DB 2

11 - Sorting and Grouping

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1 A Family of Q_9 : The Ubiquitous Sort



Recall table indexed (with B+Tree index indexed_a only):

- 1 SELECT i.*
 FROM indexed AS i
 ORDER BY i.c
- 2 SELECT DISTINCT i.c FROM indexed AS i

- SELECT i.c, SUM(i.a) AS s FROM indexed AS i GROUP BY i.c
- **SELECT DISTINCT** i1.a FROM indexed AS i1, indexed AS i2
 WHERE i1.a = i2.c :: int

All four queries are evaluated using the Sort plan operator.



- Operator Sort may be costly to evaluate and RDBMSs try to plan query execution without sorting if possible:
 - In queries 1 to 4 above, replace i.c (i2.c) by i.a and PostgreSQL will use Index Only Scans on a-ordered B+Tree indexed_a instead of Sort.
- Sort is a blocking operator and intoduces plan latency:

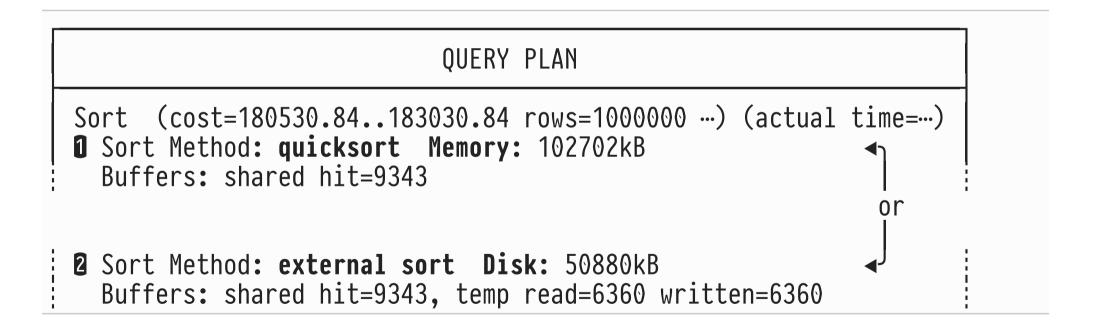
```
QUERY PLAN

Sort (cost=180530.84..183030.84 rows=1000000 width=41)
Output: a, b, c
```



Sorting may need (lots of) temporary working memory:

- 1 Try to stay RAM-resident if possible,
- ② otherwise, resort to a disk-based sorting algorithm:





Now assume the following typical scenario:

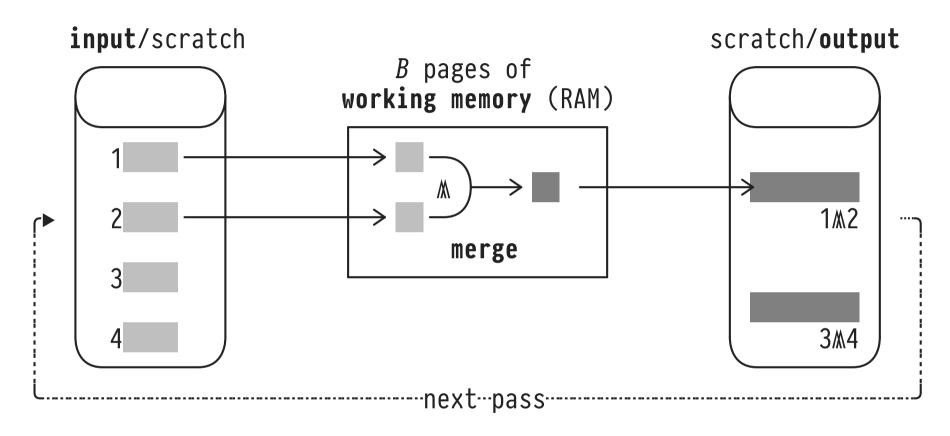
- input heap file T to be sorted: N pages,
- size of temporary working memory (RAM): $B \ll N$ pages,
- size of secondary scratch memory (disk): ≥ 2 × N blocks.

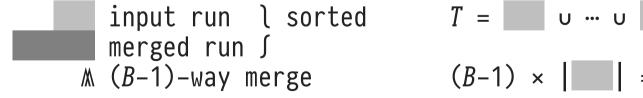
External Merge Sort can sort heap files of any size as long as $B \ge 3$ pages of working memory are available:

- reads unsorted input file, writes sorted output file,
- creates partially sorted sub-files (runs) on disk,
- \bullet multiple passes (the larger B, the fewer passes).

An External Merge Sort Pass (B = 3)







$$T = \bigcup_{v \in V} \bigcup_{v \in V}$$

$$(B-1) \times | = |$$



```
ExternalMergeSort(T,B):
  N \leftarrow \#pages of T;
  R \leftarrow \lceil N/B \rceil;
                                               } R: current number of runs
  split input T into R partitions p_i of B pages;
    run r_i \leftarrow \text{in-memory sort of } p_i;
   while R > 1
     R \leftarrow \lceil R / (B-1) \rceil;

for each i \in 1...R

\lfloor M: merge next B-1 runs into one run;
   return single sorted run;
```

External Merge Sort: Passes and I/O Operations



pass	input: #runs	input: run size	output: #runs	output: run size
1	$\lceil N/B \rceil$	В		$B \times (B-1)$
2 3	$\lceil N/B \rceil / (B-1)$ $\lceil N/B \rceil / (B-1)^2$	$B \times (B-1)$ $B \times (B-1)^2$	$[N/B] / (B-1)^2$ $[N/B] / (B-1)^3$	$B \times (B-1)^{2}$ $B \times (B-1)^{3}$
i n	$\lceil N/B \rceil / (B-1)^{n-1}$	$B \times (B-1)^{n-1}$	$\lceil N/B \rceil / (B-1)^n$	$B \times (B-1)^n$

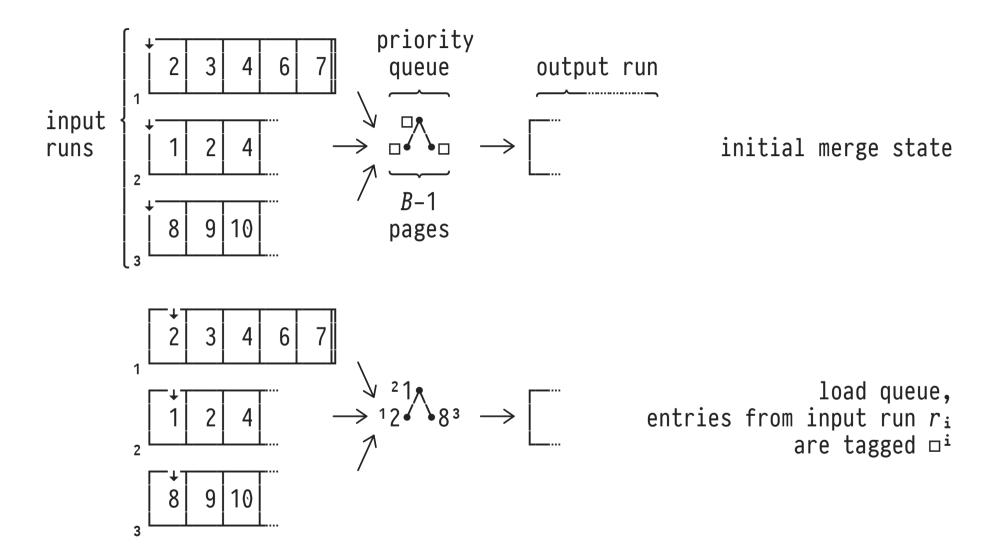
In each pass:

 $N = input (\#runs \times run size) = output (\#runs \times run size).$

- \circ Each pass performs 2 \times N I/O operations.
- Passes required by External Merge Sort with B buffers:

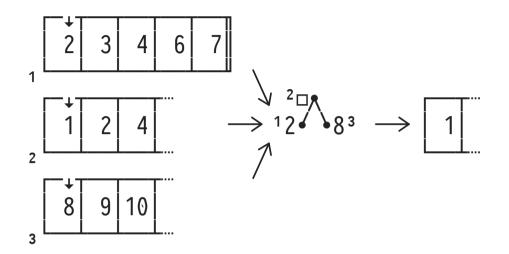




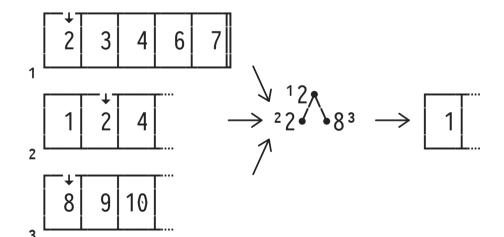


(B-1)-Way Merge (Passes 1,2,...)





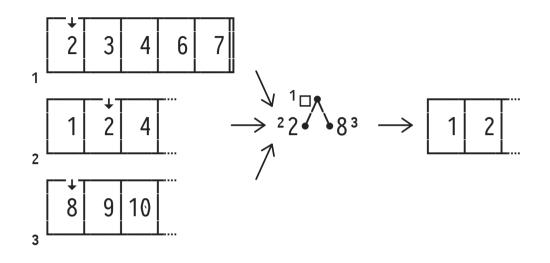
queue head → output run



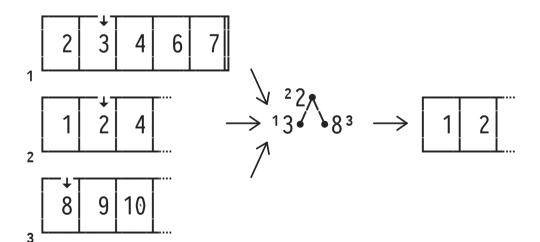
refill queue from input run

(B-1)-Way Merge (Passes 1,2,...)





queue head → output run



refill queue from input run

:

External Merge Sort: Access Patterns and Blocked I/O



- I/O access patterns in
 - \circ pass 0: sequential read/write chunks of B pages, \bigcirc
 - \circ merge passes 1,...: random reads from the B-1 runs. \P
- Perform **blocked I/O** in merge passes 1,2,...:
 - ∘ Seek once to read b > 1 pages at a time from each run. Reduces per-page I/O cost by a factor of $\approx b$.
 - \circ Reduced fan-in: can only merge |(B-1)/b| runs per pass.

External Merge Sort Parameters (Interactive)



I/O Characteristics and Performance of External Sorting

Database Characteristics

Database page size: 8 KiB
Available working space in database buffer (B): 16384 pages (that's 128.0 MiB)
I/O blocking factor (b): 64 pages

Disk Characteristics

Disk seek time: 3.4 ms Disk read/write speed: 163 MiB/s

Resulting transfer time for a 8 KiB block: 0.049 ms

Size of Sort Problem

Size of input file to be sorted: $0.5 \, \text{GiB}$ (this makes for $N = 65536 \, \text{pages}$ of input)

Resulting External Sort Behavior

Pass 0 will produce 4 runs, each of size 16384 pages . We will need 1 merge passes, with a fan-in of 255.

Resulting I/O and Disk Seek Effort

The sort process will initiate 262144 I/O operations (reads and writes) and 2056 disk head seeks.

Resulting Overall Time for Sort Process

Disk seeking will need 0.1 minutes, while 0.2 minutes is spent on I/O itself. Overall, we end up waiting 0.3 minutes for the sort result.

Made with Tangle.js.





 The initial number of runs created in pass 0 influence overall sort performance:

```
# I/O operations = 2 \times N \times (1 + \lceil \log_{B-1} \lceil N/B \rceil \rceil)
```

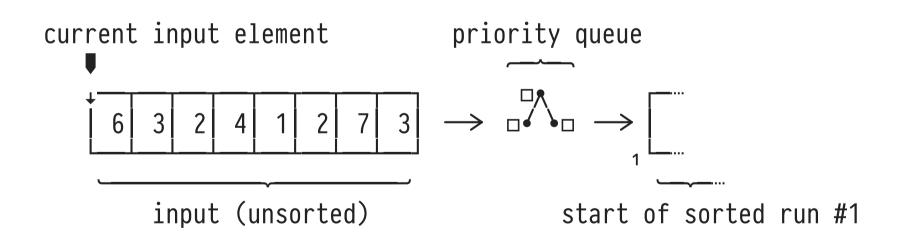
runs created in pass 0

- Q: Given only B buffers, can we create sorted runs longer than B pages?
 - A: Yes! In pass 0, use Replacement Sort (instead of QuickSort, for example).



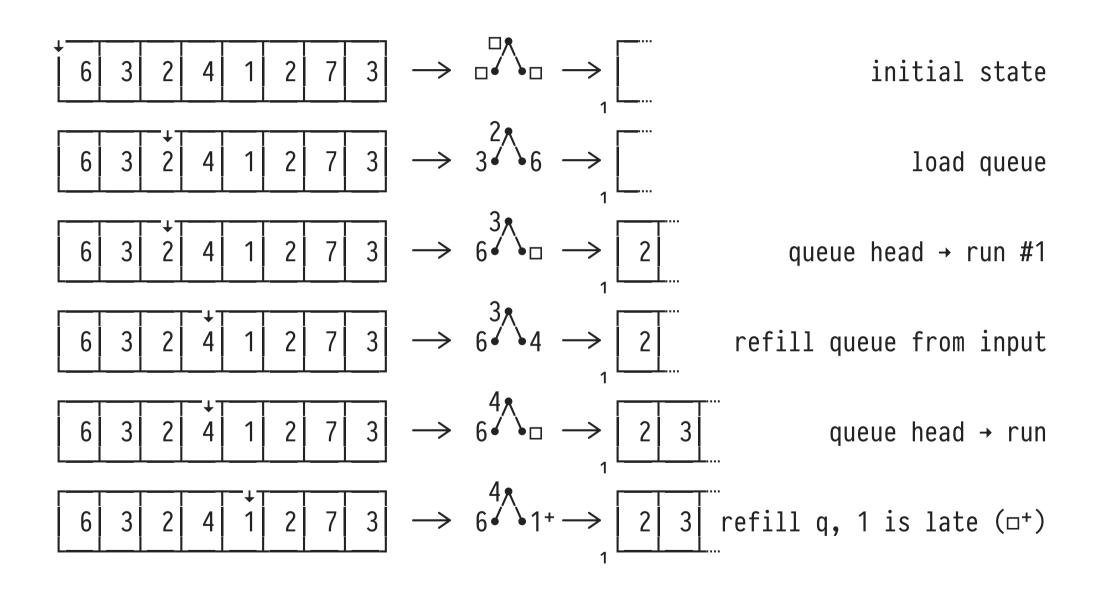
Again, use B-1 buffer pages to set up a priority queue:

- 1. Elements arriving too late for inclusion in current run are marked (□+) and receive lower priority.
- 2. When all elements in queue are marked, close the current run, unmark all elements, open a new run.



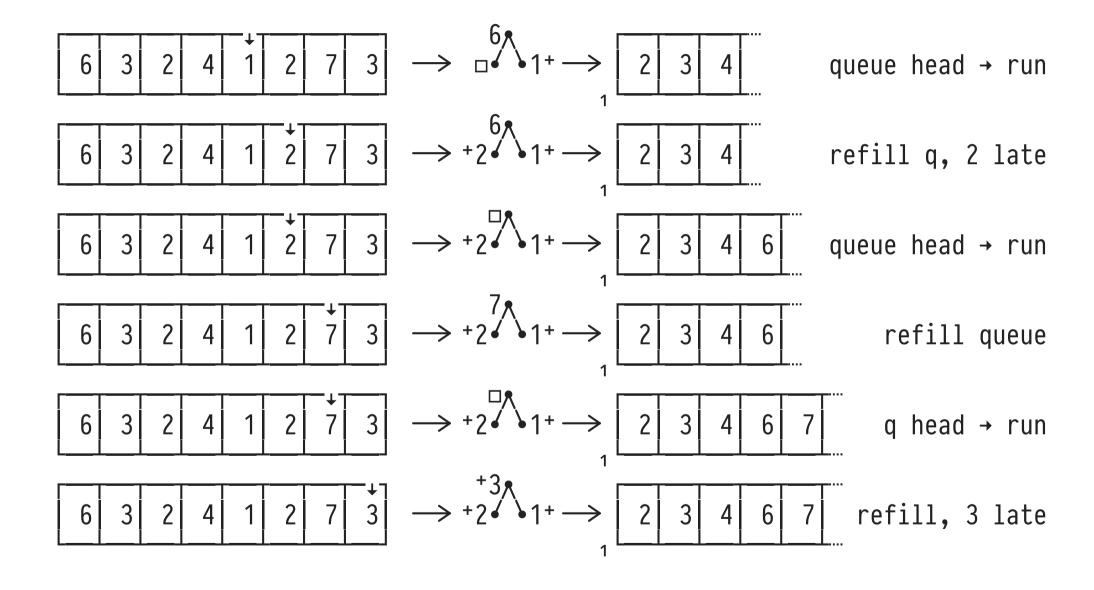
Replacement Sort (B = 4)





Replacement Sort (B = 4)





Replacement Sort (B = 4)



All entries in queue are late (□+):

- Close current run #1, open new run #2.
- Reorder entries in queue, continue processing.

$\begin{bmatrix} 6 & 3 & 2 & 4 & 1 & 2 & 7 & 3 \end{bmatrix} \rightarrow 2 & 3 \rightarrow \begin{bmatrix} 2 & 3 & 4 & 6 & 7 \end{bmatrix}$	ı							T	_+1		1∱						Т		
		6	3	2	4	1	2	7 l	3	\rightarrow	24 3	\rightarrow	2	3	4	6	7		
	į			_							_	4						֡֞֞֞֞֞֞֞֞֞֞֞֞֞֞֞֞֓֓֓֞֞֞֞֓֡֓֞֡֓֡֡֡֡֡֡֡֡֓	

- Replacement Sort produces runs of length $\approx 2 \times (B-1) > B$ (see Knuth, TAoCP, volume 3, p. 254).
- Replacement Sort generates longer runs if input file is almost sorted (e.g., consider a heap file that was once clustered but has received a few updates since then).



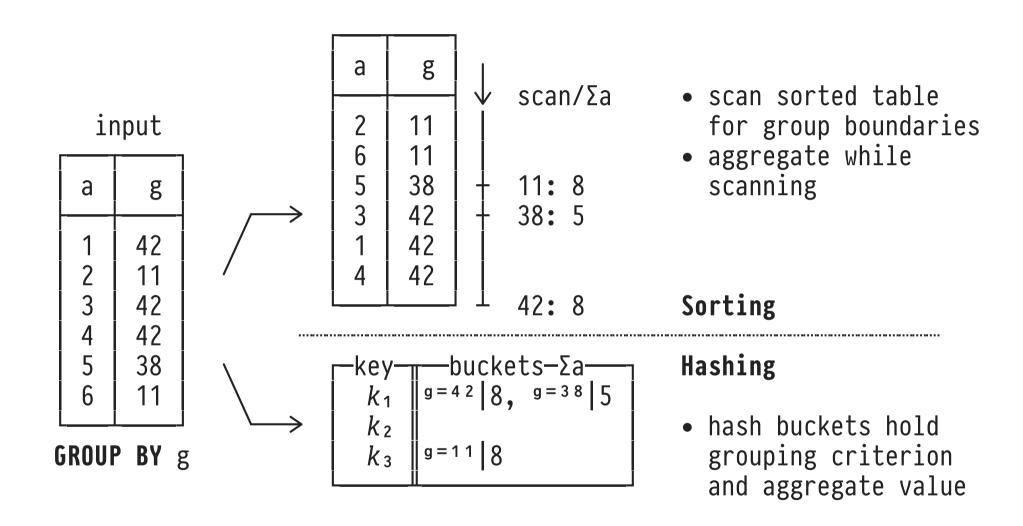
Grouping coarsens the granularity of data processing (individual rows ➤ groups of rows):

```
2 SELECT g.c, SUM(g.g) AS s -- out: 10<sup>4</sup> groups (aggregates) FROM grouped AS g -- in: 10<sup>6</sup> rows
1 GROUP BY g.g
```

- Partition table indexed by criterion g.g (all rows agreeing on g.g form one group),
- output group criterion and aggregates of the group's member rows (the group member rows themselves are never output).

Grouping: Sorting vs. Hashing



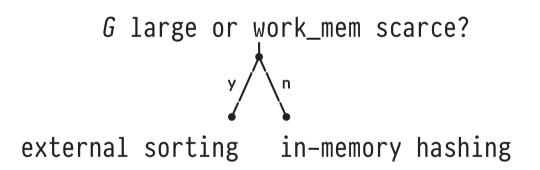


Grouping: Sorting vs. Hashing



PostgreSQL plans for sorting vs. hashing based on

- 1. the available working memory (work_mem) and
- 2. the estimated number G of resulting groups:



• Often, G is unknown or cannot be derived (e.g., GROUP BY g.g % 2 \Rightarrow $G \leq$ 2 not understood by PostgreSQL).

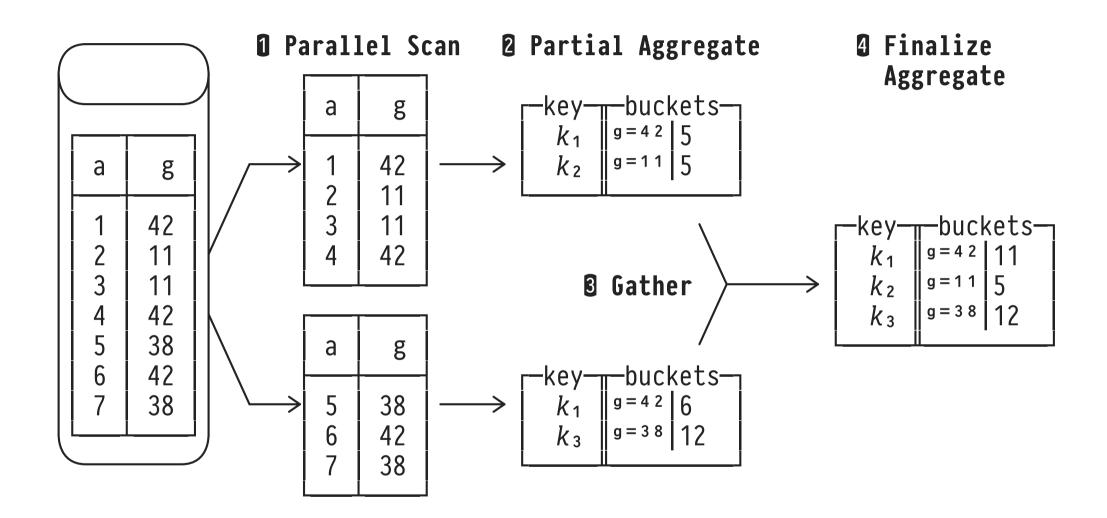
• \circ \Rightarrow Overestimate G conservatively, use sorting.

Grouping and aggregation are query operations that are straightforward to parallelize:

- Spawn workers, each of which execute in // (on dedicated CPU core). Constrain max number of workers to fit host.
- Try to evenly distribute work (e.g., data volume) among workers.
- Assign a leader thread/process that coordinates workers and gathers partial query results.
- After gathering, merge/finalize partial results to produce a single complete query result.

Parallel Grouping (GROUP BY g — SUM(a))







```
EXPLAIN
  SELECT g.g, SUM(g.a) AS s
  FROM grouped AS g
  GROUP BY g.g;
```

QUERY PLAN

```
Finalize HashAggregate (cost=13869.28..13969.02 ...)
Group Key: g
-> Gather (cost=11675.00..13769.54 ...)
Workers Planned: 2 — ||ism degree: 3 (2 worker + 1 leader)
-> Partial HashAggregate (cost=10675.00..10774.74 ...)
Group Key: g
-> Parallel Seq Scan on grouped g (cost=0.00..8591.67 ...)
```

Partial Aggregation and Finalization



 Parallel evaluation of aggregate AGG depends on the distributivity over ⊎ (bag union):

$$AGG(X \uplus Y) = AGG(\{AGG(X)\} \uplus \{AGG(Y)\}).$$

Many SQL aggregates (COUNT, SUM, MAX, MIN, AVG, bool_and, bool_or, ...) exhibit this property:

```
SUM(X \uplus Y) = SUM(\{SUM(X)\} \uplus \{SUM(Y)\}) = SUM(X) + SUM(Y)
distribute partial aggregates finalize work
```

7 Q₉: Sorting in MonetDB





```
CREATE TABLE sorted (a text, s int);

SELECT s.a, s.s
FROM sorted AS s
ORDER BY s.s [, s.a] -- single- or multi-column criteria
```

MonetDB's BATs already provide **ordered row storage.**Some ORDER BY queries will thus be no-ops (recall tail properties sorted, revsorted).

Otherwise, use **order indexes**—either persistent or computed on the fly—to apply column re-ordering.

Recall: Order Indexes (ORDER BY s.s)



	a	S	oi	dx s	a	ord(s)	S ^{ord(}	s)	
head	tail	tail	head	tail	head	tail	tail		
0@0 1@0 2@0 3@0 4@0 5@0 6@0 7@0 8@0 9@0	a b c d e f g h i j	40 0 50 30 50 10 10 10 20	0@0 1@0 2@0 3@0 4@0 5@0 6@0 7@0 8@0 9@0	1@0 7@0 8@0 5@0 9@0 3@0 0@0 2@0 6@0 4@0	0@0 1@0 2@0 3@0 4@0 5@0 6@0 7@0 8@0 9@0	b h i f j d a c g e	0 10 10 10 20 30 40 50 50		

Order Indexes on the Fly: algebra.sort



```
EXPLAIN
 SELECT s.a, s.s
 FROM sorted AS s
 ORDER BY s.s;
sorted :bat[:oid] := sql.tid(sql, "sys", "sorted");
s0 :bat[:int] := sql.bind(sql, "sys", "sorted", "s", ...);
s :bat[:int] := algebra.projection(sorted, s0);
(Sord(s). oidxs. gidxs) desc_ fstable
                 := algebra.sort(s, false, false);
a0 :bat[:str] := sql.bind(sql, "sys", "sorted", "a", ...);
a :bat[:str] := algebra.projection(sorted, a0);
aord(s):bat[:str] := algebra.projectionpath(oidxs, sorted, a0);
io.print(aord(s), sord(s)):
```



If sorting is central to the query workload, create a persistent order index that is immediately applicable:

ALTER TABLE sorted SET READ ONLY;



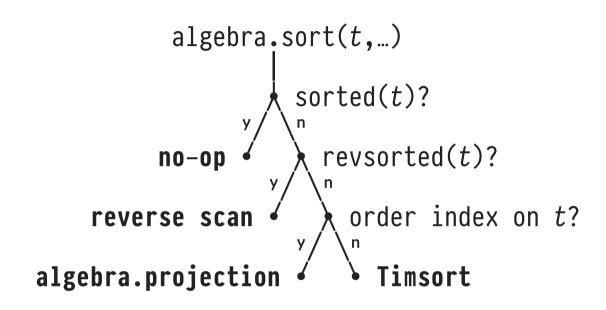
CREATE ORDERED INDEX oidx on sorted(s);

- Order indexes are **static** structures that are *not* dynamically maintained (as opposed to B+Trees). If order index has been created...
 - 1. on the fly: throw away on table update,
 - 2. persistent: read-only table, no updates at all.

Tactical Optimization for algebra.sort



ullet algebra.sort aims to avoid actual sorting effort based on properties of BAT t and the presence of order indexes:



• If all else fails, apply in-memory sort algorithm **Timsort** (1993; hybrid of merge/insertion sort, run-aware).



Multi-column ordering criteria require special treatment: algebra.sort(s) only receives single criterion s.

```
SELECT s.a, s.s
FROM sorted AS s
ORDER BY s.s, s.a -- s_1 < s_2 \Leftrightarrow s_1.s < s_2.s \lor
                                       (S_1.S = S_2.S \land S_1.a < S_2.a)
```

- Q Let algebra.sort(s) return three result BATs:
 - 1. sord(s) (the ordered input s) ✓
 - 2. oidx^s (order index) ✓
 - 3. gidx^s (groups rows that agree on criterion s).

Multi-Criteria ORDER BY: Group Index gidx



s ^{ord(s)} ✓ oidx ^s ✓ gidx ^s		<i>,</i>	S
head tail head tail head tail		head	tail
0@0 1 0 1 0 1 0 0 0 0 1 0 0 0 1 0	o	0@0 1@0 2@0 3@0 4@0 5@0 6@0 7@0 8@0 9@0	40 0 50 30 50 10 10 10 20

3 output BATs

input BAT

Multi-Criteria ORDER BY s,a: Refine ORDER BY s by a



