Design Report concurrency multithreading

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1 Introduction

This paper describes a naive solution for a multi-threaded program which takes a graph structure and accepted states as input and detects whether any accepting cycles can be found in said graph. This kind of task is needed for LTL-model-checking, where we can create a state graph by converting the memory snapshot of any arbitrary program and feed it into our code. If we can detect a cycle within this graph which contains an accepting state, we can safely claim that the program corresponding to the memory snapshot will terminate. Our multi-threaded software achieves this by implementing an algorithm described in a paper by laarman et al. [1]. We will present a naive approach and an improved version, as well as showing better performance of the second version.

2 Previous work

At the start of the course, we were provided with a base program written by *Pieter Hijma*. It contained examples on how to implement multiple threads in a java program and a single core Implementation of laarman's algorithm [1]. We also implemented the algorithms described in this paper in our program. The single core implementation is the following:

```
proc \operatorname{nndfs}(s_I)
                                     11 proc dfs blue(s)
     dfs blue (s_I)
                                          s.color := cyan
                                     12
     report no cycle
                                          for all t in post(s) do
                                     13
                                            if t.color=white
4 proc dfs red(s)
                                               dfs blue(t)
                                     15
     for all t in post(s) do
                                          if s \in A
                                     16
       if t.color=cvan
6
                                     17
                                            dfs red(s)
         report cycle & exit
                                            s.color := red
                                     18
       else if t.color=blue
                                          else
                                     19
         t.color := red
9
                                            s.color := blue
                                     20
         dfs_red(t)
10
```

Figure 1: single core algorithm; Source: [1]

As you can see, there are two procedures: dfsBlue and dfsRed. DfsBlue traverses the graph recursively and looks for accepting states; if such a state is found, it starts the DfsRed, which checks for cycles by seeing if a node was already colored cyan, meaning that the blue procedure has been here recently. If such a node is found, it exits and terminates, else it marks the node red so it gets ignored in the future. After the blue procedure is done, it also marks the field which was cyan as blue, which makes it possible to mark it red.

Our task was to implement a multi-threaded version of this algorithm, by expanding on the already given program which we just explained. The procedure for the multi-threaded program works like this:

```
proc mc-ndfs(s, N)
                                      13 proc dfs red(s, i)
     dfs blue(s,1)||..||dfs blue(s,N) 14
                                           s.pink[i] := true
     report no cycle
                                           for all t in post i(s) do
                                      15
                                              if t.color[i]=cyan
                                      16
  proc dfs blue (s, i)
                                                report cycle & exit all
                                      17
     s.color[i] := cyan
                                              if \neg t.pink[i] \land \neg t.red
                                      18
     for all t in post_{i}^{b}(s) do
6
                                                dfs red(t, i)
                                      19
       if t.color[i]=white \land \neg t.red
                                           if s \in A
         dfs blue (t, i)
                                             s.count := s.count - 1
                                      21
     if s \in A
9
                                              await s.count=0
       s.count := s.count + 1
10
                                           s.red := true
       dfs red(s, i)
11
                                           s.pink[i] := false
     s.color[i] := blue
```

Figure 2: multi core algorithm; Source: [1]

The main changes in this algorithm compared to the last is that each blue procedure is started for each thread, and that each thread works on its own copy of the graph. The only shared data is the information of which states are having the color red, and a counter variable which expresses how many threads are active on one accepting node. This is necessary because we have to wait until all threads have moved on from a node before coloring it red. Red nodes still imply that they can be ignored, which is why they are shared between threads: the area to search gets incrementally smaller. Furthermore, a new local color pink is introduced: pink nodes won't be explored by dfsRed again (since they are already on red's stack).

3 Design and implementation

3.1 Naive approach

The framework already provided us with a class for the different colors for the nodes. It consists of a map with the state of the node as key and an enumeration for the colors (e.g. RED) as value, and methods to access and modify the map. The colors class is created in each thread locally and acts as a copy of the state graph. We decided to implement the color pink within this class. However, we define a new, separate map for the pink values: the reason for this is that nodes in the algorithm by Laarman could theoretically be both cyan and pink at the same time: A different boolean field is used for the color pink, instead of assigning the value pink to the variable color. Furthermore, we created two additional maps which get passed to the single threads: a map assigning a boolean value to states called red states and a map containing the counter variables for said states. The critical section of our program is comprised of these two maps, which is why we used Java's ConcurrentHashmap for these two data structures. Furthermore, the counter map contains AtomicInteger values for additional security and to guarantee all operations on the counter are atomic. It should be noted that this duplicate use of thread-safe data structures has been done for additional security. It isn't fast, but this is a naive approach, which should be improved further.

3.2 Improved version

4 Performance comparison

4.1 Naive approach

The naive approach with two threads takes a total time of 2ms on the DAS4-cluster for *accept-cycle.prom*. For comparison, the sequential solution takes 1 ms to detect a cycle for the same input. If we decide to run the naive approach with 10 threads, it takes 11ms. It becomes apparent that this solution comes with significant performance overhead.

4.2 Improved version

5 Conclusion

References

[1] Alfons Laarman, Rom Langerak, Jaco van de Pol, Michael Weber, and Anton Wijs. Multi-core nested depth-first search. In Tevfik Bultan and Pao-Ann Hsiung, editors, *Automated Technology for Verification and Analysis*, pages 321–335, Berlin, Heidelberg, 2011. Springer Berlin Heidelberg.