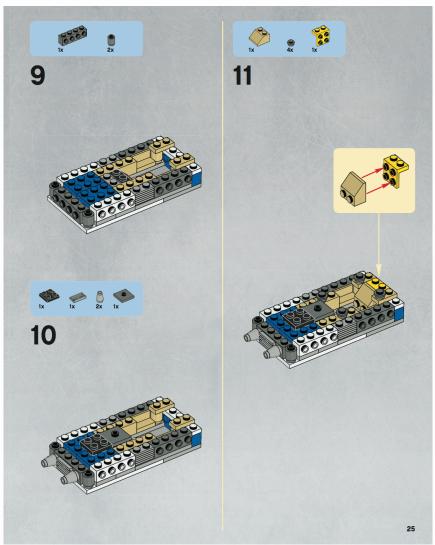
INTRODUCTION TO RELATIONAL DATABASE SYSTEMS DATENBANKSYSTEME 1 (INF 3131)

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LEGO BUILDING INSTRUCTIONS

- Each LEGO set comes with building instructions, an illustrated booklet that details the individual steps of model construction.
 - One page in the booklet holds one or more instruction steps (steps are numbered 1, 2, ...).
 - Each step lists the *pieces* (with *color* and *quantity*) required to complete the step.
 - Each step comes with an *illustration* of where the listed pieces find their place in the model.
- What would be a reasonable design for a building instructions table? Clearly:
- 1. Do not include LEGO set details in instructions: instead, use a foreign key to refer to table sets.
- 2. Do not include LEGO piece details in instructions: instead, use a foreign key to refer to table bricks.
- 3. Represent page numbers, step numbers, image sizes as integers but formulate constraints that avoid data entry errors (e.g. negative page/step numbers).

LEGO BUILDING INSTRUCTIONS



Page 25 in Building Instruction for LEGO Set 9495 (Y-Wing)

LEGO BUILDING INSTRUCTIONS (TABLE DESIGN)

instructions

<u>set</u>	<u>step</u>	<u>piece</u>	<u>color</u>	quantity	page	img	width	height
•	•	•	•	•	•	•	•	•
9495-1	7	3010	2	2	24	<pre><image07></image07></pre>	639	533
9495-1	7	3023	2	2	24	<pre><image07></image07></pre>	639	533
9495-1	7	2877	86	1	24	<pre><image07></image07></pre>	639	533
9495-1	8	3002	7	2	24	<pre><image08></image08></pre>	650	522
9495-1	8	30414	1	2	24	<pre><image08></image08></pre>	650	522
9495-1	9	30414	85	1	25	<pre><image09></image09></pre>	541	638
9495-1	9	3062b	85	2	25	<pre><image09></image09></pre>	541	638
9495-1	10	30033	11	1	25	<pre><image10></image10></pre>	540	662
9495-1	10	2412b	86	1	25	<pre><image10></image10></pre>	540	662
9495-1	10	4589b	86	2	25	<pre><image10></image10></pre>	540	662
9495-1	10	87580	85	1	25	<pre><image10></image10></pre>	540	662
9495-1	11	3039	2	1	25	<pre><image11></image11></pre>	1042	558
9495-1	11	4073	85	4	25	<pre><image11></image11></pre>	1042	558
9495-1	11	44728	3	1	25	<pre><image11></image11></pre>	1042	558
•	•	•	•	•	•	•	•	•

REDUNDANCY

- The design of table instructions appears reasonable. We immediately spot a fair amount of **redundancy**, though. For example:
- 1. Step 10 of Set 9495 is printed on page 25. [represented 4 ×]
- 2. Step 7 of Set 9495 is illustrated by <image07>. [3 ×]
- 3. $\langle image09 \rangle$ has dimensions 541 \times 638 pixels. [2 \times]
- Redundancy comes with a number of serious problems, most importantly:
 - Storage space is wasted.

 Tables occupy more disk space than needed. Query processor has to touch/move more bytes. Archival storage (backup) requires more resources.
 - Redundant copies will go out of sync.

 Eventually, an update operation will miss a copy. The database instance now contains "multiple truths." Typically, this goes unnoticed by DBMS and user.

EMBEDDED FUNCTIONS AND REDUNDANCY

- In table instructions, the source of redundancy is the presence of **functions** that are **embedded in the table**.

Leibniz Principle

If f is a function defined on x and y, then

$$x = y \land f(x) = z \Rightarrow f(y) = z$$

- Table instructions embeds the materialized functions
- 1. printed_on(): maps set, step to the page it is printed on
- 2. illustrated_by(): maps set, step to the illustration stored in image img
- 3. image_size(): maps an image img to its width and height

Functional Dependency (FD)

Let (R, α) denote a relational schema. Given $\beta \subseteq \alpha$ and $c \in \alpha$, the **functional dependency** $\beta \rightarrow c$ holds in R if

$$\forall t,u \in inst(R) : t.\beta = u.\beta \Rightarrow t.c = u.c$$

Read: "If two rows agree on the columns in β , they also agree on column c." (β : function arguments, c: function result).

Notation: the FD $\beta \to \{c_1,...,c_n\}$ abbreviates the set of FDs $\beta \to c_1$, ..., $\beta \to c_n$.

- Note: If $c \in \beta$, then $\beta \to c$ is called a **trivial FD** that obviously holds for any instance of R. No interesting insight into R here.

- FDs are **constraints** that document universally valid mini-world facts (e.g., "a step is associated with one illustration"). FDs thus need to hold in all database instances.

instructions

<u>set</u>	<u>step</u>	<u>piece</u>	<u>color</u>	quantity	page	img	width	height
•	:	•	•	•	•	•	•	•
9495-1	7	3010	2	2	24	<pre><image07></image07></pre>	639	533
9495-1	7	3023	2	2	24	<pre><image07></image07></pre>	639	533
9495-1	7	2877	86	1	24	<pre><image07></image07></pre>	639	533
9495-1	8	3002	7	2	24	<pre><image08></image08></pre>	650	522
9495-1	8	30414	1	2	24	<pre><image08></image08></pre>	650	522
9495-1	9	30414	85	1	25	<pre><image09></image09></pre>	541	638
9495-1	9	3062b	85	2	25	<pre><image09></image09></pre>	541	638
•	•	•	•	•	•	•	•	•

- Which functional dependencies hold in table instructions?

- Given table R, check whether the FD $\{b_1, ..., b_n\} \rightarrow c$ holds in the current table instance:

```
SELECT DISTINCT 'The FD \{b_1, ..., b_n\} \rightarrow c does not hold' FROM R AS r GROUP BY r.b_1, ..., r.b_n HAVING COUNT(DISTINCT r.c) > 1
```

Aggregate Functions

Optional modifier DISTINCT affects the computation of aggregate functions:

```
<aggregate>([ ALL ] expression) -- aggregate all non-NULL values
<aggregate>(DISTINCT expression) -- aggregate all distinct non-NULL
values
<aggregate>(*) -- aggregate all rows (count(*))
```

$KEY \rightarrow FD$

- Note that a **key** implicitly defines a **particularly strong FD:** the key columns functionally determine *all* columns of the table.

```
Keys vs FDs (1)
Assume table (R, \{a_1,...,a_k, a_{k+1},...,a_n\}).
\{a_1,...,a_k\} \text{ is a key of } R \Leftrightarrow \{a_1,...,a_k\} \rightarrow \{a_{k+1},...,a_n\} \text{ holds.}
```

- So, keys are special FDs.
- Turning this around: FDs are a generalization of keys.

FD → (LOCAL, PARTIAL) KEY

Keys vs FDs (2) Assume table R and FD $\beta \to c$. Then β is key in the sub-table of R defined by

SELECT DISTINCT β , c FROM R

- Example: for table instructions and FD $\{\text{set, step}\} \rightarrow \text{page}$ the sub-table is

<u>set</u>	<u>step</u>	page
•	•	•
9495-1	7	24
9495-1	8	24
9495-1	9	25
9495-1	10	25
9495-1	11	25
•	•	•

(i.e., exactly the table materializing the function printed_on(), see above).

- Example: recall table stores of the LEGO Data Warehouse scenario:

store	city	state	country
•	0 0	•	•
7	HAMBURG	Hamburg	Germany
8	LEIPZIG	Sachsen	Germany
9	MÜNCHEN	Bayern	Germany
10	MÜNCHEN PASING	Bayern	Germany
11	NÜRNBERG	Bayern	Germany
•	• •	•	•
16	ARDEN FAIR MALL	CA	USA
17	DISNEYLAND RESORT	CA	USA
18	FASHION VALLEY	CA	USA
•	•	•	•

- List the FDs that hold in table stores.
- Does the mini-world suggest FDs not implied by the rows shown above?

- An FD indicates the presence of a materialized function. Consider the following variant of the users and ratings table:

user rating stars Alex 3 *** Bert 1 * Cora 4 **** Drew 5 ***** Erik 1 * Fred 3 ***

- FD {rating} \rightarrow stars materializes the **computable function** stars = f(rating) = repeat('*', rating) [see PostgreSQL's string function library].
- In such cases, good database design should consider to **trade materialization for computation**. Removes redundancy.



SQL: VIEWS

CREATE VIEW

Binds query to name which is **globally** visible. Whenever table name is referenced in subsequent queries, query is **re-evaluated** and its result returned (no materialization of the result of query is performed):

-- TEMPORARY: automatically drop view after current session
CREATE [OR REPLACE] [TEMPORARY] VIEW name
AS query

- Compare with CTEs: local visibility in surrounding WITH statement only.
- A temporary view named *name* shadows a (regular, persistent) table of the same name.

SQL: VIEWS

- Views provide **data independence:** users and applications continue to refer to *name*, while the database designer may decide to replace a persistent table with a computed query or vice versa.
- **Example:** turn the materialized function stars = f(rating) into a computed function:

```
-- drop the materialized function from the table
ALTER TABLE users
   DROP COLUMN stars;

-- provide the three-column table that users/applications expect
CREATE TEMPORARY VIEW users(user, rating, stars)
   AS SELECT u.user, u.rating, repeat('*', u.rating) AS stars
   FROM users AS u;
```

- Since PostgreSQL's repeat() is a pure function, the FD rating → stars trivally holds in the view.



DERIVING FUNCTIONAL DEPENDENCIES

- Given a set F of FDs over table R, simple inference rules—the Armstrong Axioms—suffice to generate all FDs following from those in F.

```
Armstrong Axioms
Apply exhaustively to generate all FDs implied by FD set F.

Reflexivity:
If \gamma \subseteq \beta, then \beta \to \gamma.

Augmentation (with c \in sch(R)):
If \beta \to \gamma, then \beta \cup \{c\} \to \gamma \cup \{c\}

Transitivity:
If \alpha \to \beta and \beta \to \gamma, then \alpha \to \gamma.
```

- Note: transitivity closely relates to **function composition**: if f, g are functions, so is $g \circ f$.

DERIVING FDS (COVER)

- **Problem:** Given a set $\alpha \subseteq sch(R)$ of columns and a set of FDs F over R, compute the **cover** α^+ , i.e., the set of all columns functionally determined by α .

Cover

The **cover** α^+ of a set of columns α is the set of all columns c that are functionally determined by the columns in α (with respect to a given FD set F):

$$\alpha^+ := \{ c \mid F \text{ implies } \alpha \rightarrow c \}$$

- A Should we find that $\alpha^+ = sch(R)$, then α is a super key for R.

DERIVING FDS (COVER)

- Compute the cover α^+ for a given set of FDs:

DERIVING FDS (COVER)

- Example: In table instructions, compute $\{\text{set}, \text{step}\}^+ \text{ with } F = \{ \{\text{set}, \text{step}\} \rightarrow \text{page}, \{\text{set}, \text{step}\} \rightarrow \text{img}, \{\text{img}\} \rightarrow \text{width}, \{\text{img}\} \rightarrow \text{height} \}.$

instructions

<u>set step piece color quantity page img width height</u>

- Tracing column set X:

```
Of X := {set,step}

PD {set,step} → page, {set,step} ⊆ X: X := X ∪ {page}

FD {set,step} → img, {set,step} ⊆ X: X := X ∪ {img}

FD {img} → width, {img} ⊆ X: X := X ∪ {width}

FD {img} → height, {img} ⊆ X: X := X ∪ {height}

All FDs considered. X = {set, step, page, img, width, height}

Repetition of Of Office of Note that the page is not add new columns to X.

Return {set, step, page, img, width, height}.

Office the page is not add new columns to X.

Return {set, step, page, img, width, height}.

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```

DERIVING CANDIDATE KEYS

- Invoke via $key(\phi, sch(R), F)$.
- Can optimize at \triangleright : invoke $key(K \cup \{c\}, U \setminus cover(K \cup \{c\}, F), F)$ instead.

DATABASE DESIGN WITH FDS

- Typically it is a severe sign of **poor database design if tables embed functions**, i.e., if a table contains

FDs that are not implied by the primary key. \triangle

- Consequences of table designs with non-key FDs / embedded functions:
- 1. Redundancy (see above ✓)
- 2. Update/Insertion/Deletion Anomalies
- 3. RDBMS cannot protect the integrity of non-key FDs, thus risk of inconsistency over time:
 - SQL DDL does *not* implement an ALTER TABLE ... ADD FUNCTIONAL DEPENDENCY ... statement.
 - Although FDs embody important mini-world facts they are easily violated without protection. (Can simulate this protection using SQL triggers or rewrite rules. Cumbersome. Inefficient.)

UPDATE/INSERTION/DELETION ANOMALIES

- Recall table instructions and embedded FD {img} → {width, height}:

instructions

set step piece color quantity page img width height

- Update anomaly:

Changing a **single mini-world fact** requires the modification of **multiple rows**. [Modifying image size requires to search/update entire **instruction** table.]

- Insertion anomaly:

A new mini-world **fact cannot be stored** unless it is put in larger context. [No place to record width/height dimension of a new image yet unused in an instruction manual.]

- Deletion anomaly:

A formerly stored mini-world fact vanishes once its (last) context is deleted.

[Information about image width/height is lost once last instruction manual including that image is deleted from instructions.]

BOYCE-CODD NORMAL FORM

Boyce-Codd Normal Form (BCNF)

Table R is in **Boyce-Codd Normal Form (BCNF)** if and only if all its FDs are already implied by its key constraints.

For table R in BCNF and any FD $\beta \rightarrow c$ of R one of the following holds:

- 1. The FD is trivial, i.e., $c \in \beta$.
- 2. The FD follows from a key because β (or a subset of it) already is a key of R.
- A table in BCNF does not exhibit the three anomalies (no embedded functions).
- All FDs in table in BCNF are protected by the RDBMS through PRIMARY KEY (or UNIQUE) constraints.

BOYCE-CODD NORMAL FORM

- Examples:

- Table instructions is not in BCNF: key FD {set, step, piece, color} →
 {quantity, page, img, width, height} does not imply {set, step} → {page,
 img} or {img} → {width, height}:
 instructions

set step piece color quantity page img width height

- Table users not in BCNF: {rating} → {stars} not implied by key FD:

users

name rating stars

- Table stores not in BCNF: {state} → {country} not implied by key FD: stores

store city state country

BCNF SCHEMA DECOMPOSITION

```
\mathbf{split}(R,F) (input: table R with FD set F output: splitted relation schemata)

if \beta \to c \in F with c \notin \beta and \beta does not contain a key of R then split and replace R:

R_1((sch(R) \setminus \mathbf{cover}(\beta, F)) \cup \beta)
R_2(\mathbf{cover}(\beta, F))
\mathbf{split}(R_1, F|sch(R_1))
\mathbf{split}(R_2, F|sch(R_2))
```

- Notes:

- $F \mid C$ denotes FD set F restricted to those $\beta \rightarrow c$ for which $\beta \cup \{c\} \subseteq C$.
- For each split: $sch(R_1) \cup sch(R_2) = sch(R)$ and $sch(R_1) \cap sch(R_2) = \beta$.

BCNF: AFTER DECOMPOSITION (1)

- Resultant BCNF tables after **split**(instructions, F) has been completed:

parts (1/3)

	. , - ,			
<u>set</u>	<u>step</u>	<u>piece</u>	<u>color</u>	quantity
•	•	•	•	•
9495-1	7	3010	2	2
9495-1	7	3023	2	2
9495-1	7	2877	86	1
9495-1	8	3002	7	2
9495-1	8	30414	1	2
9495-1	9	30414	85	1
9495-1	9	3062b	85	2
•	•	•	•	•

- Note: It is rather straightforward to name the newly generated tables: these tables represent a *single* real-world concept.

BCNF: AFTER DECOMPOSITION (2)

- Resultant BCNF tables after **split**(instructions, F) has been completed:

layouts (2/3)

<u>set</u>	<u>step</u>	page	img
•	•	•	:
9495-1	7	24	<pre><image07></image07></pre>
9495-1	8	24	<pre><image08></image08></pre>
9495-1	9	24	<pre><image09></image09></pre>
•	•	•	•

illustrations (3/3)

<u>img</u>	width	height
•	•	•
<pre><image07></image07></pre>	639	533
<pre><image08></image08></pre>	650	522
<pre><image09></image09></pre>	541	638
•	•	•

- To tie the BNCF tables together, establish foreign keys pointing from parts to layouts and from layouts to illustrations.

BCNF: RECONSTRUCTION

- Use an **equi-join to reconstruct** the original wide table **instructions** from its constituent tables:

Reconstruction after BCNF decomposition

Perform an equi-join over the (non-empty) schema intersections of the BCNF tables:

- It may make sense to use CREATE VIEW to reestablish the wide table for users and applications.

BCNF: AFTER DECOMPOSITION

- Decomposition for table users:



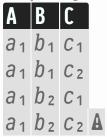
- The RDBMS protects the FDs (keys): translation from rating to stars in table render is always consistent. No redundancy in table render.

BCNF DECOMPOSITION: LOSSLESS SPLITS

- BNCF decomposition builds on the assumption that **no information is lost** during the splits: original table R can be reconstructed by an equi-join of R_1 and R_2 .
- Not all decompositions are **lossless**, however. Consider:

R
A B C
a₁ b₁ c₁
a₁ b₁ c₂
a₁ b₂ c₁

and its decomposition into $R_1(A, B)$, $R_2(A, C)$. This is a somewhat arbitrary split, not suggested by an FD. The equi-join of R_1 and R_2 (on A) is:



⇒ An extra (bogus!) row has been reconstructed by the join. **Information has** been **lost**.

BCNF: LOSSLESS SPLITS

Decomposition Theorem

```
Consider the decomposition of table R into R_1 and R_2. The reconstruction of R from R_1, R_2 via an equi-join on sch(R_1) \cap sch(R_2) is lossless if
```

- 1. $sch(R_1) \cup sch(R_2) = sch(R)$ and
- 2. $sch(R_1) \cap sch(R_2)$ is a key of R_1 or R_2 (or both).
- The splits "along the FD $\beta \to c$ " performed by ${\bf split}(R,F)$ will always be lossless:
- 1. $sch(R_1) \cup sch(R_2) = sch(R)$ and $sch(R_1) \cap sch(R_2) = \beta$
- 2. Since $sch(R_2) = cover(\beta, F)$, β is a key for $R_2 \checkmark$
- We will never lose information through BCNF decomposition.

BCNF: NON-DETERMINISM, LOSS OF FDS

- \triangle BCNF is **not deterministic:** arbitrary choice of the "split FD" in algorithm **split**(R,F) leads to different decompositions, in general:
- 1. For table instructions: splitting along FD {set,step} \rightarrow {page, img} or {img} \rightarrow {width,height} first makes no difference. (Try it.)
- 2. But consider $R(\underline{A},\underline{B},C,D,E)$ with FDs $\{C,D\} \rightarrow E$ and $\{B\} \rightarrow E$.
- A BCNF decomposition may fail to preserve dependencies: given FD $\beta \to c$, the column set $\beta \cup \{c\}$ may be distributed across multiple tables. The FD is "lost" (cannot be enforced by the system).
 - Consider FDs {zip} \to {city, state} and {street, city, state} \to zip in table zipcodes.
 - 1. What are the candidate keys for zipcodes?
 - 2. What is a BCNF decomposition for zipcodes?

zipcodes
zip street city state

DENORMALIZATION VS. DECOMPOSITION

- BCNF and decomposition come with significant benefits but are no panacea. There are valid reasons to leave database tables in **denormalized form:**

1. Performance:

Decomposition requires table reconstruction via equi-joins which incur query evaluation costs. Denormalized table save this effort at the cost of storing information redundantly.

2. Preservation of FDs:

In specific applications, preservation of mission-critical FDs may be a higher priority than the removal of redundancy.

- Columnar database systems perform full decomposition (beyond the splits required by BCNF normalization): $R(\underline{id}, A, B, C, ...)$ decomposed into $R_1(\underline{id}, A)$, $R_2(\underline{id}, B)$, $R_3(\underline{id}, C)$, ... (binary tables).
 - Queries other than SELECT r.* FROM R AS r can selectively access the R_i , reading less bytes from persistent storage.
 - DBMS internals simplified: every row is guaranteed to have exactly two fields.