

Module 9 Self Check

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1 Probabilities

1.1 Safe?

$$P(\text{Safe} = \text{Yes}) = 7/15 = 0.467$$

$$P(\text{Safe} = \text{No}) = 8/15 = 0.533$$

1.2 Shape

$$P(\text{Shape} = \text{Round} \ \& \ \text{Safe} = \text{Yes}) = 4/7 = 0.571$$

$$P(\text{Shape} = \text{Round} \ \& \ \text{Safe} = \text{No}) = 3/7 = 0.429$$

$$P(\text{Shape} = \text{Square} \ \& \ \text{Safe} = \text{Yes}) = 3/8 = 0.375$$

$$P(\text{Shape} = \text{Square} \ \& \ \text{Safe} = \text{No}) = 5/8 = 0.625$$

1.3 Size

$$P(\text{Size} = \text{Large} \ \& \ \text{Safe} = \text{Yes}) = 6/8 = 0.75$$

$$P(\text{Size} = \text{Large} \ \& \ \text{Safe} = \text{No}) = 2/8 = 0.25$$

$$P(\text{Size} = \text{Small} \ \& \ \text{Safe} = \text{Yes}) = 1/7 = 0.143$$

$$P(\text{Size} = \text{Small} \ \& \ \text{Safe} = \text{No}) = 6/7 = 0.857$$

1.4 Color

$$P(\text{Color} = \text{Blue} \ \& \ \text{Safe} = \text{Yes}) = 0/3 = 0$$

$$P(\text{Color} = \text{Blue} \ \& \ \text{Safe} = \text{No}) = 3/3 = 1$$

$$P(\text{Color} = \text{Green} \ \& \ \text{Safe} = \text{Yes}) = 4/6 = 0.667$$

$$P(\text{Color} = \text{Green} \ \& \ \text{Safe} = \text{No}) = 2/6 = 0.333$$

$$P(\text{Color} = \text{Red} \ \& \ \text{Safe} = \text{Yes}) = 3/6 = 0.5$$

$$P(\text{Color} = \text{Red} \ \& \ \text{Safe} = \text{No}) = 3/6 = 0.5$$

2 Normalized Probability Example

$$\begin{aligned} P(\text{Safe} = \text{Yes} \ \& \ \text{Shape} = \text{square} \ \& \ \text{Size} = \text{large} \ \& \ \text{Color} = \text{red}) = \\ \frac{P(\text{Safe}=\text{Yes}) * (P(\text{Shape}=\text{square} \ \& \ \text{Safe}=\text{Yes}) * P(\text{Size}=\text{large} \ \& \ \text{Safe}=\text{Yes}) * P(\text{Color}=\text{red} \ \& \ \text{Safe}=\text{Yes}))}{P(\text{Shape}=\text{square} \ \& \ \text{Size}=\text{Large} \ \& \ \text{Color}=\text{Red})} = \\ 0.467 * 0.375 * 0.75 * 0.5 = 0.066 \end{aligned}$$

$$\begin{aligned} P(\text{Safe} = \text{No} \ \& \ \text{Shape} = \text{square} \ \& \ \text{Size} = \text{large} \ \& \ \text{Color} = \text{red}) = \\ \frac{P(\text{Safe}=\text{No}) * (P(\text{Shape}=\text{square} \ \& \ \text{Safe}=\text{No}) * P(\text{Size}=\text{large} \ \& \ \text{Safe}=\text{No}) * P(\text{Color}=\text{red} \ \& \ \text{Safe}=\text{No}))}{P(\text{Shape}=\text{square} \ \& \ \text{Size}=\text{Large} \ \& \ \text{Color}=\text{Red})} = \\ 0.533 * 0.625 * 0.25 * 0.5 = 0.0415 \end{aligned}$$

$$P(\text{Safe} = \text{Yes} \ \& \ \text{Shape} = \text{square} \ \& \ \text{Size} = \text{large} \ \& \ \text{Color} = \text{red}) = \frac{0.066}{0.066+0.0415} = 0.612$$

$$P(\text{Safe} = \text{No} \ \& \ \text{Shape} = \text{square} \ \& \ \text{Size} = \text{large} \ \& \ \text{Color} = \text{red}) = \frac{0.0415}{0.066+0.0415} = 0.388$$