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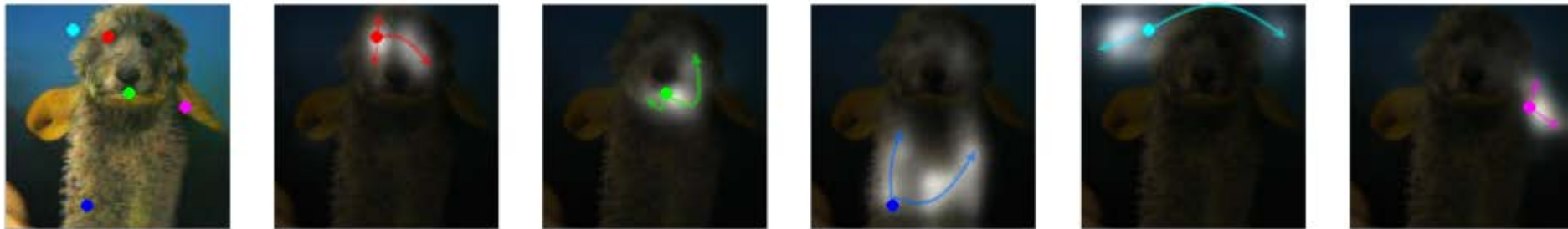
# Self-Attention Generative Adversarial Networks

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*Han Zhang, et al., arXiv*  
2019/02/19, KangYeol Kim

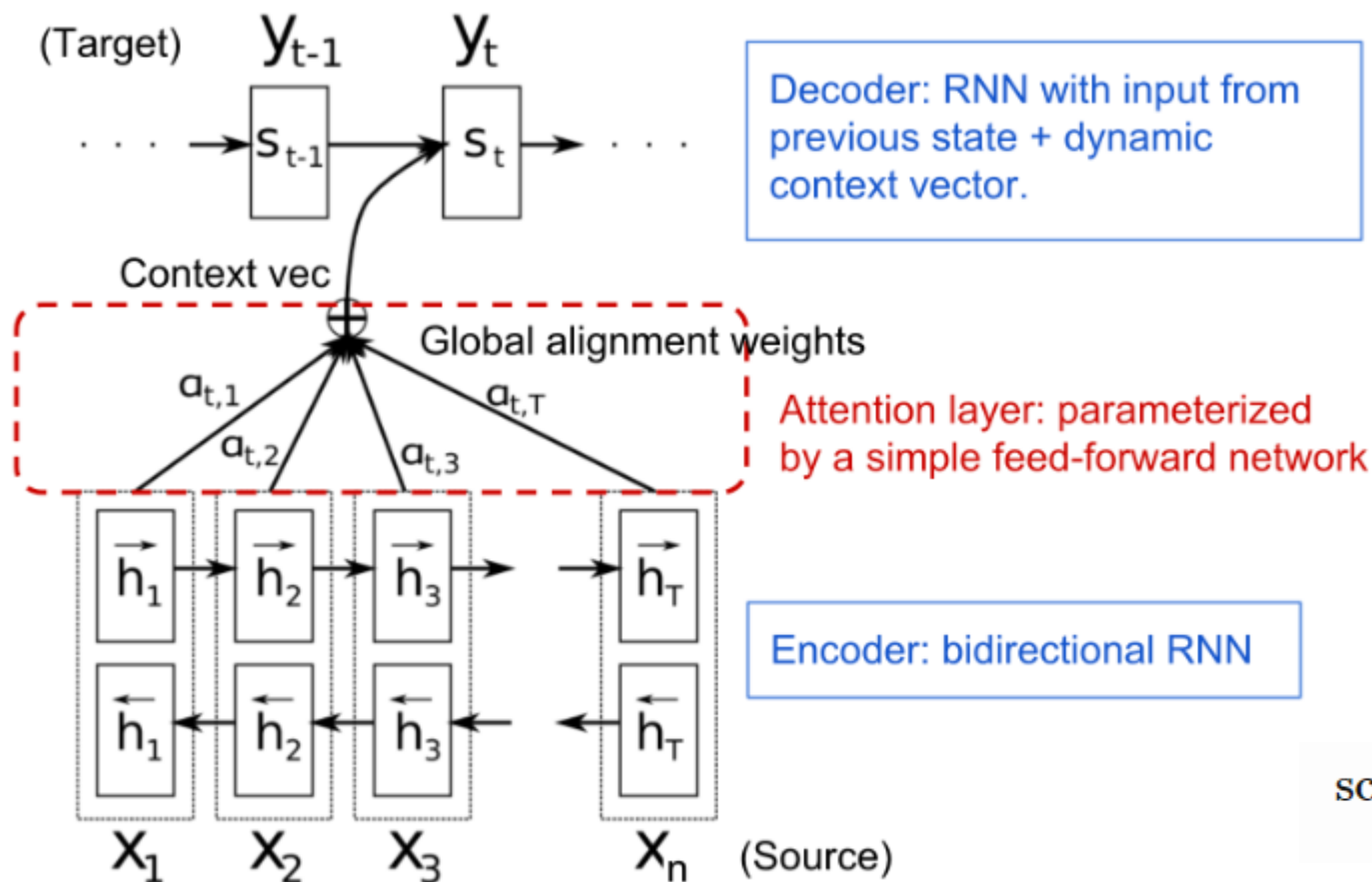
# Motivation

- Previous GAN models bear the limitation that they **fail to capture geometric or structural patterns** that occur consistently in some classes (for example, dogs are often drawn with realistic fur texture but without clearly defined separate feet).
- One possible explanation for this is it mainly due to limited range of receptive field, thus model **cannot learn about long-term dependencies** (i.e. relationship between distant regions)
- The self-attention module calculates response at a position **as a weighted sum of the features at all positions**, where the weights – or attention vectors – are calculated with only a small computational cost.



The most-attended regions depending on each different colored query

# What is Attention in NMT ?



$$c_t = \sum_{i=1}^n \alpha_{t,i} h_i$$

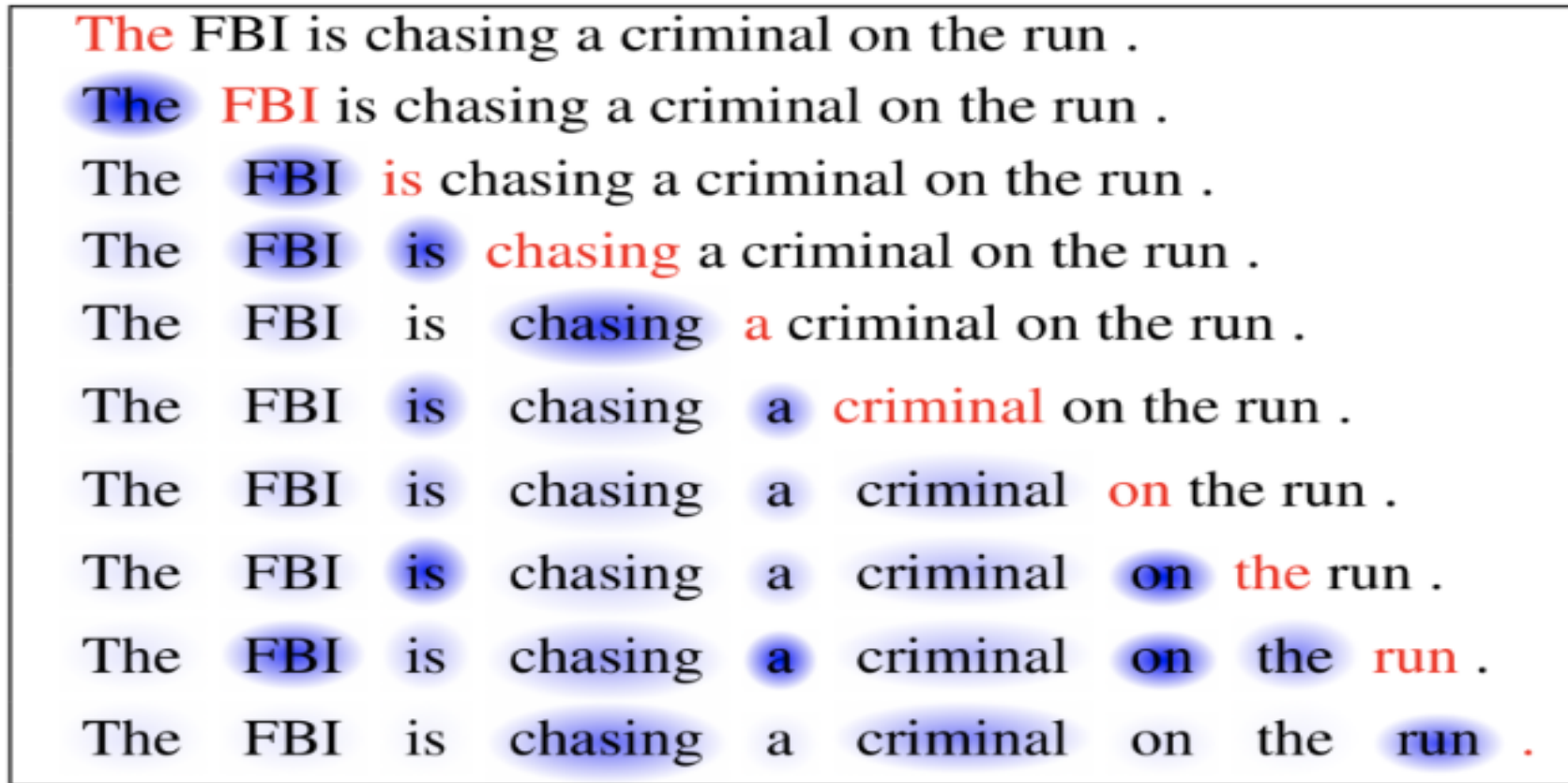
$$\alpha_{t,i} = \text{align}(y_t, x_i) = \frac{\exp(\text{score}(s_{t-1}, h_i))}{\sum_{i'=1}^n \exp(\text{score}(s_{t-1}, h_{i'}))}$$

$$\text{score}(s_t, h_i) = \mathbf{v}_a^\top \tanh(\mathbf{W}_a[s_t; h_i])$$

SO SO MANY score functions!!!

# What is Self-Attention in NMT ?

- Machine can learn **where to attend** by the relationship with other words in the sentence.
- We can represent same words differently based on the contexts.(Same in images)



The diagram illustrates self-attention in NMT by showing 10 sentences where different words are highlighted in red and blue. The sentences are:

- The FBI is chasing a criminal on the run .
- The FBI is chasing a criminal on the run .
- The FBI is chasing a criminal on the run .
- The FBI is chasing a criminal on the run .
- The FBI is chasing a criminal on the run .
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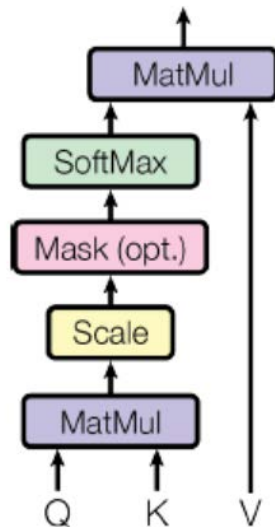
In each sentence, the words are highlighted in red and blue to show different attention weights. The words are: The, FBI, is, chasing, a, criminal, on, the, run, .

# Query, Key, Value Computation

## Assume,

- Encoded representation of the input -  $(\mathbf{K}, \mathbf{V})$  ( $n \times p$ )
- Target Query –  $\mathbf{Q}$  ( $n \times p$ )
- $n$  = # of words in sequence /  $p$  = embedded dimension

$$\text{Attention}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \text{softmax}\left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{n}}\right)\mathbf{V}$$



$$1) \begin{matrix} Q \\ \left( \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right) \\ p \end{matrix} \times \begin{matrix} K^T \\ \left( \begin{array}{c} | \\ | \\ | \end{array} \right) \\ n \end{matrix} = \begin{matrix} C \\ \left( \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right) \\ n \end{matrix} ; \text{Correlation upon Query}$$

$$2) \text{row-wise softmax} \left( \begin{matrix} C \\ \left( \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right) \\ n \end{matrix} \times \frac{1}{\sqrt{n}} \right) = \begin{matrix} \text{Attn} \\ \left( \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right) \\ n \end{matrix} ; \text{Attention Weight}$$

$$3) \begin{matrix} \text{Attn} \\ \left( \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right) \\ n \end{matrix} \times \begin{matrix} V \\ \left( \begin{array}{c} | \\ | \\ | \end{array} \right) \\ p \end{matrix} = \begin{matrix} Z \\ \left( \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right) \\ p \end{matrix} ; \text{Attended Value}$$

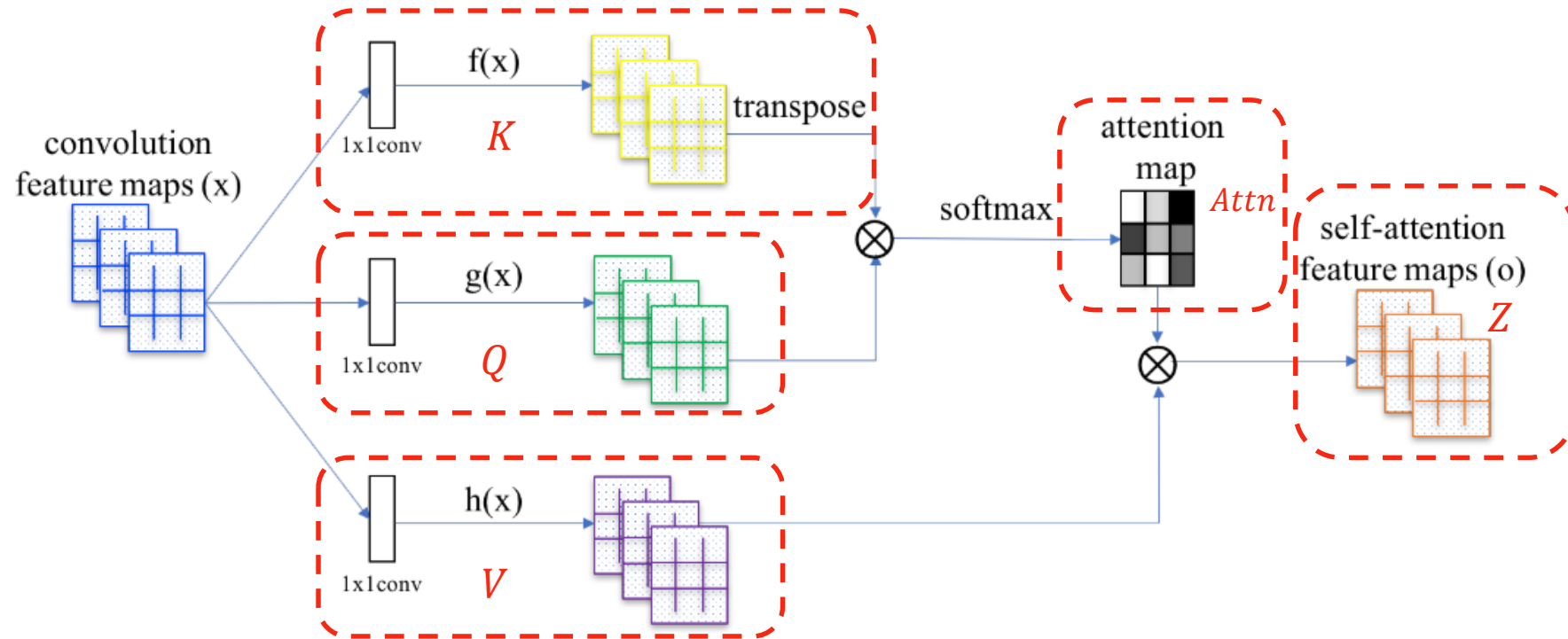
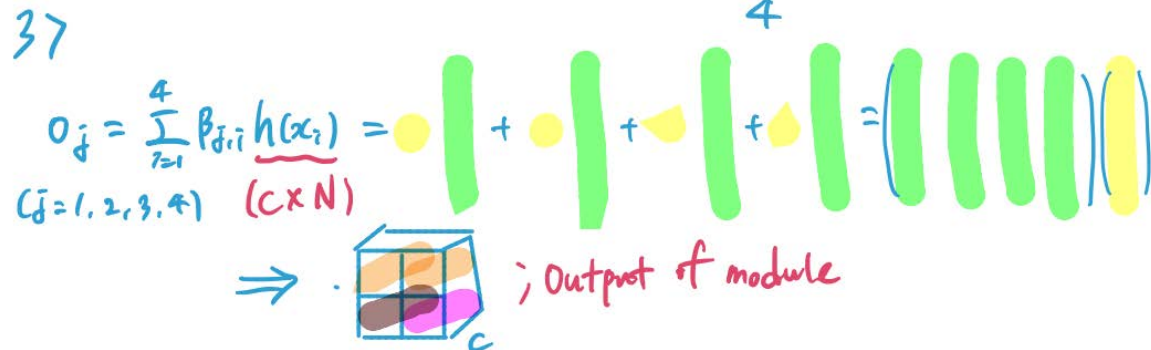
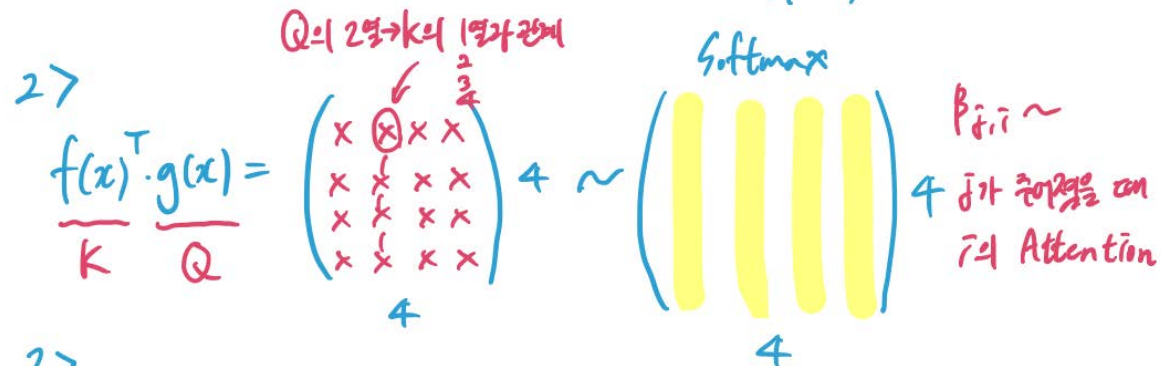
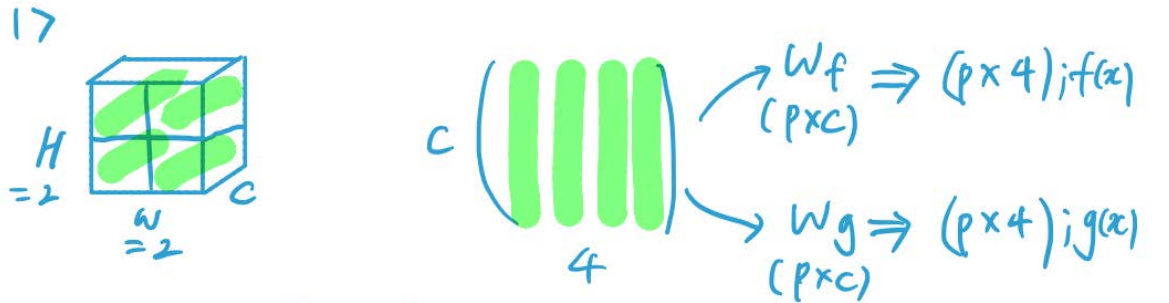


Figure 2: The proposed self-attention mechanism. The  $\otimes$  denotes matrix multiplication. The softmax operation is performed on each row.



$$(1) \quad x \in \mathbb{R}^{C \times N}$$

$$f(x) = W_f x, \quad g(x) = W_g x$$

(2)

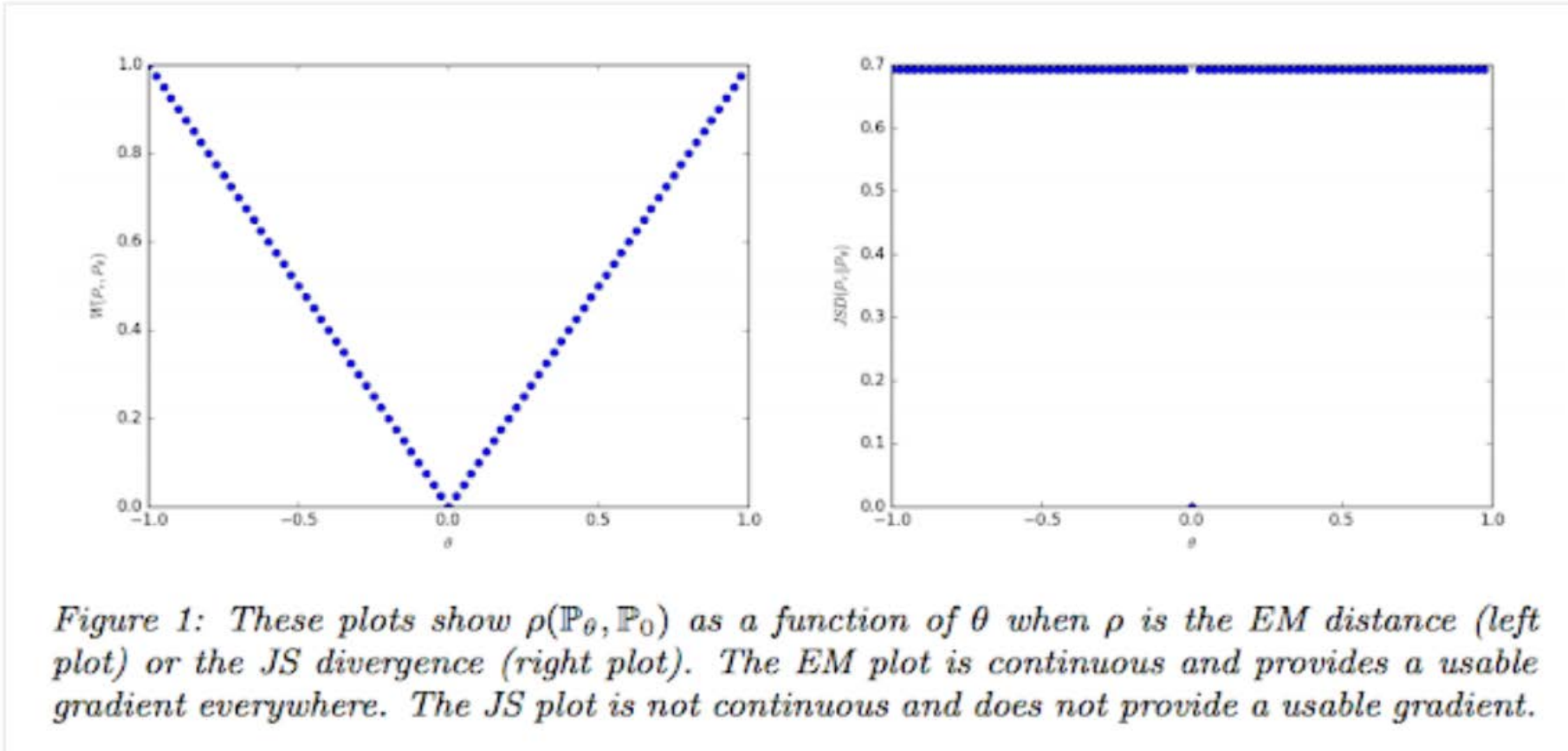
$$\beta_{j,i} = \frac{\exp(s_{ij})}{\sum_{i=1}^N \exp(s_{ij})}, \text{ where } s_{ij} = f(x_i)^T g(x_j),$$

(3)

$$o_j = \sum_{i=1}^N \beta_{j,i} h(x_i), \text{ where } h(x_i) = W_h x_i.$$

1. 행렬  $A$ 의 *spectral norm* = 행렬  $A$ 의 가장 큰 *singular value*
2. 행렬의 *singular value*는 어떤 벡터  $a$ 를 곱했을 때, 이리저리 늘어나는 방향의 늘어나는 정도를 의미함, 따라서 대충  $A$ 의 *spectral norm*를 제약하는 것은 곱해지는 벡터가 삐죽 삐죽하게 나오는 것이 아니라 smooth하게 나오는 것을 의미함
3. 모델  $g$ 에 대해서 *Lipschitz norm*,  $\|g\|_{Lip}$ 는  $g$ 의 gradient( $\nabla g$ )의 *spectral norm*이다. 그러면  $g$ 의 *Lipschitz norm*를 제한하는 것은 gradient의 *spectral norm*를 제약해서 gradient space가 smooth하게 될 수 있도록 해준다.
4. 계산을 해보면  $\|g\|_{Lip} \leq \prod sn(W^l)$ ,  $W = \text{weight matrix}$  (참고로 *relu*같은 activation function은 일정 상수로 *Lipschitz norm*이 계산됨)
5. 따라서  $W_{SN} \leftarrow W/sn(W)$ 로 normalization 시켜서 모델의 *Lipschitz norm*를 제약한다.





Parameter space after  
gradient space smoothed

Parameter space before  
gradient space smoothed

# Stabilization Result

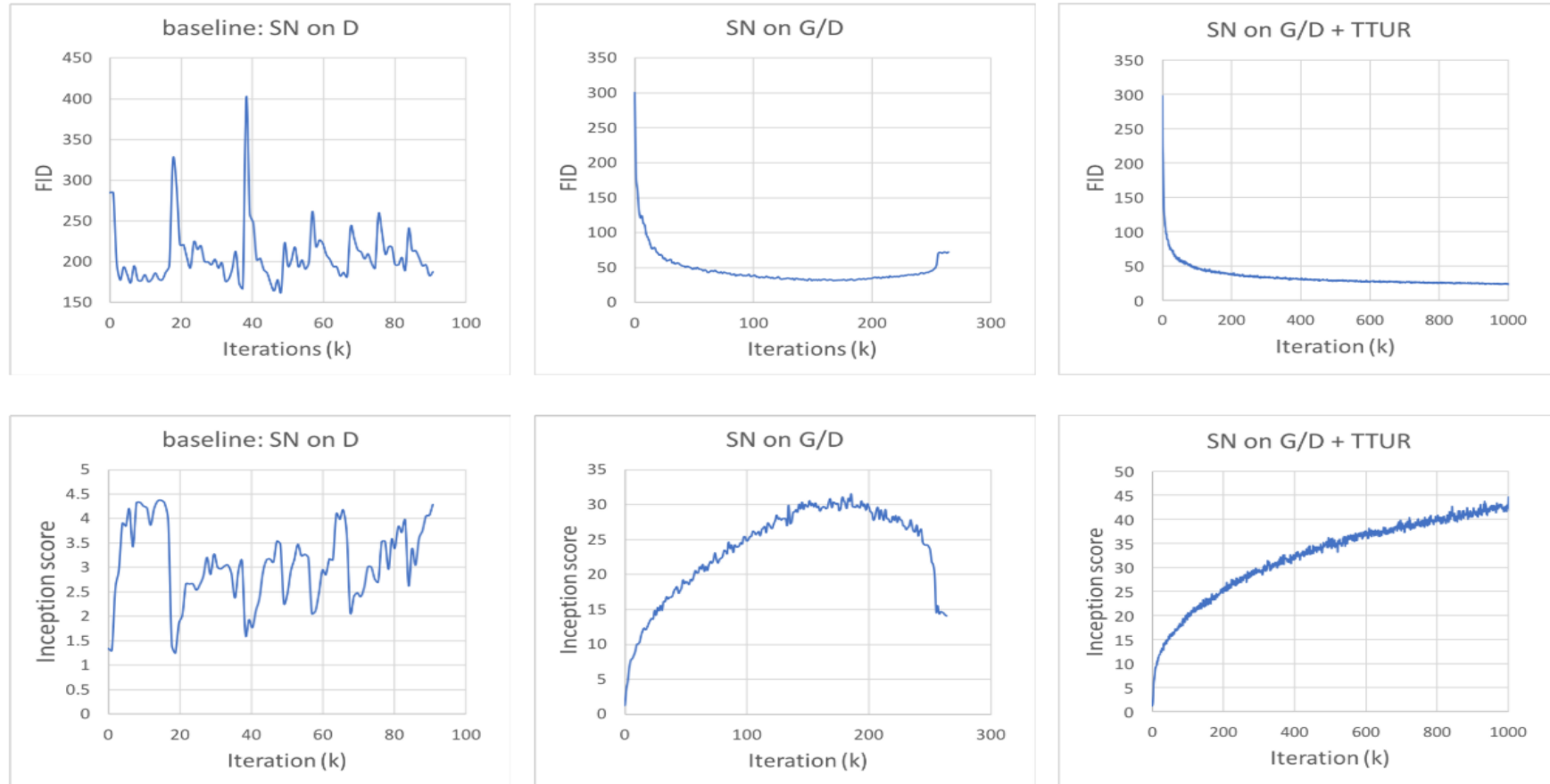


Figure 3: Training curves for the baseline model and our models with the proposed stabilization techniques, “SN on  $G/D$ ” and two-timescale learning rates (TTUR). All models are trained with 1:1 balanced updates for  $G$  and  $D$ .

# Generation Result (1)



Figure 4:  $128 \times 128$  examples randomly generated by the baseline model and our models “SN on  $G/D$ ” and “SN on  $G/D+TTUR$ ”.

## Generation Result (2)

Model	no attention	SAGAN				Residual			
		$feat_8$	$feat_{16}$	$feat_{32}$	$feat_{64}$	$feat_8$	$feat_{16}$	$feat_{32}$	$feat_{64}$
FID	22.96	22.98	22.14	<b>18.28</b>	18.65	42.13	22.40	27.33	28.82
IS	42.87	43.15	45.94	51.43	<b>52.52</b>	23.17	44.49	38.50	38.96

Table 1: Comparison of Self-Attention and Residual block on GANs. These blocks are added into different layers of the network. All models have been trained for one million iterations, and the best Inception scores (IS) and Fréchet Inception distance (FID) are reported.

Thanks a lot !!  
Any Questions?