

Foundations of Probability and Statistics: Project Report

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17 agosto 2019

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Descriptive analysis on Y

```
data<- data1 <- read.csv("../data/Laptop2.csv")
str(data)
```

```
## 'data.frame':    1303 obs. of  22 variables:
## $ X              : int  1 2 3 4 5 6 7 8 9 10 ...
## $ Company        : Factor w/ 19 levels "Acer","Apple",...: 2 2 8 2 2 1 2 2 3 1 ...
## $ Product        : Factor w/ 618 levels "110-15ACL (A6-7310/4GB/500GB/W10)",...: 302 300 51 302 302 59 302 300 6
## $ TypeName       : Factor w/ 6 levels "2 in 1 Convertible",...: 5 5 4 5 5 4 5 5 5 5 ...
## $ Inches         : num  13.3 13.3 15.6 15.4 13.3 15.6 15.4 13.3 14 14 ...
## $ ScreenResolution : Factor w/ 40 levels "1366x768","1440x900",...: 24 2 9 26 24 1 26 2 9 16 ...
## $ Cpu            : Factor w/ 118 levels "AMD A10-Series 9600P 2.4GHz",...: 55 53 64 75 57 15 74 53 96 73 ...
## $ Ram            : int   8 8 8 16 8 4 16 8 16 8 ...
## $ Memory         : Factor w/ 38 levels "1024GB HDD","1024GB HDD + 1024GB HDD",...: 8 6 17 29 17 26 16 16 29 17
## $ Gpu            : Factor w/ 110 levels "AMD FirePro W4190M",...: 59 52 54 10 60 18 61 52 98 62 ...
## $ OpSys          : Factor w/ 9 levels "Android","Chrome OS",...: 5 5 6 5 5 7 4 5 7 7 ...
## $ Weight         : num   1.37 1.34 1.86 1.83 1.37 2.1 2.04 1.34 1.3 1.6 ...
## $ Price          : num   1340 899 575 2537 1804 ...
## $ Frequenza      : num    2.3 1.8 2.5 2.7 3.1 3 2.2 1.8 1.8 1.6 ...
## $ Risoluzione    : Factor w/ 15 levels "1366x768","1440x900",...: 11 2 4 13 11 1 13 2 4 4 ...
## $ Pixel          : int  4096000 1296000 2073600 5184000 4096000 1049088 5184000 1296000 2073600 2073600 ...
## $ GpuCompany     : Factor w/ 4 levels "AMD","ARM","Intel",...: 3 3 3 1 3 1 3 3 4 3 ...
## $ MemoriaSSD     : int   128 0 256 512 256 0 0 0 512 256 ...
## $ SolidStateDisk : Factor w/ 2 levels "False","True": 2 1 2 2 2 1 1 1 2 2 ...
## $ TotalMemory    : int   128 128 256 512 256 500 256 256 512 256 ...
## $ dedicated_GPU  : Factor w/ 2 levels "False","True": 1 1 1 2 1 2 1 1 2 1 ...
## $ Aggregated_Company: Factor w/ 10 levels "Acer","Apple",...: 2 2 5 2 2 1 2 2 3 1 ...
```

```
head(data,3)
```

```
##   X Company      Product  TypeName Inches
## 1 1   Apple MacBook Pro Ultrabook  13.3
## 2 2   Apple Macbook Air Ultrabook   13.3
```

```

## 3 3      HP      250 G6  Notebook  15.6
##          ScreenResolution          Cpu Ram
## 1 IPS Panel Retina Display 2560x1600      Intel Core i5 2.3GHz  8
## 2          1440x900      Intel Core i5 1.8GHz  8
## 3          Full HD 1920x1080 Intel Core i5 7200U 2.5GHz  8
##          Memory          Gpu OpSys Weight  Price
## 1          128GB SSD Intel Iris Plus Graphics 640 macOS  1.37 1339.69
## 2 128GB Flash Storage      Intel HD Graphics 6000 macOS  1.34 898.94
## 3          256GB SSD      Intel HD Graphics 620 No OS  1.86 575.00
## Frequenza Risoluzione Pixel GpuCompany MemoriaSSD SolidStateDisk
## 1          2.3 2560x1600 4096000      Intel      128      True
## 2          1.8 1440x900 1296000      Intel      0      False
## 3          2.5 1920x1080 2073600      Intel      256      True
## TotalMemory dedicated_GPU Aggregated_Company
## 1          128      False      Apple
## 2          128      False      Apple
## 3          256      False      HP

```

summary(data)

```

##          X          Company          Product
## Min. : 1.0 Dell :297 XPS 13 : 30
## 1st Qu.: 331.5 Lenovo :297 Inspiron 3567 : 29
## Median : 659.0 HP :274 250 G6 : 21
## Mean : 660.2 Asus :158 Legion Y520-15IKBN: 19
## 3rd Qu.: 990.5 Acer :103 Vostro 3568 : 19
## Max. :1320.0 MSI : 54 Inspiron 5570 : 18
##          (Other):120 (Other) :1167
##          TypeName          Inches
## 2 in 1 Convertible:121 Min. :10.10
## Gaming :205 1st Qu.:14.00
## Netbook : 25 Median :15.60
## Notebook :727 Mean :15.02
## Ultrabook :196 3rd Qu.:15.60
## Workstation : 29 Max. :18.40
##
##          ScreenResolution
## Full HD 1920x1080 :507
## 1366x768 :281
## IPS Panel Full HD 1920x1080 :230
## IPS Panel Full HD / Touchscreen 1920x1080: 53
## Full HD / Touchscreen 1920x1080 : 47
## 1600x900 : 23
## (Other) :162
##          Cpu          Ram
## Intel Core i5 7200U 2.5GHz :190 Min. : 2.000
## Intel Core i7 7700HQ 2.8GHz:146 1st Qu.: 4.000
## Intel Core i7 7500U 2.7GHz :134 Median : 8.000
## Intel Core i7 8550U 1.8GHz : 73 Mean : 8.382
## Intel Core i5 8250U 1.6GHz : 72 3rd Qu.: 8.000
## Intel Core i5 6200U 2.3GHz : 68 Max. :64.000
## (Other) :620
##          Memory          Gpu
## 256GB SSD :412 Intel HD Graphics 620 :281
## 1024GB HDD :224 Intel HD Graphics 520 :185
## 500GB HDD :132 Intel UHD Graphics 620 : 68
## 512GB SSD :118 Nvidia GeForce GTX 1050: 66
## 128GB SSD + 1024GB HDD: 94 Nvidia GeForce GTX 1060: 48
## 128GB SSD : 76 Nvidia GeForce 940MX : 43
## (Other) :247 (Other) :612
##          OpSys          Weight          Price          Frequenza
## Windows 10:1072 Min. :0.690 Min. : 174 Min. :0.900

```

```
## No OS      : 66  1st Qu.:1.500  1st Qu.: 599  1st Qu.:2.000
## Linux      : 62  Median :2.040  Median : 977  Median :2.500
## Windows 7  : 45  Mean    :2.039  Mean    :1124  Mean    :2.299
## Chrome OS  : 27  3rd Qu.:2.300  3rd Qu.:1488  3rd Qu.:2.700
## macOS      : 13  Max.    :4.700  Max.    :6099  Max.    :3.600
## (Other)    : 18
##   Risoluzione      Pixel      GpuCompany  MemoriaSSD
## 1920x1080:841  Min.    :1049088  AMD    :180  Min.    : 0.0
## 1366x768 :308  1st Qu.:1440000  ARM    : 1  1st Qu.: 0.0
## 3840x2160: 43  Median :2073600  Intel  :722  Median :128.0
## 3200x1800: 27  Mean    :2168807  Nvidia:400  Mean    :170.5
## 1600x900 : 23  3rd Qu.:2073600              3rd Qu.:256.0
## 2560x1440: 23  Max.    :8294400              Max.    :512.0
## (Other) : 38
## SolidStateDisk TotalMemory dedicated_GPU Aggregated_Company
## False:476      Min.    : 8.0  False:723  Dell    :297
## True :827      1st Qu.: 256.0  True :580  Lenovo  :297
##              Median : 500.0              HP      :274
##              Mean    : 620.1              Asus   :158
##              3rd Qu.:1024.0              Acer   :103
##              Max.    :2560.0              MSI    : 54
##              (Other):120
```

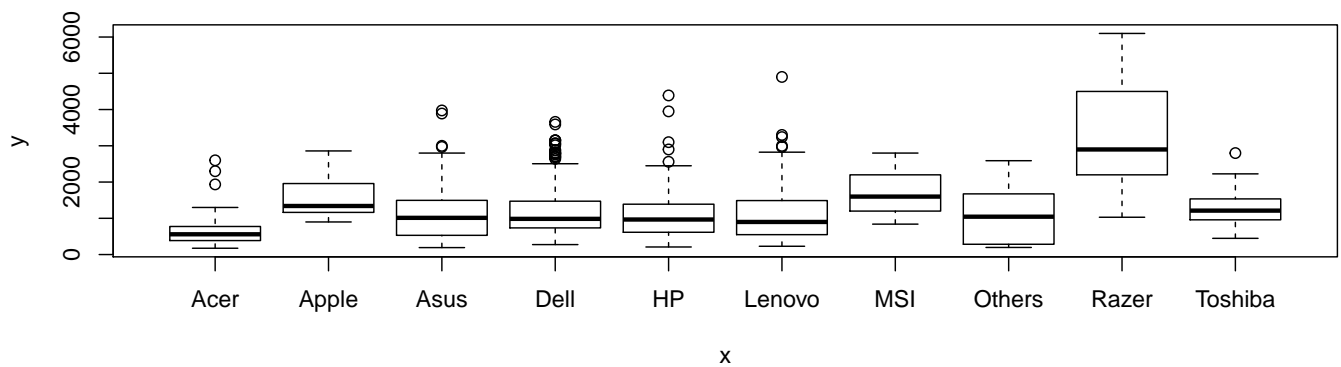
```
nums <- sapply(data, is.numeric)
var_numeric <- data[,nums]
head(var_numeric)
```

```
## X Inches Ram Weight Price Frequenza Pixel MemoriaSSD TotalMemory
## 1 1 13.3 8 1.37 1339.69 2.3 4096000 128 128
## 2 2 13.3 8 1.34 898.94 1.8 1296000 0 128
## 3 3 15.6 8 1.86 575.00 2.5 2073600 256 256
## 4 4 15.4 16 1.83 2537.45 2.7 5184000 512 512
## 5 5 13.3 8 1.37 1803.60 3.1 4096000 256 256
## 6 6 15.6 4 2.10 400.00 3.0 1049088 0 500
```

```
sapply(data, function(x)(sum(is.na(x)))) # Non ci sono missing data!
```

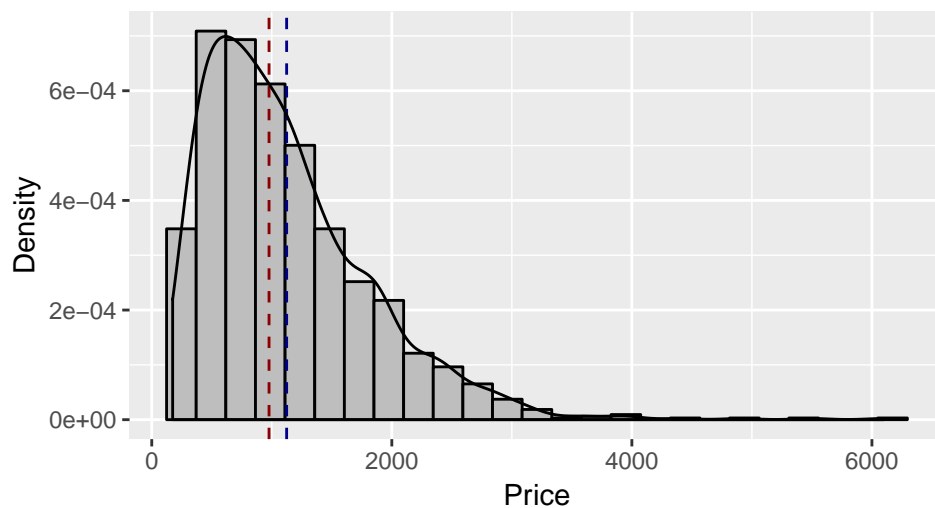
```
## X Company Product
## 0 0 0
## TypeName Inches ScreenResolution
## 0 0 0
## Cpu Ram Memory
## 0 0 0
## Gpu OpSys Weight
## 0 0 0
## Price Frequenza Risoluzione
## 0 0 0
## Pixel GpuCompany MemoriaSSD
## 0 0 0
## SolidStateDisk TotalMemory dedicated_GPU
## 0 0 0
## Aggregated_Company
## 0
```

```
plot(data$Aggregated_Company,data$Price)
```



```
library(ggplot2)
ggplot(data,aes(x = Price)) + geom_histogram(aes(y =..density..), bins= 25, fill = "grey",color ="black") +
  geom_vline(xintercept = quantile(data$Price, 0.50), color = "dark red", lty = 2) +geom_vline(xintercept = mean(
  Price), color = "dark blue", lty = 2) +
  labs(x = "Price", y ="Density") + ggtitle("Price Distribution with mean and median") +geom_density()
```

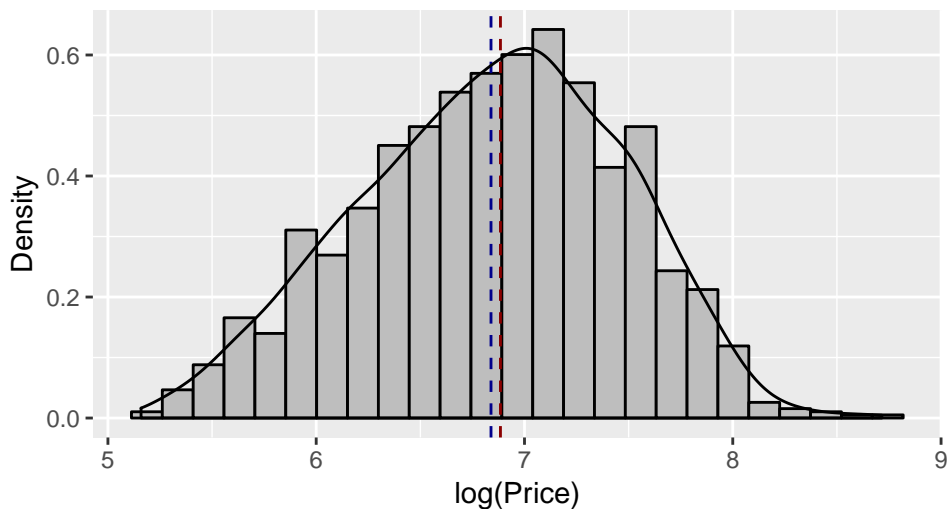
Price Distribution with mean and median



Quite skewed to the right, mean > median: we could try to apply a correction like Log(Y)

```
ggplot(data,aes(x = log(Price))) + geom_histogram(aes(y =..density..),bins= 25, fill = "grey", color ="black") +
  geom_vline(xintercept = quantile(log(data$Price), 0.50), color = "dark red", lty = 2) + geom_vline(xintercept = mean(
  log(Price)), color = "dark blue", lty = 2) +
  labs(x = "log(Price)", y ="Density") +ggtitle("log(Price) Distribution with mean and median")+ geom_density()
```

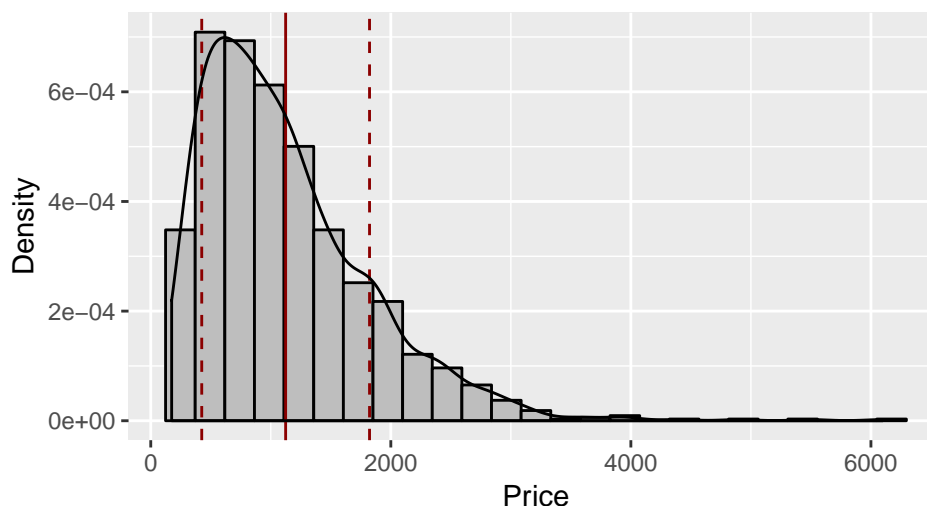
log(Price) Distribution with mean and median



Now the distribution is looking a bit better (as regards normality)

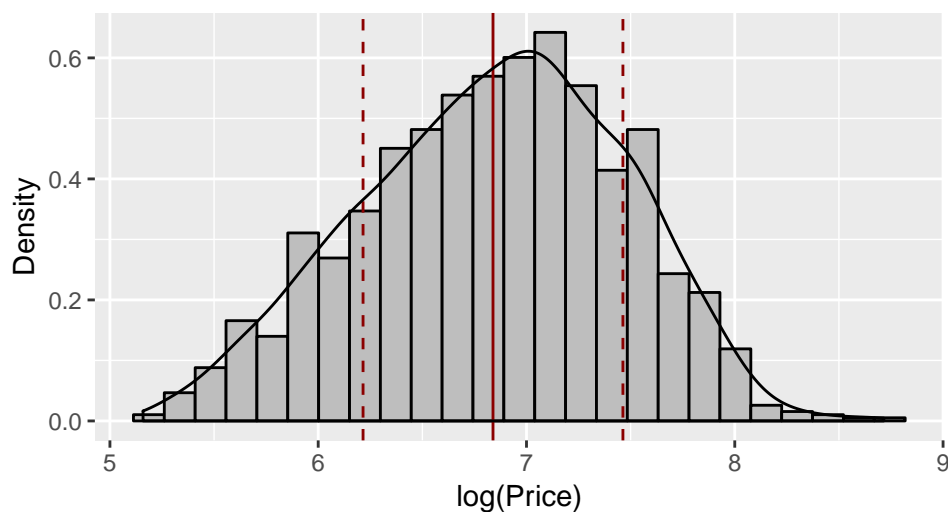
```
ggplot(data,aes(x = Price)) + geom_histogram(aes(y =..density..), bins= 25, fill = "grey", color ="black") +
  geom_vline(xintercept = mean(data$Price), color = "dark red") + geom_vline(xintercept = mean(data$Price) + sd(data$P
  geom_vline(xintercept = mean(data$Price) - sd(data$Price), color = "dark red", lty = 2) +labs(x = "Price", y ="Densi
```

Price Distribution (mean \pm sd)



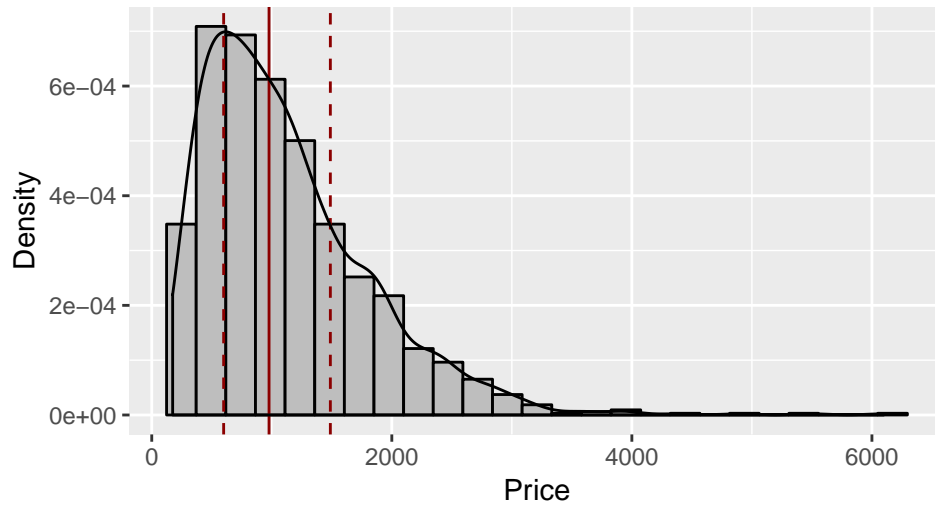
```
ggplot(data,aes(x = log(Price))) +geom_histogram(aes(y =..density..), bins= 25,fill = "grey",color ="black") +
  geom_vline(xintercept = mean(log(data$Price)), color = "dark red") + geom_vline(xintercept = mean(log(data$Price)) +
  geom_vline(xintercept = mean(log(data$Price)) - sd(log(data$Price)), color = "dark red", lty = 2) + labs(x = "log(Pr
```

log(Price) Distribution (mean \pm sd)



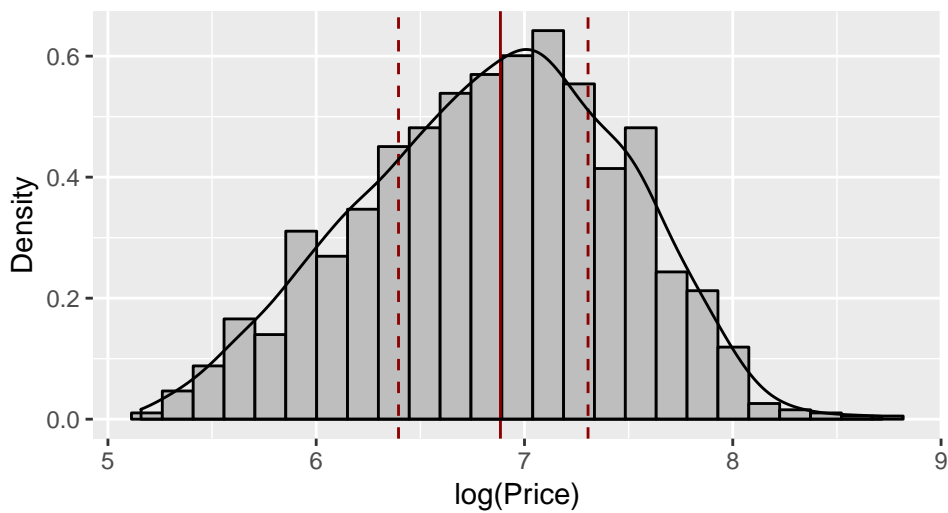
```
ggplot(data,aes(x = Price)) + geom_histogram(aes(y =..density..), bins= 25, fill = "grey", color ="black") +
  geom_vline(xintercept = quantile(data$Price, 0.25), color = "dark red",lty = 2) + geom_vline(xintercept = quantile(d
  geom_vline(xintercept = quantile(data$Price, 0.75), color = "dark red", lty = 2) + labs(x = "Price", y ="Density") +
```

Price Distribution (quartiles)



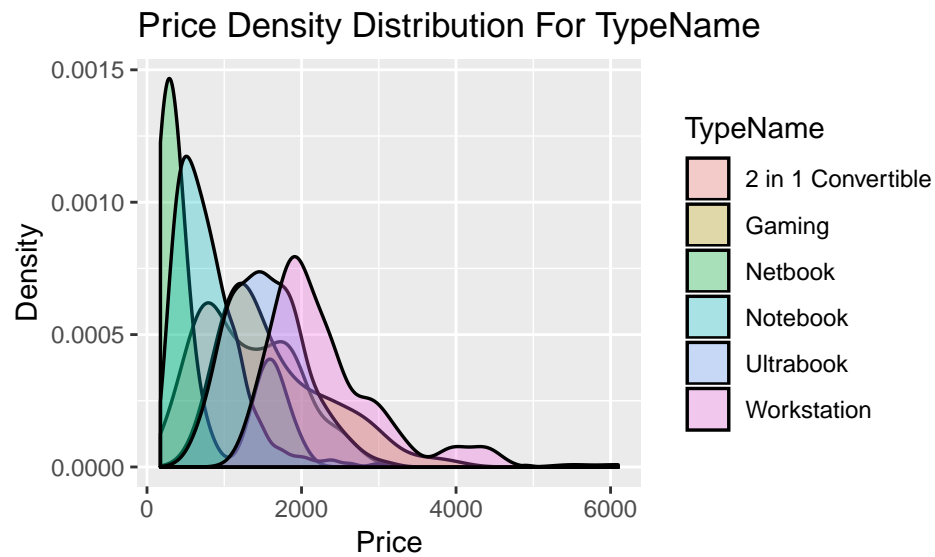
```
ggplot(data,aes(x = log(Price))) + geom_histogram(aes(y =..density..), bins= 25, fill = "grey", color ="black") +
  geom_vline(xintercept = quantile(log(data$Price), 0.25), color = "dark red",lty = 2) + geom_vline(xintercept = quantile(log(data$Price), 0.75), color = "dark red", lty = 2) + labs(x = "log(Price)", y ="Density")
```

log(Price) Distribution (quartiles)

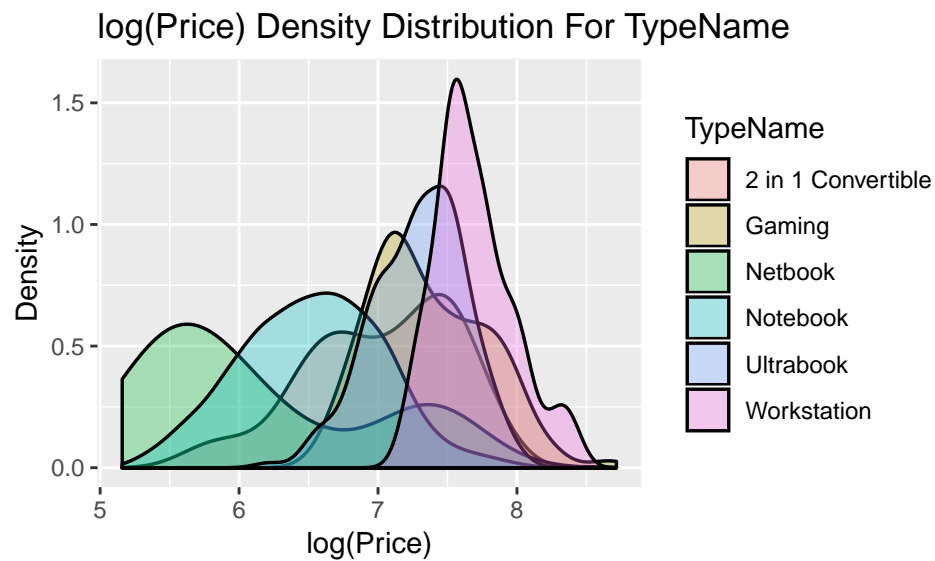


Descrittive variabile dipendente price

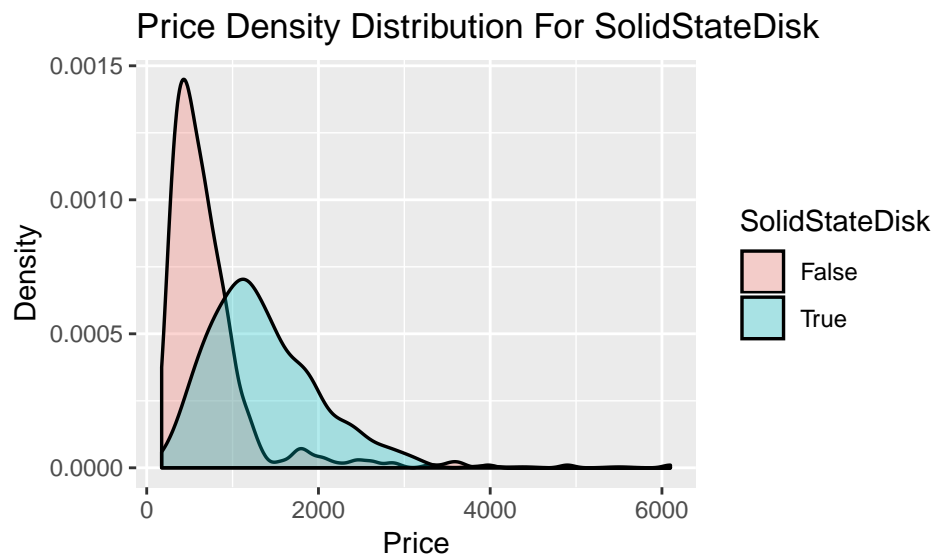
```
ggplot(data, aes(x = Price, fill = TypeName)) + geom_density(size = 0.6, alpha = .3) + labs(x = "Price", y ="Density",
```



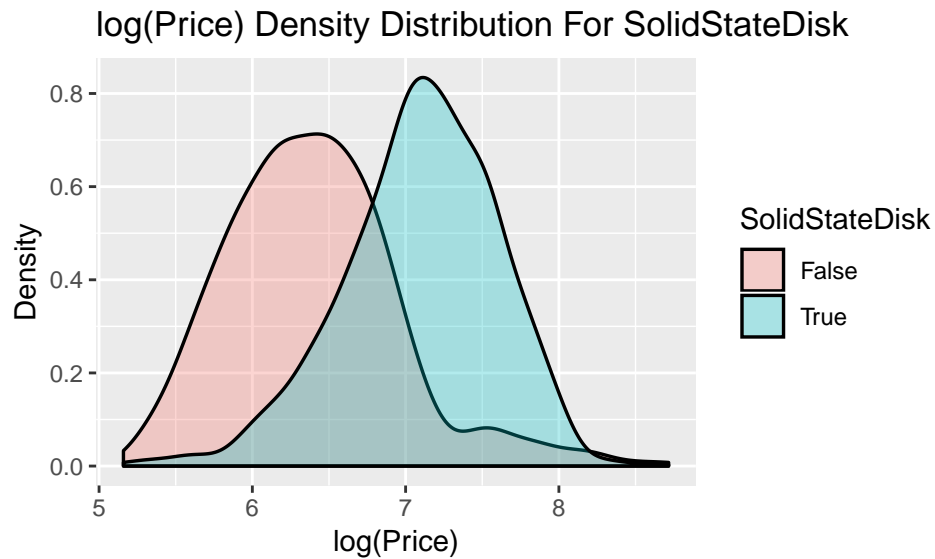
```
ggplot(data, aes(x = log(Price), fill = TypeName)) + geom_density(size = 0.6, alpha = .3) + labs(x = "log(Price)", y = "Density")
```



```
ggplot(data, aes(x = Price, fill = SolidStateDisk)) + geom_density(size = 0.6, alpha = .3) + labs(x = "Price", y = "Density")
```



```
ggplot(data, aes(x = log(Price), fill = SolidStateDisk)) + geom_density(size = 0.6, alpha = .3) + labs(x = "log(Price)
```



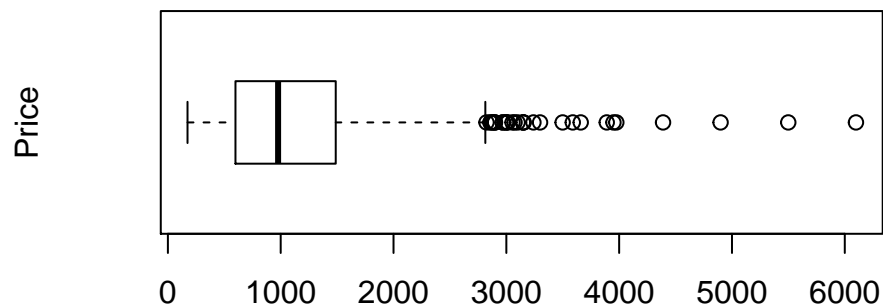
```
library(psych)
describe(data$Price)
```

```
##      vars      n   mean      sd median trimmed   mad min  max range skew
## X1      1 1303 1123.69 699.01   977 1038.47 619.73 174 6099 5925 1.52
##      kurtosis    se
## X1      4.34 19.36
```

```
describe(log(data$Price))
```

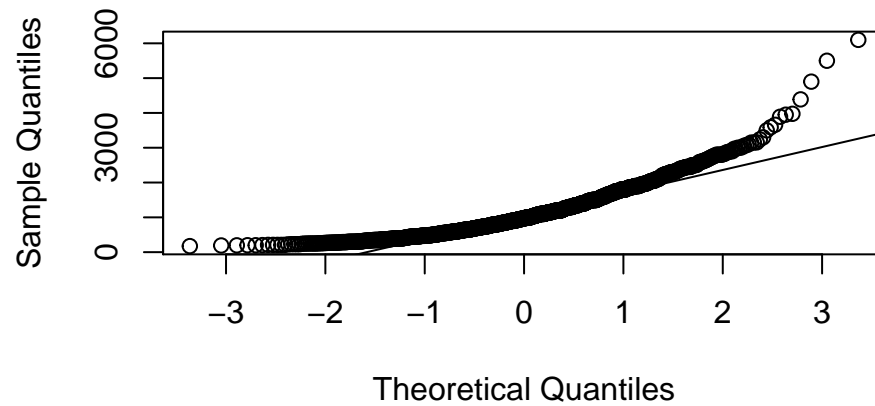
```
##      vars      n mean      sd median trimmed   mad min  max range skew kurtosis
## X1      1 1303  6.84  0.62   6.88   6.85 0.65 5.16 8.72  3.56 -0.17   -0.47
##      se
## X1 0.02
```

```
library(nortest) # test per ipotesi di normalità
boxplot(data$Price, horizontal = T, ylab = c("Price") )
```



```
qqnorm(data$Price);qqline(data$Price)
```


Normal Q-Q Plot



```
shapiro.test(data$Price)
```

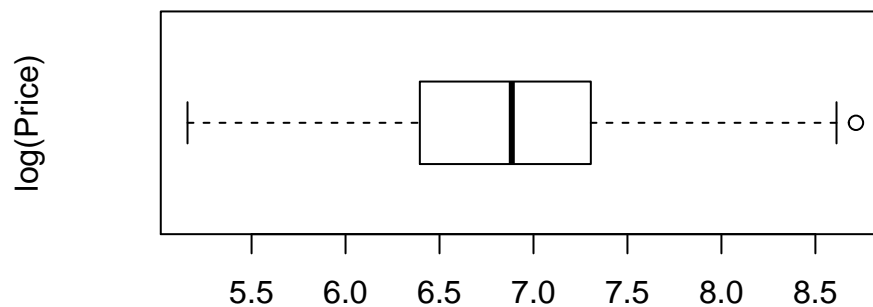
```
##
##  Shapiro-Wilk normality test
##
## data:  data$Price
## W = 0.89382, p-value < 2.2e-16
```

```
ad.test(data$Price)
```

```
##
##  Anderson-Darling normality test
##
## data:  data$Price
## A = 28.319, p-value < 2.2e-16
```

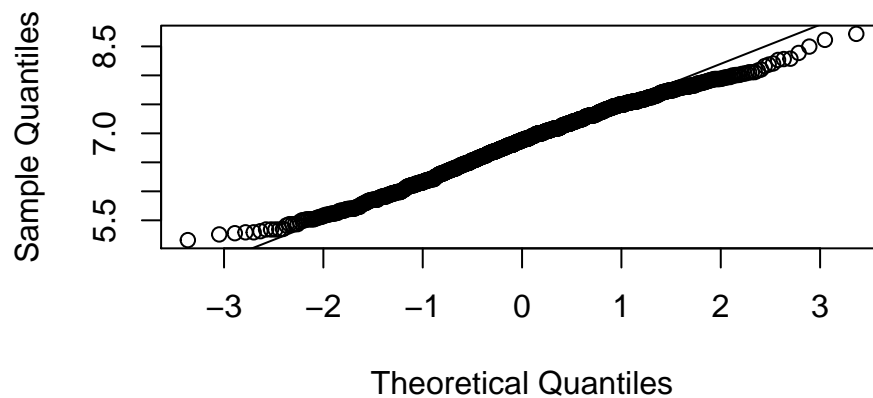
Trying with the log correction:

```
# Correzione NORMALITA'
library(nortest)
boxplot(log(data$Price), ylab="log(Price)", horizontal = T)
```



```
qqnorm(log(data$Price));qqline(log(data$Price))
```

Normal Q-Q Plot



```
shapiro.test(log(data$Price)) #better than before, but still not normal according to shapiro
```

```
##
## Shapiro-Wilk normality test
##
## data: log(data$Price)
## W = 0.99252, p-value = 3.628e-06
ad.test(log(data$Price))
```

```
##
## Anderson-Darling normality test
##
## data: log(data$Price)
## A = 2.5942, p-value = 1.515e-06
```

Test on a mean (justify H0) on Y and confidence limits.

T-test

One sample

```
ref <-666 #prezzo medio di mercato pc 2019 (€)
```

```
t.test(log(data$Price),mu=log(ref),alternative = "greater")
```

```
##
## One Sample t-test
##
## data: log(data$Price)
## t = 19.551, df = 1302, p-value < 2.2e-16
## alternative hypothesis: true mean is greater than 6.50129
## 95 percent confidence interval:
## 6.810726 Inf
## sample estimates:
## mean of x
## 6.839173
```

Wilcoxon Signed Rank Test

```
wilcox.test(log(data$Price), mu=log(ref), conf.int = TRUE)
```

```
##
## Wilcoxon signed rank test with continuity correction
##
## data: log(data$Price)
```

```
## V = 657855, p-value < 2.2e-16
## alternative hypothesis: true location is not equal to 6.50129
## 95 percent confidence interval:
##  6.814806 6.886491
## sample estimates:
## (pseudo)median
##      6.850673
```

Test two means, two variances (Y vs X) .

```
#Two sample
Razer<-data$Price[data$Company=="Razer"]
Other <-data$Price[data$Company!="Apple"]
t.test(log(Razer),log(Other),alternative = "greater")

##
##  Welch Two Sample t-test
##
## data:  log(Razer) and log(Other)
## t = 4.8187, df = 6.0666, p-value = 0.001428
## alternative hypothesis: true difference in means is greater than 0
## 95 percent confidence interval:
##  0.6772006      Inf
## sample estimates:
## mean of x mean of y
##  7.964967  6.831639

wilcox.test(log(Razer), log(Other), alternative = "g")

##
##  Wilcoxon rank sum test with continuity correction
##
## data:  log(Razer) and log(Other)
## W = 8103.5, p-value = 0.0001159
## alternative hypothesis: true location shift is greater than 0

# F test sulla varianza
var.test(log(Razer), log(Other), alternative = "two.sided")

##
##  F test to compare two variances
##
## data:  log(Razer) and log(Other)
## F = 0.98671, num df = 6, denom df = 1281, p-value = 0.8654
## alternative hypothesis: true ratio of variances is not equal to 1
## 95 percent confidence interval:
##  0.4080583 4.7898266
## sample estimates:
## ratio of variances
##      0.9867142
```

Association/chi square among some couples of categorical Xj

Variabili qualitative: tabella di contingenza e chi quadro

```
b<-data
b.table<-table(b$SolidStateDisk,b$TypeName)
b.table

##
```

```
##           2 in 1 Convertible Gaming Netbook Notebook Ultrabook Workstation
## False           29      32      13      376      19      7
## True            92     173      12     351     177     22
```

```
prop.table(b.table,2)
```

```
##
##           2 in 1 Convertible      Gaming      Netbook      Notebook      Ultrabook
## False           0.23966942 0.15609756 0.52000000 0.51719395 0.09693878
## True            0.76033058 0.84390244 0.48000000 0.48280605 0.90306122
##
##           Workstation
## False 0.24137931
## True  0.75862069
```

```
# chi square test
```

```
chisq.test(b.table)
```

```
##
## Pearson's Chi-squared test
##
## data:  b.table
## X-squared = 184.66, df = 5, p-value < 2.2e-16
```

```
chi=chisq.test(b.table)
chi_norm=chi$statistic/(nrow(b)*min(nrow(b.table)-1,ncol(b.table)-1))
chi_norm
```

```
## X-squared
## 0.1417156
```

```
#Proviamo SolidStateDisk vs dedicated_GPU
```

```
b<-data
b.table<-table(b$SolidStateDisk,b$dedicated_GPU)
b.table
```

```
##
##           False True
## False      285  191
## True       438  389
```

```
prop.table(b.table,2)
```

```
##
##           False      True
## False 0.3941909 0.3293103
## True  0.6058091 0.6706897
```

```
# chi square test
```

```
chisq.test(b.table)
```

```
##
## Pearson's Chi-squared test with Yates' continuity correction
##
## data:  b.table
## X-squared = 5.5664, df = 1, p-value = 0.01831
```

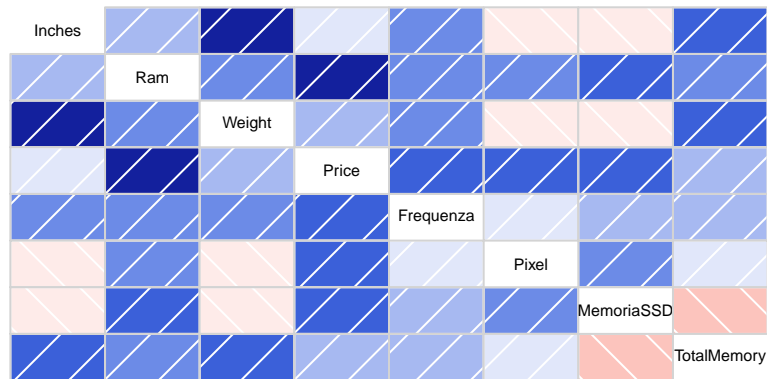
```
chi=chisq.test(b.table)
chi_norm=chi$statistic/(nrow(b)*min(nrow(b.table)-1,ncol(b.table)-1))
chi_norm
```

```
## X-squared
## 0.00427199
```

Correlazione per variabili quantitative

```
# seleziona solo variabili quantitative
nums <- sapply(data, is.numeric)
var_numeric <- data[,nums]
var_numeric$X=NULL

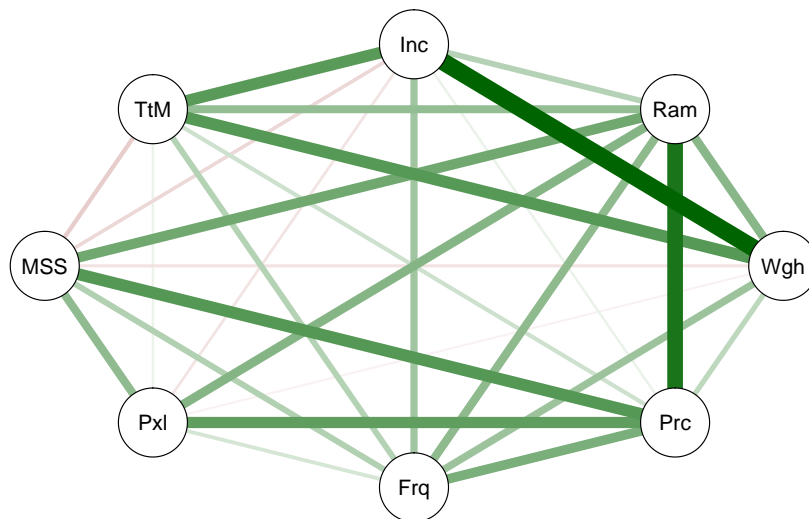
# Test di correlazione. (Spearman's o Kendall tau)
#if(!require(corrgram)) install.packages("corrgram")
library(corrgram)
corrgram(var_numeric)
```



```
# Correlazione come grafo
library(qgraph)
detcor=cor(as.matrix(var_numeric), method="pearson")
round(detcor, 2)
```

```
##          Inches  Ram Weight Price Frequenza Pixel MemoriaSSD
## Inches      1.00 0.24 0.83 0.07      0.31 -0.09      -0.13
## Ram         0.24 1.00 0.38 0.74      0.37 0.40       0.46
## Weight      0.83 0.38 1.00 0.21      0.32 -0.04      -0.10
## Price       0.07 0.74 0.21 1.00      0.43 0.52       0.55
## Frequenza   0.31 0.37 0.32 0.43      1.00 0.14       0.25
## Pixel      -0.09 0.40 -0.04 0.52      0.14 1.00       0.36
## MemoriaSSD -0.13 0.46 -0.10 0.55      0.25 0.36       1.00
## TotalMemory 0.54 0.35 0.55 0.16      0.24 0.06      -0.16
##
##          TotalMemory
## Inches          0.54
## Ram             0.35
## Weight          0.55
## Price           0.16
## Frequenza       0.24
## Pixel           0.06
## MemoriaSSD     -0.16
## TotalMemory     1.00
```

```
# plot corr matrix: green positive red negative
qgraph(detcor, shape="circle", posCol="darkgreen", negCol="darkred")
```



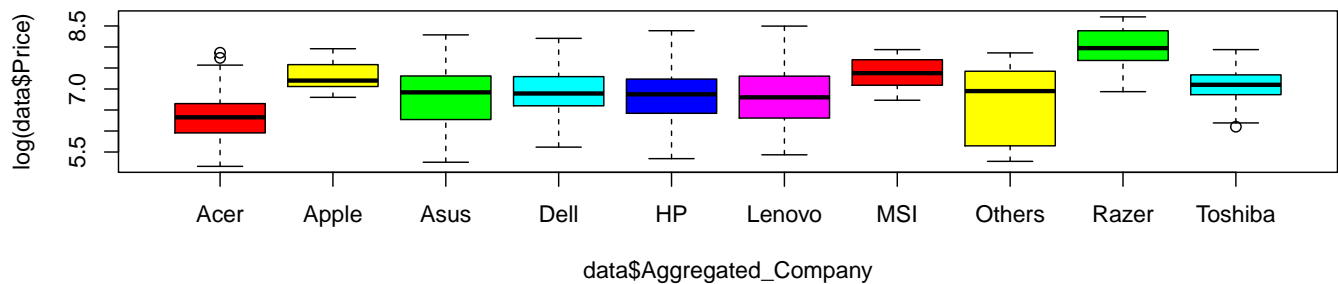
```
cor.test(var_numeric$Inches, var_numeric$Weight)
```

```
##
## Pearson's product-moment correlation
##
## data: var_numeric$Inches and var_numeric$Weight
## t = 53.187, df = 1301, p-value < 2.2e-16
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
##  0.8097181 0.8440031
## sample estimates:
##      cor
## 0.8276311
```

Boxplot di confronto (pre-anova)

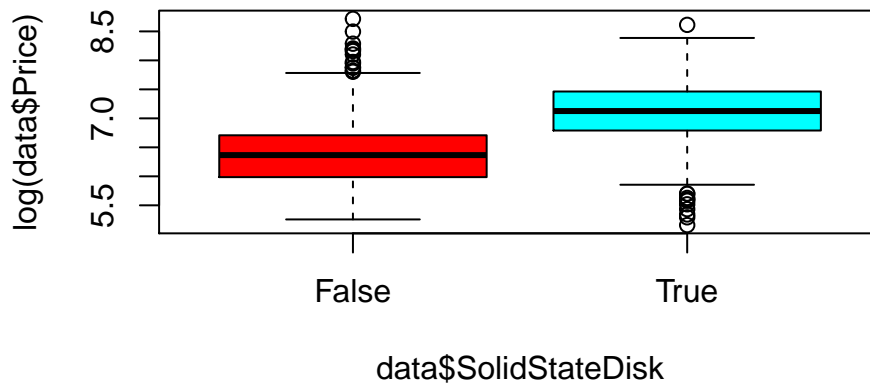
```
boxplot(log(data$Price)~data$Aggregated_Company, main="Boxplot Prezzo per compagnia", col= rainbow(6), horizontal = F)
```

Boxplot Prezzo per compagnia



```
boxplot(log(data$Price)~data$SolidStateDisk, main="Prezzo vs ssd", col= rainbow(2), horizontal = F)
```

Prezzo vs ssd



Anova one way $Y = X_j$, for a categorical X

```
library(lsmmeans)
lmC = lm(Price ~ TypeName, data=data)
summary(lmC)
```

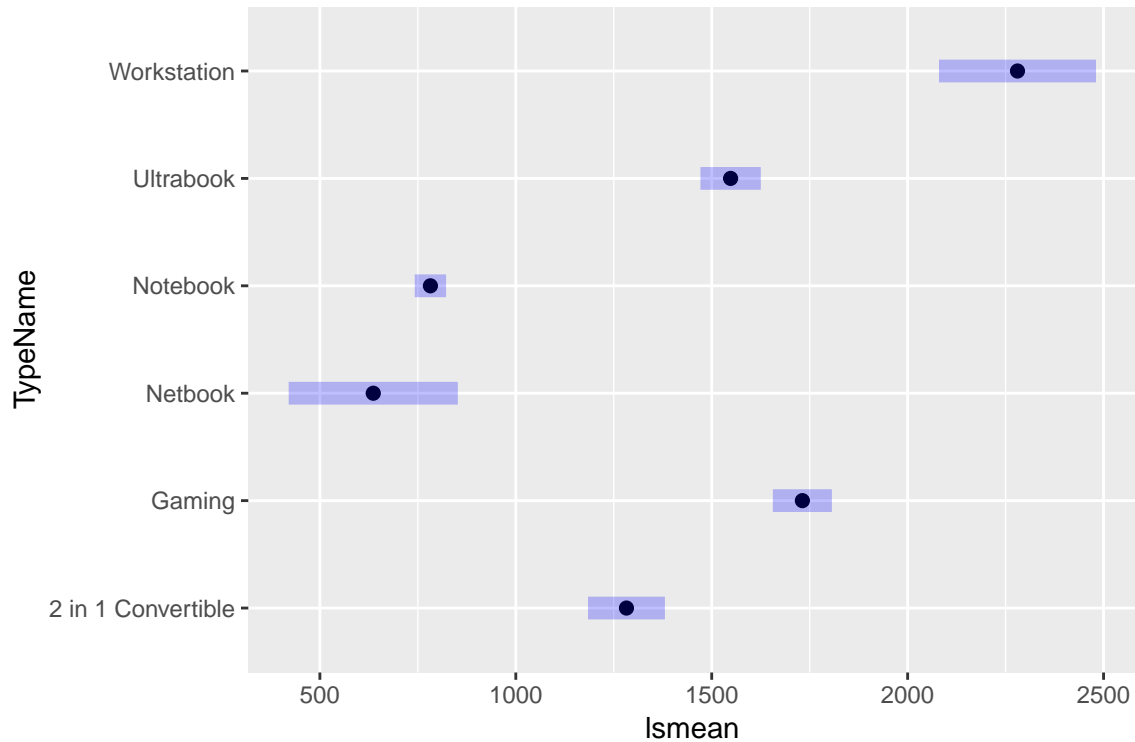
```
##
## Call:
## lm(formula = Price ~ TypeName, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1049.2  -381.7   -98.1    267.6   4367.6
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    1282.40     50.01  25.642 < 2e-16 ***
## TypeNameGaming     448.98     63.07   7.119 1.79e-12 ***
## TypeNameNetbook   -646.17    120.86  -5.347 1.06e-07 ***
## TypeNameNotebook  -500.32     54.01  -9.263 < 2e-16 ***
## TypeNameUltrabook   265.83     63.60   4.180 3.12e-05 ***
## TypeNameWorkstation 997.96    113.74   8.774 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 550.1 on 1297 degrees of freedom
## Multiple R-squared:  0.383, Adjusted R-squared:  0.3806
## F-statistic: 161 on 5 and 1297 DF, p-value: < 2.2e-16
drop1(lmC, test = 'F')
```

```
## Single term deletions
##
## Model:
## Price ~ TypeName
##      Df Sum of Sq      RSS   AIC F value    Pr(>F)
## <none>                 392518380 16450
## TypeName  5 243656581 636174961 17069  161.02 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
ls_TypeName = lsmmeans(lmC, pairwise ~ TypeName, adjust = 'tukey')
ls_TypeName$lsmmeans
```

```
## TypeName      lsmean    SE    df lower.CL upper.CL
## 2 in 1 Convertible 1282  50.0 1297    1184    1381
## Gaming            1731  38.4 1297    1656    1807
## Netbook           636 110.0 1297     420     852
## Notebook          782  20.4 1297     742     822
## Ultrabook         1548  39.3 1297    1471    1625
## Workstation       2280 102.2 1297    2080    2481
##
```

```
## Confidence level used: 0.95
```

```
plot(ls_TypeName$lsmeans, alpha = .05)
```



```
ls_TypeName$contrasts
```

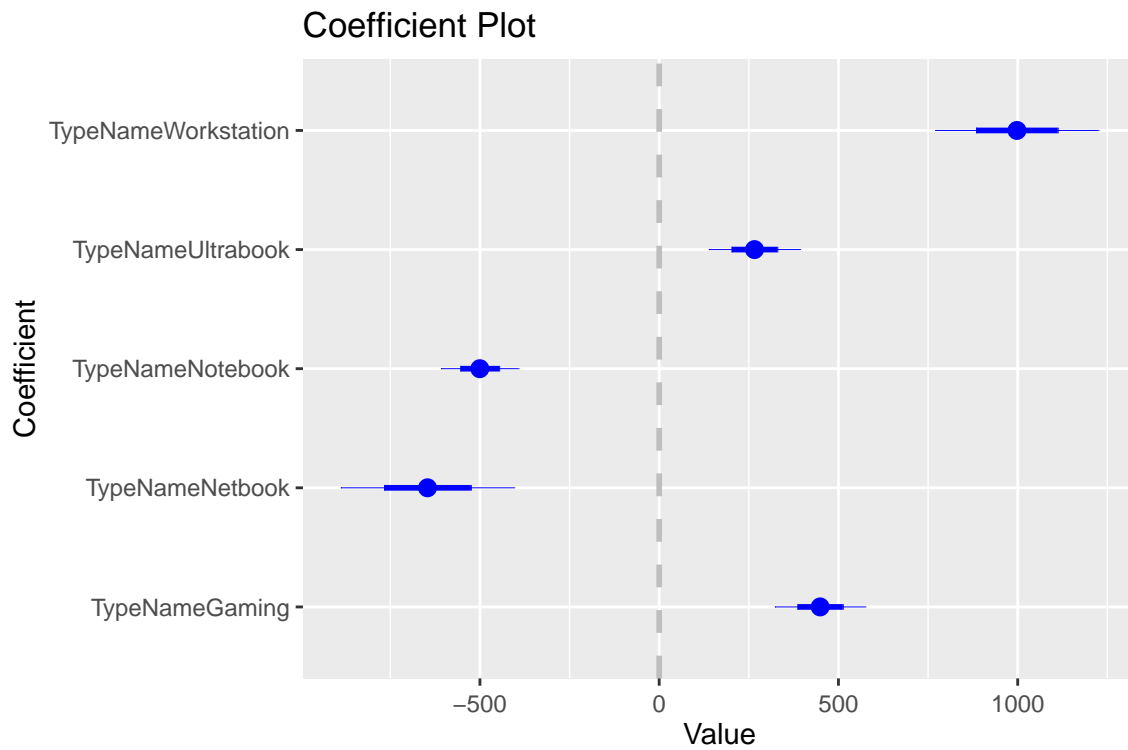
```
## contrast          estimate    SE    df t.ratio p.value
## 2 in 1 Convertible - Gaming      -449  63.1 1297  -7.119 <.0001
## 2 in 1 Convertible - Netbook      646 120.9 1297   5.347 <.0001
## 2 in 1 Convertible - Notebook     500  54.0 1297   9.263 <.0001
## 2 in 1 Convertible - Ultrabook   -266  63.6 1297  -4.180 0.0004
## 2 in 1 Convertible - Workstation -998 113.7 1297  -8.774 <.0001
## Gaming - Netbook                1095 116.5 1297   9.397 <.0001
## Gaming - Notebook                949  43.5 1297  21.821 <.0001
## Gaming - Ultrabook              183  55.0 1297   3.333 0.0114
## Gaming - Workstation            -549 109.1 1297  -5.030 <.0001
## Netbook - Notebook              -146 111.9 1297  -1.303 0.7833
## Netbook - Ultrabook             -912 116.8 1297  -7.806 <.0001
## Netbook - Workstation          -1644 150.1 1297 -10.951 <.0001
## Notebook - Ultrabook            -766  44.3 1297 -17.304 <.0001
## Notebook - Workstation          -1498 104.2 1297 -14.383 <.0001
## Ultrabook - Workstation          -732 109.5 1297  -6.689 <.0001
##
```

```
## P value adjustment: tukey method for comparing a family of 6 estimates
```

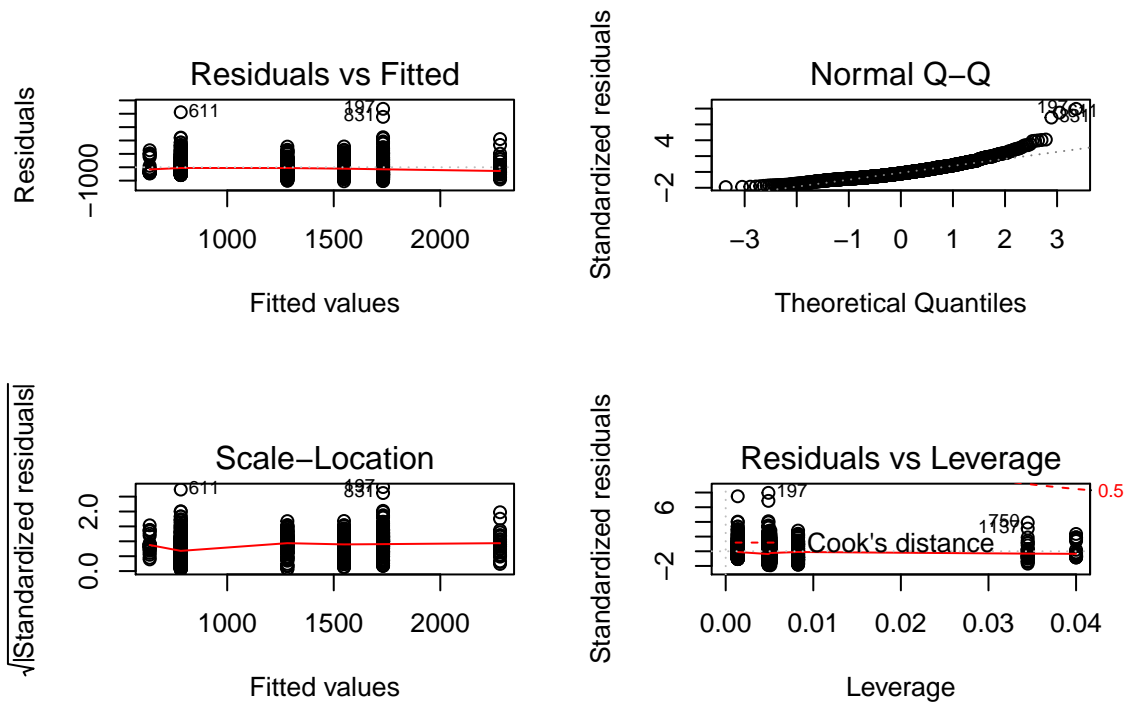
```
library(coefplot)
```

```
#library(forestmodel)
```

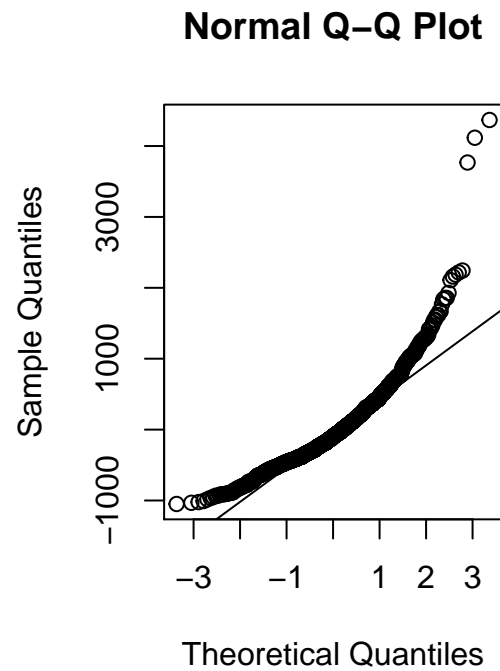
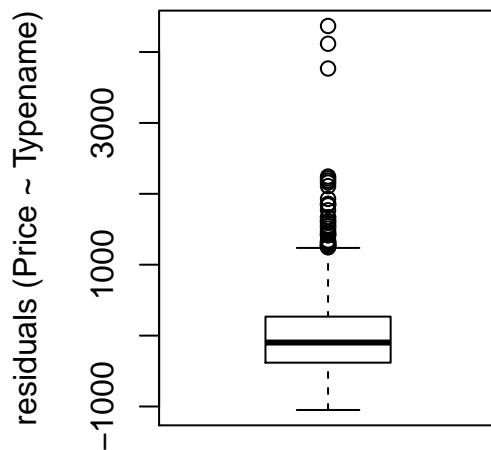
```
coefplot(lmC, intercept = FALSE)
```

```
par(mfrow = c(2,2))
plot(lmC)
```



```
 #(not) normal distribution of residuals
par(mfrow=c(1,2))
boxplot(lmC$residuals, ylab="residuals (Price ~ Typename)")
qqnorm(lmC$residuals);qqline(lmC$residuals)
```



```
ad.test(lmC$residuals)
```

```
##
## Anderson-Darling normality test
##
## data:  lmC$residuals
## A = 22.667, p-value < 2.2e-16
```

```
shapiro.test(lmC$residuals)
```

```
##
## Shapiro-Wilk normality test
##
## data:  lmC$residuals
## W = 0.89641, p-value < 2.2e-16
```

```
#let's try again with the log correction
lmC_log = lm(log(Price) ~ TypeName, data=data)
summary(lmC_log) #R^2 increases
```

```
##
## Call:
## lm(formula = log(Price) ~ TypeName, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.40971 -0.33589  0.00698  0.33215  1.96853
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    7.02648    0.04379  160.456 < 2e-16 ***
## TypeNameGaming    0.33865    0.05522   6.133 1.15e-09 ***
## TypeNameNetbook  -0.91149    0.10583  -8.613 < 2e-16 ***
## TypeNameNotebook -0.49823    0.04729 -10.534 < 2e-16 ***
## TypeNameUltrabook  0.26648    0.05569   4.785 1.91e-06 ***
## TypeNameWorkstation 0.66479    0.09959   6.675 3.65e-11 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4817 on 1297 degrees of freedom
```

```
## Multiple R-squared:  0.4061, Adjusted R-squared:  0.4038
## F-statistic: 177.4 on 5 and 1297 DF,  p-value: < 2.2e-16
```

```
drop1(lmC_log, test = 'F')
```

```
## Single term deletions
```

```
##
```

```
## Model:
```

```
## log(Price) ~ TypeName
```

```
##          Df Sum of Sq    RSS      AIC F value    Pr(>F)
```

```
## <none>                 300.95 -1897.5
```

```
## TypeName  5      205.76 506.71 -1228.7  177.36 < 2.2e-16 ***
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
ls_TypeName_log = lsmeans(lmC_log, pairwise ~ TypeName, adjust = 'tukey')
```

```
ls_TypeName_log$lsmeans
```

```
##   TypeName      lsmean      SE    df lower.CL upper.CL
```

```
## 2 in 1 Convertible  7.03 0.0438 1297      6.94      7.11
```

```
## Gaming             7.37 0.0336 1297      7.30      7.43
```

```
## Netbook            6.11 0.0963 1297      5.93      6.30
```

```
## Notebook           6.53 0.0179 1297      6.49      6.56
```

```
## Ultrabook          7.29 0.0344 1297      7.23      7.36
```

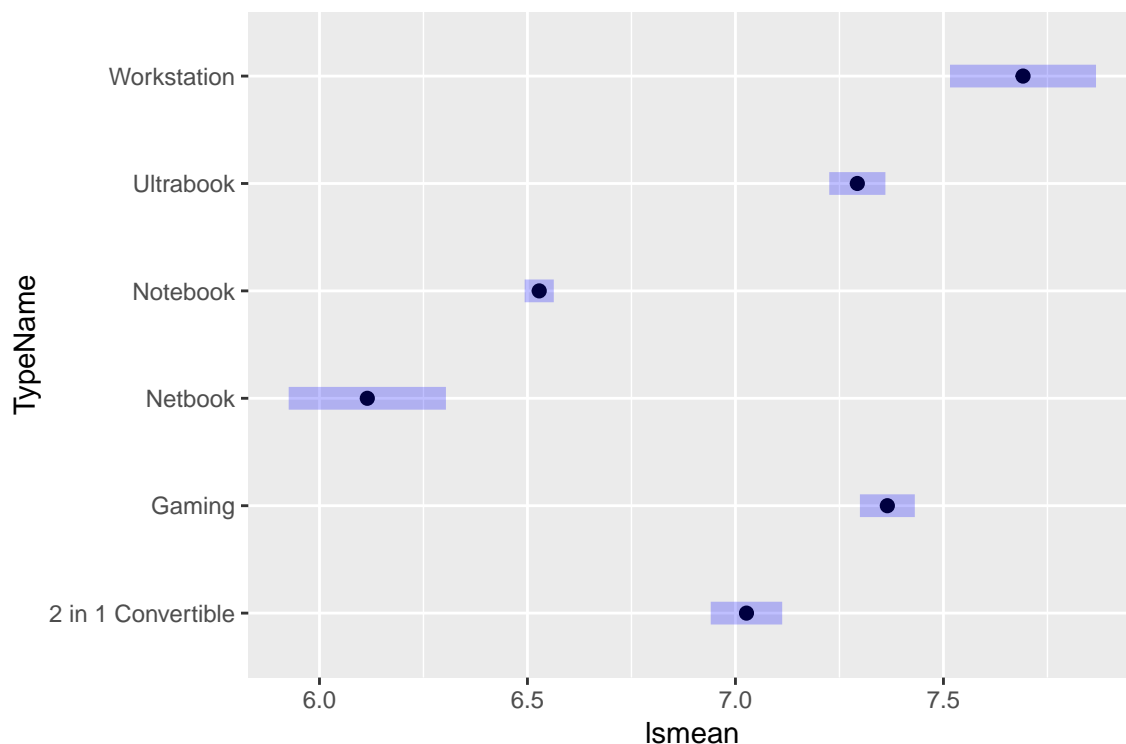
```
## Workstation        7.69 0.0894 1297      7.52      7.87
```

```
##
```

```
## Results are given on the log (not the response) scale.
```

```
## Confidence level used: 0.95
```

```
plot(ls_TypeName_log$lsmeans, alpha = .05)
```



```
ls_TypeName_log$contrasts
```

```
## contrast          estimate      SE    df t.ratio p.value
```

```
## 2 in 1 Convertible - Gaming    -0.3387 0.0552 1297   -6.133 <.0001
```

```
## 2 in 1 Convertible - Netbook     0.9115 0.1058 1297    8.613 <.0001
```

```
## 2 in 1 Convertible - Notebook    0.4982 0.0473 1297   10.534 <.0001
```

```
## 2 in 1 Convertible - Ultrabook  -0.2665 0.0557 1297   -4.785 <.0001
```

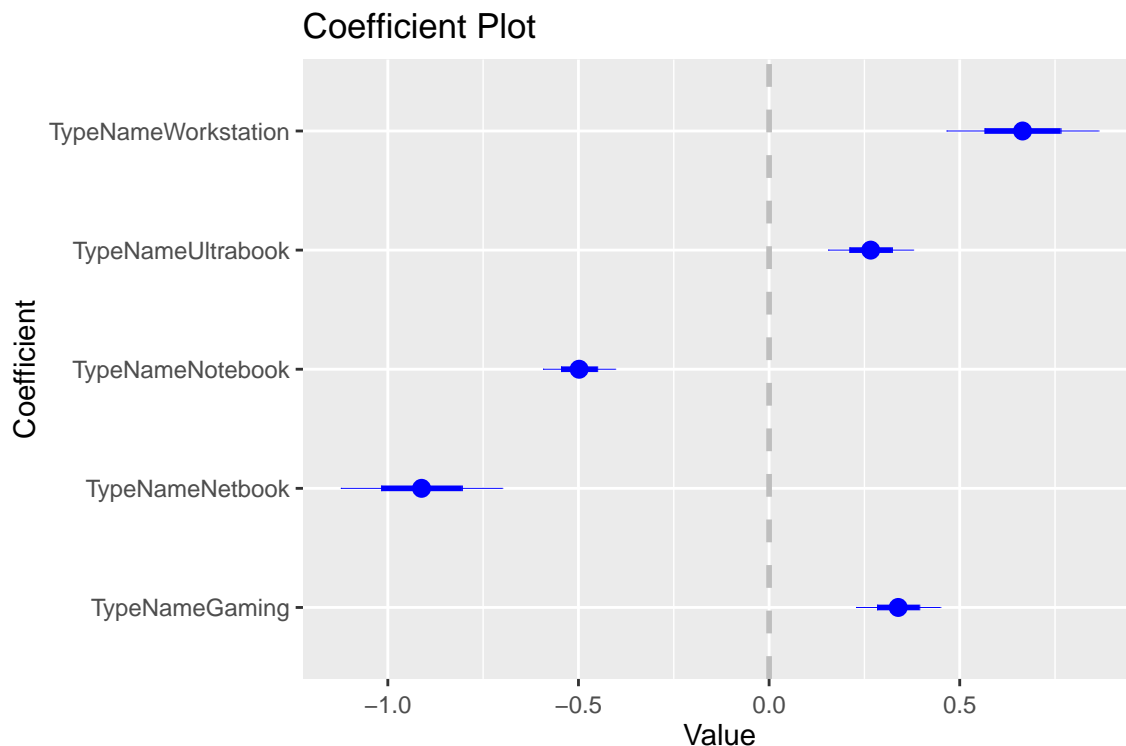
```

## 2 in 1 Convertible - Workstation -0.6648 0.0996 1297 -6.675 <.0001
## Gaming - Netbook 1.2501 0.1020 1297 12.251 <.0001
## Gaming - Notebook 0.8369 0.0381 1297 21.970 <.0001
## Gaming - Ultrabook 0.0722 0.0481 1297 1.500 0.6644
## Gaming - Workstation -0.3261 0.0956 1297 -3.413 0.0087
## Netbook - Notebook -0.4133 0.0980 1297 -4.218 0.0004
## Netbook - Ultrabook -1.1780 0.1023 1297 -11.515 <.0001
## Netbook - Workstation -1.5763 0.1315 1297 -11.990 <.0001
## Notebook - Ultrabook -0.7647 0.0388 1297 -19.725 <.0001
## Notebook - Workstation -1.1630 0.0912 1297 -12.750 <.0001
## Ultrabook - Workstation -0.3983 0.0958 1297 -4.156 0.0005
##
## Results are given on the log (not the response) scale.
## P value adjustment: tukey method for comparing a family of 6 estimates
c= contrast(ls_TypeName_log , method = "eff") # contrast among predicted lsmeans and overall lsmean
c

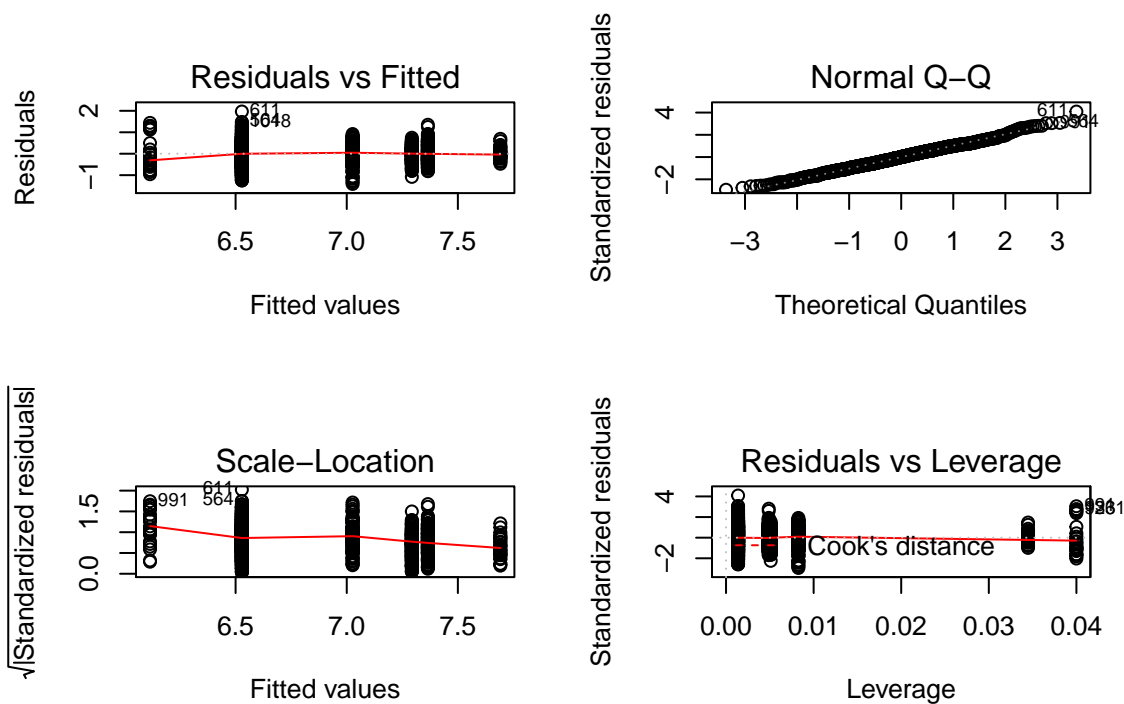
## $lsmeans
## contrast estimate SE df t.ratio p.value
## 2 in 1 Convertible effect 0.0233 0.0434 1297 0.537 0.5916
## Gaming effect 0.3620 0.0369 1297 9.811 <.0001
## Netbook effect -0.8882 0.0824 1297 -10.776 <.0001
## Notebook effect -0.4749 0.0286 1297 -16.592 <.0001
## Ultrabook effect 0.2898 0.0374 1297 7.756 <.0001
## Workstation effect 0.6881 0.0771 1297 8.927 <.0001
##
## P value adjustment: fdr method for 6 tests
##
## $contrasts
## contrast estimate SE df t.ratio
## 2 in 1 Convertible - Gaming effect -0.1039 0.0588 1297 -1.767
## 2 in 1 Convertible - Netbook effect 1.1462 0.1113 1297 10.295
## 2 in 1 Convertible - Notebook effect 0.7329 0.0464 1297 15.795
## 2 in 1 Convertible - Ultrabook effect -0.0318 0.0509 1297 -0.625
## 2 in 1 Convertible - Workstation effect -0.4301 0.0674 1297 -6.380
## Gaming - Netbook effect 1.4849 0.1115 1297 13.315
## Gaming - Notebook effect 1.0716 0.0468 1297 22.882
## Gaming - Ultrabook effect 0.3069 0.0513 1297 5.988
## Gaming - Workstation effect -0.0914 0.0677 1297 -1.350
## Netbook - Notebook effect -0.1786 0.0978 1297 -1.826
## Netbook - Ultrabook effect -0.9433 0.1000 1297 -9.437
## Netbook - Workstation effect -1.3416 0.1093 1297 -12.273
## Notebook - Ultrabook effect -0.5300 0.0481 1297 -11.029
## Notebook - Workstation effect -0.9283 0.0653 1297 -14.213
## Ultrabook - Workstation effect -0.1636 0.0746 1297 -2.194
## p.value
## 0.0894
## <.0001
## <.0001
## 0.5324
## <.0001
## <.0001
## <.0001
## <.0001
## 0.1898
## 0.0850
## <.0001
## <.0001
## <.0001
## <.0001
## 0.0388

```

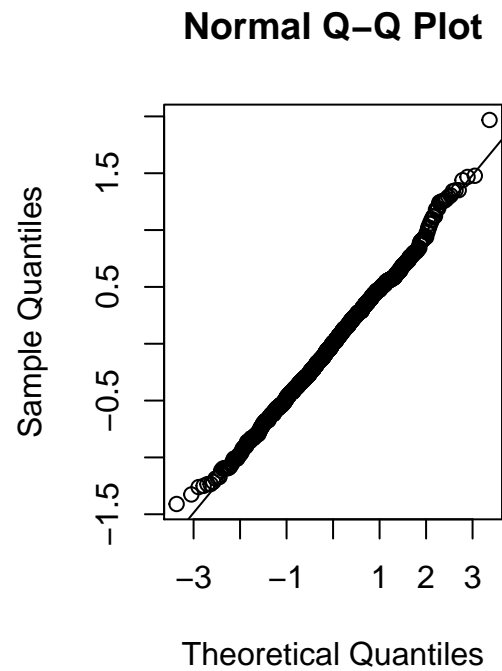
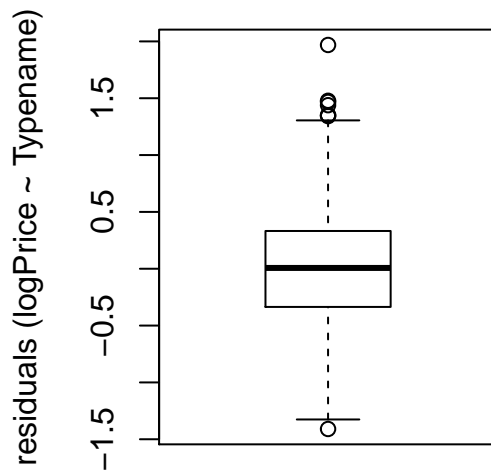
```
##
## P value adjustment: fdr method for 15 tests
coefplot(lmC_log, intercept = FALSE)
```



```
par(mfrow = c(2,2))
plot(lmC_log)
```



```
##(not) normal distribution of residuals
par(mfrow=c(1,2))
boxplot(lmC_log$residuals, ylab="residuals (logPrice ~ Typename)")
qqnorm(lmC_log$residuals);qqline(lmC_log$residuals)
```



```
ad.test(lmC_log$residuals) #normal now!
```

```
##
## Anderson-Darling normality test
##
## data: lmC_log$residuals
## A = 0.51757, p-value = 0.1886
```

```
shapiro.test(lmC_log$residuals) #borderline now!
```

```
##
## Shapiro-Wilk normality test
##
## data: lmC_log$residuals
## W = 0.99764, p-value = 0.05462
```

Anova two way $Y = X_j X_k$ for some categorical X

A due vie

```
lmC = lm(log(Price) ~ SolidStateDisk*TypeName, data=data)
summary(lmC)
```

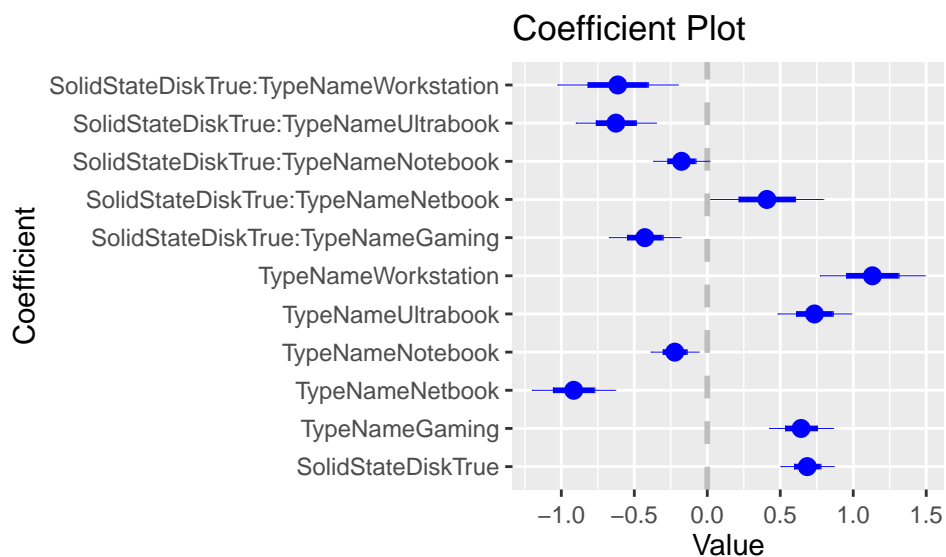
```
##
## Call:
## lm(formula = log(Price) ~ SolidStateDisk * TypeName, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.52448 -0.29389  0.00263  0.28844  2.21396
##
## Coefficients:
##              Estimate Std. Error t value
## (Intercept)      6.50558    0.07912  82.227
## SolidStateDiskTrue    0.68510    0.09073   7.551
## TypeNameGaming      0.64246    0.10924   5.881
## TypeNameNetbook    -0.91541    0.14221  -6.437
## TypeNameNotebook   -0.22276    0.08211  -2.713
```

```
## TypeNameUltrabook          0.73415    0.12575    5.838
## TypeNameWorkstation        1.13137    0.17942    6.306
## SolidStateDiskTrue:TypeNameGaming -0.42785    0.12229   -3.499
## SolidStateDiskTrue:TypeNameNetbook  0.40827    0.19319    2.113
## SolidStateDiskTrue:TypeNameNotebook -0.17676    0.09609   -1.840
## SolidStateDiskTrue:TypeNameUltrabook -0.62616    0.13716   -4.565
## SolidStateDiskTrue:TypeNameWorkstation -0.61349    0.20595   -2.979
##                               Pr(>|t|)
## (Intercept)                < 2e-16 ***
## SolidStateDiskTrue          8.16e-14 ***
## TypeNameGaming              5.17e-09 ***
## TypeNameNetbook             1.71e-10 ***
## TypeNameNotebook            0.006760 **
## TypeNameUltrabook           6.67e-09 ***
## TypeNameWorkstation         3.93e-10 ***
## SolidStateDiskTrue:TypeNameGaming  0.000484 ***
## SolidStateDiskTrue:TypeNameNetbook  0.034771 *
## SolidStateDiskTrue:TypeNameNotebook 0.066065 .
## SolidStateDiskTrue:TypeNameUltrabook 5.47e-06 ***
## SolidStateDiskTrue:TypeNameWorkstation 0.002948 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4261 on 1291 degrees of freedom
## Multiple R-squared:  0.5375, Adjusted R-squared:  0.5336
## F-statistic: 136.4 on 11 and 1291 DF,  p-value: < 2.2e-16
```

```
drop1(lmC, test="F")
```

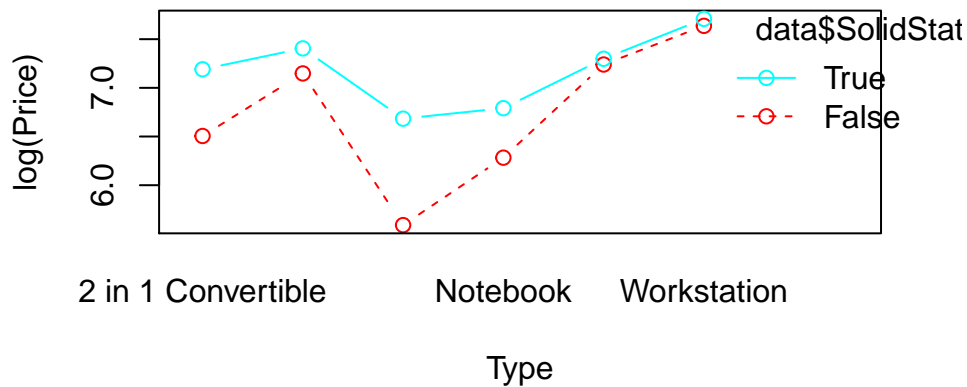
```
## Single term deletions
##
## Model:
## log(Price) ~ SolidStateDisk * TypeName
##               Df Sum of Sq  RSS      AIC F value    Pr(>F)
## <none>                234.35 -2211.4
## SolidStateDisk:TypeName  5    8.6744 243.03 -2174.1    9.557 5.745e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
library(coefplot)
coefplot(lmC, intercept=FALSE)
```



```
interaction.plot(x.factor = data$TypeName, trace.factor = data$SolidStateDisk, response = log(data$Price), fun=mean, t
```

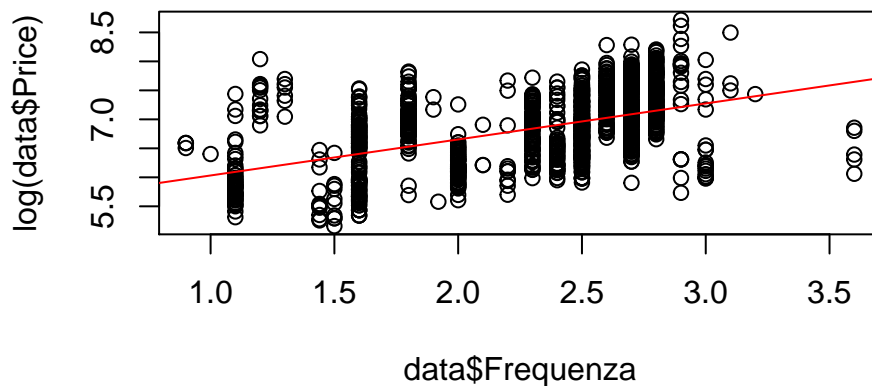
Interaction Plot



Regressione lineare

```
lmA1<-lm(log(Price) ~ Frequenza , data=data)
summary(lmA1)
```

```
##
## Call:
## lm(formula = log(Price) ~ Frequenza, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.58596 -0.43023  0.00587  0.40113  1.88247
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   5.41132    0.06944   77.93  <2e-16 ***
## Frequenza     0.62114    0.02950   21.06  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.539 on 1301 degrees of freedom
## Multiple R-squared:  0.2542, Adjusted R-squared:  0.2536
## F-statistic: 443.3 on 1 and 1301 DF,  p-value: < 2.2e-16
plot(data$Frequenza,log(data$Price))
abline(lmA1,col="red")
```

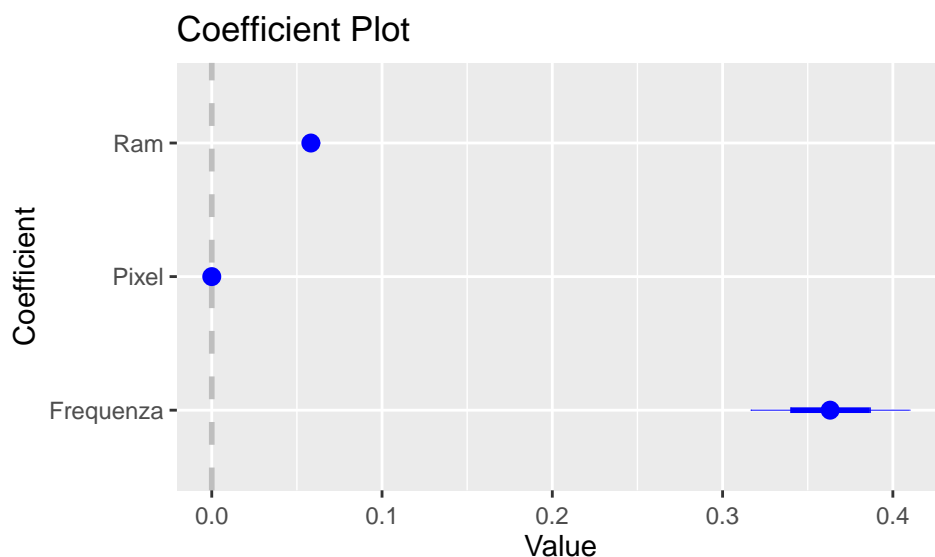


```
lmA2<-lm(log(Price) ~ Frequenza+Pixel+Ram , data=data)
summary(lmA2)
```

```
##
## Call:
## lm(formula = log(Price) ~ Frequenza + Pixel + Ram, data = data)
```



```
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.92388 -0.29048  0.00741  0.28110  1.36597
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  5.266e+00  5.227e-02  100.76  <2e-16 ***
## Frequenza    3.632e-01  2.331e-02   15.58  <2e-16 ***
## Pixel        1.152e-07  8.591e-09    13.41  <2e-16 ***
## Ram          5.821e-02  2.505e-03    23.24  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3959 on 1299 degrees of freedom
## Multiple R-squared:  0.5981, Adjusted R-squared:  0.5972
## F-statistic: 644.5 on 3 and 1299 DF,  p-value: < 2.2e-16
coefplot(lmA2, intercept=FALSE)
```



Ancova Y = all covariates (qualitative +quantitative)

```
lmK = lm(log(Price) ~ Aggregated_Company+TypeName+SolidStateDisk+ Frequenza+Pixel+Ram , data=data)
```

```
summary(lmK)
```

```
##
## Call:
## lm(formula = log(Price) ~ Aggregated_Company + TypeName + SolidStateDisk +
##     Frequenza + Pixel + Ram, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.06590 -0.20002 -0.00696  0.21244  1.11366
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  5.484e+00  5.830e-02  94.070  < 2e-16 ***
## Aggregated_CompanyApple  3.718e-01  7.910e-02  4.701  2.87e-06 ***
## Aggregated_CompanyAsus   9.850e-02  4.027e-02  2.446  0.01458 *
## Aggregated_CompanyDell   2.147e-01  3.626e-02  5.922  4.08e-09 ***
```

```
## Aggregated_CompanyHP      2.644e-01  3.628e-02  7.290 5.42e-13 ***
## Aggregated_CompanyLenovo   1.469e-01  3.605e-02  4.076 4.87e-05 ***
## Aggregated_CompanyMSI      2.374e-01  5.871e-02  4.044 5.57e-05 ***
## Aggregated_CompanyOthers   2.731e-02  5.724e-02  0.477 0.63332
## Aggregated_CompanyRazer     3.069e-01  1.254e-01  2.446 0.01457 *
## Aggregated_CompanyToshiba   3.693e-01  5.533e-02  6.674 3.70e-11 ***
## TypeNameGaming             -8.882e-02  4.201e-02  -2.114 0.03468 *
## TypeNameNetbook            -4.098e-01  6.969e-02  -5.880 5.23e-09 ***
## TypeNameNotebook           -2.964e-01  3.188e-02  -9.298 < 2e-16 ***
## TypeNameUltrabook          9.970e-02  3.768e-02  2.646 0.00825 **
## TypeNameWorkstation         3.371e-01  6.576e-02  5.127 3.40e-07 ***
## SolidStateDiskTrue          2.891e-01  2.031e-02  14.234 < 2e-16 ***
## Frequenza                   2.751e-01  1.989e-02  13.831 < 2e-16 ***
## Pixel                       6.417e-08  7.187e-09  8.929 < 2e-16 ***
## Ram                         4.562e-02  2.227e-03  20.488 < 2e-16 ***
```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.3098 on 1284 degrees of freedom
## Multiple R-squared:  0.7568, Adjusted R-squared:  0.7533
## F-statistic: 221.9 on 18 and 1284 DF,  p-value: < 2.2e-16
```

```
drop1(lmK, .~, test="F")
```

```
## Single term deletions
##
## Model:
## log(Price) ~ Aggregated_Company + TypeName + SolidStateDisk +
##      Frequenza + Pixel + Ram
##
##           Df Sum of Sq    RSS      AIC F value    Pr(>F)
## <none>                    123.25 -3034.7
## Aggregated_Company    9    10.390 133.65 -2947.2  12.026 < 2.2e-16 ***
## TypeName               5    29.658 152.91 -2763.8  61.792 < 2.2e-16 ***
## SolidStateDisk         1    19.450 142.71 -2845.8 202.620 < 2.2e-16 ***
## Frequenza              1    18.364 141.62 -2855.7 191.304 < 2.2e-16 ***
## Pixel                   1     7.653 130.91 -2958.2  79.724 < 2.2e-16 ***
## Ram                     1    40.293 163.55 -2668.1 419.752 < 2.2e-16 ***
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
ls=lsmeans(lmK,pairwise ~ Aggregated_Company ,adjust="tukey")
c= contrast(ls, method = "eff")
c
```

```
## $lsmeans
## contrast      estimate      SE    df t.ratio p.value
## Acer effect    -0.2037 0.0333 1284 -6.113 <.0001
## Apple effect     0.1681 0.0664 1284  2.532 0.0229
## Asus effect     -0.1052 0.0281 1284 -3.749 0.0006
## Dell effect      0.0110 0.0234 1284  0.471 0.6378
## HP effect        0.0607 0.0249 1284  2.442 0.0246
## Lenovo effect   -0.0568 0.0241 1284 -2.359 0.0264
## MSI effect       0.0337 0.0470 1284  0.717 0.5260
## Others effect   -0.1764 0.0459 1284 -3.847 0.0006
## Razer effect     0.1031 0.1089 1284  0.947 0.4299
## Toshiba effect   0.1655 0.0447 1284  3.705 0.0006
```

```
##
## Results are averaged over the levels of: TypeName, SolidStateDisk
## P value adjustment: fdr method for 10 tests
##
```

```
## $contrasts
## contrast      estimate      SE    df t.ratio p.value
## Acer - Apple effect -0.31706 0.0893 1284 -3.550 0.0014
```

```

## Acer - Asus effect      -0.04376 0.0442 1284 -0.990 0.4146
## Acer - Dell effect      -0.16000 0.0396 1284 -4.042 0.0002
## Acer - HP effect        -0.20970 0.0396 1284 -5.293 <.0001
## Acer - Lenovo effect    -0.09218 0.0387 1284 -2.380 0.0388
## Acer - MSI effect       -0.18267 0.0572 1284 -3.195 0.0038
## Acer - Others effect    0.02743 0.0553 1284 0.496 0.7154
## Acer - Razer effect     -0.25213 0.1071 1284 -2.355 0.0388
## Acer - Toshiba effect   -0.31453 0.0498 1284 -6.320 <.0001
## Apple - Asus effect     0.32805 0.0714 1284 4.594 <.0001
## Apple - Dell effect     0.21180 0.0681 1284 3.110 0.0048
## Apple - HP effect       0.16211 0.0690 1284 2.349 0.0388
## Apple - Lenovo effect   0.27962 0.0687 1284 4.071 0.0002
## Apple - MSI effect      0.18913 0.0812 1284 2.330 0.0391
## Apple - Others effect   0.39924 0.0757 1284 5.275 <.0001
## Apple - Razer effect    0.11968 0.1181 1284 1.013 0.4146
## Apple - Toshiba effect  0.05727 0.0749 1284 0.765 0.5558
## Asus - Dell effect      -0.06150 0.0392 1284 -1.568 0.1890
## Asus - HP effect        -0.11120 0.0402 1284 -2.768 0.0136
## Asus - Lenovo effect    0.00632 0.0388 1284 0.163 0.9279
## Asus - MSI effect       -0.08417 0.0538 1284 -1.566 0.1890
## Asus - Others effect    0.12593 0.0552 1284 2.283 0.0424
## Asus - Razer effect     -0.15363 0.1054 1284 -1.458 0.2176
## Asus - Toshiba effect   -0.21603 0.0500 1284 -4.322 0.0001
## Dell - HP effect        0.00505 0.0366 1284 0.138 0.9279
## Dell - Lenovo effect    0.12257 0.0353 1284 3.471 0.0016
## Dell - MSI effect       0.03207 0.0543 1284 0.591 0.6569
## Dell - Others effect    0.24218 0.0526 1284 4.602 <.0001
## Dell - Razer effect     -0.03738 0.1044 1284 -0.358 0.8105
## Dell - Toshiba effect   -0.09978 0.0470 1284 -2.123 0.0611
## HP - Lenovo effect      0.17226 0.0357 1284 4.828 <.0001
## HP - MSI effect         0.08177 0.0556 1284 1.470 0.2176
## HP - Others effect      0.29187 0.0532 1284 5.491 <.0001
## HP - Razer effect       0.01231 0.1057 1284 0.116 0.9279
## HP - Toshiba effect     -0.05009 0.0471 1284 -1.064 0.4044
## Lenovo - MSI effect     -0.03575 0.0550 1284 -0.650 0.6272
## Lenovo - Others effect  0.17436 0.0535 1284 3.257 0.0033
## Lenovo - Razer effect   -0.10520 0.1054 1284 -0.999 0.4146
## Lenovo - Toshiba effect -0.16760 0.0474 1284 -3.533 0.0014
## MSI - Others effect     0.26485 0.0739 1284 3.582 0.0013
## MSI - Razer effect      -0.01471 0.1133 1284 -0.130 0.9279
## MSI - Toshiba effect    -0.07711 0.0698 1284 -1.104 0.3915
## Others - Razer effect   -0.22482 0.1159 1284 -1.939 0.0912
## Others - Toshiba effect -0.28722 0.0678 1284 -4.233 0.0001
## Razer - Toshiba effect  -0.00766 0.1454 1284 -0.053 0.9580

```

```

##
## Results are averaged over the levels of: TypeName, SolidStateDisk
## P value adjustment: fdr method for 45 tests

```

```

data$Product=NULL
data$X=NULL
data$Company=NULL #uso solo Aggregated_Company
data$Gpu=NULL #uso solo Gpu_company
data$dedicated_GPU=NULL
data$ScreenResolution=NULL #uso solo Pixels
data$Risoluzione=NULL #uso solo Pixels
data$Cpu=NULL #uso solo Frequenza
data$Memory=NULL #uso solo MemorySSD, TotalMemory e SolidStateDisk

```

```

lm_full = lm(log(Price) ~ ., data = data)
summary(lm_full)

```

```

##

```

```
## Call:
## lm(formula = log(Price) ~ ., data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.92215 -0.18933 -0.00294  0.18376  1.01631
##
## Coefficients: (1 not defined because of singularities)
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      5.295e+00  2.419e-01  21.887 < 2e-16 ***
## TypeNameGaming    -1.522e-01  4.890e-02  -3.113 0.001890 **
## TypeNameNetbook    -4.176e-01  6.844e-02  -6.102 1.39e-09 ***
## TypeNameNotebook   -2.480e-01  3.357e-02  -7.387 2.72e-13 ***
## TypeNameUltrabook   8.461e-02  3.570e-02   2.370 0.017947 *
## TypeNameWorkstation 2.386e-01  6.678e-02   3.573 0.000366 ***
## Inches           -2.686e-02  1.281e-02  -2.097 0.036174 *
## Ram               3.658e-02  2.401e-03  15.233 < 2e-16 ***
## OpSysChrome OS     2.837e-01  2.143e-01   1.323 0.185942
## OpSysLinux         2.184e-01  2.121e-01   1.030 0.303317
## OpSysMac OS X      9.874e-01  2.329e-01   4.240 2.40e-05 ***
## OpSysmacOS         6.901e-01  2.262e-01   3.051 0.002329 **
## OpSysNo OS         6.266e-02  2.112e-01   0.297 0.766688
## OpSysWindows 10    3.412e-01  2.081e-01   1.640 0.101289
## OpSysWindows 10 S  4.502e-01  2.345e-01   1.920 0.055075 .
## OpSysWindows 7     6.572e-01  2.126e-01   3.092 0.002033 **
## Weight            4.250e-02  2.830e-02   1.502 0.133381
## Frequenza         2.606e-01  1.918e-02  13.584 < 2e-16 ***
## Pixel            5.252e-08  6.815e-09   7.706 2.61e-14 ***
## GpuCompanyARM      2.396e-01  2.983e-01   0.803 0.422027
## GpuCompanyIntel    1.590e-01  2.735e-02   5.814 7.70e-09 ***
## GpuCompanyNvidia   2.521e-01  3.075e-02   8.197 5.97e-16 ***
## MemoriaSSD         4.321e-04  9.656e-05   4.475 8.32e-06 ***
## SolidStateDiskTrue 2.196e-01  3.042e-02   7.218 9.05e-13 ***
## TotalMemory        1.361e-04  2.417e-05   5.630 2.21e-08 ***
## Aggregated_CompanyApple      NA         NA         NA         NA
## Aggregated_CompanyAsus      9.357e-02  3.837e-02   2.439 0.014876 *
## Aggregated_CompanyDell      2.535e-01  3.464e-02   7.320 4.38e-13 ***
## Aggregated_CompanyHP        2.672e-01  3.531e-02   7.568 7.26e-14 ***
## Aggregated_CompanyLenovo     1.732e-01  3.528e-02   4.910 1.03e-06 ***
## Aggregated_CompanyMSI        2.091e-01  5.729e-02   3.650 0.000273 ***
## Aggregated_CompanyOthers     8.039e-02  5.647e-02   1.424 0.154815
## Aggregated_CompanyRazer      4.003e-01  1.174e-01   3.408 0.000674 ***
## Aggregated_CompanyToshiba    3.659e-01  5.276e-02   6.935 6.45e-12 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2862 on 1270 degrees of freedom
## Multiple R-squared:  0.7947, Adjusted R-squared:  0.7895
## F-statistic: 153.6 on 32 and 1270 DF, p-value: < 2.2e-16
```

```
anova(lm_full, test="F")
```

```
## Analysis of Variance Table
##
## Response: log(Price)
##              Df Sum Sq Mean Sq  F value    Pr(>F)
## TypeName      5 205.762   41.152  502.4427 < 2.2e-16 ***
## Inches        1   2.374    2.374   28.9820 8.694e-08 ***
## Ram           1 101.674  101.674 1241.3753 < 2.2e-16 ***
## OpSys         8  23.287    2.911   35.5399 < 2.2e-16 ***
## Weight        1   0.145    0.145    1.7725  0.1833
## Frequenza     1  24.973   24.973  304.9023 < 2.2e-16 ***
```

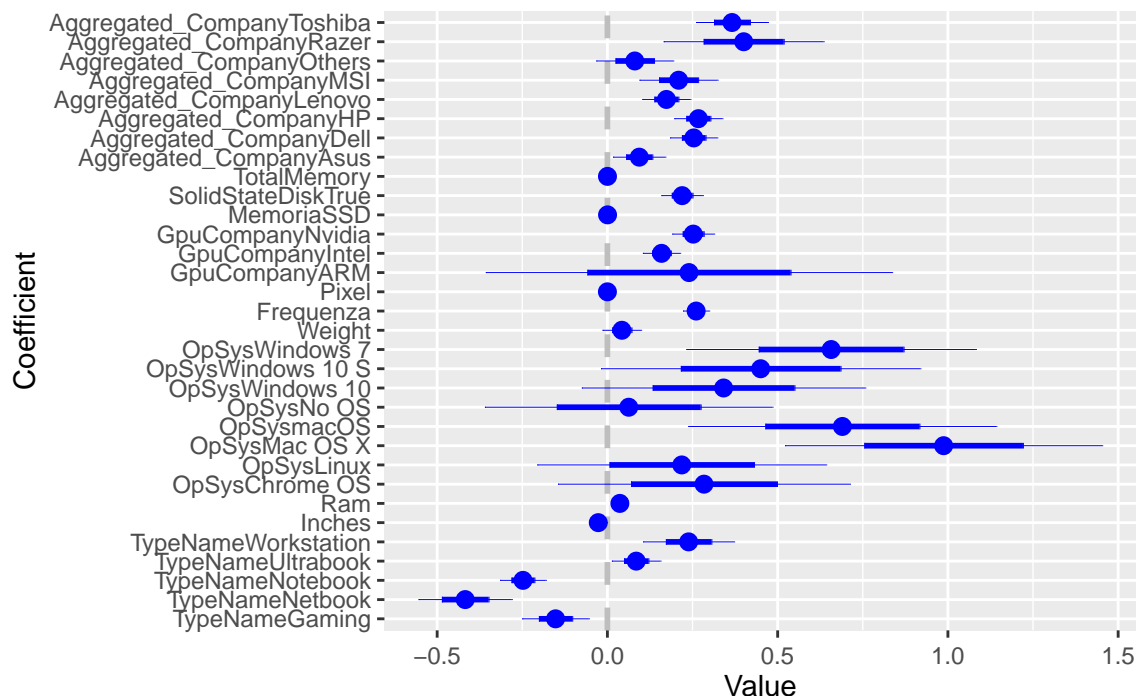
```
## Pixel          1  10.680  10.680  130.3919 < 2.2e-16 ***
## GpuCompany      3   3.748   1.249   15.2515 9.402e-10 ***
## MemoriaSSD      1  15.007  15.007  183.2197 < 2.2e-16 ***
## SolidStateDisk  1   3.231   3.231   39.4446 4.626e-10 ***
## TotalMemory     1   2.734   2.734   33.3833 9.509e-09 ***
## Aggregated_Company 8   9.075   1.134   13.8504 < 2.2e-16 ***
## Residuals      1270 104.019   0.082
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

drop1(lm_full, test="F")

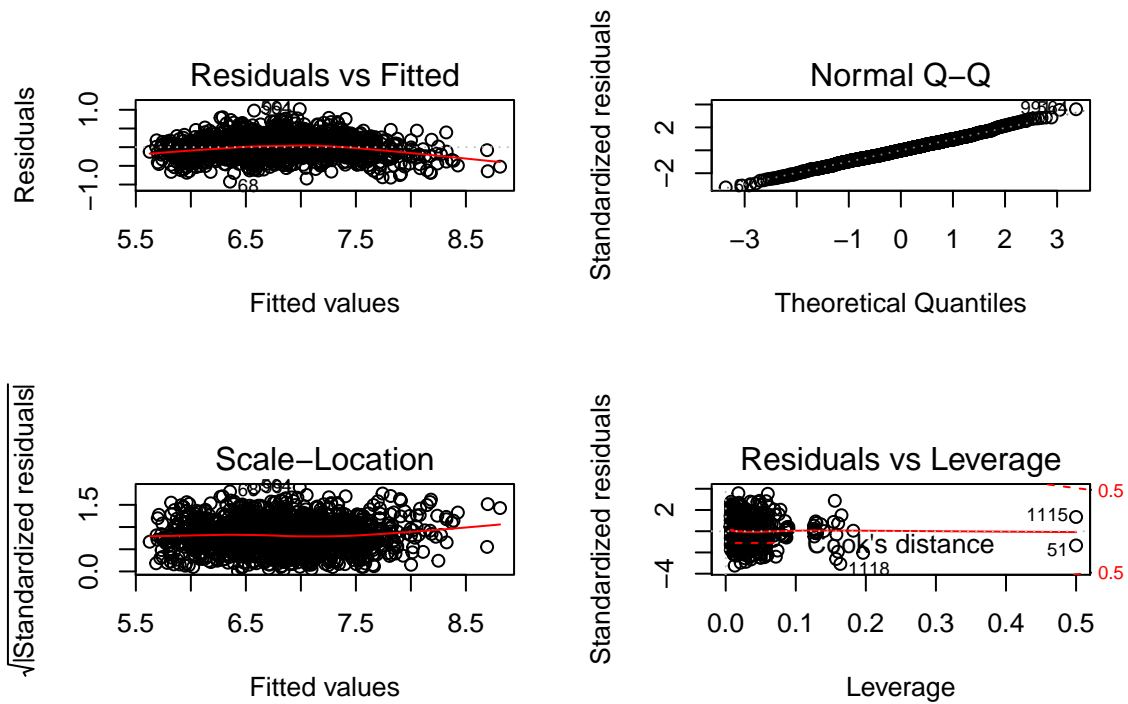
## Single term deletions
##
## Model:
## log(Price) ~ TypeName + Inches + Ram + OpSys + Weight + Frequenza +
## Pixel + GpuCompany + MemoriaSSD + SolidStateDisk + TotalMemory +
## Aggregated_Company
##              Df Sum of Sq  RSS    AIC  F value    Pr(>F)
## <none>                    104.02 -3227.8
## TypeName                 5  17.2030 121.22 -3038.4  42.0072 < 2.2e-16 ***
## Inches                   1   0.3602 104.38 -3225.3   4.3982  0.03617 *
## Ram                      1  19.0067 123.03 -3011.1 232.0592 < 2.2e-16 ***
## OpSys                    7  10.0159 114.03 -3122.0  17.4697 < 2.2e-16 ***
## Weight                   1   0.1847 104.20 -3227.5   2.2556  0.13338
## Frequenza                1  15.1135 119.13 -3053.0 184.5257 < 2.2e-16 ***
## Pixel                    1   4.8634 108.88 -3170.2  59.3792 2.608e-14 ***
## GpuCompany               3   5.6591 109.68 -3164.8  23.0314 1.610e-14 ***
## MemoriaSSD               1   1.6403 105.66 -3209.4  20.0266 8.322e-06 ***
## SolidStateDisk           1   4.2673 108.29 -3177.4  52.1009 9.048e-13 ***
## TotalMemory              1   2.5966 106.62 -3197.7  31.7023 2.210e-08 ***
## Aggregated_Company       8   9.0753 113.09 -3134.8  13.8504 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

coefplot(lm_full, intercept=FALSE)
```

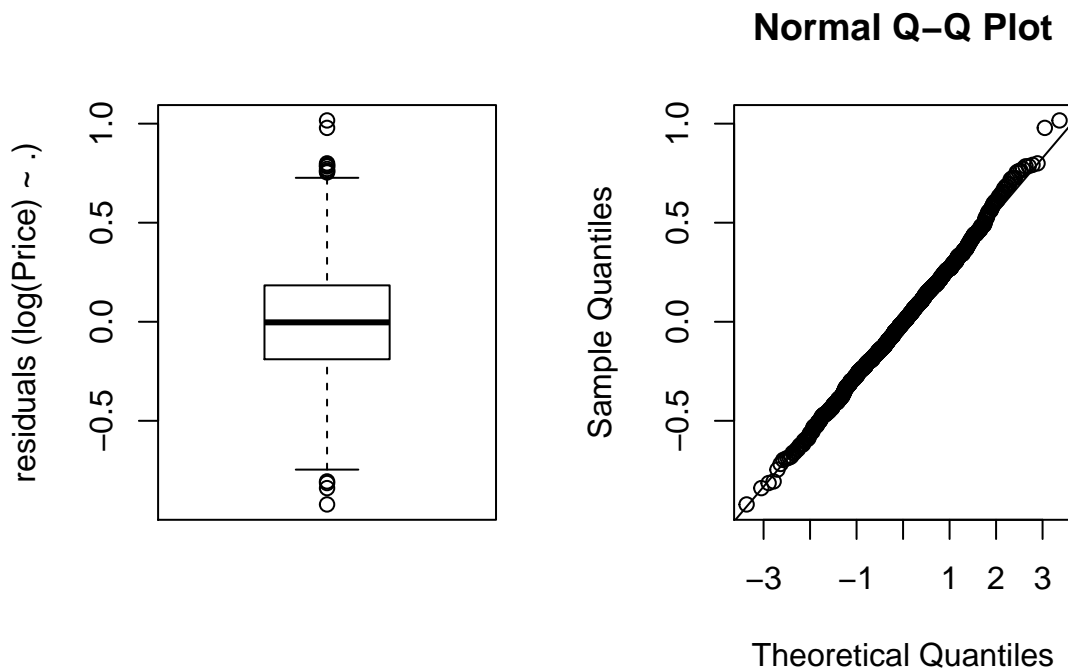
Coefficient Plot



```
par(mfrow=c(2,2))
plot(lm_full)
```



```
par(mfrow=c(1,1))
par(mfrow=c(1,2))
boxplot(lm_full$residuals, ylab="residuals (log(Price) ~ .)")
qqnorm(lm_full$residuals);qqline(lm_full$residuals)
```



```
#normality tests
ad.test(lm_full$residuals)
```

```
##
## Anderson-Darling normality test
##
```

```
## data: lm_full$residuals
## A = 0.47935, p-value = 0.2341
shapiro.test(lm_full$residuals)

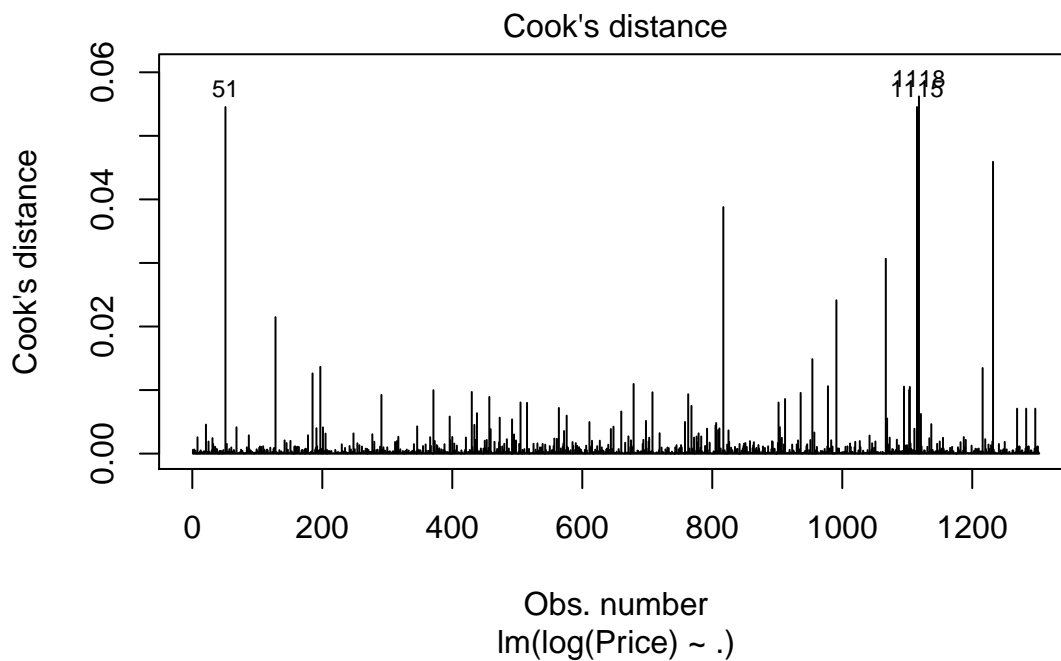
##
## Shapiro-Wilk normality test
##
## data: lm_full$residuals
## W = 0.99827, p-value = 0.2046
```

APPENDIX

A look over outliers

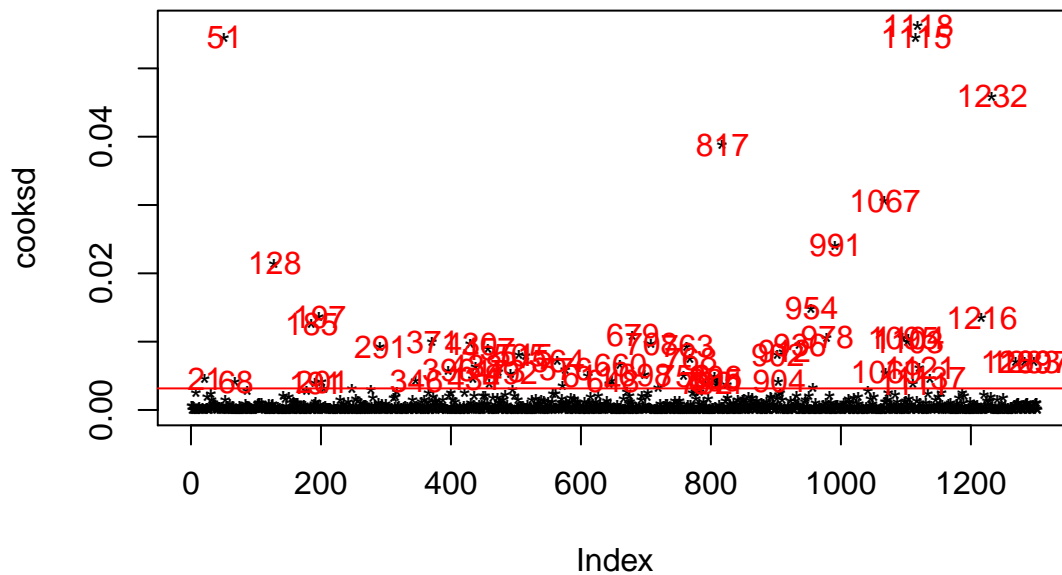
```
cooksda <- cooks.distance(lm_full) #Cook's Distance
cooksda=data.frame(cooksda)
summary(cooksda)
```

```
##      Min.   1st Qu.   Median     Mean   3rd Qu.     Max.    NA's
## 0.0000000 0.0000602 0.0002372 0.0009733 0.0006906 0.0562069      1
cutoff <- 4/((nrow(data)-length(lm_full$coefficients)-2)) # identify D values > 4/(n-k-1)
plot(lm_full, which=4, cook.levels=cutoff)# Cook's D plot
```



```
plot(cooksda, pch="*", cex=1, main="Influential Obs by Cooks distance") # plot cook's distance
abline(h = cutoff, col="red") # add cutoff line
text(x=1:length(cooksda)+1, y=cooksda, labels=ifelse(cooksda>4*mean(cooksda, na.rm=T),names(cooksda),""), col="red")#add labels
```

Influential Obs by Cooks distance



```
#extract influential obs
influential <- as.numeric(names(cooks)[(cooks > cutoff)]) # influential row numbers
influ=data.frame(data[cooks > cutoff, ])
filtered_data <- data[ !(row.names(data) %in% c(influential)), ]
dim(influ); dim(data); dim(filtered_data)
```

```
## [1] 68 13
```

```
## [1] 1303 13
```

```
## [1] 1236 13
```

```
#removed outliers
```

```
lm_full_t_no_OUTliers = lm(log(Price) ~ ., data = filtered_data)
summary(lm_full_t_no_OUTliers)
```

```
##
```

```
## Call:
```

```
## lm(formula = log(Price) ~ ., data = filtered_data)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max
## -0.61803 -0.17506 -0.00775  0.17186  0.77302
```

```
##
```

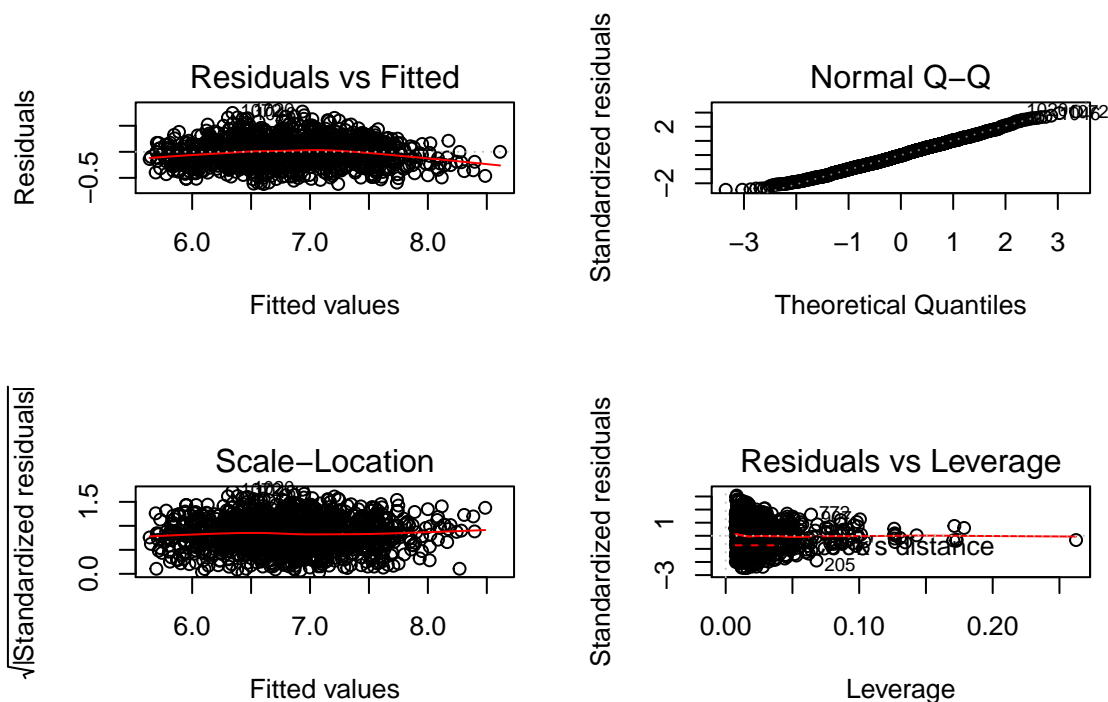
```
## Coefficients: (1 not defined because of singularities)
```

```
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    5.657e+00  1.536e-01  36.824 < 2e-16 ***
## TypeNameGaming -1.166e-01  4.534e-02  -2.573  0.01021 *
## TypeNameNetbook -3.902e-01  7.902e-02  -4.938  8.99e-07 ***
## TypeNameNotebook -2.145e-01  3.057e-02  -7.018  3.74e-12 ***
## TypeNameUltrabook  7.777e-02  3.263e-02   2.383  0.01731 *
## TypeNameWorkstation  2.963e-01  6.291e-02   4.710  2.77e-06 ***
## Inches        -3.568e-02  1.167e-02  -3.058  0.00228 **
## Ram           3.731e-02  2.564e-03  14.555 < 2e-16 ***
## OpSysLinux     -5.027e-02  7.745e-02  -0.649  0.51640
## OpSysMac OS X  7.106e-01  1.158e-01   6.139  1.13e-09 ***
## OpSysmacOS     4.042e-01  1.029e-01   3.929  9.00e-05 ***
## OpSysNo OS    -2.267e-01  7.859e-02  -2.884  0.00400 **
## OpSysWindows 10  7.851e-02  7.050e-02   1.114  0.26571
## OpSysWindows 10 S  2.550e-01  1.295e-01   1.969  0.04916 *
## OpSysWindows 7   3.791e-01  8.149e-02   4.652  3.65e-06 ***
```



```
## Weight          3.921e-02  2.627e-02   1.493  0.13582
## Frequenza       2.577e-01  1.745e-02  14.763 < 2e-16 ***
## Pixel           6.074e-08  6.667e-09   9.111 < 2e-16 ***
## GpuCompanyARM    3.010e-01  2.685e-01   1.121  0.26259
## GpuCompanyIntel  1.636e-01  2.450e-02   6.675  3.76e-11 ***
## GpuCompanyNvidia 2.450e-01  2.773e-02   8.835 < 2e-16 ***
## MemoriaSSD       3.895e-04  9.203e-05   4.232  2.49e-05 ***
## SolidStateDiskTrue 2.479e-01  2.826e-02   8.774 < 2e-16 ***
## TotalMemory      1.621e-04  2.316e-05   7.000  4.24e-12 ***
## Aggregated_CompanyApple NA      NA      NA      NA
## Aggregated_CompanyAsus  7.400e-02  3.467e-02   2.135  0.03298 *
## Aggregated_CompanyDell  2.272e-01  3.102e-02   7.326  4.35e-13 ***
## Aggregated_CompanyHP    2.369e-01  3.171e-02   7.472  1.52e-13 ***
## Aggregated_CompanyLenovo 1.443e-01  3.162e-02   4.562  5.58e-06 ***
## Aggregated_CompanyMSI   1.640e-01  5.141e-02   3.190  0.00146 **
## Aggregated_CompanyOthers 2.303e-02  5.698e-02   0.404  0.68613
## Aggregated_CompanyRazer  2.530e-01  2.614e-01   0.968  0.33331
## Aggregated_CompanyToshiba 3.475e-01  4.710e-02   7.378  2.98e-13 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2529 on 1204 degrees of freedom
## Multiple R-squared:  0.8244, Adjusted R-squared:  0.8198
## F-statistic: 182.3 on 31 and 1204 DF, p-value: < 2.2e-16
```

```
par(mfrow=c(2,2))
plot(lm_full_t_no_OUTliers)
```



```
library(car)
ncvTest(lm_full_t_no_OUTliers)

## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 0.001667699, Df = 1, p = 0.96743

null = lm(log(Price) ~ 1, data = filtered_data)
full = lm(log(Price) ~ ., data = filtered_data)
library(MASS)
lm_fit = stepAIC(null, scope = list(upper = full), direction = "both", trace = FALSE)
```

```
summary(lm_fit)
```

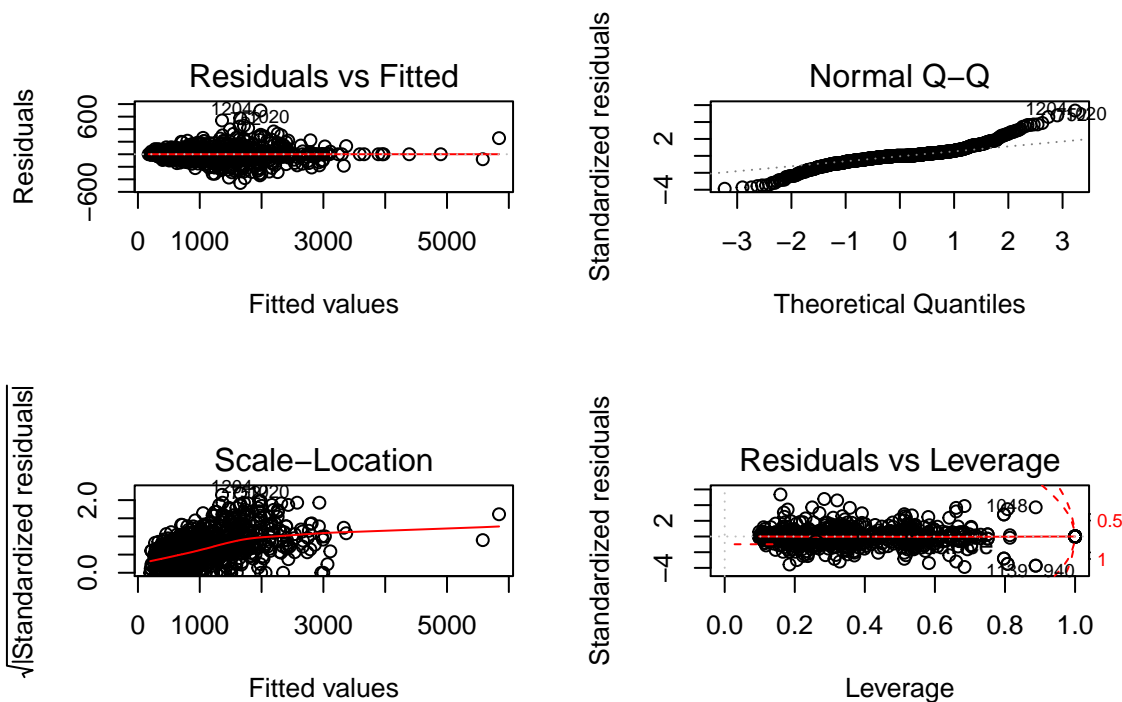
```
##
## Call:
## lm(formula = log(Price) ~ Ram + TypeName + SolidStateDisk + Frequenza +
##     OpSys + Pixel + Aggregated_Company + GpuCompany + TotalMemory +
##     MemoriaSSD + Inches + Weight, data = filtered_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.61803 -0.17506 -0.00775  0.17186  0.77302
##
## Coefficients: (1 not defined because of singularities)
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    5.657e+00  1.536e-01  36.824 < 2e-16 ***
## Ram            3.731e-02  2.564e-03  14.555 < 2e-16 ***
## TypeNameGaming -1.166e-01  4.534e-02  -2.573  0.01021 *
## TypeNameNetbook -3.902e-01  7.902e-02  -4.938  8.99e-07 ***
## TypeNameNotebook -2.145e-01  3.057e-02  -7.018  3.74e-12 ***
## TypeNameUltrabook 7.777e-02  3.263e-02   2.383  0.01731 *
## TypeNameWorkstation 2.963e-01  6.291e-02   4.710  2.77e-06 ***
## SolidStateDiskTrue 2.479e-01  2.826e-02   8.774 < 2e-16 ***
## Frequenza      2.577e-01  1.745e-02  14.763 < 2e-16 ***
## OpSysLinux     -5.027e-02  7.745e-02  -0.649  0.51640
## OpSysMac OS X   7.106e-01  1.158e-01   6.139  1.13e-09 ***
## OpSysmacOS      4.042e-01  1.029e-01   3.929  9.00e-05 ***
## OpSysNo OS     -2.267e-01  7.859e-02  -2.884  0.00400 **
## OpSysWindows 10 7.851e-02  7.050e-02   1.114  0.26571
## OpSysWindows 10 S 2.550e-01  1.295e-01   1.969  0.04916 *
## OpSysWindows 7  3.791e-01  8.149e-02   4.652  3.65e-06 ***
## Pixel          6.074e-08  6.667e-09   9.111 < 2e-16 ***
## Aggregated_CompanyApple NA      NA      NA      NA
## Aggregated_CompanyAsus 7.400e-02  3.467e-02   2.135  0.03298 *
## Aggregated_CompanyDell 2.272e-01  3.102e-02   7.326  4.35e-13 ***
## Aggregated_CompanyHP  2.369e-01  3.171e-02   7.472  1.52e-13 ***
## Aggregated_CompanyLenovo 1.443e-01  3.162e-02   4.562  5.58e-06 ***
## Aggregated_CompanyMSI 1.640e-01  5.141e-02   3.190  0.00146 **
## Aggregated_CompanyOthers 2.303e-02  5.698e-02   0.404  0.68613
## Aggregated_CompanyRazer 2.530e-01  2.614e-01   0.968  0.33331
## Aggregated_CompanyToshiba 3.475e-01  4.710e-02   7.378  2.98e-13 ***
## GpuCompanyARM      3.010e-01  2.685e-01   1.121  0.26259
## GpuCompanyIntel     1.636e-01  2.450e-02   6.675  3.76e-11 ***
## GpuCompanyNvidia    2.450e-01  2.773e-02   8.835 < 2e-16 ***
## TotalMemory        1.621e-04  2.316e-05   7.000  4.24e-12 ***
## MemoriaSSD         3.895e-04  9.203e-05   4.232  2.49e-05 ***
## Inches            -3.568e-02  1.167e-02  -3.058  0.00228 **
## Weight             3.921e-02  2.627e-02   1.493  0.13582
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2529 on 1204 degrees of freedom
## Multiple R-squared:  0.8244, Adjusted R-squared:  0.8198
## F-statistic: 182.3 on 31 and 1204 DF, p-value: < 2.2e-16
drop1(lm_fit, test = 'F')
```

```
## Single term deletions
##
## Model:
## log(Price) ~ Ram + TypeName + SolidStateDisk + Frequenza + OpSys +
##     Pixel + Aggregated_Company + GpuCompany + TotalMemory + MemoriaSSD +
##     Inches + Weight
```

```
##           Df Sum of Sq   RSS     AIC  F value    Pr(>F)
## <none>                76.981 -3367.2
## Ram                1   13.5450  90.526 -3168.9 211.8485 < 2.2e-16 ***
## TypeName           5   13.0233  90.004 -3184.1  40.7378 < 2.2e-16 ***
## SolidStateDisk      1    4.9216  81.902 -3292.6  76.9749 < 2.2e-16 ***
## Frequenza           1   13.9357  90.916 -3163.6 217.9593 < 2.2e-16 ***
## OpSys               6    9.8885  86.869 -3229.9  25.7766 < 2.2e-16 ***
## Pixel              1    5.3071  82.288 -3286.8  83.0054 < 2.2e-16 ***
## Aggregated_Company  8    7.6931  84.674 -3265.5  15.0404 < 2.2e-16 ***
## GpuCompany          3    5.2492  82.230 -3291.7  27.3661 < 2.2e-16 ***
## TotalMemory         1    3.1331  80.114 -3319.9  49.0032 4.235e-12 ***
## MemoriaSSD          1    1.1450  78.126 -3351.0  17.9087 2.494e-05 ***
## Inches              1    0.5978  77.578 -3359.7   9.3505 0.002278 **
## Weight              1    0.1424  77.123 -3367.0   2.2277 0.135818
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

no log model and a log justification

```
lm_full_no_log = lm(Price ~ ., data = data1)
#summary(lm_full_no_log)
par(mfrow=c(2,2))
plot(lm_full_no_log)
```



```
ad.test(lm_full_no_log$residuals)
```

```
##
## Anderson-Darling normality test
##
## data:  lm_full_no_log$residuals
## A = 113.24, p-value < 2.2e-16
```

```
shapiro.test(lm_full_no_log$residuals)
```

```
##
## Shapiro-Wilk normality test
##
## data:  lm_full_no_log$residuals
## W = 0.77262, p-value < 2.2e-16
```

```
library(MASS)
boxcoxreg1<-boxcox(lm_full_no_log, plotit=T) #to justify log correction

#lambda=boxcoxreg1$x[which.max(boxcoxreg1$y)]
#lambda #not exactly lambda= 0 but compatible, one could also apply  $y'=((y^\lambda) - 1) / \lambda$ 
```

