With TF 1.0!



Lab 9 NN for XOR

Sung Kim < hunkim+ml@gmail.com>

Code: https://github.com/hunkim/DeepLearningZeroToAll/



Call for comments

Please feel free to add comments directly on these slides

Other slides: https://goo.gl/jPtWNt



With TF 1.0!



Lab 9-1 NN for XOR

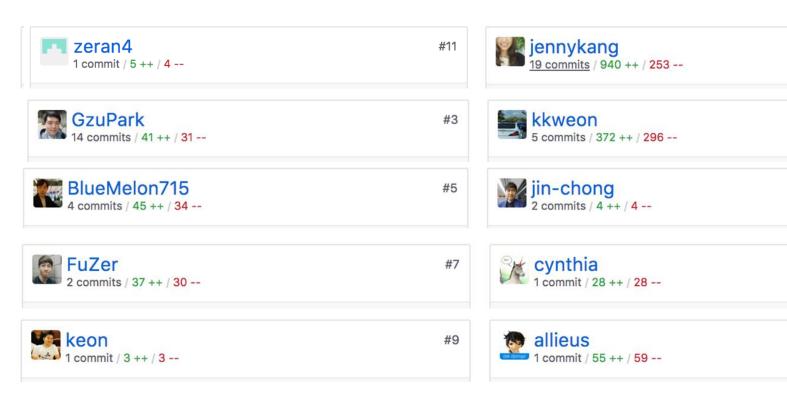
Sung Kim < hunkim+ml@gmail.com>

Code: https://github.com/hunkim/DeepLearningZeroToAll/



https://github.com/hunkim/DeepLearningZeroToAll/

#10



XOR data set

Boolean Expression	Logic Diagram Symbol	Truth Table		
	A ,	Α	В	Х
$X = A \oplus B$		0	0	0
	В	0	1	1
		1	0	1
		1	1	0

```
Y = tf.placeholder(tf.float32)
W = tf.Variable(tf.random normal([2, 1]), name='weight')
                                                                                 logistic regression?
b = tf.Variable(tf.random normal([1]), name='bias')
# Hypothesis using sigmoid: tf.div(1., 1. + tf.exp(tf.matmul(X, W)))
hypothesis = tf.sigmoid(tf.matmul(X, W) + b)
# cost/loss function
cost = -tf.reduce mean(Y * tf.log(hypothesis) + (1 - Y) * tf.log(1 - hypothesis))
train = tf.train.GradientDescentOptimizer(learning rate=0.1).minimize(cost)
# Accuracy computation
# True if hypothesis>0.5 else False
predicted = tf.cast(hypothesis > 0.5, dtype=tf.float32)
accuracy = tf.reduce mean(tf.cast(tf.equal(predicted, Y), dtype=tf.float32))
# Launch graph
with tf.Session() as sess:
   # Initialize TensorFlow variables
   sess.run(tf.global_variables_initializer())
   for step in range(10001):
       sess.run(train, feed dict={X: x data, Y: y data})
       if step % 100 == 0:
           print(step, sess.run(cost, feed dict={X: x data, Y: y data}), sess.run(W))
   # Accuracy report
   h, c, a = sess.run([hypothesis, predicted, accuracy], feed dict={X: x data, Y: y data})
   print("\nHypothesis: ", h, "\nCorrect: ", c, "\nAccuracy: ", a)
                                                                        https://github.com/hunkim/DeepLearningZeroToAll/blob/master/lab-09-1-xor.py
```

XOR with

 $x_{data} = np.array([[0, 0], [0, 1], [1, 0], [1, 1]], dtype=np.float32)$

y_data = np.array([[0], [1], [1], [0]], dtype=np.float32)

X = tf.placeholder(tf.float32)

```
W = tf.Variable(tf.random_normal([2, 1]), name='weight')
                                                                               logistic regression?
b = tf.Variable(tf.random normal([1]), name='bias')
# Hypothesis using sigmoid: tf.div(1., 1. + tf.exp(tf.matmul(X, W)))
hypothesis = tf.sigmoid(tf.matmul(X, W) + b)
                                                                                                  But
# cost/loss function
cost = -tf.reduce mean(Y * tf.log(hypothesis) + (1 - Y) * tf.log(1 - hypothesis))
                                                                                   it doesn't work!
train = tf.train.GradientDescentOptimizer(learning rate=0.1).minimize(cost)
# Accuracy computation
# True if hypothesis>0.5 else False
                                                                                                 Hypothesis:
predicted = tf.cast(hypothesis > 0.5, dtype=tf.float32)
                                                                                                 [[0.5]]
accuracy = tf.reduce mean(tf.cast(tf.equal(predicted, Y), dtype=tf.float32))
                                                                                                 [ 0.5]
# Launch graph
                                                                                                [ 0.5]
with tf.Session() as sess:
  # Initialize TensorFlow variables
                                                                                                [ 0.5]]
   sess.run(tf.global variables initializer())
                                                                                                 Correct:
                                                                                                [[ 0.]
  for step in range(10001):
      sess.run(train, feed dict={X: x data, Y: y data})
                                                                                                [ 0.]
      if step % 100 == 0:
                                                                                                [ 0.]
          print(step, sess.run(cost, feed dict={X: x data, Y: y data}), sess.run(W))
                                                                                                [ 0.]]
  # Accuracy report
                                                                                                 Accuracy: 0.5
   h, c, a = sess.run([hypothesis, predicted, accuracy], feed dict={X: x data, Y: y data})
   print("\nHypothesis: ", h, "\nCorrect: ", c, "\nAccuracy: ", a)
                                                                      https://github.com/hunkim/DeepLearningZeroToAll/blob/master/lab-09-1-xor.py
```

XOR with

 $x_{data} = np.array([[0, 0], [0, 1], [1, 0], [1, 1]], dtype=np.float32)$

y_data = np.array([[0], [1], [1], [0]], dtype=np.float32)

X = tf.placeholder(tf.float32)
Y = tf.placeholder(tf.float32)

Neural Net

```
W = tf.Variable(tf.random_normal([2, 1]), name='weight')
b = tf.Variable(tf.random_normal([1]), name='bias')

# Hypothesis using sigmoid: tf.div(1., 1. + tf.exp(tf.matmul(X, W)))
hypothesis = tf.sigmoid(tf.matmul(X, W) + b)
```

W=[5,-7], B=[-8, 3]

Neural Net

```
W1 = tf.Variable(tf.random_normal([2, 2]), name='weight1')
b1 = tf.Variable(tf.random_normal([2]), name='bias1')
layer1 = tf.sigmoid(tf.matmul(X, W1) + b1)

W2 = tf.Variable(tf.random_normal([2, 1]), name='weight2')
b2 = tf.Variable(tf.random_normal([1]), name='bias2')
hypothesis = tf.sigmoid(tf.matmul(layer1, W2) + b2)
```

W=[5,-7], B=[-8, 3]

```
W2 = tf.Variable(tf.random_normal([2, 1]), name='weight2')
b2 = tf.Variable(tf.random_normal([1]), name='bias2')
hypothesis = tf.sigmoid(tf.matmul(layer1, W2) + b2)
# cost/loss function
                                                                                                 Hypothesis:
cost = -tf.reduce mean(Y * tf.log(hypothesis) + (1 - Y) * tf.log(1 - hypothesis))
                                                                                                 [[ 0.01338218]
train = tf.train.GradientDescentOptimizer(learning rate=0.1).minimize(cost)
# Accuracy computation
                                                                                                 [ 0.98166394]
# True if hypothesis>0.5 else False
                                                                                                 [ 0.98809403]
predicted = tf.cast(hypothesis > 0.5, dtype=tf.float32)
accuracy = tf.reduce mean(tf.cast(tf.equal(predicted, Y), dtype=tf.float32))
                                                                                                 [ 0.01135799]]
# Launch graph
                                                                                                 Correct:
with tf.Session() as sess:
                                                                                                 [0.1]
   # Initialize TensorFlow variables
   sess.run(tf.global variables initializer())
                                                                                                 [1.]
   for step in range(10001):
                                                                                                 [1.]
       sess.run(train, feed_dict={X: x_data, Y: y_data})
       if step % 100 == 0:
                                                                                                 [ 0.]]
           print(step, sess.run(cost, feed_dict={X: x_data, Y: y_data}), sess.run([W1, W2]))
                                                                                                 Accuracy: 1.0
   # Accuracy report
   h, c, a = sess.run([hypothesis, predicted, accuracy],
                      feed_dict={X: x_data, Y: y_data})
   print("\nHypothesis: ", h, "\nCorrect: ", c, "\nAccuracy: ", a)
                                                                       https://github.com/hunkim/DeepLearningZeroToAll/blob/master/lab-09-2-xor-nn.py
```

NN for XOR

 $x_{data} = np.array([[0, 0], [0, 1], [1, 0], [1, 1]], dtype=np.float32)$

y data = np.array([[0], [1], [1], [0]], dtype=np.float32)

W1 = tf.Variable(tf.random_normal([2, 2]), name='weight1')

b1 = tf.Variable(tf.random_normal([2]), name='bias1')

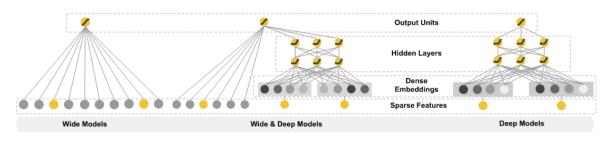
layer1 = tf.sigmoid(tf.matmul(X, W1) + b1)

X = tf.placeholder(tf.float32)
Y = tf.placeholder(tf.float32)

Wide NN for XOR

```
W1 = tf.Variable(tf.random_normal([2, 10]), name='weight1')
b1 = tf.Variable(tf.random_normal([10]), name='bias1')
layer1 = tf.sigmoid(tf.matmul(X, W1) + b1)

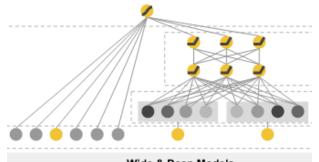
W2 = tf.Variable(tf.random_normal([10, 1]), name='weight2')
b2 = tf.Variable(tf.random_normal([1]), name='bias2')
hypothesis = tf.sigmoid(tf.matmul(layer1, W2) + b2)
```



```
[2,10], [10,1]
                    [2,2], [2,1]
Hypothesis:
                    Hypothesis:
[[ 0.00358802]
                    [[ 0.01338218]
[ 0.99366933]
                    [ 0.98166394]
[ 0.99204296]
                    [ 0.98809403]
[ 0.0095663 ]]
                    [ 0.01135799]]
Correct:
                    Correct:
[0]
                    [0]
[ 1.]
                    [ 1.]
[ 1.]
                    [ 1.]
[[.0]
                    [0.1]
Accuracy: 1.0
                    Accuracy: 1.0
```

Deep NN for XOR

```
W1 = tf.Variable(tf.random normal([2, 10]), name='weight1')
b1 = tf.Variable(tf.random normal([10]), name='bias1')
layer1 = tf.sigmoid(tf.matmul(X, W1) + b1)
W2 = tf.Variable(tf.random normal([10, 10]), name='weight2')
b2 = tf.Variable(tf.random normal([10]), name='bias2')
layer2 = tf.sigmoid(tf.matmul(layer1, W2) + b2)
W3 = tf.Variable(tf.random normal([10, 10]), name='weight3')
b3 = tf.Variable(tf.random normal([10]), name='bias3')
layer3 = tf.sigmoid(tf.matmul(layer2, W3) + b3)
W4 = tf.Variable(tf.random normal([10, 1]), name='weight4')
b4 = tf.Variable(tf.random normal([1]), name='bias4')
hypothesis = tf.sigmoid(tf.matmul(layer3, W4) + b4)
```



Wide & Deep Models

```
4 layers
Hypothesis:
[[ 7.80e-04]
 [ 9.99e-01]
[ 9.98e-01]
[ 1.55e-03]]
Correct:
[0]
[ 1.]
[1.]
[[.0]
Accuracy: 1.0
```

```
2 layers
Hypothesis:
[[ 0.01338218]
[ 0.98166394]
[ 0.98809403]
[ 0.01135799]]
Correct:
[0.1]
[ 1.]
[ 1.]
[0.1]
Accuracy: 1.0
```

Exercise

Wide and Deep NN for MNIST

With TF 1.0!



Lab 9-2

Tensorboard for XOR NN

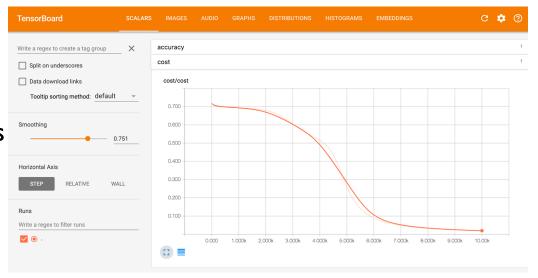
Sung Kim < hunkim+ml@gmail.com>

Code: https://github.com/hunkim/DeepLearningZeroToAll/



TensorBoard: TF logging/debugging tool

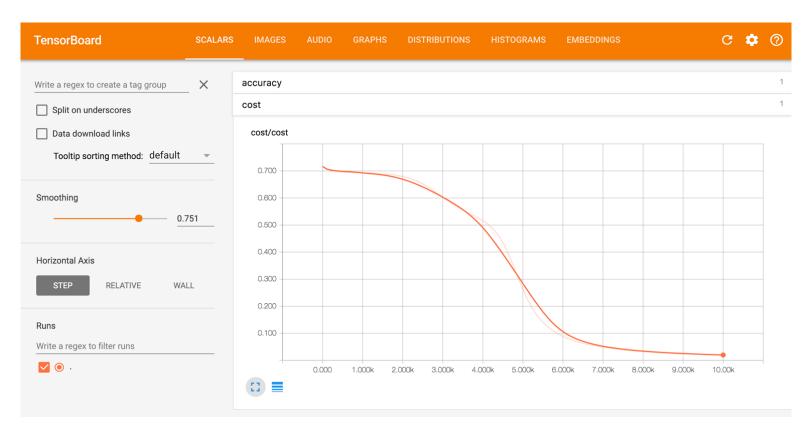
- Visualize your TF graph
- Plot quantitative metrics
- Show additional data



Old fashion: print, print, print

```
9400 0.0151413 [array([[ 6.21692038, 6.05913448],
    [-6.33773184, -5.75189114]], dtype=float32), array([[ 9.93581772],
    [-9.43034935]], dtvpe=float32)]
9500 0.014909 [array([ 6.22498751, 6.07049847],
    [-6.34637976, -5.76352596]], dtype=float32), array([[ 9.96414757],
    [-9.45942593]], dtype=float32)]
9600 0.0146836 [array([ 6.23292685, 6.08166742],
    [-6.35489035, -5.77496052]], dtype=float32), array([[ 9.99207973],
    [-9.48807526]], dtype=float32)]
9700 0.0144647 [array([ 6.24074268, 6.09264851],
    [-6.36326933, -5.78619957]], dtype=float32), array([[ 10.01962471],
    [-9.51631165]], dtype=float32)]
9800 0.0142521 [array([[ 6.24843407, 6.10344648],
    [-6.37151814, -5.79724932]], dtype=float32), array([[ 10.04679298],
    [-9.54414845]], dtype=float32)]
9900 0.0140456 [array([[ 6.25601053, 6.11406422],
    [-6.3796401, -5.80811596]], dtype=float32), array([[ 10.07359505],
    [-9.57159519]], dtvpe=float32)]
10000 0.0138448 [array([ 6.26347113, 6.12451124],
    [-6.38764334, -5.81880617]], dtype=float32), array([[ 10.10004139],
    [-9.59866238]], dtype=float32)]
```

New way!



```
from TF graph, decide which tensors you want to log
    w2_hist = tf.summary.histogram("weights2", W2)
    cost_summ = tf.summary.scalar("cost", cost)
```

Merge all summaries
summary = tf.summary.merge_all()

5 steps of using TensorBoard

Create writer and add graph

```
# Create summary writer
writer = tf.summary.FileWriter('./logs')
writer.add graph(sess.graph)
```

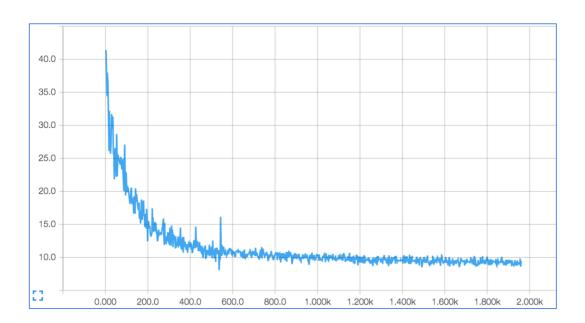
4 Run summary merge and add_summary

```
s, _ = sess.run([summary, optimizer], feed_dict=feed_dict)
writer.add_summary(s, global_step=global_step)
```

Launch TensorBoard tensorboard --logdir=./logs

Scalar tensors

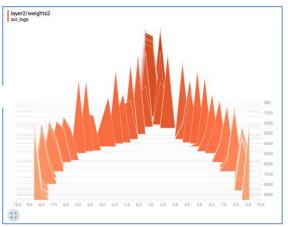
cost_summ = tf.summary.scalar("cost", cost)



Histogram (multi-dimensional tensors)

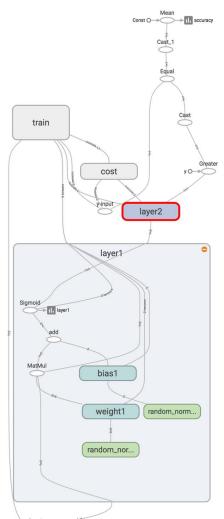
```
W2 = tf.Variable(tf.random_normal([2, 1]), name='weight2')
b2 = tf.Variable(tf.random_normal([1]), name='bias2')
hypothesis = tf.sigmoid(tf.matmul(layer1, W2) + b2)

w2_hist = tf.summary.histogram("weights2", W2)
b2_hist = tf.summary.histogram("biases2", b2)
hypothesis hist = tf.summary.histogram("hypothesis", hypothesis)
```



Add scope for better graph hierarchy

```
with tf.name scope("layer1") as scope:
  W1 = tf.Variable(tf.random normal([2, 2]), name='weight1')
   b1 = tf.Variable(tf.random normal([2]), name='bias1')
   layer1 = tf.sigmoid(tf.matmul(X, W1) + b1)
  w1_hist = tf.summary.histogram("weights1", W1)
   b1_hist = tf.summary.histogram("biases1", b1)
   layer1 hist = tf.summary.histogram("layer1", layer1)
with tf.name_scope("layer2") as scope:
  W2 = tf.Variable(tf.random normal([2, 1]), name='weight2')
   b2 = tf.Variable(tf.random normal([1]), name='bias2')
   hypothesis = tf.sigmoid(tf.matmul(layer1, W2) + b2)
  w2 hist = tf.summary.histogram("weights2", W2)
   b2_hist = tf.summary.histogram("biases2", b2)
   hypothesis hist = tf.summary.histogram("hypothesis", hypothesis
```



Merge summaries and create writerafter creating session

```
# Summary
summary = tf.summary.merge all()
# initialize
sess = tf.Session()
sess.run(tf.global_variables_initializer())
# Create summary writer
writer = tf.summary.FileWriter(TB SUMMARY DIR)
writer.add graph(sess.graph) # Add graph in the tensorboard
```

4 Run merged summary and write (add summary)

```
s, _ = sess.run([summary, optimizer], feed_dict=feed_dict)
writer.add_summary(s, global_step=global_step)
global_step += 1
```

5 Launch tensorboard (local)

```
writer = tf.summary.FileWriter("./logs/xor_logs")
```

```
$ tensorboard -logdir=./logs/xor_logs
```

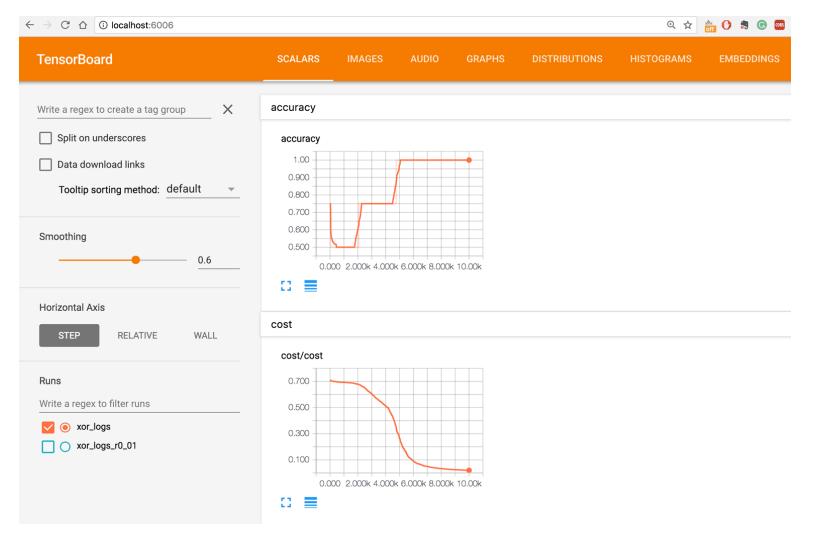
Starting TensorBoard b'41' on port 6006 (You can navigate to http://127.0.0.1:6006)

5 Launch tensorboard (remote server)

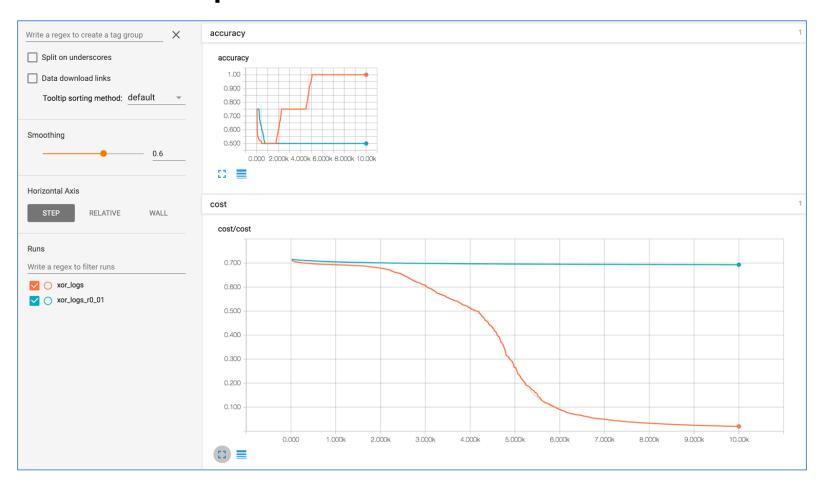
```
ssh -L local_port:127.0.0.1:remote_port username@server.com
```

```
local> $ ssh -L 7007:121.0.0.0:6006 hunkim@server.com
server> $ tensorboard —logdir=./logs/xor_logs
```

(You can navigate to http://127.0.0.1:7007)



learning_rate=0.1 VS learning_rate=0.01

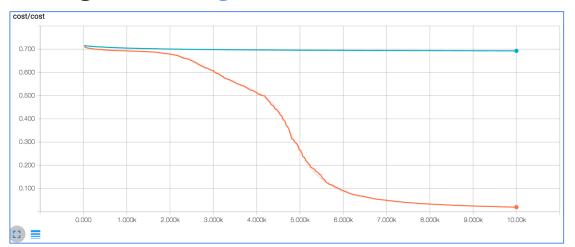


Multiple runs

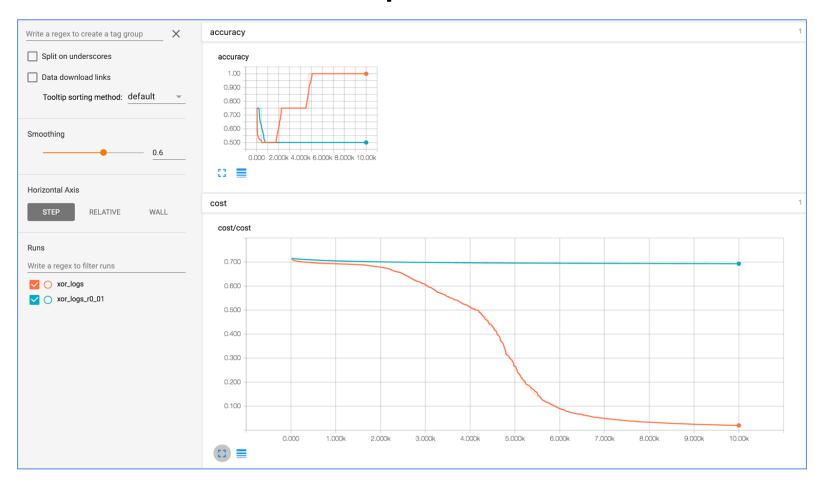
```
tensorboard -logdir=./logs/xor_logs
    train = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)
    ...
    writer = tf.summary.FileWriter("./logs/xor_logs")

tensorboard -logdir=./logs/xor_logs_r0_01
    train = tf.train.GradientDescentOptimizer(learning_rate=0.01).minimize(cost)
    ...
    writer = tf.summary.FileWriter(""./logs/xor_logs_r0_01"")
```

tensorboard —logdir=./logs



Multiple runs



```
from TF graph, decide which tensors you want to log
    w2_hist = tf.summary.histogram("weights2", W2)
    cost_summ = tf.summary.scalar("cost", cost)
```

Merge all summaries
summary = tf.summary.merge_all()

5 steps of using TensorBoard

Create writer and add graph

```
# Create summary writer
writer = tf.summary.FileWriter('./logs')
writer.add graph(sess.graph)
```

4 Run summary merge and add_summary

```
s, _ = sess.run([summary, optimizer], feed_dict=feed_dict)
writer.add_summary(s, global_step=global_step)
```

Launch TensorBoard tensorboard --logdir=./logs

Exercise

- Wide and Deep NN for MNIST
- Add tensorboard

With TF 1.0!



Lab 9-2-E Tensorboard for MNIST

Sung Kim < hunkim+ml@gmail.com>

Code: https://github.com/hunkim/DeepLearningZeroToAll/



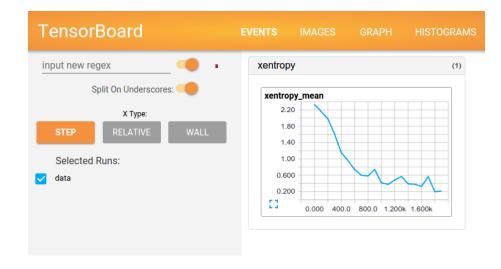
Visualizing your Deep learning using

TensorBoard (TensorFlow)

Sung Kim <hunkim+ml@gmail.com>

TensorBoard: TF logging/debugging tool

- Visualize your TF graph
- Plot quantitative metrics
- Show additional data



Old fashion: print, print, print

```
2000 [0.69364417, array([[ 0.50981331, 0.50592244],
       [ 0.37054271, 0.37088916],
       [ 0.6810087 , 0.38607275],
       [ 0.54717511, 0.26581794]], dtype=float32), array([[ 0.50861073],
       [ 0.51602864].
       [ 0.4826754 ].
       [ 0.49036184]], dtype=float32), array([[ 0.71915275, -0.48754135],
       [-0.56914777, -0.55209494]], dtype=float32), array([[-0.44138899],
       [ 0.23536676]], dtype=float32), array([ 0.03925836,  0.02369077], dtype=float32), array([ 0.14039496], dtype=float32)]
4000 [0.69332385, array([[ 0.52235132, 0.50927138],
       [ 0.38598102. 0.37814924].
       [ 0.69650716, 0.39592981],
       [ 0.56881481, 0.27748841]], dtvpe=float32), array([[ 0.50748861],
       [ 0.51554251].
       [ 0.48338425],
       [ 0.49113813]], dtype=float32), array([[ 0.74125487, -0.45954311],
       [-0.55370271, -0.53450096]], dtype=float32), array([[-0.42565805],
       [ 0.19686614]], dtype=float32), array([ 0.08946501,  0.03708982], dtype=float32), array([ 0.15204136], dtype=float32)]
6000 [0.69306737, array([[ 0.53439337, 0.51197231],
       [ 0.39961013, 0.38383543],
       [ 0.71191686, 0.40380618],
       [ 0.58899951, 0.2868301 ]], dtype=float32), array([[ 0.50660294].
       [ 0.51538038],
```

New way!



```
1 From TF graph, decide which tensors you want to log
    with tf.variable_scope('layer1') as scope:
        tf.summary.image('input', x_image, 3)
        tf.summary.histogram("layer", L1)
        tf.summary.scalar("loss", cost)
```

Merge all summaries
 summary = tf.summary.merge_all()

5 steps of using TensorBoard

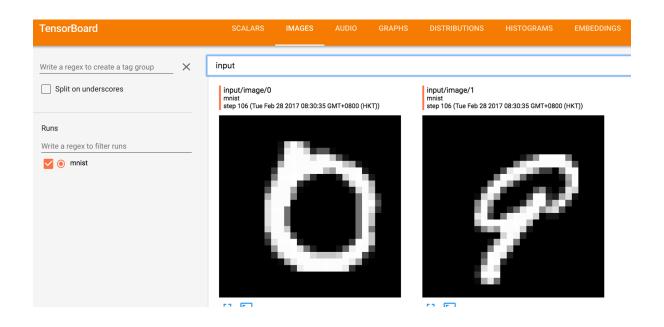
3 Create writer and add graph
 # Create summary writer
 writer = tf.summary.FileWriter(TB_SUMMARY_DIR)
 writer.add graph(sess.graph)

4 Run summary merge and add_summary
s, _ = sess.run([summary, optimizer], feed_dict=feed_dict)
writer.add_summary(s, global_step=global_step)

5 Launch TensorBoard tensorboard --logdir=/tmp/mnist logs

Image Input

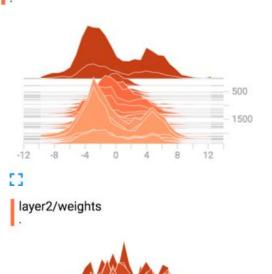
```
# Image input
x_image = tf.reshape(X, [-1, 28, 28, 1])
tf.summary.image('input', x_image, 3)
```



Histogram (multi-dimensional tensors)

```
with tf.variable_scope('layer1') as scope:
    W1 = tf.get_variable("W", shape=[784, 512])
    b1 = tf.Variable(tf.random_normal([512]))
    L1 = tf.nn.relu(tf.matmul(X, W1) + b1)
    L1 = tf.nn.dropout(L1, keep_prob=keep_prob)

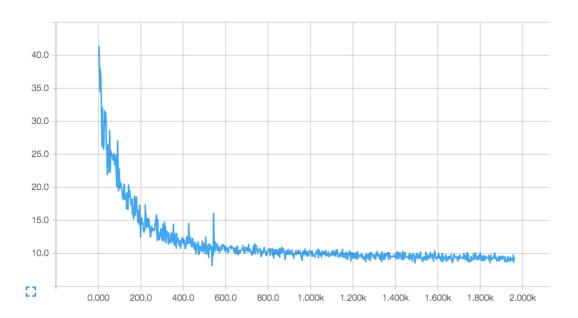
    tf.summary.histogram("X", X)
    tf.summary.histogram("weights", W1)
    tf.summary.histogram("bias", b1)
    tf.summary.histogram("layer", L1)
```



layer2/layer

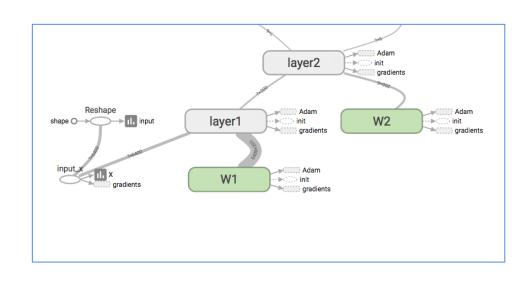
Scalar tensors

tf.summary.scalar("loss", cost)



Add scope for better hierarchy

```
with tf.variable scope('layer1') as scope:
  W1 = tf.get_variable("W", shape=[784, 512],...
  b1 = tf.Variable(tf.random_normal([512]))
  L1 = tf.nn.relu(tf.matmul(X, W1) + b1)
  L1 = tf.nn.dropout(L1, keep prob=keep prob)
  tf.summary.histogram("X", X)
  tf.summary.histogram("weights", W1)
  tf.summary.histogram("bias", b1)
  tf.summary.histogram("layer", L1)
with tf.variable scope('layer2') as scope:
with tf.variable scope('layer3') as scope:
   . . .
with tf.variable scope('layer4') as scope:
   . . .
with tf.variable scope('layer5') as scope:
```



Merge summaries and create writerafter creating session

```
# Summary
summary = tf.summary.merge all()
# initialize
sess = tf.Session()
sess.run(tf.global variables initializer())
# Create summary writer
writer = tf.summary.FileWriter(TB SUMMARY DIR)
writer.add graph(sess.graph)
```

Run merged summary and write (add summary)

```
s, _ = sess.run([summary, optimizer], feed_dict=feed_dict)
writer.add_summary(s, global_step=global_step)
global_step += 1
```

Launch tensorboard (local)

```
writer = tf.summary.FileWriter("/tmp/mnist_logs")
```

```
$ tensorboard -logdir=/tmp/mnist_logs
```

Starting TensorBoard b'41' on port 6006 (You can navigate to http://127.0.0.1:6006)

Launch tensorboard (remote server)

```
ssh -L local_port:127.0.0.1:remote_port username@server.com
```

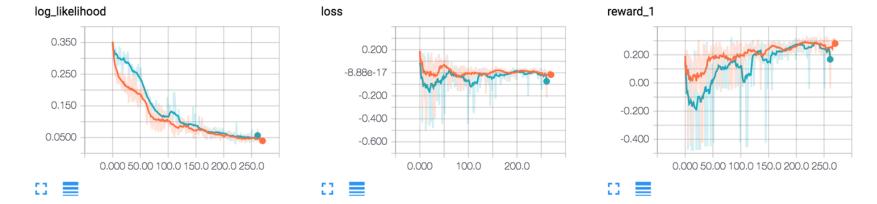
```
local> $ ssh -L 7007:127.0.0.1:6006 hunkim@server.com
server> $ tensorboard —logdir=/tmp/mnist_logs
```

(You can navigate to http://127.0.0.1:7007)

Multiple runs

```
tensorboard -logdir=/tmp/mnist_logs/run1
  writer = tf.summary.FileWriter("/tmp/mnist_logs/run1")
tensorboard -logdir=/tmp/mnist_logs/run2
  writer = tf.summary.FileWriter("/tmp/mnist_logs/run1")
```

tensorboard —logdir=/tmp/mnist_logs



```
1 From TF graph, decide which tensors you want to log
    with tf.variable_scope('layer1') as scope:
        tf.summary.image('input', x_image, 3)
        tf.summary.histogram("layer", L1)
        tf.summary.scalar("loss", cost)
```

Merge all summaries
 summary = tf.summary.merge_all()

5 steps of using TensorBoard

3 Create writer and add graph
 # Create summary writer
 writer = tf.summary.FileWriter(TB_SUMMARY_DIR)
 writer.add graph(sess.graph)

4 Run summary merge and add_summary
s, _ = sess.run([summary, optimizer], feed_dict=feed_dict)
writer.add_summary(s, global_step=global_step)

5 Launch TensorBoard tensorboard --logdir=/tmp/mnist logs

With TF 1.0!



Lab 9-3 (optional)

NN Backpropagation

Sung Kim < hunkim+ml@gmail.com>

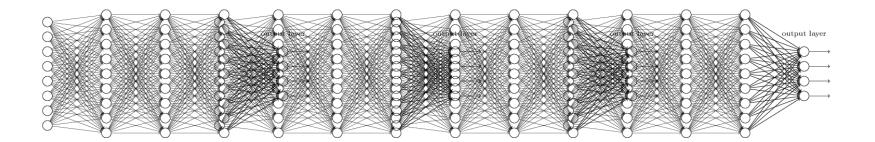
Code: https://github.com/hunkim/DeepLearningZeroToAll/



https://github.com/hunkim/DeepLearningZeroToAll/



How to train?



Gradient descent algorithm

$$W := W - \alpha \frac{1}{m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})x^{(i)}$$

$$w = w - \alpha \frac{\partial E}{\partial w}$$



$$w = w - \alpha \frac{\partial E}{\partial w}$$



train = tf.train.GradientDescentOptimizer(learning rate=0.1).minimize(cost)

"Yes you should understand backprop"

- "If you try to ignore how it works under the hood because *TensorFlow automagically makes my networks learn*"
- "You will not be ready to wrestle with the dangers it presents"
- "You will be much less effective at building and debugging neural networks."
- "The good news is that backpropagation is not that difficult to understand"
 - -"if presented properly."

Back propagation (chain rule)

$$f = \omega x + b, g = \omega x, f = g + b$$

$$\int_{\frac{\partial g}{\partial \omega}} = 1$$

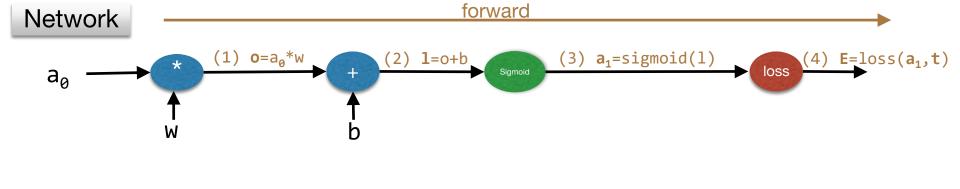
 $\frac{\partial n}{\partial t} = \frac{\partial l}{\partial t} = \frac{\partial N}{\partial t} = 1 + x = 2$

http://cs231n.stanford.edu/

Back propagation (chain rule)

Logistic Regression Network

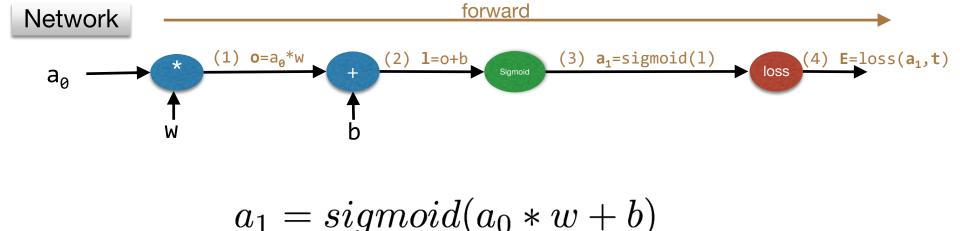




$$a_1 = sigmoid(a_0 * w + b)$$

$$E = loss(a_1, t) = -\sum_{i=1}^{n} t * log(a_1) + (1 - t) * log(1 - a_1)$$

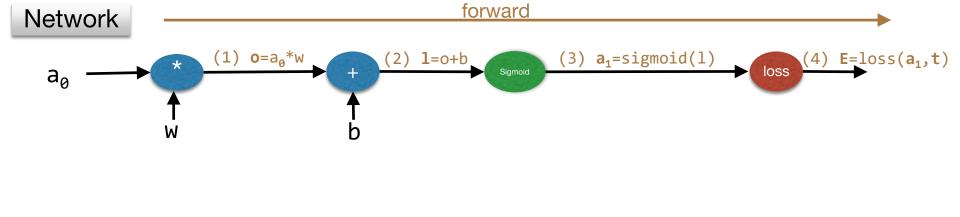
Forward pass, OK? Just follow (1), (2), (3) and (4)



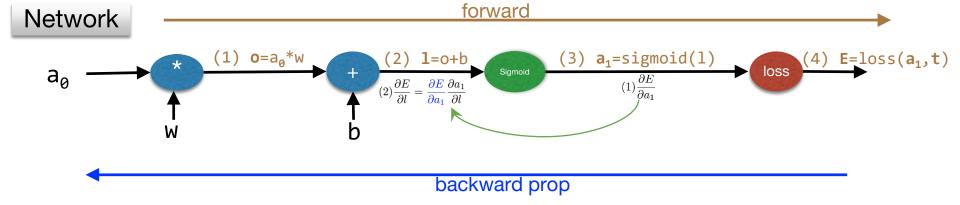
$$\sum_{i=1}^{n} I_{i+1}(x_i) + (1-x_i) + (1-x_i)$$

$$E = loss(a_1, t) = -\sum_{i=1}^{n} t * log(a_1) + (1 - t) * log(1 - a_1)$$

$$a_0 = 0.1, t = 0, w = 0.1, b = 0.3$$



$$w = w - \alpha \frac{\partial E}{\partial w}$$

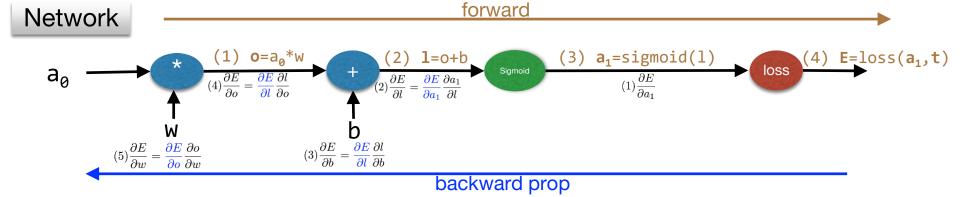


$$w = w - \alpha \frac{\partial E}{\partial w}$$

Let's do back propagation!

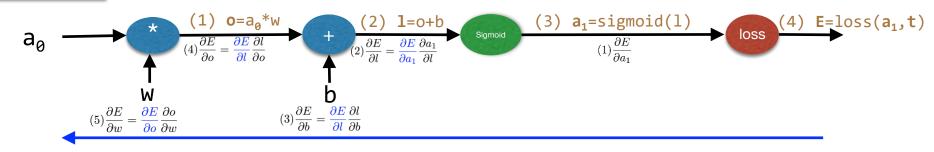
will be given. What would be

We can use the chain rule.



In the same manner, we can get back prop (4), (3), (1) and (1)!

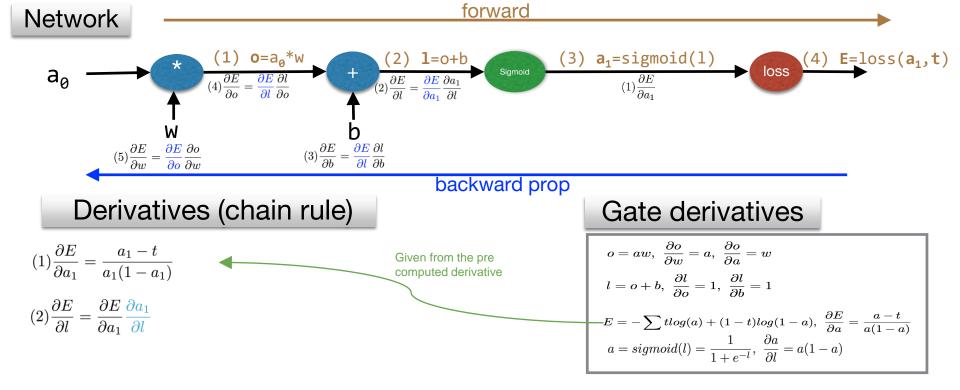




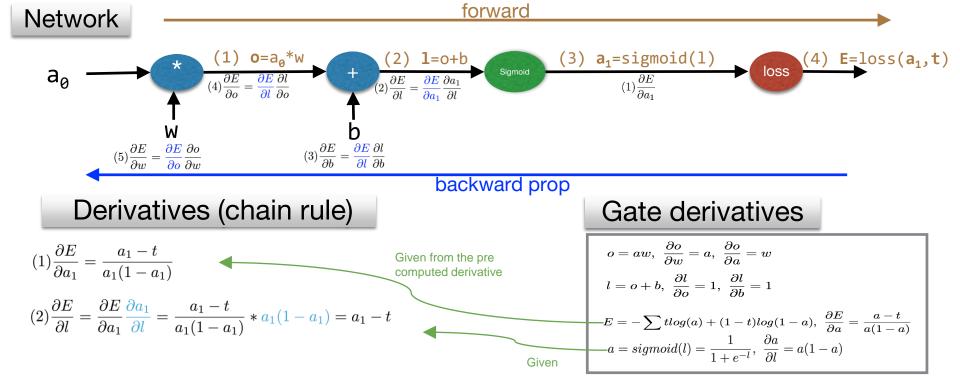
Gate derivatives

$$\begin{split} o &= aw, \ \frac{\partial o}{\partial w} = a, \ \frac{\partial o}{\partial a} = w \\ l &= o + b, \ \frac{\partial l}{\partial o} = 1, \ \frac{\partial l}{\partial b} = 1 \\ E &= -\sum tlog(a) + (1 - t)log(1 - a), \ \frac{\partial E}{\partial a} = \frac{a - t}{a(1 - a)} \\ a &= sigmoid(l) = \frac{1}{1 + e^{-l}}, \ \frac{\partial a}{\partial l} = a(1 - a) \end{split}$$

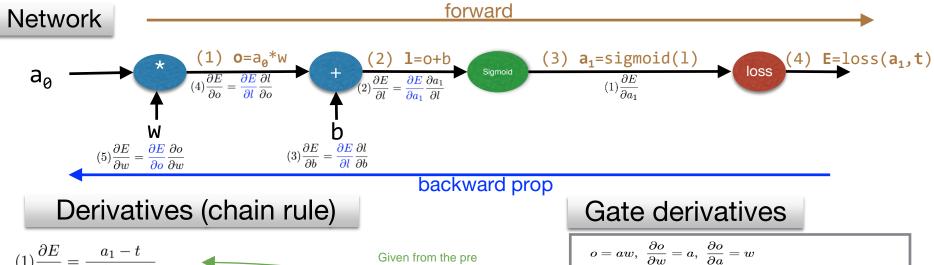
These derivatives for each gate will be given. We can just use them in the chain rule.



Just apply them one by one and solve each derivative one by one!



Just apply them one by one and solve each derivative one by one!



$$(1)\frac{\partial E}{\partial a_1} = \frac{a_1 - t}{a_1(1 - a_1)}$$

$$(2)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(2)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(2)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(3)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(4)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(5)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(6)\frac{\partial E}{\partial a_1} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = a_1 - t$$

$$(7)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(8)\frac{\partial E}{\partial a_1} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(9)\frac{\partial E}{\partial a_1} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(9)\frac{\partial E}{\partial a_1} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(9)\frac{\partial E}{\partial a_1} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(9)\frac{\partial E}{\partial a_1} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(9)\frac{\partial E}{\partial a_1} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = a_1 - t$$

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$$(9)\frac{\partial E}{\partial a_1} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = a_1 - t$$

$$(9)\frac{\partial E}{\partial a_1} = a_1 - t$$

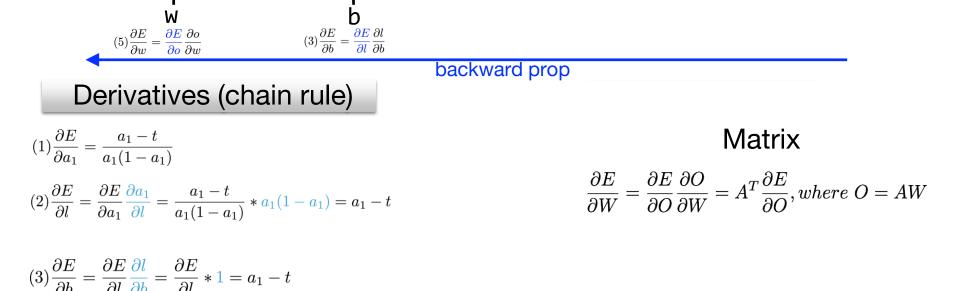
Given

$$(3)\frac{\partial E}{\partial h} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial h} = \frac{\partial E}{\partial l}*1 = a_1 - t$$

$$(4)\frac{\partial E}{\partial o} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial o} = \frac{\partial E}{\partial l} * 1 = a_1 - t$$

$$(5)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w} = \frac{\partial E}{\partial o}a_0 = (a_1 - t)a_0$$

Just apply them one by one and solve each derivative one by one!



(3) a_1 =sigmoid(1)

Network

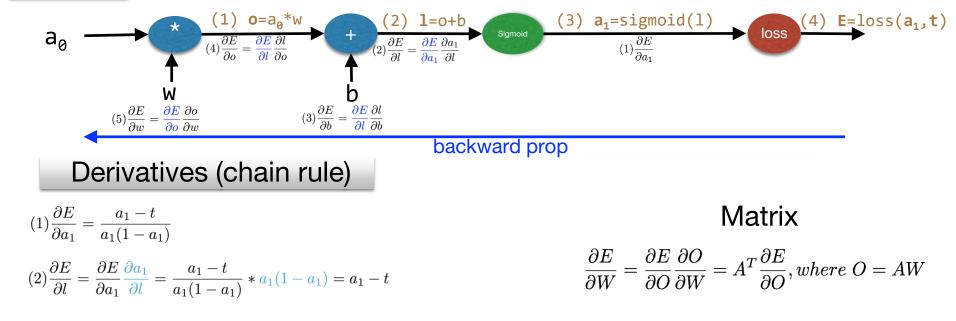
 $(4)\frac{\partial E}{\partial a} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial a} = \frac{\partial E}{\partial l} * 1 = a_1 - t$

 $(5)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w} = a_0^T \frac{\partial E}{\partial o} = a_0^T (a_1 - t)$

 a_{θ}

For Matrix: http://cs231n.github.io/optimization-2/#staged

(4) $E=loss(a_1,t)$



Network

$$(3)\frac{\partial E}{\partial b} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial b} = \frac{\partial E}{\partial l}*1 = a_1 - t$$

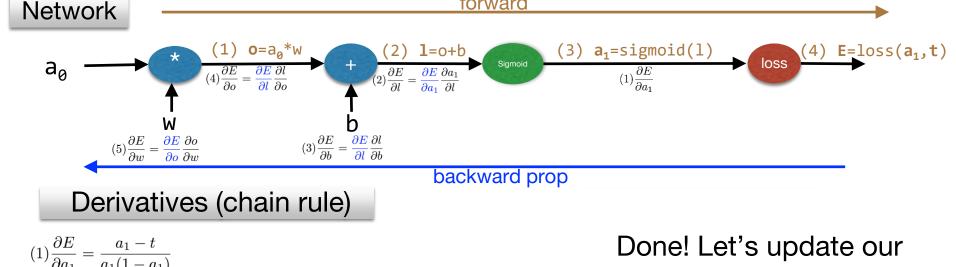
$$(4)\frac{\partial E}{\partial o} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial o} = \frac{\partial E}{\partial l}*1 = a_1 - t$$

$$(5)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w} = a_0^T\frac{\partial E}{\partial o} = a_0^T(a_1 - t)$$

$$(6)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w} = a_0^T\frac{\partial E}{\partial o} = a_0^T(a_1 - t)$$

$$(7)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w} = a_0^T\frac{\partial E}{\partial o} = a_0^T(a_1 - t)$$

$$(8)\frac{\partial E}{\partial v} = \frac{\partial E}{\partial v}\frac{\partial o}{\partial w} = a_0^T\frac{\partial E}{\partial o} = a_0^T(a_1 - t)$$



$$\partial a_1 = a_1(1-a_1)$$

$$\partial E = \partial E \partial a_1 = a_1 - t \qquad (1 - a_1)$$

$$(2)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$$

$$(3)\frac{\partial E}{\partial b} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial b} = \frac{\partial E}{\partial l}*1 = a_1 - t$$

$$(4)\frac{\partial E}{\partial o} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial o} = \frac{\partial E}{\partial l} * 1 = a_1 - t$$

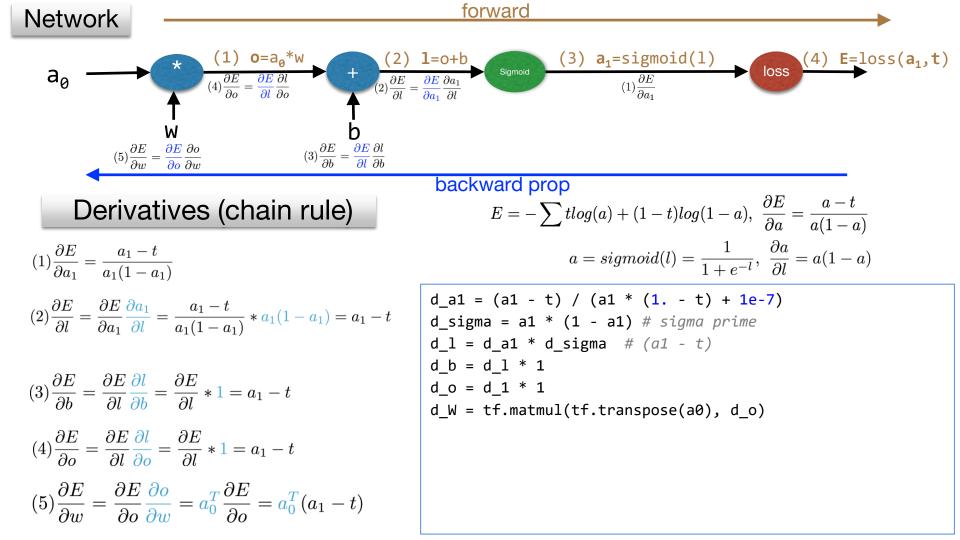
$$(4)\frac{\partial E}{\partial o} = \frac{\partial E}{\partial l}\frac{\partial o}{\partial o} = \frac{\partial E}{\partial l} * 1 = a_1 - t$$

$$(5)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w} = a_0^T\frac{\partial E}{\partial o} = a_0^T(a_1 - t)$$

network using derivatives!

$$w = w - \alpha \frac{\partial E}{\partial w}$$

$$b = b - \alpha \frac{\partial E}{\partial b}$$



Network $(4) E = loss(a_1, t)$ (3) a_1 =sigmoid(1) a_{θ} $(3)\frac{\partial E}{\partial b} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial b}$ $(5)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w}$ backward prop $E = -\sum t log(a) + (1-t)log(1-a), \ \frac{\partial E}{\partial a} = \frac{a-t}{a(1-a)}$ Derivatives (chain rule) $a = sigmoid(l) = \frac{1}{1 + e^{-l}}, \ \frac{\partial a}{\partial l} = a(1 - a)$ $(1)\frac{\partial E}{\partial a_1} = \frac{a_1 - t}{a_1(1 - a_1)}$ d a1 = (a1 - t) / (a1 * (1. - a1) + 1e-7) $(2)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$ d sigma = a1 * (1 - a1) # sigma prime d l = d a1 * d sigma # (a1 - t)d b = d 1 * 1 $(3)\frac{\partial E}{\partial h} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial h} = \frac{\partial E}{\partial l}*1 = a_1 - t$ d o = d 1 * 1d W = tf.matmul(tf.transpose(a0), d o) # Updating network using gradients $(4)\frac{\partial E}{\partial a} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial a} = \frac{\partial E}{\partial l}*1 = a_1 - t$ learning rate = 0.01 train step = [$(5)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w} = a_0^T \frac{\partial E}{\partial o} = a_0^T (a_1 - t)$

tf.assign(W, W - learning_rate * d_W), tf.assign(b, b - learning rate * d b)]

forward

 $(4) E = loss(a_1, t)$ (3) a_1 =sigmoid(1) a_{θ} $(5)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w}$ $(3)\frac{\partial E}{\partial b} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial b}$ backward prop $E = -\sum t log(a) + (1-t)log(1-a), \ \frac{\partial E}{\partial a} = \frac{a-t}{a(1-a)}$ Derivatives (chain rule) $a = sigmoid(l) = \frac{1}{1 + e^{-l}}, \ \frac{\partial a}{\partial l} = a(1 - a)$ $(1)\frac{\partial E}{\partial a_1} = \frac{a_1 - t}{a_1(1 - a_1)}$ d a1 = (a1 - t) / (a1 * (1. - a1) + 1e-7) $(2)\frac{\partial E}{\partial l} = \frac{\partial E}{\partial a_1}\frac{\partial a_1}{\partial l} = \frac{a_1 - t}{a_1(1 - a_1)} * a_1(1 - a_1) = a_1 - t$ d sigma = a1 * (1 - a1) # sigma prime d l = d a1 * d sigma # (a1 - t)d b = d 1 * 1 $(3)\frac{\partial E}{\partial h} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial h} = \frac{\partial E}{\partial l}*1 = a_1 - t$ d o = d 1 * 1d W = tf.matmul(tf.transpose(a0), d o) # Updating network using gradients $(4)\frac{\partial E}{\partial a} = \frac{\partial E}{\partial l}\frac{\partial l}{\partial a} = \frac{\partial E}{\partial l}*1 = a_1 - t$ learning rate = 0.01 train step = [$(5)\frac{\partial E}{\partial w} = \frac{\partial E}{\partial o}\frac{\partial o}{\partial w} = a_0^T \frac{\partial E}{\partial o} = a_0^T (a_1 - t)$ tf.assign(W, W - learning_rate * d_W / N), # sample size

tf.assign(b, b - learning rate * tf.reduce sum(d b))]

forward

Network

Exercise

- See more backprop code samples at https://github.com/hunkim/DeepLearningZeroToAll
- https://github.com/hunkim/DeepLearningZeroToAll/blob/mast er/lab-09-7-sigmoid_back_prop.py
- Solve XOR using NN backprop