# TADAM: Task dependent adaptive metric for improved few-shot learning

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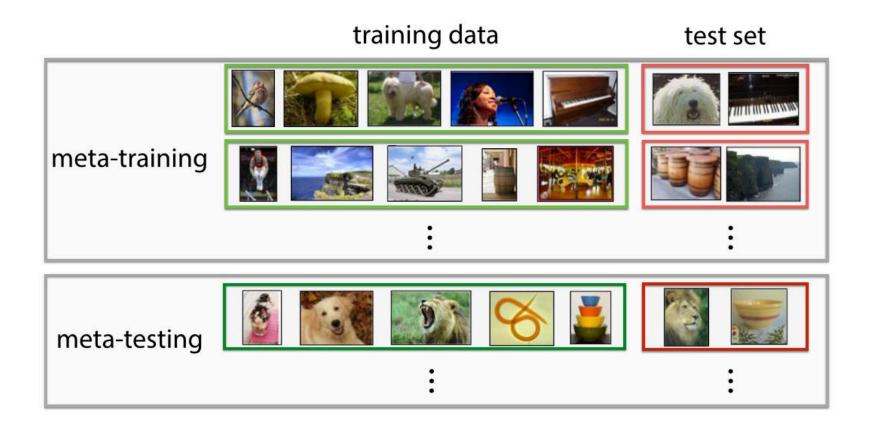




### 1

#### Introduction

Few-shot learning



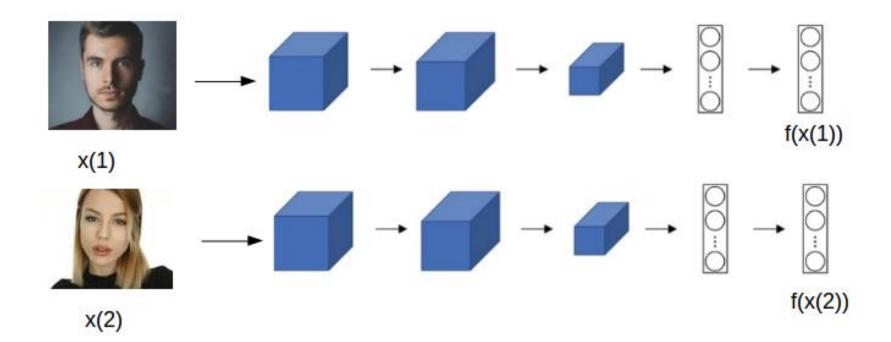




### 1

#### Introduction

Metric Learning







# 2 Abstract Metric Learning

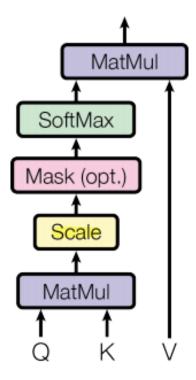
- Metric scaling

- Metric task conditioning





#### Scaled Dot-Product Attention

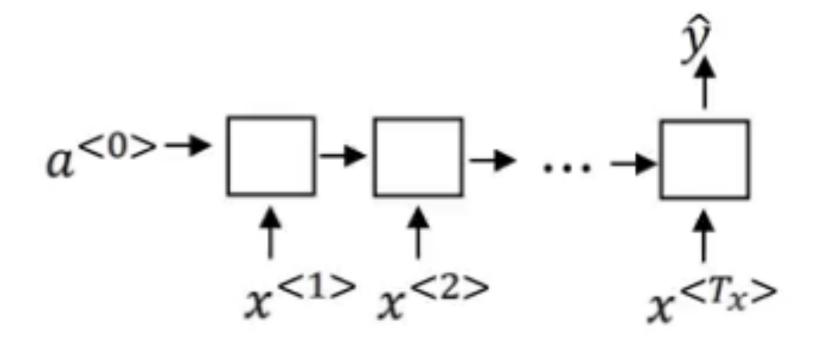






#### Abstract

Metric task conditioning







# Contribution Task-dependent metric space

- Learner를 task sample set에 한정해서 task-dependent metric space를 학습

- Task-dependent metric space를 학습시키기 위해서 auxiliary task co-training을 기반으로 한 end-to-end optimization을 제안

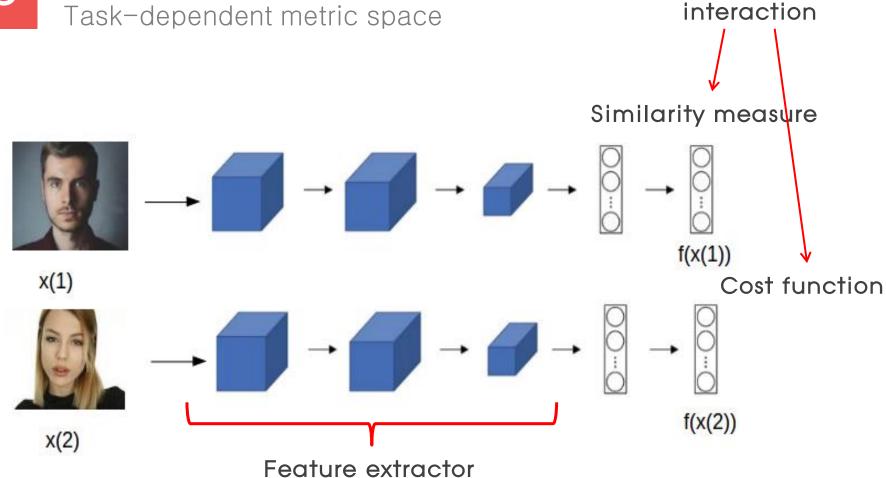






#### Contribution

Task-dependent metric space





Auxiliary task co-training







#### Background

Task-dependent metric space

$$\mathcal{S} = \{(\mathbf{x}_i, y_i)\}_{i=1}^{MK}$$

$$-\log p_{\phi}(y=k|\mathbf{x})$$

$$\mathcal{Q} = \{(\mathbf{x}_i, y_i)\}_{i=1}^q$$

$$p_{\phi}(y = k | \mathbf{x}) = \operatorname{softmax}(-d(f_{\phi}(\mathbf{x}), \mathbf{c}_k))$$

$$\mathbf{x}_i \in \mathbb{R}^{D_{\mathbf{x}}}$$

$$f_{\phi}: \mathbb{R}^{D_{\mathbf{z}}} o \mathbb{R}^{D_{\mathbf{z}}}$$

$$S_k$$
:  $\mathbf{c}_k = \frac{1}{K} \sum_{\mathbf{x}_i \in S_k} f_{\phi}(\mathbf{x}_i)$ 





#### Model

Class-wise cross-entropy loss

$$J_k(\phi, \alpha) = \sum_{\mathbf{x}_i \in \mathcal{Q}_k} \left[ \alpha d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_k) + \log \sum_j \exp(-\alpha d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_j)) \right]$$

$$\frac{\partial}{\partial \phi} J_k(\phi, \alpha) = \alpha \sum_{\mathbf{x}_i \in \mathcal{Q}_k} \left[ \frac{\partial}{\partial \phi} d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_k) - \frac{\sum_j \exp(-\alpha d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_j)) \frac{\partial}{\partial \phi} d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_j)}{\sum_j \exp(-\alpha d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_j))} \right]$$





#### Model

#### Class-wise cross-entropy loss

#### Lemma 1 (Metric scaling). If the following assumptions hold:

$$\mathcal{A}_1: d(f_{\phi}(\mathbf{x}), \mathbf{c}_k) \neq d(f_{\phi}(\mathbf{x}'), \mathbf{c}_k), \forall k, \mathbf{x} \neq \mathbf{x}' \in \mathcal{Q}_k; \quad \mathcal{A}_2: \left| \frac{\partial}{\partial \phi} d(f_{\phi}(\mathbf{x}), \mathbf{c}) \right| < \infty, \forall \mathbf{x}, \mathbf{c}, \phi,$$

then it is true that:

$$\lim_{\alpha \to 0} \frac{1}{\alpha} \frac{\partial}{\partial \phi} J_k(\phi, \alpha) = \sum_{\mathbf{x}_i \in \mathcal{Q}_k} \left[ \frac{K - 1}{K} \frac{\partial}{\partial \phi} d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_k) - \frac{1}{K} \sum_{j \neq k} \frac{\partial}{\partial \phi} d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_j) \right],$$

$$\lim_{\alpha \to \infty} \frac{1}{\alpha} \frac{\partial}{\partial \phi} J_k(\phi, \alpha) = \sum_{\mathbf{x}_i \in \mathcal{Q}_k} \left[ \frac{\partial}{\partial \phi} d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_k) - \frac{\partial}{\partial \phi} d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_{j_i^*}) \right];$$

where  $j_i^* = \arg\min_j d(f_{\phi}(\mathbf{x}_i), \mathbf{c}_j)$ .

*Proof.* Please refer to Appendix A.

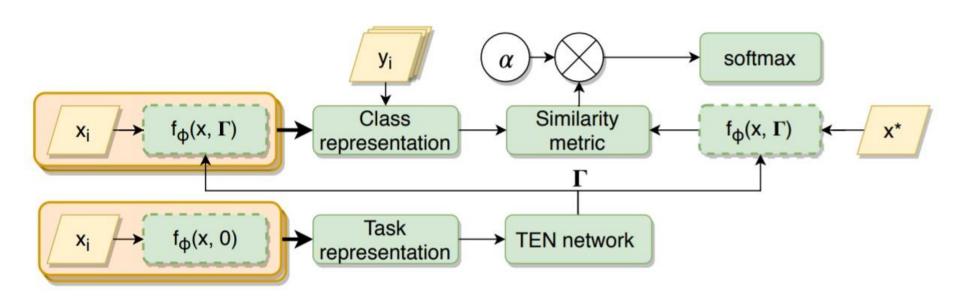




### 5

#### Model

#### Task representation







# 5 Model Task conditioning

Table 1: mini-Imagenet (Vinyals et al. [33]), 5-way classification results. †Our re-implementation.

	1-shot	5-shot	10-shot
Meta Nets [22]	43.4	60.6	-
Matching Networks [33]	46.6	60.0	-
MAML [6]	48.7	63.1	-
Proto Nets [28]	49.4	68.2	$74.3^{\dagger}$
Relation Net [29]	50.4	65.3	-
SNAIL [16]	55.7	68.9	-
Discriminative k-shot [1]	56.3	73.9	78.5
adaResNet [17]	56.9	71.9	-
Ours	58.5	76.7	80.8



