

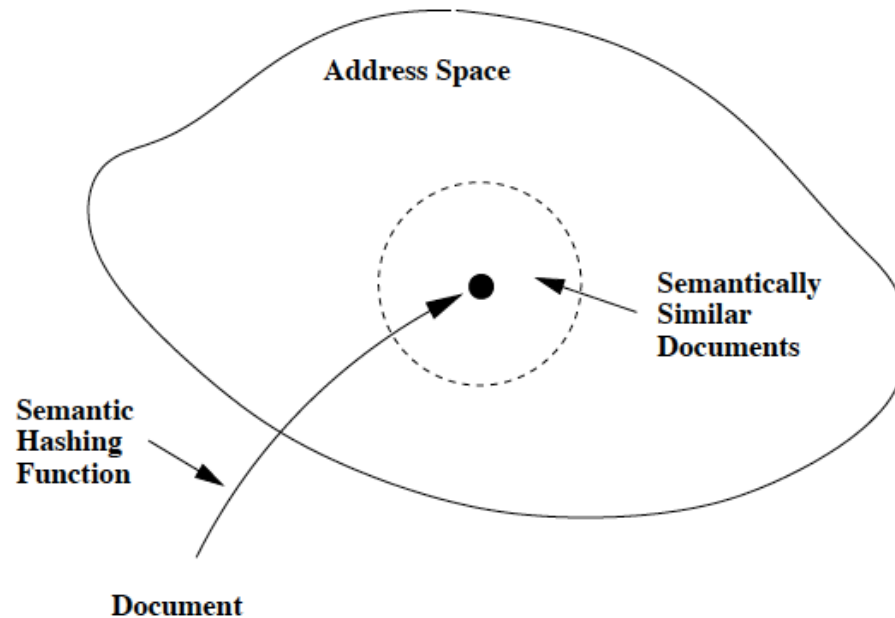
Theory and Experiments on Vector Quantized Autoencoders

Van den Oord et al.

Park Jungsoo

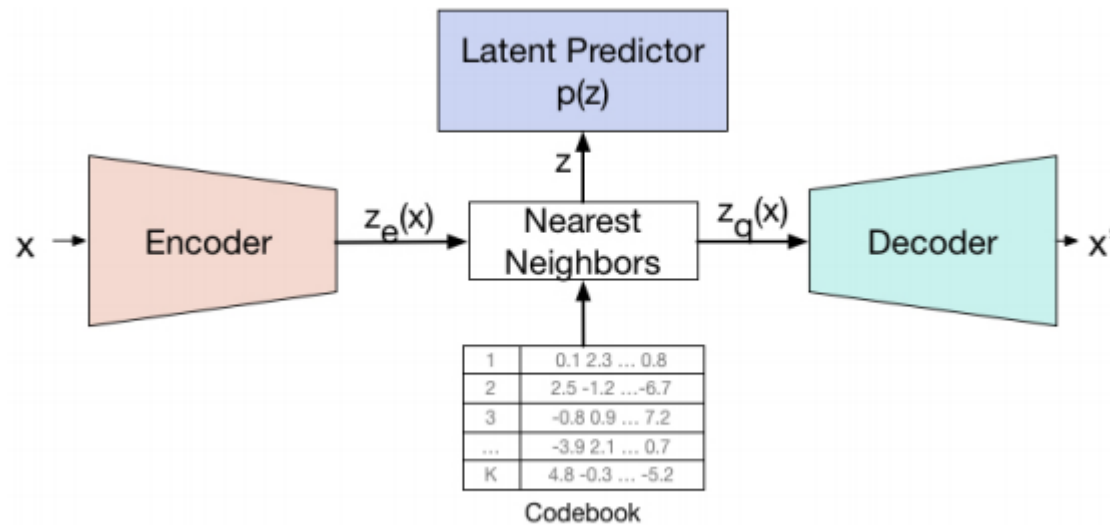
Data Mining & Information Systems Lab.
Department of Computer Science and Engineering,
College of Informatics, Korea University

Why Discrete Latent Representation?



- Computational Efficiency
- Interpretability and Communication
- More Natural

VQ-VAE



$$z_i = \arg \min_{j \in [K]} \|z_e(x_i) - e_j\|_2$$

$$L = l_r + \beta \|z_e(x_i) - \text{sg}(z_q(x_i))\|_2,$$

$$z_q(x_i) = e_{z_i}$$

$$\text{sg}(x) = \begin{cases} x & \text{forward pass} \\ 0 & \text{backward pass} \end{cases}$$

EMA Update ver.

$$c_j \leftarrow \lambda c_j + (1 - \lambda) \sum_i \mathbb{1} [z_q(x_i) = e_j],$$

$$e_j \leftarrow \lambda e_j + (1 - \lambda) \sum_i \frac{\mathbb{1} [z_q(x_i) = e_j] z_e(x_i)}{c_j},$$

- Calculation of averages of different subsets of the full data set.
- When used in updating embedding vectors, (instead of gradient) more stable in training.

EM Algorithm

1. **E step:** $(z_1, \dots, z_N) \leftarrow \arg \max_{z_1, \dots, z_N} P_{\Theta}(x_1, \dots, x_N, z_1, \dots, z_N),$
2. **M step:** $\Theta \leftarrow \arg \max_{\Theta} P_{\Theta}(x_1, \dots, x_N, z_1, \dots, z_N)$

K-Means Clustering is one of EM-Algorithm

$$\Theta = \langle \mu^1, \dots, \mu^K \rangle, \quad \mu^k \in R^D.$$

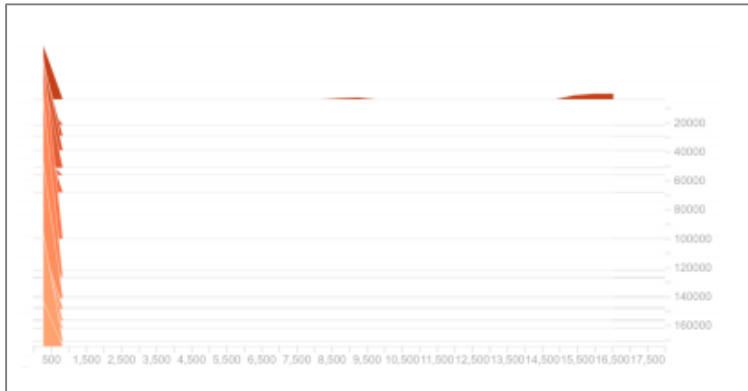
1. **E step:** Cluster assignment is given by,

$$z_i \leftarrow \arg \min_{j \in [K]} \|\mu^j - x_i\|_2^2,$$

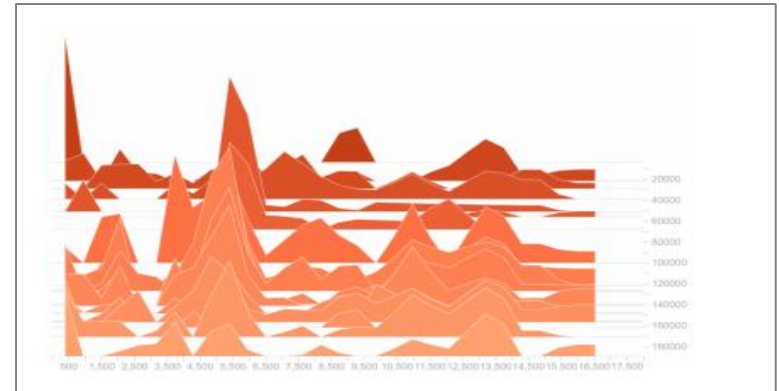
2. **M step:** The means of the clusters are updated as,

$$c_j \leftarrow \sum_{i=1}^N \mathbb{1}[z_i = j]; \quad \mu^j \leftarrow \frac{1}{c_j} \sum_{i=1}^N \mathbb{1}[z_i = j] x_i.$$

Index Collapse



Index Collapse



Ideal Case

- X axis corresponds to the different possible discrete latent codes, Y axis corresponds to the progression of training steps.
- Only few latent embedding vectors are selected, and updated.

VQ-VAE training with EM

Instead of **indexing**

$P_{\Theta}(z_i | z_e(x_i)) \propto e^{-\|e_{z_i} - z_e(x_i)\|_2^2}$ Define probability distribution over embedding vectors

$$z_i^1, \dots, z_i^m \sim \text{Multinomial} \left(-\|e_1 - z_e(x_i)\|_2^2, \dots, -\|e_K - z_e(x_i)\|_2^2 \right)$$

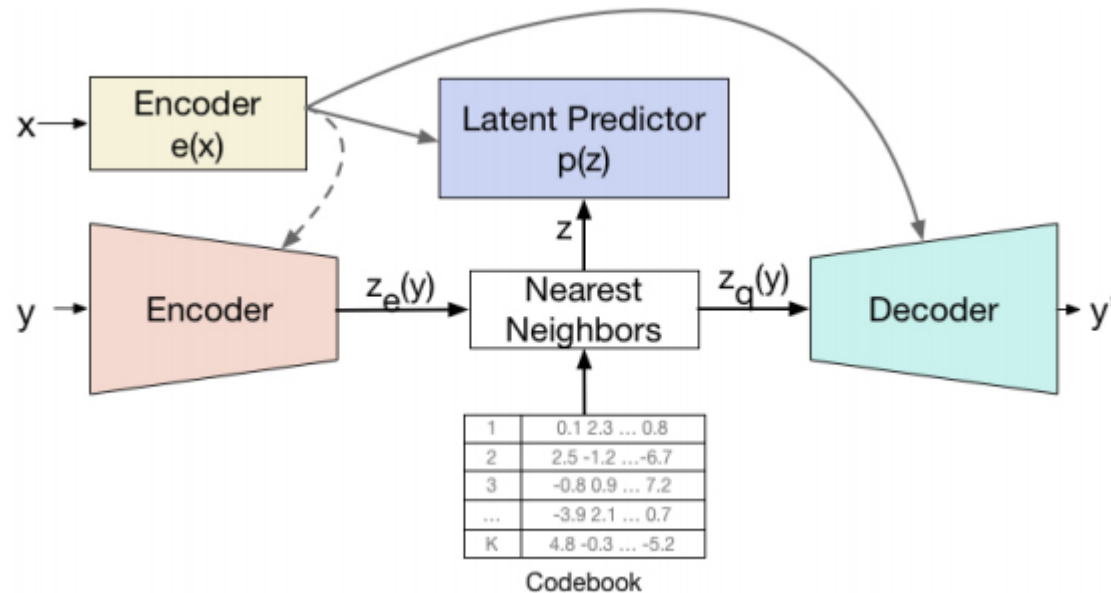
**Monte Carlo
Approximate**

E step: $z_i^1, \dots, z_i^m \leftarrow \text{Multinomial} \left(-\|e_1 - z_e(x_i)\|_2^2, \dots, -\|e_K - z_e(x_i)\|_2^2 \right)$

M step: $c_j \leftarrow \frac{1}{m} \sum_{i=1}^N \sum_{l=1}^m \mathbb{1}[z_i^l = j]; \quad e_j \leftarrow \frac{1}{mc_j} \sum_{i=1}^N \sum_{l=1}^m \mathbb{1}[z_i^l = j] z_e(x_i).$

$$z_q(x_i) = \frac{1}{m} \sum_{l=1}^m e_{z_i^l}.$$

Machine Translation



- Encoder function is a series of convolutional layers with residual connections
- Source sentence is encoded in to sequence of hidden states through multiple causal self-attention layers
- Decoder consists of **transpose convolutional layers** whose output is fed to a transformer decoder with causal attention.

Machine Translation

| Model | n_c | n_s | BLEU | Latency | Speedup |
|--|-------|-------|-------------|---------|---------|
| Autoregressive Model (beam size=4) | - | - | 28.1 | 331 ms | 1× |
| Autoregressive Baseline (no beam-search) | - | - | 27.0 | 265 ms | 1.25× |
| NAT + distillation | - | - | 17.7 | 39 ms | 15.6× |
| NAT + distillation + NPD=10 | - | - | 18.7 | 79 ms | 7.68× |
| NAT + distillation + NPD=100 | - | - | 19.2 | 257 ms | 2.36× |
| LT + Semhash | - | - | 19.8 | 105 ms | 3.15× |
| Our Results | | | | | |
| VQ-VAE | 3 | - | 21.4 | 81 ms | 4.08× |
| VQ-VAE with EM | 3 | 5 | 22.4 | 81 ms | 4.08× |
| VQ-VAE + distillation | 3 | - | 26.4 | 81 ms | 4.08× |
| VQ-VAE with EM + distillation | 3 | 10 | 26.7 | 81 ms | 4.08× |
| VQ-VAE with EM + distillation | 4 | 10 | 25.4 | 58 ms | 5.71× |

Image Generation

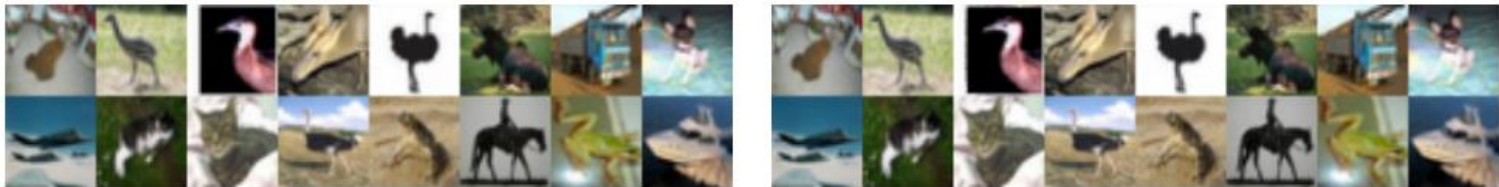


Figure 4: Samples of original and reconstructed images from CIFAR-10 using VQ-VAE trained using EM with a code-book of size 2^8 .

| Model | n_s | Log perplexity |
|------------------|-------|----------------|
| ImageTransformer | - | 2.92 |
| VAE | - | 4.51 |
| VQ-VAE [31] | - | 4.67 |
| VQ-VAE (Ours) | - | 4.83 |
| EM | 5 | 4.80 |