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ECN2316

## Lecture 15: Monopoly Regulation and Monopolistic Competition

Finding MR in a monopoly

$$Q_d = 10 - 2P, \text{ what is MR? } Q_d = 10 - 2P$$

$$TR = PQ = Q \cdot \left( \frac{10-Q}{2} \right) \\ = \frac{10Q - Q^2}{2}$$

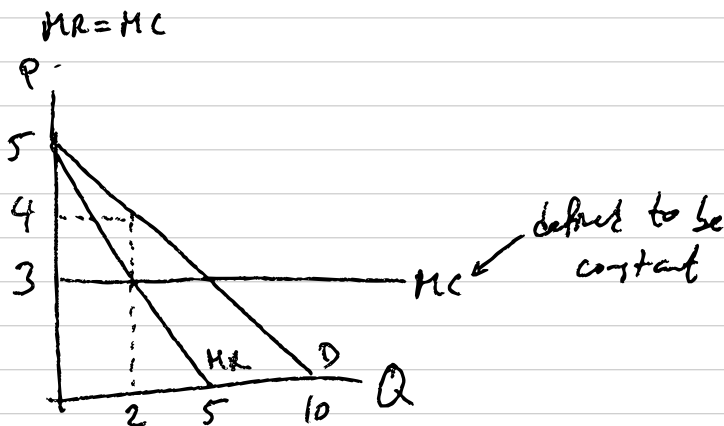
$$= 5Q - \frac{1}{2}Q^2 \quad \frac{\partial TR}{\partial Q}$$

$$Q_d + 2P = 10 \\ P = \frac{10 - Q_d}{2} \\ \uparrow \text{inverse demand}$$

$$MR = 5 - Q$$

$$MC = 3 \Rightarrow \text{what is } P_{\text{ymc}}?$$

$$\underbrace{5 - Q}_{MR=MC} = 3 \Rightarrow Q = 2, P = \frac{10 - 2}{2} = 4$$



Example:

$$P = 60 - 2Q$$

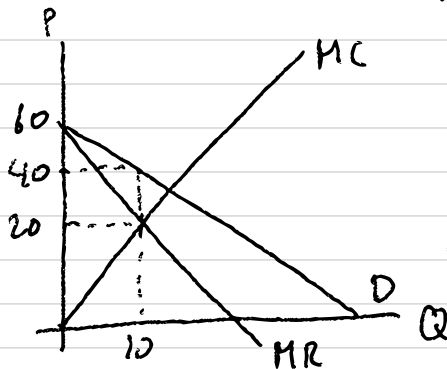
$$TC = 50 + Q^2$$

What are CS and PS in monopoly?

$$TR = Q(60 - 2Q) \quad MC = 2Q$$
$$= 60Q - 2Q^2$$

$$MR = 60 - 4Q$$

$$60 - 4Q = 2Q \Rightarrow Q = 10, P = 40$$



$$CS = \frac{1}{2}(20)(10)$$
$$= 100$$

$$PS = 20(10) + \frac{1}{2}(20)(10)$$
$$= 300$$

or

$$TR - VC$$
$$= PQ - Q^2$$
$$= 400 - 100$$
$$= 300$$

Can you figure out  
how many  
firms  
exit?

$$P = 60 - 2Q, \quad TC = 50 + Q^2$$

9 identical perfectly competitive firms

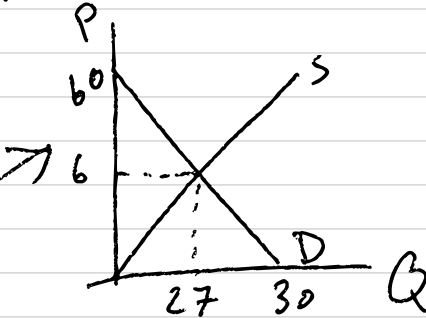
What are CS and PS here?

• Find firm supply

$$MC = 2q, \text{ since } P = MC \text{ in P.C.}$$

$$P = 2q \Rightarrow q_s = \frac{P}{2} \Rightarrow Q_s = 4.5P$$

Market:



Market Demand

$$P = 60 - 2Q$$

$$P + 2Q = 60$$

$$2Q = 60 - P$$

$$Q_d = 30 - 0.5P$$

$$30 - 0.5P = 4.5P \Rightarrow P = 6$$

$$CS = \frac{1}{2}(27)(54) = 729$$

$$PS = \frac{1}{2}(6)(27) = 81$$

$$\left. \begin{array}{l} CS = 729 \\ PS = 81 \end{array} \right\} TS = 810$$

## Cost-Plus Pricing

To maximize profit - need to know MC,  $\epsilon_d$

if  $MR = MC$ , we can show:

$$P = \frac{MC}{\left(1 + \frac{1}{\epsilon_d}\right)}$$

Maximizing Profit: set derivative of profit = 0

$$\pi = PQ - TC$$

$$\frac{\partial \pi}{\partial q} = \underbrace{\frac{dP}{dq} \cdot q + P}_{\text{product rule}} - MC = 0$$

Recall!  $\epsilon_d = \frac{P}{Q} \frac{dQ}{dP}$

$$\left\{ \frac{\frac{dP}{dq} \cdot \frac{q}{P} + 1}{\frac{1}{\epsilon_d P}} \right\} = \frac{MC}{P} \quad \left\{ \frac{1}{\epsilon} + 1 = \frac{MC}{P} \right.$$

$$\frac{P - MC}{P} = \frac{1}{-\epsilon_P}$$

$$\frac{1}{\epsilon} = \frac{MC}{P} - \frac{P}{P}$$

$$\frac{1}{\epsilon} = \frac{MC - P}{P} = \frac{-(P - MC)}{P}$$

$$P = \frac{MC}{1 + \frac{1}{\epsilon_d}}$$

$$\text{Lerner Index} = \frac{P - MC}{P} = \frac{-1}{\epsilon_d} = L$$

$\nwarrow$  markup relative to market clearing P

## Natural Monopoly

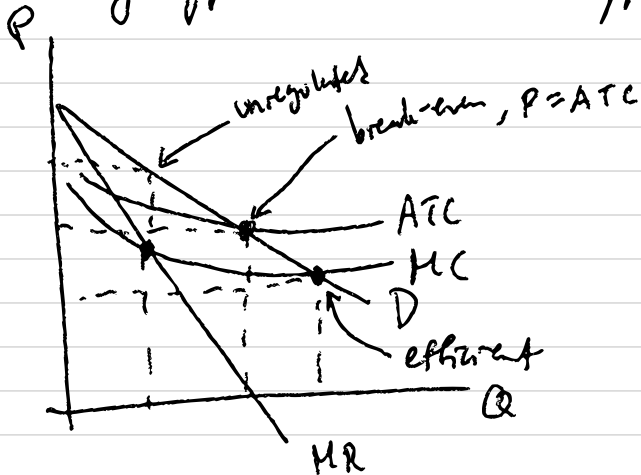
- one firm makes sense
- produces output at a lower ATC than if we had 2+ firms

## Cost Structure

- high fixed costs
- heavy economies of scale

Ex.

- utility suppliers (ie. a water supplier)



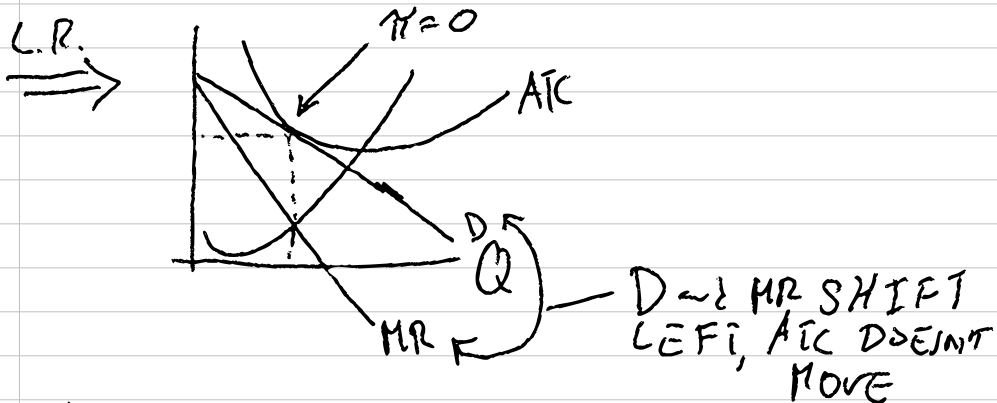
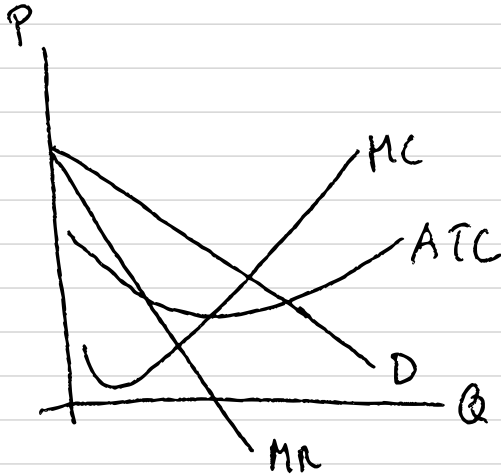
## Anti-trust Law

Prohibitions against:

- Parallel conduct - implicit collusion
- Predatory pricing
- Price fixing
- Price discrimination
- etc...

## Monopolistic Competition

- differentiated products
- many firms
- free entry + exit in LR
- Profit in LR = 0



## Oligopoly

- few firms
- high barriers

Monopolistically competitive firm behaves like a monopolist

-  $MR = MC$

- choose highest possible price

in LR -  $D \downarrow \frac{1}{2}$  at competitive