



Assignment 9 (08.07.2022)

Handin until: 15.07.2022, 09:00

Important: All the queries you write for this assignment require **recursive queries**.

1. [10 Points] Perrin Numbers

Write a SQL query which calculates each value of the Perrin sequence¹ up to any value $i \in \mathbb{N}$ starting with 0. For example, for $i = 7$, your query produces:

n	per
0	3
1	0
2	2
3	3
4	2
5	5
6	5
7	7

2. [10 Points] Bill of Materials

Recursive queries shine whenever they are used to process hierarchical data. Consider the tables **products** and **parts**:

```

1 CREATE TABLE products (
2   id   int PRIMARY KEY,
3   name text NOT NULL
4 );
1 CREATE TABLE parts (
2   part   int NOT NULL REFERENCES products(id),
3   sub    int NOT NULL REFERENCES products(id),
4   quantity int CHECK (quantity > 0)
5 );

```

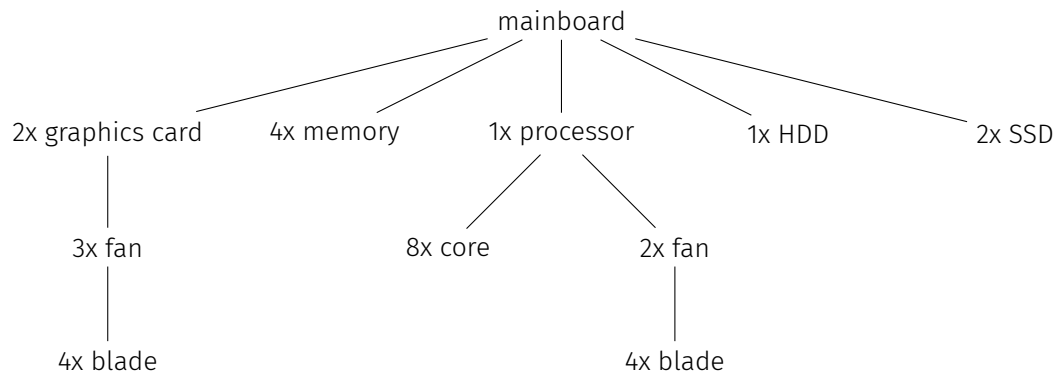
If a product consists of other products, it has an entry in table **parts**. For example, consider a mainboard:

```

1 INSERT INTO products(id, name) VALUES
2 (1, 'mainboard'),
3 (2, 'graphics Card'),
4 (3, 'memory'),
5 (4, 'processor'),
6 (5, 'HDD'),
7 (6, 'SSD'),
8 (7, 'core'),
9 (8, 'fan'),
10 (9, 'blade');
1 INSERT INTO parts(part, sub, quantity) VALUES
2 (1,2,2),(1,3,4),(1,4,1),(1,5,1),(1,6,2),
3 (2,8,3),
4 (4,7,8),(4,8,2),
5 (8,9,4);

```

¹https://en.wikipedia.org/wiki/Perrin_number



Construct a SQL query that lists all parts (and their overall quantity) contained in a mainboard (i.e., the product with `id = 1`). For the example above, we expect the following result:

name	total quantity
graphics card	2
memory	4
HDD	1
fan	8
processor	1
SSD	2
blade	32
core	8

3. [10 Points] Tree Labels

Table `trees` represents a number of trees as previously defined in the slides of Chapter 03 (Tree Encoding) and Assignment 05 Exercise 03.

```

1 CREATE TABLE trees (tree int PRIMARY KEY,
2                       parents int[] NOT NULL,
3                       labels text[] NOT NULL);

```

This query (also contained in SQL file `path-to-root.sql` distributed with the material of Chapter 6) finds all nodes on a path from a node with label `f` to the root node. This query expects each tree to have unique node labels.

```

1
2 -- Which nodes are on the path from node labeled 'f' to the
3 -- root and on which position on the path are these nodes?
4 WITH RECURSIVE
5 paths(tree, pos, node) AS (
6   SELECT t.tree, 0 AS pos, array_position(t.labels, 'f') AS node
7   FROM   trees AS t
8   UNION
9   SELECT t.tree, p.pos + 1 AS pos, t.parents[p.node] AS node
10  FROM   paths AS p, trees AS t
11  WHERE  p.tree = t.tree AND p.node IS NOT NULL
12  -- avoid infinite recursion once we reach the root
13 )
14 SELECT p.tree, p.pos, p.node
15 FROM   paths AS p
16 WHERE  p.node IS NOT NULL

```

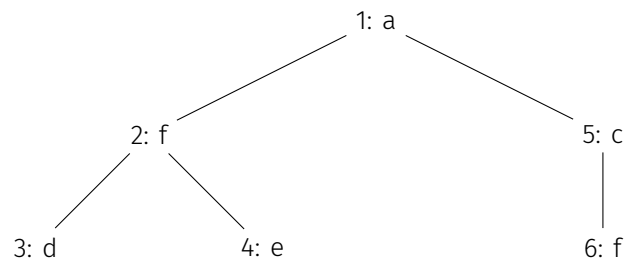
Your task is to adapt the query such that *multiple nodes of the same tree* may carry the same label (e.g., label `f` may occur more than once). Then, extend the output with a new column `path` which uniquely identifies on which of the (possibly many) paths a node has been found.

Hint: Consider using `array_positions(...)`².

²<https://www.postgresql.org/docs/current/static/arrays.html>

Example: Consider table `trees` with a simple tree:

```
1 INSERT INTO trees(tree, parents, labels)
2 VALUES
3 (1, ARRAY[NULL,1,2,2,1,5],
4  ARRAY['a','f','d','e','c','f']);
```



Your adapted query produces the following result:

tree	id	pos	node
1	1	0	2
1	1	1	1
1	2	0	6
1	2	1	5
1	2	2	1