

# DB 2

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14 – Query Optimization

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## 1 : One Query — Millions of Plans

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**Q:** Given a SQL query  $Q$ , what is *the optimal* (a reasonable)<sup>1</sup> plan to evaluate it? — **A:** It depends:

- Can we **simplify** (flatten, unnest)  $Q$ ?
- How can we **access the tables** referenced in  $Q$ ?
- How do **CPU and (sequential, random) I/O cost** compare?
- What is the **selectivity of the predicates** used in  $Q$ ?
- Which plan **operator implementations** are applicable?
- Can we **regroup/reorder the joins** in  $Q$ ?

<sup>1</sup> Here: focus on reducing the overall query evaluation time. The optimum is, generally, not reached.

# Excerpt of the TPC-H Benchmark (at Scale Factor $SF$ )

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<u>o_orderkey</u>	o_custkey	o_totalprice	o_clerk	...
$0$	$c$			

orders ( $\approx SF \times 1.5 \times 10^6$  rows)

<u>l_orderkey</u>	<u>l_linenum</u>	l_partkey	l_quantity	l_extendedprice	...
$0$					

lineitem ( $\approx SF \times 6 \times 10^6$  rows)

<u>c_custkey</u>	c_name	c_acctbal	c_nationkey	...
$c$			$n$	

customer ( $\approx SF \times 150000$  rows)

<u>n_nationkey</u>	n_name	n_regionkey	...
$n$		$r$	

nation (25 rows)

<u>r_regionkey</u>	r_name	...
$r$		

region (5 rows)



## $Q_{14}$ : Three-Way Join Against a TPC-H Instance

Price and quantity of parts ordered by customer #001:

```

SELECT 1.1_partkey, 1.1_quantity, 1.1_extendedprice
FROM   lineitem AS l JOIN orders AS o      -- } l ⋈ o
      ON (l.1_orderkey = o.o_orderkey)    -- }
JOIN   customer AS c                      -- } ⋈ c
      ON (o.o_custkey = c.c_custkey)      -- }
WHERE  c.c_name = 'Customer#001';

```

- Above SQL syntax suggests the **join order**  $(l \bowtie o) \bowtie c$ .
- Commutativity and associativity of  $\bowtie$  enable the RDBMS to **reorder** the joins—based on *estimated evaluation costs*.
  - ... unless we insist on the syntactic order. 🧐



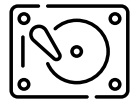


### 3 : Pre-Processing: Query Unnesting

**Nested SQL queries** suggest a (naïve, inefficient) nested-loop-style evaluation strategy. Consider:

<pre> SELECT c.c_name FROM   customer AS c,       ⚠ { (SELECT n.n_nationkey, n.n_name           { FROM   nation AS n) AS t WHERE  c.c_nationkey = t.n_nationkey       AND strpos(c.c_address, t.n_name) &gt; 0 </pre>	<pre> SELECT o.o_orderkey FROM   orders AS o WHERE  o.o_custkey IN       ⚠ { (SELECT c.c_custkey           { FROM   customer AS c             WHERE  c.c_name = '...') </pre>
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- 💡 If possible, **unnest** ⚠ queries and “inline” into parent query  $\Rightarrow$  ⚠ can participate in join reordering.



## Pre-Processing: Query Unnesting

Perform **query unnesting** on the level of

- the operator-based plan representation of the query,<sup>2</sup> or
- the internal AST representation of SQL. Re **2**:

<pre> SELECT  e<sub>1</sub> FROM    q<sub>1</sub>, ..., q<sub>i</sub> WHERE   p<sub>1</sub>       AND e<sub>2</sub> IN (SELECT e<sub>3</sub>                     FROM    q<sub>i+1</sub>, ..., q<sub>n</sub>                     WHERE   p<sub>3</sub>)         </pre>	$\cong$	<pre> SELECT  DISTINCT e<sub>1</sub> FROM    q<sub>1</sub>, ..., q<sub>i</sub>, q<sub>i+1</sub>, ..., q<sub>n</sub> WHERE   p<sub>1</sub>       AND e<sub>2</sub> = e<sub>3</sub>       AND p<sub>3</sub>         </pre>
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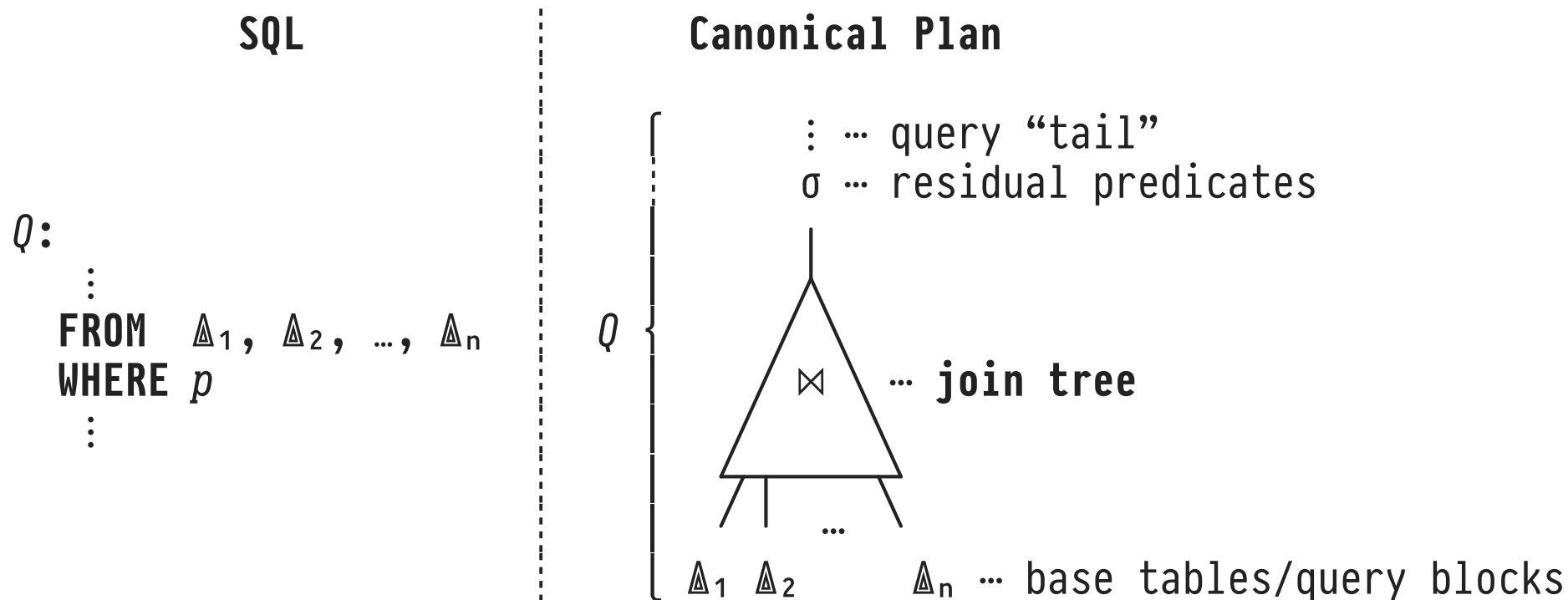
\* Precondition:  $e_1$  is key in the left-hand side query

<sup>2</sup> See *Unnesting Arbitrary Queries*, Thomas Neumann, Alfons Kemper. BTW 2015, Hamburg, Germany.



## 4 : Join Tree Optimization

Processing a SQL query  $Q$  starts out with its **FROM** and **WHERE** clauses which describe a **join tree** over  $Q$ 's inputs:

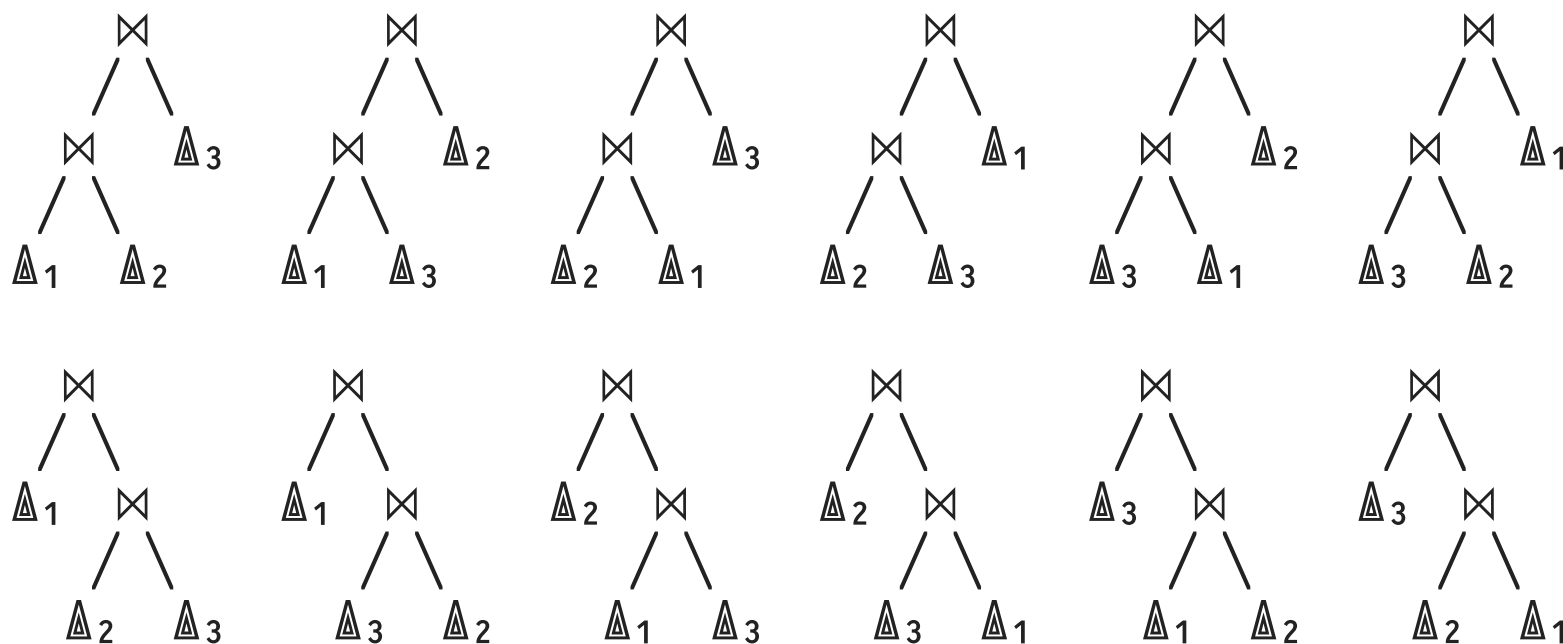






## Join Tree Optimization

Given  $n$  join inputs, the number of possible **join tree shapes** is *huge*. Consider  $n = 3$ :

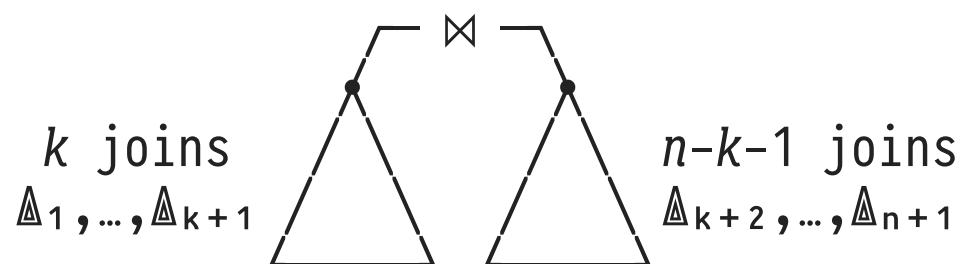


- Shapes based on associativity and commutativity of  $\Join$ .



## How Many Possible Join Trees Are There?

1. A join of  $n+1$  inputs  $\Delta$  requires  $n$  binary joins. The root  $\bowtie$  combines subtrees of  $k$  and  $n-k-1$  joins ( $0 \leq k \leq n-1$ ):<sup>3</sup>



# of join tree shapes:

$$C_n = \sum_{k=0}^{n-1} C_k \times C_{n-k-1}$$

2. Orderings of the  $\Delta$  at the join tree leaf level:  $(n+1)!$ .
3. Join algorithm choices ( $a$  available algorithms):  $a^n$ .

<sup>3</sup>  $C_n$  are the *Catalan numbers*, the number of ordered binary trees with  $n+1$  leaves.  $C_0 = 1$ .



## How Many Possible Join Trees Are There?

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Number of possible join trees given  $n$  binary joins with  $a = 3$  implementation choices:

# of $\Delta (n+1)$	$C_n$	# of join trees
2	1	6
3	2	108
4	5	3240
5	14	136080
6	42	7384320
7	132	484989120
8	429	37829151360
9	1430	3404623622400
10	4862	347271609484800

- A search space of this size is impossible to fully explore for any query optimizer.



## Join Plan Generation Through Dynamic Programming

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- **Problem:** Find optimal query plan  $opt[\{\Delta_1, \dots, \Delta_n\}]$  that joins  $n$  inputs  $\Delta_1, \dots, \Delta_n$ .
  1. **Iteration 1:** For each  $\Delta_j$ , find and memorize **best 1-input plan**  $opt[\{\Delta_j\}]$  that accesses  $\Delta_j$  only.
  2. **Iteration  $k > 1$ :** Find and memorize **best  $k$ -input plans** that join  $k \leq n$  inputs by combining (for  $1 \leq i < k$ )
    - the best  $i$ -input plans and  $\setminus$  simple lookups in
    - the best  $(k-i)$ -input plans.  $\int opt[\cdot]$  memo 👍



## Bottom-Up Dynamic Programming ( $n = 3$ )

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- $k$  Possible  $k$ -input Access/Join Plans** if  $\Delta_i$  is complex
- 1**  $opt[\{\Delta_1\}] \leftarrow \text{prune}(\{\text{Seq Scan } \Delta_1, \text{Index Scan } \Delta_1, \text{Bitmap Scan } \Delta_1, \overbrace{\Delta_1}^{\text{complex}}\})$   
 $opt[\{\Delta_2\}] \leftarrow \text{prune}(\{\text{Seq Scan } \Delta_2, \text{Index Scan } \Delta_2, \text{Bitmap Scan } \Delta_2, \Delta_2\})$   
 $opt[\{\Delta_3\}] \leftarrow \text{prune}(\{\text{Seq Scan } \Delta_3, \text{Index Scan } \Delta_3, \text{Bitmap Scan } \Delta_3, \Delta_3\})$
- 
- 2**  $opt[\{\Delta_1, \Delta_2\}] \leftarrow \text{prune}(opt[\{\Delta_1\}] \otimes opt[\{\Delta_2\}])$   
 $opt[\{\Delta_1, \Delta_3\}] \leftarrow \text{prune}(opt[\{\Delta_1\}] \otimes opt[\{\Delta_3\}])$   
 $opt[\{\Delta_2, \Delta_3\}] \leftarrow \text{prune}(opt[\{\Delta_2\}] \otimes opt[\{\Delta_3\}])$
- 
- 3**  $opt[\{\Delta_1, \Delta_2, \Delta_3\}] \leftarrow \text{prune}(opt[\{\Delta_1\}] \otimes opt[\{\Delta_2, \Delta_3\}] \cup$   
 $\quad opt[\{\Delta_2\}] \otimes opt[\{\Delta_1, \Delta_3\}] \cup$   
 $\quad opt[\{\Delta_3\}] \otimes opt[\{\Delta_1, \Delta_2\}] )$

$\text{prune}(P) \equiv \text{best (= minimal cost + interestingly ordered) plans in set } P$

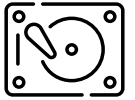
$$l \otimes r \equiv \{l \bowtie^{n1} r, r \bowtie^{n1} l, l \bowtie^{mj} r, r \bowtie^{mj} l, l \bowtie^{hj} r, r \bowtie^{hj} l\}$$



## Join Plan Generation (Notes)

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- **Access plan choices** (*access*(·)):
  - Consider sequential/index scans if  $\Delta$  is a base table, otherwise simply consume  $\Delta$ 's rows.
- **Join plan choices** ( $\_ \otimes \_$ ):
  - Considers all viable join algorithms (given  $\theta$ , available indexes, ...) and left/right input orders.
- **Principle of Optimality** (*prune*(·)): A globally optimal plan is built from optimal subplans. Thus:
  - 💡 For each subset of  $\{\Delta_1, \dots, \Delta_n\}$ , memorize in *opt*[·]
    1. ... its overall best plan and
    2. ... its best plan satisfying each **interesting order**.



## (Bushy) Join Plan Generation: Pseudo Code

```

JoinPlan( $\{\Delta_1, \dots, \Delta_n\}$ ):
  foreach  $p \in \{\Delta_1, \dots, \Delta_n\}$  } 1-input plans
  |  $opt[\{p\}] \leftarrow prune(access(p))$ ;

  for  $k$  in  $2, \dots, n$  }  $k$ -input plans
  |   foreach  $S \subseteq \{\Delta_1, \dots, \Delta_n\}$  with  $|S| = k$  } enumerate subsets
  |   |    $opt[S] \leftarrow \phi$ ;
  |   |   foreach  $T \subset S$  with  $T \neq \phi$   $\Join^a \setminus$ 
  |   |   |    $opt[S] \leftarrow opt[S] \cup \{ opt[T] \Join^a opt[S \setminus T] \}$ ;
  |   |   |    $opt[S] \leftarrow prune(opt[S])$ ;

  return  $opt[\{\Delta_1, \dots, \Delta_n\}]$ ;

```

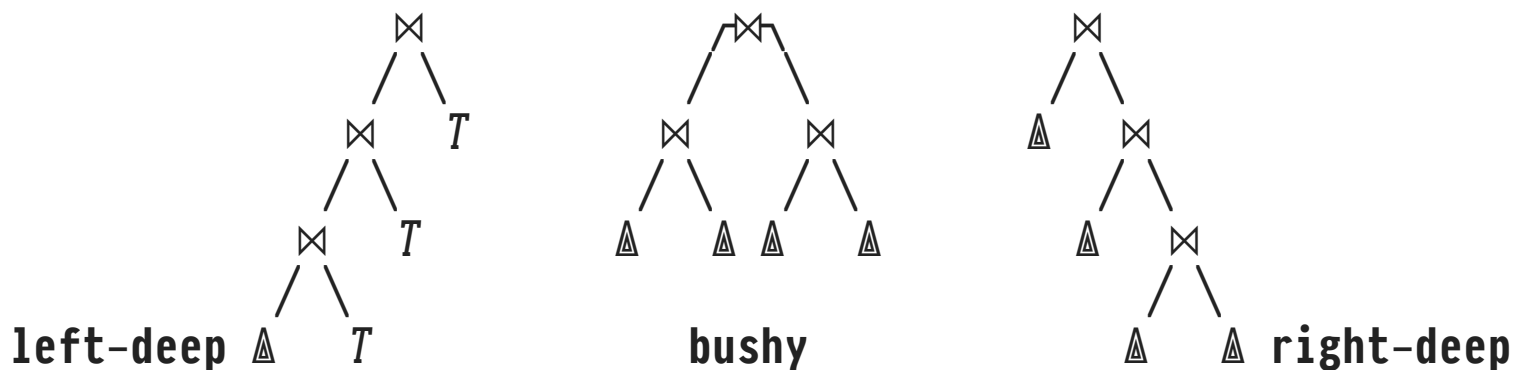
- $access(\cdot)$ ,  $prune(\cdot)$  defined as above,  
 $\Join^a \setminus$  builds all join algorithm choices ( $a \in \{nl, mj, hj\}$ ).



## Reducing the Search Space

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- Avoid generating costly **Cartesian products**: don't form joins between inputs w/o join predicate (`_  $\theta$  _ = true`).
- Generate **left-deep** join plans only: right join input (NL $\bowtie$ : inner input) is a scan over base table  $T$ .
  - Admits use of Index Nested Loop Join.
  - Straightforward Volcano-style execution (reset inner).







## 5 : Estimating Plan Cost

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The query optimizer explores the vast plan search space to find the **optimal** (“best”, “cheapest”) plan.

- Typically, RDBMSs measure **plan cost** in terms of *total execution time* (time until last result row delivered).
- These total plan costs are **estimated** *before* plan execution begins (`EXPLAIN: ... cost=c1..c2← ...`).
- A **cost model**—measured in abstract “space\$”—reflects the true costs (measured in *ms*, CPU time, # I/O ops, ...) of plans  $p_1$ ,  $p_2$ :

$$\text{space}\$(p_1) < \text{space}\$(p_2) \Rightarrow \text{true cost}(p_1) < \text{true cost}(p_2)$$



## PostgreSQL: Plan Cost

**EXPLAIN** shows estimated costs (unit: space\$) and cardinalities (# of rows):

QUERY PLAN		
	startup cost ?	total cost ?
Hash Join	(cost=299.00..15443.31	rows=505183 width=50)
⋮		?
		cardinality

- **run cost**  $\stackrel{\text{def}}{=} \text{total cost} - \text{startup cost}$ <sup>4</sup> (not shown).
- Optimizer decisions are based on estimated **total cost**.

<sup>4</sup> To implement `set enable_<op> = off`, PostgreSQL sets the operator's **startup cost** to  $10^{10}$  ( $\equiv \infty$ ).



## Cost Model Configuration

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Model Configuration	Default	Description
<code>seq_page_cost</code>	1.0	I/O cost of one sequential page access
<code>random_page_cost</code>	4.0	I/O cost of one random page access
<code>cpu_tuple_cost</code>	0.01	CPU cost to process a heap file row
<code>cpu_index_tuple_cost</code>	0.005	CPU cost to process an index leaf entry
<code>cpu_operator_cost</code>	0.0025	CPU function/operator evaluation cost
<code>parallel_tuple_cost</code>	0.1	Cost of passing one row worker→leader
<code>parallel_setup_cost</code>	1000.0	Cost of spawning a parallel worker

- Parameters are configurable:
  - Seek cost, thus `random_page_cost` » `seq_page_cost`. But...
  - ... if DB fits in RAM, `random_page_cost` = `seq_page_cost` may be more appropriate.



## Cost of Seq Scan 1

Given an occurrence of **Seq Scan** with arguments

- *in*: input table,
- *pred*: (optional) filter predicate on *in*,
- *expr*: **SELECT** clause expression(s),

how does PostgreSQL derive *startup\_cost* and *total\_cost*?

<i>in</i>	QUERY PLAN	<i>total_cost</i>
<i>?</i>	<i>?</i>	<i>?</i>
Seq Scan on public.indexed i	(cost=0.00..22.75 rows=100 width=4)	
Output: (a + 1)	<i>expr</i>	<i>?</i>
Filter: (i.a <= 100)	<i>pred</i>	<i>startup_cost</i>
		<i>#rows(out)</i>



## Cost of Seq Scan 2

Cost calculation depends on the following parameters, mostly available in PostgreSQL's internal `pg_*` meta data tables:

Parameter	Description	Available as...
<code>#rows(<i>in</i>)</code>	# rows (cardinality) of table <i>in</i>	<code>pg_class.reltuples</code>
<code>#pages(<i>in</i>)</code>	# pages in heap file of <i>in</i>	<code>pg_class.relpages</code>
<code>sel(<i>pred</i>)</code>	selectivity of filter <i>pred</i> <sup>5</sup>	see below

- Meta data like `#rows(in)`, `#pages(in)` and others are updated whenever the system performs an `ANALYZE` run on table *in*.
- Predicate selectivity `sel(pred)` is estimated based on sampled table data and the syntactic structure of *pred*.

<sup>5</sup> `sel(pred)`  $\in \{0, \dots, 1\}$  with `sel(pred) = 0`  $\equiv$  no row satisfies filter *pred*.



## Cost of Seq Scan 3

$\nwarrow$  typically = 0  $\nearrow$   
**startup\_cost**  $\stackrel{\text{def}}{=}$   $\text{startup\_cost}(\text{pred}) + \text{startup\_cost}(\text{expr})$

$\text{cpu\_run\_cost} \stackrel{\text{def}}{=} \underbrace{\#rows(in) \times (\text{cpu\_tuple\_cost} + \text{run\_cost}(\text{pred}))}_{\text{decode heap row}} + \underbrace{\#rows(in) \times \text{sel}(\text{pred}) \times \text{run\_cost}(\text{expr})}_{\text{evaluate filter}}$   
 $\quad \quad \quad = \#rows(out) \quad \quad \quad \text{evaluate SELECT clause}$

$\text{disk\_run\_cost} \stackrel{\text{def}}{=} \underbrace{\#pages(in) \times \text{seq\_page\_cost}}_{\text{sequentially read entire input heap file}}$

**total\_cost**  $\stackrel{\text{def}}{=} \text{startup\_cost} + \underbrace{\text{cpu\_run\_cost} + \text{disk\_run\_cost}}_{= \text{run\_cost}}$



## Cost of Index Scan 1

Modeling the cost for an **Index Scan** has to reflect that *two* data structures (heap file & B+Tree) are involved:

<i>idx</i>	<i>in</i>	QUERY PLAN
<i>idx</i>	<i>in</i>	Index Scan using indexed_a on indexed i (cost=0.42..443.12 rows=10885 ... Output: (c + '1'::numeric) <i>expr</i> Index Cond: (i.a <= 10000) <i>pred</i> #rows( <i>out</i> )

The model separately accounts for

1. the B+Tree descent (startup of the **Index Scan**),
2. the index leaf level scan, and
3. heap file access (clustered vs. non-clustered).



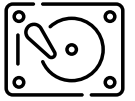
## Cost of Index Scan

Cost model parameters:

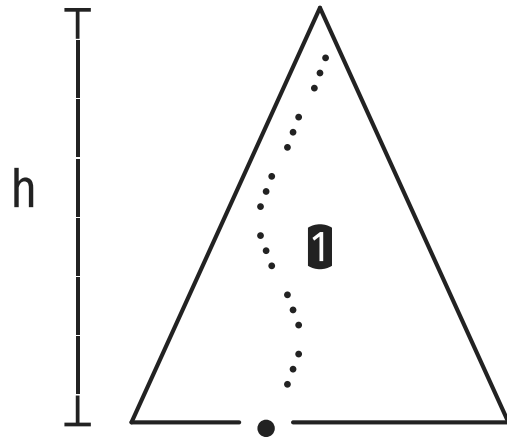
Parameter	Description	Available as...
<code>#rows(<i>in</i>)</code>	# rows (cardinality) of table <i>in</i>	<code>pg_class.reltuples</code>
<code>#pages(<i>in</i>)</code>	# pages in heap file of <i>in</i>	<code>pg_class.relpages</code>
<code>sel(<i>pred</i>)</code>	selectivity of filter <i>pred</i>	see below
<code>h(<i>idx</i>)</code>	height of B+Tree <i>idx</i>	<code>bt_metap(.)</code>
<code>#rows(<i>idx</i>)</code>	# leaf entries in index <i>idx</i>	<code>pg_class.reltuples</code>
<code>#pages(<i>idx</i>)</code>	# pages in leaf level of <i>idx</i>	<code>pg_class.relpages</code>
<code>corr(<i>idx</i>)</code>	$\approx$ clustering factor for index <i>idx</i>	<code>pg_stats.correlation</code>

- `corr(idx)`  $\in \{-1.0, \dots, 1.0\}$  characterizes how much the physical orderings of index leaves and heap file deviate.
  - After `CLUSTER in ON idx`, we have `corr(idx) = 1.0`.





## Cost of Index Scan **E** (B+Tree Descent)



- B+Tree height  $h = \log_{2 \times o}(\#rows(idx))$

⇒ # of key comparisons during B+Tree descent **1**:

$$\underbrace{[\log_2(2 \times o) \times h]}_{\text{binary search in inner B+Tree node with fan-out } F = 2 \times o} = [\log_2(\#rows(idx))]$$

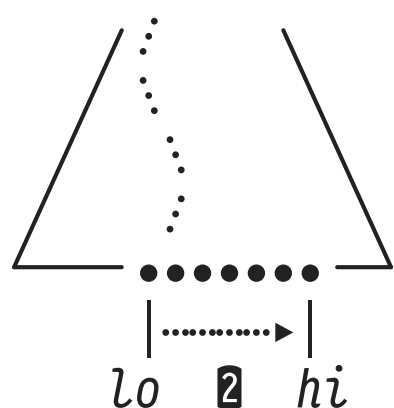
binary search in inner B+Tree  
node with fan-out  $F = 2 \times o$

$$\begin{aligned} \text{startup\_cost} &\stackrel{\text{def}}{=} \text{startup\_cost}(pred) + \text{startup\_cost}(expr) \\ &+ \underbrace{([\log_2(\#rows(idx))])}_{\text{B+Tree descent}} + \underbrace{(h + 1)}_{\text{index node processing}} \times \underbrace{50}_{\text{index node processing}} \times \text{cpu\_operator\_cost} \end{aligned}$$



## Cost of Index Scan ④ (Leaf Level Scan)

The index leaf level (sequence set) scan ② incurs CPU as well as I/O cost that contribute to the overall **run\_cost**:



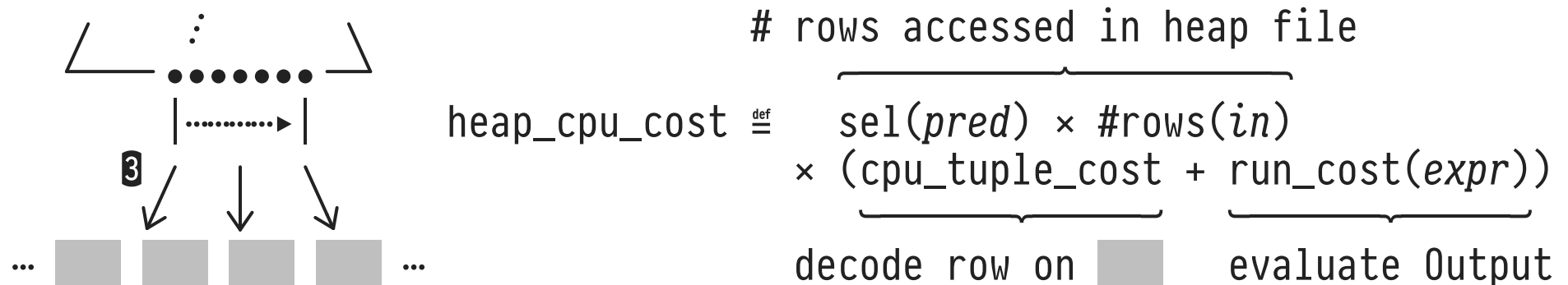
$$\text{index\_cpu\_cost} \stackrel{\text{def}}{=} \underbrace{\text{sel}(\text{pred}) \times \text{\#rows}(\text{idx})}_{\text{\# rows in scanned range } |\text{.....}\rangle|} \times \underbrace{(\text{cpu\_index\_tuple\_cost})}_{\text{decode index leaf entry}} + \underbrace{\text{run\_cost}(\text{pred})}_{\text{evaluate } \leq hi}$$

$$\text{index\_IO\_cost} \stackrel{\text{def}}{=} \underbrace{[\text{sel}(\text{pred}) \times \text{\#pages}(\text{idx})]}_{\text{\# of pages } \bullet \text{ in scanned range}} \times \underbrace{\text{random\_page\_cost}}_{\text{B+Tree leaves not clustered}}$$



## Cost of Index Scan 5 (Heap File Access)

Heap file accesses ③ incur additional CPU and I/O costs (no I/O cost if we perform an **Index Only Scan**):



- The more **clustered** the index, the cheaper the heap I/O. Linearly interpolate between the clustered and non-clustered scenarios:

$$\text{heap\_IO\_cost} \stackrel{\text{def}}{=} \text{unclustered\_IO\_cost} + \text{corr}(\text{idx})^2 \times (\text{clustered\_IO\_cost} - \text{unclustered\_IO\_cost})$$

$\text{corr}(\text{idx}) \approx \text{clustering factor} \in \{0, \dots, 1\}$

# Cost of Index Scan ([Non-]Clustered Heap File Access)



$$\text{clustered\_IO\_cost} \stackrel{\text{def}}{=} 1 \times \text{random\_page\_cost} (\blacksquare) + (\text{sel}(\text{pred}) \times \text{\#pages}(\text{in}) - 1) \times \text{seq\_page\_cost} (\blacksquare)$$

$$\text{unclustered\_IO\_cost} \stackrel{\text{def}}{=} \text{\#pages}(\text{in}) \times \text{random\_page\_cost} (\blacksquare)$$

$$\text{total\_cost} \stackrel{\text{def}}{=} \text{startup\_cost} + \text{index\_cpu\_cost} + \text{index\_IO\_cost} + \text{heap\_cpu\_cost} + \text{heap\_IO\_cost}$$



## Index Correlation (Clustering Factor)

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Given ordered index  $idx$  over column  $A$  with values  $a_1 \leq a_2 \leq \dots \leq a_n$ , where  $pos(a_i) \in \{1, \dots, n\}$  gives the position of  $a_i$  in the heap file for  $A$ .<sup>6</sup>

- **Index Correlation**  $corr(idx) \in \{-1, \dots, 1\}$  measures how far  $[pos(a_1), \dots, pos(a_n)]$  deviates from  $[1, \dots, n]$ , i.e.,  $idx$ 's clustering degree:

$$corr(idx) = \frac{n \times (\sum_{i=1 \dots n} i \times pos(a_i)) - (\sum_{i=1 \dots n} i)^2}{n \times (\sum_{i=1 \dots n} i \times i) - (\sum_{i=1 \dots n} i)^2}$$

<sup>6</sup> After `CLUSTER <table> USING idx`, we have  $pos(a_i) = i$  and thus  $corr(idx) = 1$ .