



Clustering Analysis US Stock Return Correlation

Group 3 - 2021 April 3













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Steps

- Downloaded 1000+ Nasdaq stock
 + 2000+ NYSE stock prices from Yahoo! Finance
- Calculated daily return for the stocks and calculated correlation among the returns (SP500 component stocks etc.)

- Transfer the correlation to distance -> $d = \sqrt{\frac{1}{2}(1-\rho)}$
- Clustering based on the distance (for SP500 companies, sectors, industries)

- Prepared symbol list file (tickers of small, mid, large, mega cap companies) (Nasdaq 1358, NYSE 2061)
- Use downloading script to get historical price data from Yahoo! Finance (time interval from 2011-03-16 to 2021-03-16)
- Use concurrency: futures. ThreadPoolExecutor with max 4 workers -> slightly faster

- Took around 30 minutes to download the data set
- Alternatively, you can use the shared data set here:

https://drive.google.com/file/d/1Uy0VmrkbKUAskGKAAQo4 5F8unrphAF14/view?usp=sharing

```
def download one(symbol):
                                                              def download many(symbols: list[str]) -> None:
    if os.path.exists(FILEDIR + '{}.csv'.format(symbol)):
                                                                  with futures. ThreadPoolExecutor (max workers=4) as
        # logging.info('already downloaded, skip')
                                                              executor:
        return
                                                                      res = executor.map(download one, symbols)
    logging.info('downloading for symbol:
                                                             def main():
{}'.format(symbol))
                                                                  logging.info('start downloading process...')
    try:
        abc = downloader.downloader(symbol,start,end)
        abc = abc.decode('utf-8')
                                                                  nasdaq symbols = read symbols('nasdaq symbols.csv')
                                                                  nyse symbols = read symbols('nyse symbols.csv')
                                                                  symbols = nasdaq symbols + nyse symbols
        with open(FILEDIR + '{}.csv'.format(symbol), "w")
as f:
            f.writelines(str(abc))
                                                                  download many(symbols)
        logging.info('downloaded successfully')
    except:
        logging.error('got error when trying to download:
                                                                 logging.info('finished downloading process!')
{}'.format(symbol))
```



Clustering Analysis - Data Downloading

Code: downloader.py (https://stackoverflow.com/questions/44030983/yahoo-finance-url-not-working)

```
import requests
import re
import json
import time as time
def run(symbol, initial, final):
    start = int(time.mktime(time.strptime(str(initial),
'%Y-%m-%d')))
    end = int(time.mktime(time.strptime(str(final), '%Y-
%m-%d')))
    abc = downloader(symbol, start, end)
    abc = abc.decode('utf-8')
    with open('{}.csv'.format(symbol), "w") as f:
        f.writelines(str(abc))
def downloader(symbol, start, end):
    ses = requests.session()
    resp = ses.get(
f'https://finance.yahoo.com/quote/{symbol}/history?period
1={start} &period2={end} &interval=1d&filter=history&freque
ncy=1d'
```

```
resp.raise_for_status()
  data = resp.content.decode('utf-8')
    crumb_m =
re.search(r'"CrumbStore":\{"crumb":("[^"]+")\}', data)
  assert crumb_m
    crumb = json.loads(crumb_m.group(1))
    csvresp = ses.get(

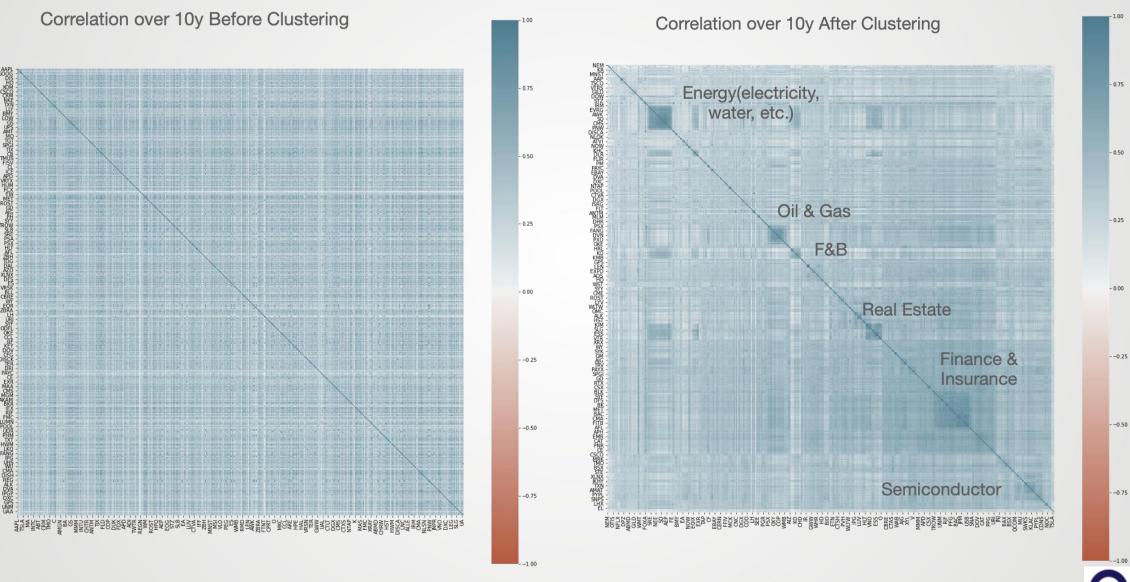
f'https://query1.finance.yahoo.com/v7/finance/download/{symbol}?period1={start}&period2={end}&interval=1d&events=history&crumb={crumb}'
  )
    csvresp.raise_for_status()
  return csvresp.content
```



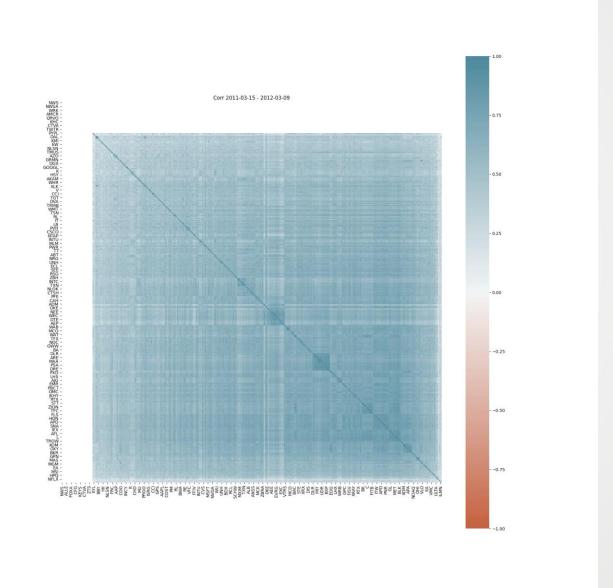
Code: auto download.py

```
import time
import logging
                                                                                          return syms
import downloader
import os
                                                                                      def download one(symbol):
                                                                                          if os.path.exists(FILEDIR + '{}.csv'.format(symbol)):
import argparse
from concurrent import futures
                                                                                              # logging.info('already downloaded, skip')
                                                                                             return
FILEDIR = os.path.join('downloaded data', 'data')
initial = '2011-3-16'
                                                                                          logging.info('downloading for symbol: {}'.format(symbol))
final = '2021-3-16'
                                                                                          try:
                                                                                             abc = downloader.downloader(symbol, start, end)
formatter = '%(asctime)s - %(name)s - %(levelname)s - %(message)s'
                                                                                             abc = abc.decode('utf-8')
logging.basicConfig(filename='auto download.log', filemode='w',
level=logging.INFO, format=formatter)
                                                                                             with open(FILEDIR + '{}.csv'.format(symbol), "w") as f:
                                                                                                  f.writelines(str(abc))
parser = argparse.ArgumentParser()
                                                                                             logging.info('downloaded successfully')
parser.add argument("-i", "--initial", help="initial date in %Y-%m-%d format")
parser.add argument("-f", "--final", help="final date in %Y-%m-%d format")
                                                                                             logging.error('got error when trying to download: {}'.format(symbol))
args = parser.parse args()
if args.initial:
    initial = args.initial
                                                                                      def download many(symbols: list[str]) -> None:
                                                                                          with futures. ThreadPoolExecutor (max workers=4) as executor:
if args.final:
                                                                                              res = executor.map(download one, symbols)
    final = args.final
                                                                                      def main():
logging.info('date range: from {} to {}'.format(initial, final))
                                                                                          logging.info('start downloading process...')
start = int(time.mktime(time.strptime(str(initial), '%Y-%m-%d')))
                                                                                          nasdag symbols = read symbols('nasdag symbols.csv')
end = int(time.mktime(time.strptime(str(final), '%Y-%m-%d')))
                                                                                          nyse symbols = read symbols('nyse symbols.csv')
                                                                                          symbols = nasdaq symbols + nyse symbols
if not os.path.exists(FILEDIR):
    os.makedirs(FILEDIR)
                                                                                          download many(symbols)
def read symbols(symfile):
                                                                                          logging.info('finished downloading process!')
   syms = []
    with open(symfile, 'r') as f:
        content = f.readlines()
                                                                                     if name == ' main ':
       for s in content:
                                                                                              main()
            syms.append(s.strip())
```

S&P500 Correlation



S&P500 Correlation Clustering

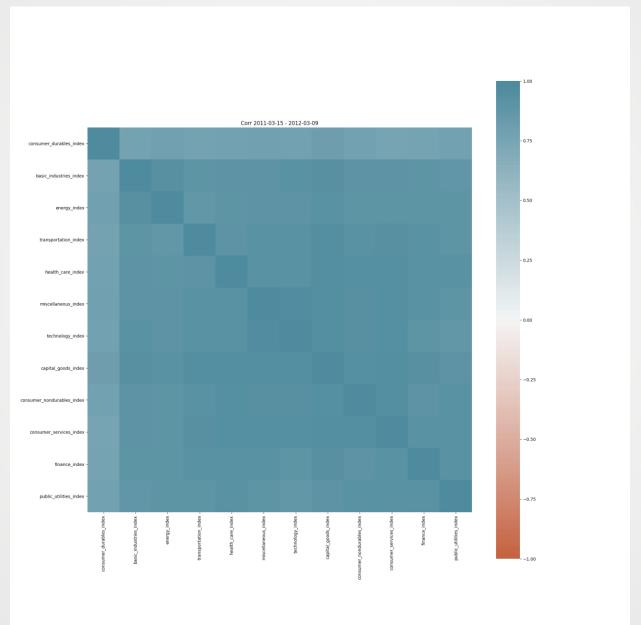


Sectors

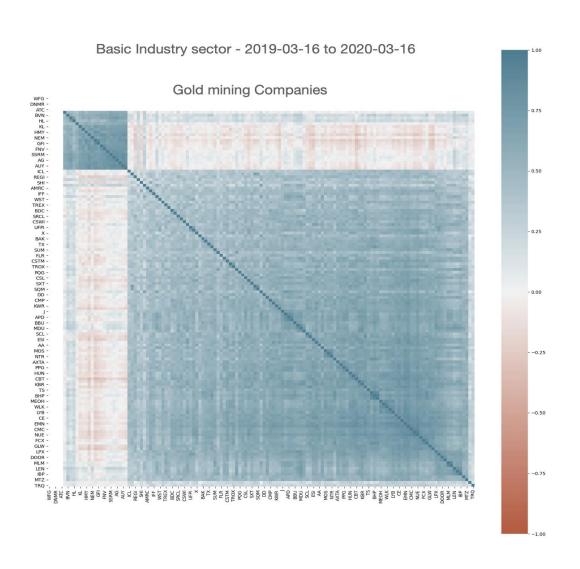
- basic industries
- capital goods
- consumer durables
- consumer nondurables
- consumer services
- energy
- finance
- health care
- public utilities
- technology
- transportation
- miscellaneous



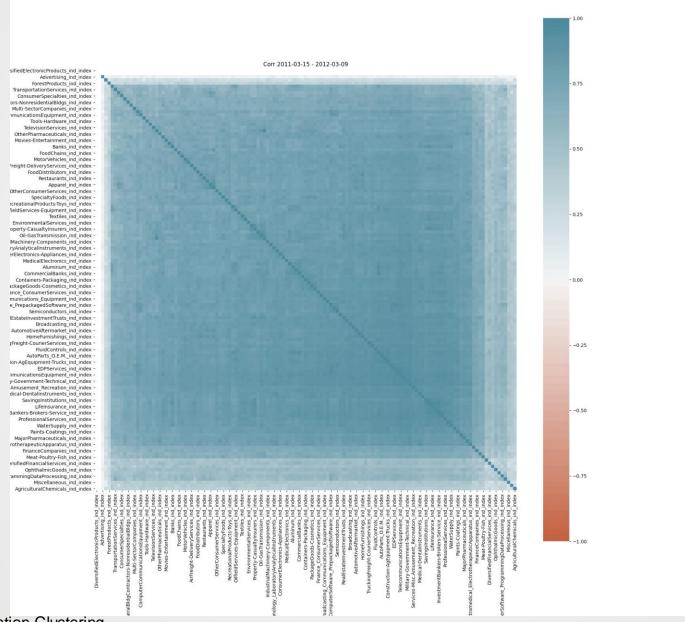
Correlation among Sectors



Correlation within Sector



Industries





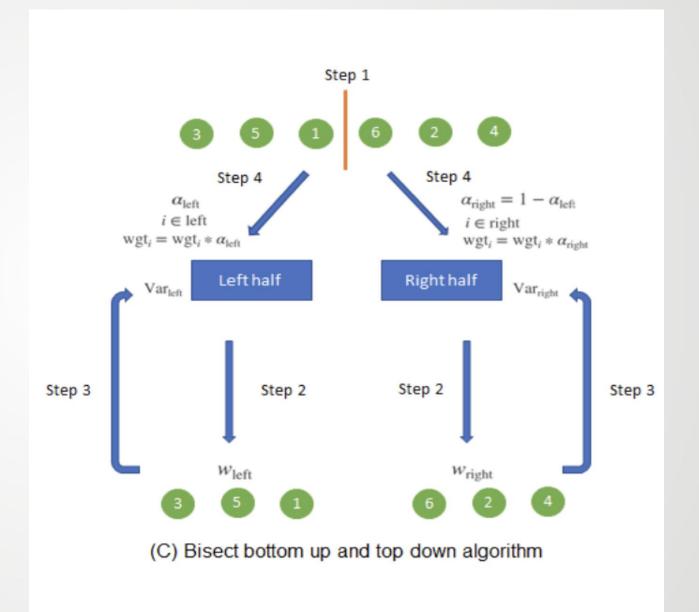
HRP (hierarchical risk parity)

$$w = \frac{(diag(V))^{-1}}{trace(diag(V)^{-1})}$$

$$\tilde{V} = w'Vw$$

$$\alpha_{left} = 1 - \frac{V_{left}}{\tilde{V}_{left} + \tilde{V}_{right}}$$

$$\alpha_{right} = 1 - \alpha_{left}$$



Backtest Result

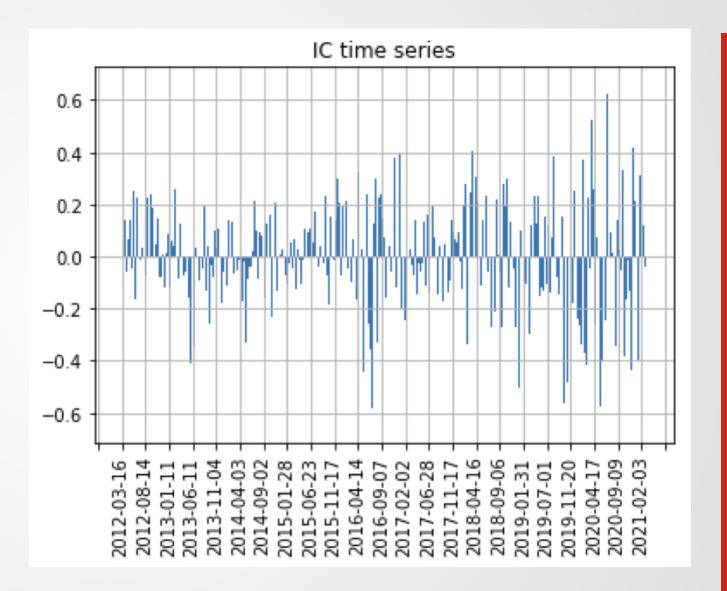
- We use HRP method to compute daily weight of stock in SP500 with the past 252 days stock return.
- It is a long only strategy since the weight is all positive.



	Performance
IC	0.0048
IR	0.0231
annual_return	0.1902
Sharpe	1.2309
Maxdrawdown	1.1372

Result Analysis

- Average IC = 0.005
- IR = 0.023
- It has relative strong signal but not stable



Result Analysis

 It can beat SP500 index in the past 8 years especially in the bull market.

 It has larger drawdown than SP500 in bear market like the beginning of 2020.



Further Study

- HRP doesn't use the hierarchical clustering information sufficiently. It only
 use the sorted order of clustering data.
- It means this method is not exactly risk parity, e.g. our backtest of SP500 stocks.
- HCRP model use the covariance of assets, which can better weight assets with high correlation.

References

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Michaud, R. (1998): Efficient Asset Allocation: A Practical Guide to Stock Portfolio Optimization and Asset Allocation, 1st ed. Harvard Business School Press.

Ledoit, O. and M. Wolf (2003): "Improved estimation of the covariance matrix of stock returns with an application to portfolio selection." *Journal of Empirical Finance*, Vol. 10, No. 5, pp. 603–621.

Raffinot, T. (2017): "Hierarchical clustering based asset allocation." *Journal of Portfolio Management*

Rokach, L. and O. Maimon (2005): "Clustering methods," in Rokach, L. and O. Maimon, eds., *Data Mining and Knowledge Discovery Handbook*. Springer, pp. 321–352.

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Thanks for listening!