDF page 9

21

```r
page_nine <-
  svyafc(
    ~ wage + collgrad + hours ,
    design = des_nlsw88 ,
    cutoffs = list( 4, 'college grad' , 26 ) ,
    k = 1/3 , g = 0 ,
    na.rm = TRUE
  )

# MO and seMO
print( page_nine )
```

```
##      alkire-foster     SE
## [1,]      0.36991 0.0053
```

```r
# H seH and A seA
print( attr( page_nine , "extra" ) )
```

```
##       coef          SE
## H 0.8082070 0.008316807
## A 0.4576895 0.004573443
```

Replicate PDF page 10

```r
page_ten <- NULL

# loop through every poverty cutoff `k`
for( ks in seq( 0.1 , 1 , .1 ) ){

    this_ks <-
        svyafc(
            ~ wage + collgrad + hours ,
            design = des_nlsw88 ,
            cutoffs = list( 4 , 'college grad' , 26 ) ,
            k = ks ,
            g = 0 ,
            na.rm = TRUE
          )

    page_ten <-
        rbind(
          page_ten ,
          data.frame(
              k = ks ,
              MO = coef( this_ks ) ,
              seMO = SE( this_ks ) ,
              H = attr( this_ks , "extra" )[ 1 , 1 ] ,
              seH = attr( this_ks , "extra" )[ 1 , 2 ] ,
              A = attr( this_ks , "extra" )[ 2 , 1 ] ,
              seA = attr( this_ks , "extra" )[ 2 , 2 ]
          )
        )

}
```

Table 4.1: Here is a nice table!

k	MO	seMO	H	seH	A	seA
0.1	0.3699078	0.0053059	0.8082070	0.0083168	0.4576895	0.0045734
0.2	0.3699078	0.0053059	0.8082070	0.0083168	0.4576895	0.0045734
0.3	0.3699078	0.0053059	0.8082070	0.0083168	0.4576895	0.0045734
0.4	0.1865894	0.0068123	0.2582516	0.0092455	0.7225101	0.0051745
0.5	0.1865894	0.0068123	0.2582516	0.0092455	0.7225101	0.0051745
0.6	0.1865894	0.0068123	0.2582516	0.0092455	0.7225101	0.0051745
0.7	0.0432649	0.0042978	0.0432649	0.0042978	1.0000000	0.0000000
0.8	0.0432649	0.0042978	0.0432649	0.0042978	1.0000000	0.0000000
0.9	0.0432649	0.0042978	0.0432649	0.0042978	1.0000000	0.0000000
1.0	0.0432649	0.0042978	0.0432649	0.0042978	1.0000000	0.0000000

```
knitr::kable(
  page_ten , caption = 'Here is a nice table!',
  booktabs = TRUE
)
```

still need to replicate PDF page 13

https://github.com/DjalmaPessoa/convey/issues/168

then keep going replicating this

https://github.com/DjalmaPessoa/convey/issues/154

(Alkire and Foster, 2011) and (Sabina Alkire and Ballon, 2015) and (Pacifico and Poge, 2016)

4.2 Bourguignon (1999) inequality class (svybmi)

(Bourguignon, 1999) and (Ana Lugo, 2007)

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