
Engineering Circuits Analysis (ICE2002)

Chapter 1. Circuit Variables

Contents

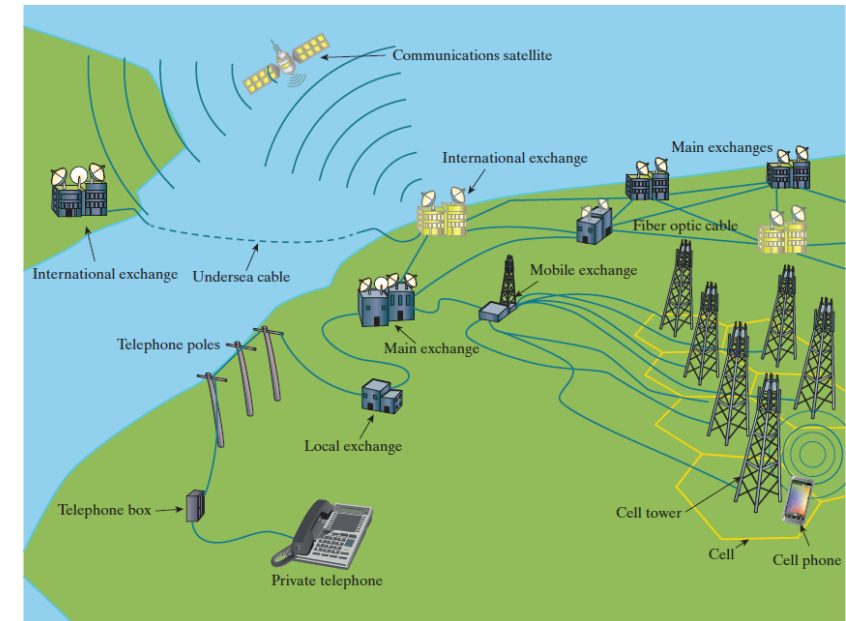
- The International System of Units (SI)
- Circuit Analysis: An Overview
- Voltage and Current
- Power and Energy

Electrical Engineering: An Overview

Electrical engineering is the profession concerned with systems that produce, transmit, and measure electric signals

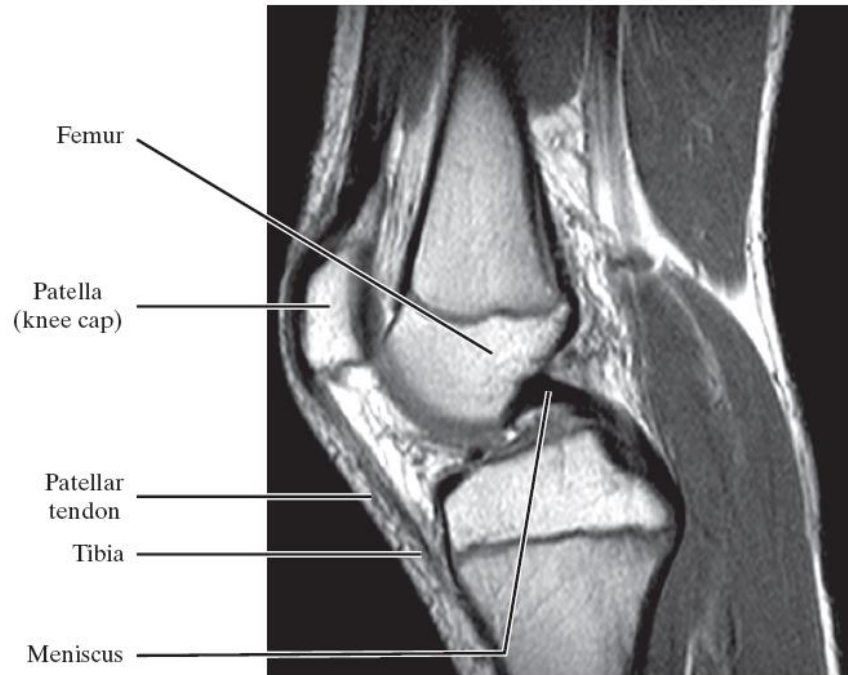
- Communication systems
- Computer systems
- Control systems
- Power systems
- Signal-processing systems

All systems are composed of electric circuits



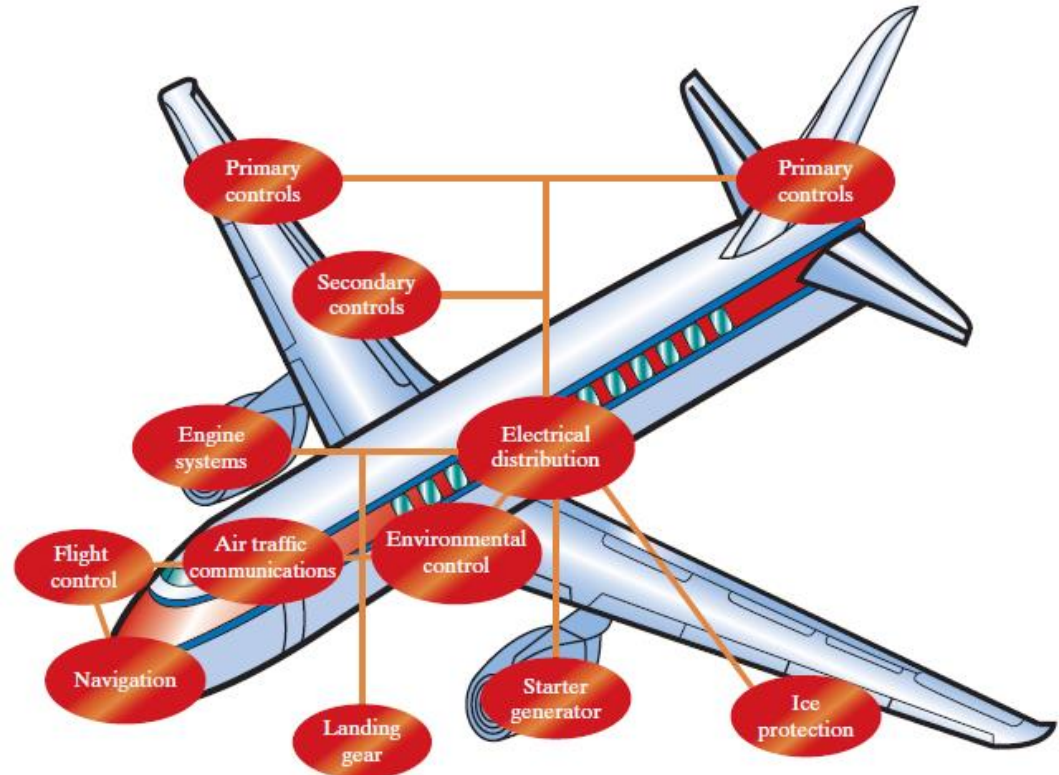
Telephone systems

Electrical Engineering: An Overview



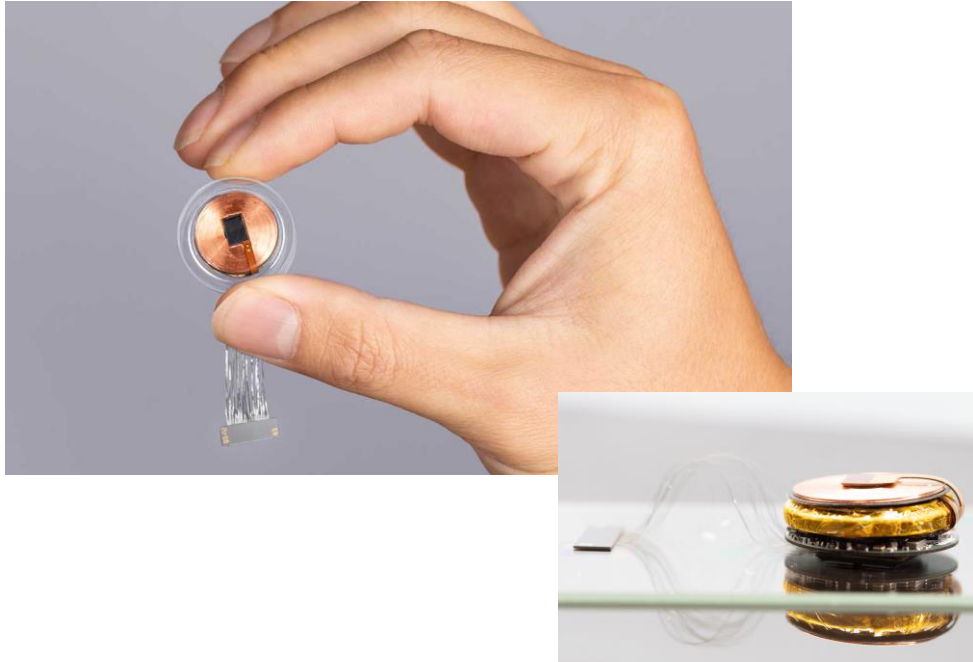
Neil Borden/Science Source/Getty Images

MRI scan of an adult knee joint



Interacting systems on a commercial aircraft

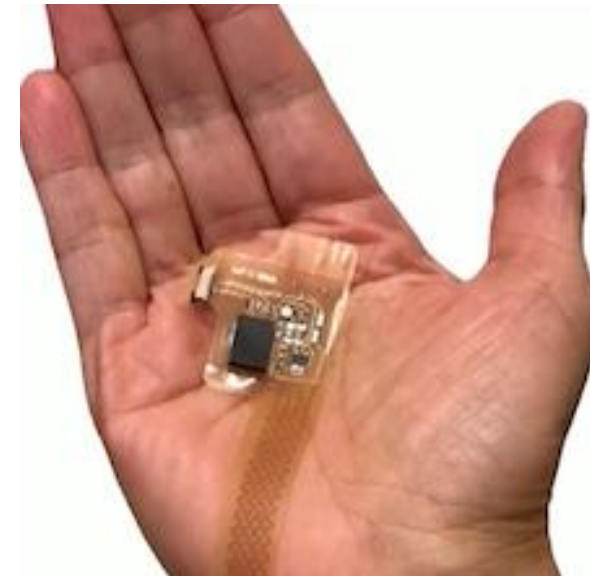
Electrical Engineering: An Overview



Implantable medical devices for brain-machine interfaces (BMI), Neuralink



UC Berkeley, USA



Stanford, USA

Wearable electronics for healthcare and medicine

Circuit Analysis

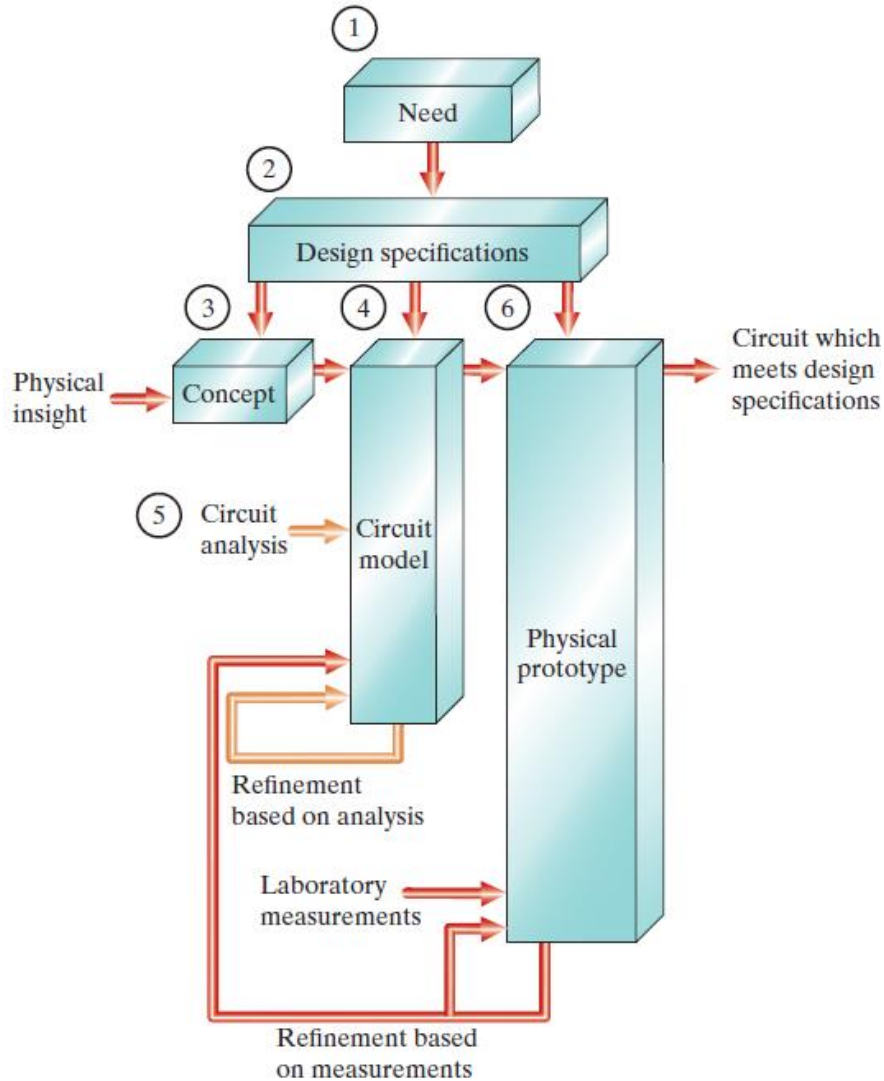
- **Electric circuits** is a **mathematical model** that approximates the behavior of an actual electrical system
- The goal of **circuit analysis** is to understand “ideal circuits” and the constraints imposed on current-voltage relationship resulting from interconnecting “ideal elements”
- The resulting interconnection (the “circuit”) will quantitatively (or approximately) predict the behaviors of the electrical system it is intended to present.

Circuit Analysis

- **Three basic assumptions**

1. Electrical effects happen instantaneously throughout a system.
2. The net charge on every components in the system is always zero.
3. There is no magnetic coupling between the components in a system.

Circuit Analysis



- **Circuit model:** mathematical model for electrical systems
- **Circuit analysis** is based on mathematical techniques and is used to predict the behavior of the circuit model and its ideal circuit components. It is based on the variables of **voltage** and **current**.
- **Physical prototype:** actual electrical system constructed from actual electrical components.

The International System of Units

- The International System of Units (SI) enables engineers to communicate in a meaningful way about quantitative results.

| QUANTITY | SI UNIT | |
|---------------------------|----------|--------|
| | NAME | SYMBOL |
| Length | meter | m |
| Mass | kilogram | kg |
| Time | second | s |
| Electric current | ampere | A |
| Thermodynamic temperature | kelvin | K |
| Amount of substance | mole | mol |
| Luminous intensity | candela | cd |

The International System of Units

Derived
units in SI

| QUANTITY | UNIT NAME | FORMULA | SYMBOL |
|-----------------------|-----------------------------|--------------------------------|----------|
| Acceleration — linear | meter per second per second | m/s^2 | |
| Velocity — linear | meter per second | m/s | |
| Frequency | hertz | s^{-1} | Hz |
| Force | newton | $\text{kg} \cdot \text{m/s}^2$ | N |
| Pressure or stress | pascal | N/m^2 | Pa |
| Density | kilogram per cubic meter | kg/m^3 | |
| Energy or work | joule | $\text{N} \cdot \text{m}$ | J |
| Power | watt | J/s | W |
| Electric charge | coulomb | $\text{A} \cdot \text{s}$ | C |
| Electric potential | volt | W/A | V |
| Electric resistance | ohm | V/A | Ω |
| Electric conductance | siemens | A/V | S |
| Electric capacitance | farad | C/V | F |
| Magnetic flux | weber | $\text{V} \cdot \text{s}$ | Wb |
| Inductance | henry | Wb/A | H |

The International System of Units

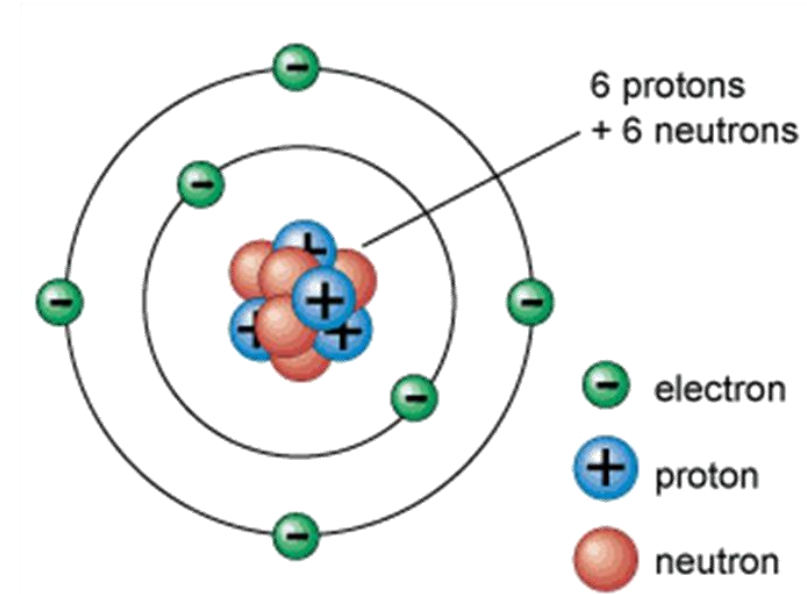
Standardized prefixes to signify power of 10

| MULTIPLE | PREFIX | SYMBOL |
|------------|--------|--------|
| 10^{12} | tera | T |
| 10^9 | giga | G |
| 10^6 | mega | M |
| 10^3 | kilo | k |
| 10^{-2} | centi | c |
| 10^{-3} | milli | m |
| 10^{-6} | micro | μ |
| 10^{-9} | nano | n |
| 10^{-12} | pico | p |
| 10^{-15} | femto | f |

Voltage and Current

■ Electric charge

- Basis for describing all electrical phenomena
- Described in positive and negative charges
- Exists in discrete quantities, which are integral multiples of the electronic charge, 1.6022×10^{-19} [C]
- Electrical effects are attributed to both the separation of charge >> electric force (voltage)
charges in motion >> electric fluid (current)



Voltage and Current

■ Voltage

- Whenever positive and negative charges are separated, energy is expended.
- Voltage is the energy per unit charge created by **charge separation**.

$$v = \frac{dw}{dq}$$

where

v = the voltage in volts,

w = the energy in joules,

q = the charge in coulombs.

Voltage and Current

■ Current

- Current is the **rate of charge flow**.

$$i = \frac{dq}{dt}$$

where

i = the current in amperes,

q = the charge in coulombs,

t = the time in seconds.

Power and Energy

■ Power

- Power is energy per unit of time; the rate of energy flow.
- If $p > 0$, power is being delivered to the circuit components.
- If $p < 0$, power is being extracted from the circuit components.

$$p = \frac{dw}{dt}$$

where

p = the power in watts,
 w = the energy in joules,
 t = the time in seconds.

$$p = \frac{dw}{dt} = \frac{dw}{dq} \cdot \frac{dq}{dt} = v \cdot i$$

Power and Energy

■ Energy

- Energy is the integral of power over time.
- If $w > 0$, energy is being stored.
- If $w < 0$, power is being dissipated.

$$p = \frac{dw}{dt}$$

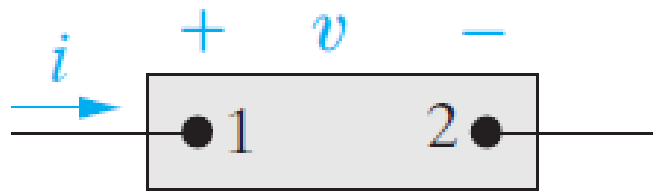
$$w = \int_{-\infty}^t p d\tau$$

where
 p = the power in watts,
 w = the energy in joules,
 t = the time in seconds.

Ideal Basic Circuit Element

■ Attributes

- Two terminals, which are points of connection to other circuit components
- Described mathematically in terms of current and/or voltage
- Cannot be subdivided into other elements



Ideal basic circuit element

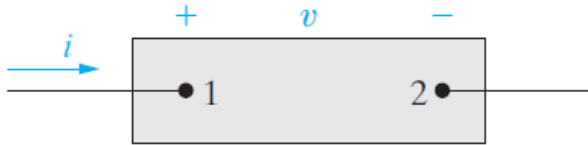
Voltage: Polarity reference for voltage can be indicated by plus (+) and minus (-) signs

Current: reference direction for the current is indicated by an arrow

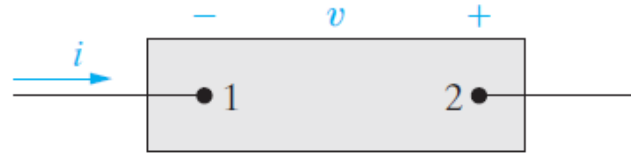
Sign Convention

■ Passive sign convention

- Reference direction for current through the element is in the direction of the reference voltage drop across the element



(a) $p = vi$



(c) $p = -vi$

If $p > 0$, power is being delivered to the box

If $p < 0$, power is being extracted from the box (battery)



(b) $p = -vi$



(d) $p = vi$

Summary

- **Electric charge**
separation of charge >> electric force (voltage)
charges in motion >> electric flow (current)
- **Current** = rate of charge flow
- **Voltage** = energy per unit charge created by charge separation
- **Power** = energy per unit time
- Ideal basic circuit element
- Passive sign convention