# P1 Chapter 7: Algebraic Methods

**Polynominal Fractions** 

# 1 :: Simplifying Algebraic Fractions

Recall that you can simplify fractions by **dividing** the numerator and

denominator by a **common factor**.

**Hint**: To identify common factors we need to factorise first.

$$\frac{x^2-1}{x^2+x} =$$
?

$$\frac{x^2 + 3x + 2}{x + 1} =$$
?

**Note**: Do not leave 1 in the denominator!

**Tip**: Factorise the easier one first because it provides clues to the factorisation of the other.

$$\frac{2x^2 + 11x + 12}{x^2 + 9x + 20} =$$

$$\frac{4 - x^2}{x^2 + 2x - 8} =$$

$$\mathbf{Tip:} \frac{a-b}{b-a} = -1$$

# 1 :: Simplifying Algebraic Fractions

Recall that you can simplify fractions by **dividing** the numerator and denominator by a **common factor**.

**Hint**: To identify common factors we need to factorise first.

$$\frac{x^2 - 1}{x^2 + x} = \frac{(x+1)(x-1)}{x(x+1)} = \frac{x-1}{x}$$

$$\frac{x^2 + 3x + 2}{x + 1} = \frac{(x + 2)(x + 1)}{x + 1} = x + 2$$

**Note**: Do not leave 1 in the denominator!

**Tip**: Factorise the easier one first because it provides clues to the factorisation of the other.

$$\frac{2x^2 + 11x + 12}{x^2 + 9x + 20} = \frac{(2x+3)(x+4)}{(x+4)(x+5)} = \frac{2x+3}{x+5}$$

$$\frac{4-x^2}{x^2+2x-8} = \frac{(2-x)(2+x)}{(x+4)(x-2)} = -\frac{x+2}{x+4}$$

 $\mathsf{Tip}: \frac{a-b}{b-a} = -1$ 

# Exercise 7.1

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### Homework Exercise

#### 1 Simplify these fractions:

a 
$$\frac{4x^4 + 5x^2 - 7x}{x}$$

**b** 
$$\frac{7x^5 - 5x^5 + 9x^3 + x^2}{x}$$

$$e^{-x^4+4x^2+6}$$

**d** 
$$\frac{7x^5 - x^3 - 4}{x}$$

e 
$$\frac{8x^4 - 4x^3 + 6x}{2x}$$

$$\mathbf{f} \ \frac{9x^2 - 12x^3 - 3x}{3x}$$

$$\frac{7x^3 - x^4 - 2}{5x}$$

$$h \frac{-4x^2 + 6x^4 - 2x}{-2x}$$

$$i \frac{-x^8 + 9x^4 - 4x^3 + 6}{-2x}$$

$$\mathbf{j} = \frac{-9x^9 - 6x^6 + 4x^4 - 2}{-3x}$$

#### 2 Simplify these fractions as far as possible:

a 
$$\frac{(x+3)(x-2)}{(x-2)}$$

**b** 
$$\frac{(x+4)(3x-1)}{(3x-1)}$$

$$\frac{(x+3)^2}{(x+3)}$$

**d** 
$$\frac{x^2 + 10x + 21}{(x+3)}$$

e 
$$\frac{x^2 + 9x + 20}{(x+4)}$$

$$f \frac{x^2 + x - 12}{(x - 3)}$$

$$\mathbf{g} \ \frac{x^2 + x - 20}{x^2 + 2x - 15}$$

h 
$$\frac{x^2 + 3x + 2}{x^2 + 5x + 4}$$

$$i \frac{x^2 + x - 12}{x^2 - 9x + 18}$$

$$\mathbf{j} \ \frac{2x^2 + 7x + 6}{(x - 5)(x + 2)}$$

$$k \frac{2x^2 + 9x - 18}{(x+6)(x+1)}$$

$$1 \frac{3x^2-7x+2}{(3x-1)(x+2)}$$

$$\mathbf{m} \; \frac{2x^2 + 3x + 1}{x^2 - x - 2}$$

n 
$$\frac{x^2 + 6x + 8}{3x^2 + 7x + 2}$$

$$\mathbf{o} \ \frac{2x^2 - 5x - 3}{2x^2 - 9x + 9}$$

3 
$$\frac{6x^3 + 3x^2 - 84x}{6x^2 - 33x + 42} = \frac{ax(x+b)}{x+c}$$
, where a, b and c are constants.

### Homework Answers

1 **a** 
$$4x^3 + 5x - 7$$
 **b**  $2x^4 + 9x^2 + x$ 

$$c -x^3 + 4x + \frac{6}{r}$$

e 
$$4x^3 - 2x^2 + 3$$

$$\mathbf{g} \quad \frac{7x^2}{5} - \frac{x^3}{5} - \frac{2}{5x} \qquad \qquad \mathbf{h} \quad 2x - 3x^3 + 1$$

i 
$$\frac{x^7}{2} - \frac{9x^3}{2} + 2x^2 - \frac{3}{x^2}$$

2 a 
$$x + 3$$

d 
$$x + 7$$

$$x = 4$$

$$g \frac{x-4}{x-3}$$

j 
$$\frac{2x+3}{x-5}$$
 k  $\frac{2x-3}{x+1}$  l  $\frac{x-2}{x+2}$ 

$$\frac{2x+1}{x-2}$$

**b** 
$$2x^4 + 9x$$

**d** 
$$7x^4 - x^2 - \frac{4}{x}$$

$$f = 3x - 4x^2 - 1$$

h 
$$2x - 3x^3 + 1$$

i 
$$\frac{x^7}{2} - \frac{9x^3}{2} + 2x^2 - \frac{3}{x}$$
 j  $3x^8 + 2x^5 - \frac{4x^3}{3} + \frac{2}{3x}$ 

2 **a** 
$$x + 3$$
 **b**  $x + 4$  **c**  $x + 3$  **d**  $x + 7$  **e**  $x + 5$  **f**  $x + 4$ 

$$\mathbf{f} = x + 4$$

g 
$$\frac{x-4}{x-3}$$
 h  $\frac{x+2}{x+4}$  i  $\frac{x+4}{x-6}$ 

$$1 \frac{x-2}{x+2}$$

m 
$$\frac{2x+1}{x-2}$$
 n  $\frac{x+4}{3x+1}$  o  $\frac{2x+1}{2x-3}$ 

3 
$$a = 1, b = 4, c = -2$$