

Prof. Torsten Grust, Björn Bamberg WSI – Database Systems Research Group



Assignment 6

Hand in this assignment until Tuesday, July 01, 12pm at the latest.

Running out of ideas?

Are you hitting a roadblock? Are some of the exercises unclear? Do you just need that one hint to get the ball rolling? Refer to the #forum channel on our Discord server—maybe you'll find just the help you need.

Exam-style Exercises

Exercises marked with © are similar in style to those you will find in the exam. You can use these to hone your expectations and gauge your skills.

Task 1: Fold

Formulate the following functions without using explicit recursion. Instead, make use of the prelude function

foldr ::
$$(a \rightarrow b \rightarrow b) \rightarrow b \rightarrow [a] \rightarrow b^1$$

Applying the function (foldr f z xs), we can fold a list (xs :: [a]) using a binary operator $f :: (a \rightarrow b \rightarrow b)$. foldr starts with initial value z and then proceeds to apply f while walking xs right to left:

```
foldr f z [x1, x2, ..., xn] ≡ x1 `f` (x2 `f` ... (xn `f` z)...)
```

Take for example a function sum' which sums all elements of a list. It can be written using foldr:

```
sum' :: [Integer] -> Integer
sum' xs = foldr (+) 0 xs
```

Applied to a list [4,2,6] the sum is evaluated as follows:

```
|\text{sum'}[4,2,6] \equiv \text{foldr}(+) \mid 0 \mid [4,2,6] \mid = 4 + (2 + (6 + 0)) \mid = 12
```

Note

Obviously you must not use specialized prelude or module functions (e.g. length, intercalate, etc.) to solve the following problems.

- (a) length':: [a] -> Integer to determine the size of a list. Hint: You can use let or where to locally define the operator to fold with.
- B reverse :: [a] -> [a] to reverse a list.
- © © commaSep :: [String] -> String to concatenate a list of strings, separated by commas (',').

Example: commaSep ["Hello", "World"] = "Hello, World"

Rewrite the following function, using foldr instead of explicit recursion. The function removes duplicate elements from a sorted list:

```
removeDups :: [Integer] -> [Integer]
removeDups [] = []
removeDups [x] = [x]
removeDups (x:y:ys) | x == y = removeDups (y:ys)
therefore is a content of the content of
```

 $^{^{1}}$ Actually, the prelude function foldr has a more general type. However, applied to lists its type can be specialized to this concrete version.

Task 2: Implementation of Typeclasses

The Haskell compiler translates any program containing type class and instance declarations into an equivalent program that does not. Figure b shows the translation of the declarations in Figure a. Here is how it works²:

• A new data type is defined for each type class declaration. This data type is the so called "method dictionary" for that class. Each field corresponds to a method of the type class. Additionally, functions to access the fields of the dictionary are defined.

Example: For class Eq the new data type EqD is defined. Values of this type can be created using the constructor EqDict, which has one entry for method (==). Accessor function eq uses pattern matching to extract the field for method (==).

• Each instance of a type class is translated into a declaration of a value of the method dictionary.

Example: For instance Eq Int, dictionary eqDInt :: EqD Int is defined.

• Finally, functions with type class constraints like (Eq a, Ord b, ...) => ... are transformed into functions without. Each constraint turns into an additional parameter: EqD a -> OrdD b -> All invocations of methods are replaced by invocations of the corresponding entry in the method dictionary.

Example: The type signature of member changes to member :: EqD $a \rightarrow [a] \rightarrow a \rightarrow Bool$. Invocations of linebreak x == y are replaced by the corresponding expression eq eqD x y, where eqD is an appropriate dictionary for type a.

Let us look at an example. Lines 3-7 of (a) define a simplified version of type class Eq and an instance of Eq for type Int. Further, function member is defined which traverses a given list [a] and checks whether the list contains a specific element. The type signature of member is read "member has type [a] -> a -> Bool, for every type a such that a is an instance of class Eq." Without the constraint Eq a, we would not be allowed to compare x and y in line 11.

```
1 import GHC.Int (eqInt)
2
3
  class Eq a where
     (==) :: a -> a -> Bool
4
5
  instance Eq Int where
6
7
     (==) = eqInt
8
9 member :: Eq a => [a] -> a -> Bool
                  = False
10 member [] y
11 member (x:xs) y = x == y
                  || member xs y
```

```
(a) Simplified version of type class Eq.
```

```
import GHC.Int (eqInt)
2
  data EqD a = EqDict (a -> a -> Bool)
3
  eq (EqDict e) = e
4
5
6 eqDInt :: EqD Int
   eqDInt = EqDict eqInt
8
9
  member :: EqD a -> [a] -> a -> Bool
10 member eqDa [] y
                       = False
member eqDa (x:xs) y = eq eqDa x y
                       || member eqDa xs y
```

(b) Equivalent program without type class and instance declarations.

File typeclass.hs contains type class declarations, instances, and function definitions. Translate the program to an equivalent one without type classes by following the method described above.

- A Define dictionaries and accessor functions for classes Comparable and Printable.
- B Translate instances Comparable Integer, Printable Weekday, and Comparable Weekday into values of the corresponding dictionary.
- C Translate functions table, and qsort.

²The type class approach to ad-hoc polymorphism has been proposed by Philip Wadler and Stephen Blott: https://db.cs.uni-tuebingen.de/teaching/ss23/FP/wadler-typeclasses.pdf **⊕**