



Birzeit University
Faculty of Engineering and Technology
Department of Electrical and Computer Engineering
First Semester – 2023/2024
ENCS4320 - Applied Cryptography

Homework # 1

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Date :8/12/2023

Section #2



Q1:

Since we only have the cyphertext and we want to know the key and the plaintext

There are two ways to identify them: The first way is to find the most frequent letter in the sentence (we know that the most frequent letter is E): So, we know the amount of displacement between the repeated letter and the letter E, and we try to move the sentence according to ironing. If the resulting sentence is understandable, it is very likely that we have arrived at the solution.

If the answer is not understood in the sentence: We work on the other method, which is to try the shift from 1 to 26, and the resulting clear sentence is the plaintext and the key.

The highest recurring letter is the H >>>The space between H and E = 3

So, the Key=3;

$$M = (C - K) \% 26$$

	#		Rot-K		#		Rot-K
I	2	$(2-3)\%26$	F	Y	2	$(24-3)\%26$	V
U	3	$(20-3)\%26$	R	V	1	$(21-3)\%26$	S
R	2	$(17-3)\%26$	O	D	2	$(3-3)\%26$	A
P	1	$(15-3)\%26$	M	O	3	$(14-3)\%26$	L
W	4	$(22-3)\%26$	T	Z	1	$(25-3)\%26$	W
K	2	$(10-3)\%26$	H	Q	1	$(16-3)\%26$	N
H	9	$(7-3)\%26$	E	E	1	$(4-3)\%26$	B
L	3	$(11-3)\%26$	I	U	3	$(20-3)\%26$	R
				S	1	$(18-3)\%26$	P

plainText is ?

From The River To The Sea Palestine
Will Be Free

جانب ال
البحر
سوا البحر

Q2:

Q2?

① number of possible Keys = 2^{56}
Test $\Rightarrow 4.2 \times 16 \times 10^9$ per second

$$\begin{aligned} \text{Time in year} &= \frac{\text{number possible Key}}{\frac{\text{Key Test per second}}{60 \times 60 \times 24 \times 365}} \\ &= \frac{2^{56}}{\frac{4.2 \times 10^9 \times 16}{60 \times 60 \times 24 \times 365}} \end{aligned}$$

≈ 34 years

② number of possible Key = 2^{128}

$$\begin{aligned} \text{Time in year} &= \frac{2^{128}}{\frac{4.2 \times 16 \times 10^9}{60 \times 60 \times 24 \times 365}} \end{aligned}$$

$\approx 1.6 \times 10^9$ years

These results show that significantly increasing the key size enhances the security of the system against brute force attack, which is one of the main ways to improve the security of a cryptography-based system.

Q3:

In order for the OTP to be completely confidential, the length of the KEY must be greater than or equal to the length of the MESSAGE

$$K=M=C=\{0,1\}^n$$

If we apply the optimization according to Alice's suggestion, that is, if you remove the keys with all zeros from the key space, we have created an encryption that cannot show complete secrecy because the length of the key is one less than the length of the key, and this breaks the O T P conditions.

Therefore, this improvement completely breaks the confidentiality, making this modified password worse than the original.

Q4:

Q4 a) $(23+28) \bmod 29$
 $= (23 \bmod 29 + 28 \bmod 29) \bmod 29$
 $= (23 + 28) \bmod 29$
 $= 51 \bmod 29$
 $= 22$

51 = 29g + R
51 = 29x1 + R
R = 22

Q4 b) $(3 - 11) \bmod 9$
 $= (3 \bmod 9 - 11 \bmod 9) \bmod 9$
 $= (3 + 7) \bmod 9$
 $= 1$

-11 mod 9
 $-11 = 9x - 2 + R$
R = 7

10 mod 9
 $10 = 9x1 + R$
R = 1

$$\begin{aligned}
 \textcircled{c} \quad & 15 \times 29 \pmod{13} \\
 &= (15 \pmod{13} \times 29 \pmod{13}) \pmod{13} \\
 &= (2 \times 3) \pmod{13} \\
 &= 6
 \end{aligned}$$

$$\begin{array}{l}
 15 \pmod{13} \\
 15 = 13 \times 1 + R \\
 R = 2 \\
 29 \pmod{13} \\
 29 = 13 \times 2 + R \\
 R = 3
 \end{array}$$

$$\begin{aligned}
 \textcircled{d} \quad & 16 \times 13 \pmod{26} \\
 &= (16 \pmod{26} \times 13 \pmod{26}) \pmod{26} \\
 &= (16 \times 13) \pmod{26} \\
 &= 208 \pmod{26} \\
 &= 0
 \end{aligned}$$

$$\begin{array}{l}
 208 = 26 \times 8 + 0 \\
 R = 0
 \end{array}$$

$$\textcircled{p} \quad 2^5 \pmod{31}$$

$$32 = 31q + R$$

$$\boxed{R = 1}$$

$$p) \quad 2^{103} \pmod{31}$$

$$\begin{aligned}
 & (2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times \\
 & 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^5 \times 2^3) \\
 & \times \pmod{31}
 \end{aligned}$$

$$= ((1 \times \dots \times 1) \times 2^3 \pmod{31}) \pmod{31}$$

$$\text{of } 20$$

$$= (1 \times 8) \pmod{31}$$

$$= 8$$

Q5:

$$Q5 \quad C \oplus M = K$$

$$(a) \text{ plaintext} = \text{thirst}$$

$$= 111 \ 011 \ 010 \ 101 \ 110 \ 111$$

$$\text{Ciphertext} = \text{KITLKE}$$

$$= 011 \ 010 \ 111 \ 100 \ 011 \ 000$$

$$\text{Key} = C \oplus M$$

$$= 100 \ 001 \ 101 \ 001 \ 101 \ 111$$

$$= \text{Lhrhrt}$$

$$(b) \text{ plaintext} = \text{hikers}$$

$$= 001 \ 010 \ 011 \ 000 \ 101 \ 110$$

$$\text{Key} = C \oplus M$$

$$= 010 \ 000 \ 100 \ 100 \ 110 \ 110$$

$$= \text{ie11ss}$$

Q6:

Q: 6

a) No, it doesn't work with either OR or And.

* in And for example if message and key one bit.

m	k	m/k
0	0	0
0	1	0
1	0	0
1	1	1

mork

m

k

mork

في مرحلة ال Dec لا يوجد شيء حتى
يكون الاوتبوت المسح و حتى انكي

So security is also broken.

- وايضا عندما يكون الاوتبوت واحد يعرف الشخص
انه Key and message واحد.

* also in OR

m	k	m v k
0	0	0
0	1	1
1	0	1
1	1	1

mork

k

m

mork

لا يمكن الحصول على Dec لانه لا يوجد شيء حتى
الى التصير بين m/k

ايضا عندما يكون الاوتبوت هفر معروف ان كلاهما
المسح وانكي هفر.

b) No, this does not have the security guarantees of a one-time pad

K	m	$E(K, M)$
00	00	00
01	00	01
10	00	10
00	01	01
01	01	00
10	01	11
00	10	10
01	10	11
10	10	00

* نلاحظ هنا انه عندما يكون $E(K, M) = 11$
 يكون دائماً $c = 1$ ليس هنو وهذا يعطي
 cipher attack على النص السري ال

$$\underline{\text{So}} \Pr[M=m] \neq \Pr[M=m/C=c]$$

so this not perfect security

(C) To solve problem in b we need an encryption Algorithm that ensures equal probability for each possible outcome.
 example we need output cipher just $\{0, 1, 2\}$ because has an equal probability of occurring and this meeting the requirements of perfect secrecy.

So $E^*(K, M) = M + K \pmod{3}$

K	M	$E^*(K, M)$
00	00	00
01	00	01
10	00	10
00	01	01
01	01	10
10	01	00
00	10	10
01	10	00
10	10	01

$$\text{pr}[M=m] = \text{pr}[M=m/C=c]$$

$$\text{pr}(b'=b) = \frac{1}{2}$$

Q7:

Shift cipher:

for a shift cipher with a standard English alphabet of 26 letters, the key space (number of possible keys) is 2^{26} because there are 26 possible shift values, the encryption of a character $m \in \{0, 1, \dots, 25\}$ is $c = m + k \bmod 26$ for some $k \in \{0, 1, \dots, 25\}$. Accordingly, and the key $k = c - m \bmod 26$.

Substitution cipher

It is better than shift cipher , but It can be hacked by using frequency /analysis to determine the most frequently used letters in the target language , There may be recurring patterns in the ciphertexts that can be detected

Vigenère ciphers

To execute a chosen-plaintext attack on the Vigenère cipher, it's crucial to acquire a ciphertext generated from a message with a length equal to the key length (t). Subsequently, the analysis is performed position-wise, treating each position as an independent Caesar cipher. The comparison of known plaintext and corresponding ciphertext at each position allows for the determination of the shift value for that part of the key.

The success of the attack is contingent upon the length and randomness of the key. A longer, more random key enhances the cipher's resistance to decryption, requiring a substantial amount of chosen plaintext to accurately deduce the key and compromise the encryption.

If we compare them

Shift coding:

Strengths: Simple and easy to understand.

Weaknesses: Vulnerable to brute force attacks due to limited key space.
Not suitable for high security applications.

Alternative encryption:

Strengths: Provides better security than base shift encryption. It can resist simple frequency analysis.

Weaknesses: Still vulnerable to more advanced frequency analysis and pattern recognition.

Vigenère encryption:

Strengths: Improved security compared to conversion and replacement ciphers. Using the keyword provides contrast.

Weaknesses: Vulnerable to plaintext attacks, especially with shorter, less random keys. Longer keys increase security but also complexity.

Q8:

When period of 2 or 4, determining the password is not possible due to the equal likelihood of keys.

⑧ $K \in \{0, 1, \dots, 25\}$

possible 1 \Rightarrow $\begin{matrix} a & b & c & d \\ 0 & 1 & 2 & 3 \end{matrix} \Rightarrow \{K, K+1, K+2, K+3\}$

possible 2 \Rightarrow $\begin{matrix} b & e & d & g \\ 1 & 4 & 3 & 6 \end{matrix} \Rightarrow \{K+1, K+4, K+3, K+6\}$

□ period 2

possible Encryption

$\begin{matrix} a & b & c & d \\ a & b & a & b \\ \hline a & c & c & e \end{matrix}$	$\begin{matrix} b & e & d & g \\ b & e & b & e \\ \hline c & 1 & e & k \end{matrix}$
--	--

$C_0 = \{K, K+1, K+2, K+3\}$ $C_1 = \{K+1, K+4, K+3, K+6\}$

∴ $C_1 = C_0$ if $K=1$ *

$C_1 = \{K+1, K+3, K+1, K+3\}$

Since they are chosen from the uniform distribution over $(\{0, 1, \dots, 25\} \times \{0, 1, \dots, 25\})$ the adversary has no way of knowing which password was encrypted.

* Period 3?

$$C_0 = \{K_1, K_2+2, K_3+2, K_1+3\}$$

a	b	c	d
a	b	c	a
<hr/>			
a	c	e	d

$$C_1 = \{K_1+1, K_2+4, K_3+3, K_1+6\}$$

b	e	d	g
b	e	d	b
<hr/>			
c	i	g	h

These two sets are disjoint due to the relationship between the first and fourth cipher text character and thus one can deduce the password.

* Period 4

a	b	c	d
a	b	c	d
<hr/>			
a	c	c	g

With Key length the same as the message length, the Vigenere One-Time pad is perfectly secret so cannot be distinguished based on the ciphertext.

b	e	d	g
b	e	d	g
<hr/>			
c	i	e	m

- **Example:** When period of 2 or 4 probability 0.5 and this The attacker does not appreciate discrimination

$\frac{1}{2}$

a	b	c	d
a	b	a	b
a	c	c	e

b	e	d	g
a	b	a	b
b	f	d	h

$\frac{1}{2}$

جیب

a	b	c	d
b	e	b	e
b	f	d	h

b	e	d	g
b	e	b	e
c	i	e	k

جیب

$\frac{3}{4}$

a	b	c	d
a	b	c	a
a	c	c	d

b	e	d	g
a	b	c	a
b	f	d	g

$\frac{3}{4}$

جیب

a	b	c	d
b	e	d	b
b	f	d	e

b	e	d	g
b	e	d	b
c	i	e	h

جیب

$\frac{1}{2}$

a	b	c	d
a	b	c	d
a	c	c	g

b	e	d	g
a	b	c	d
b	f	d	j

$\frac{1}{2}$

جیب

a	b	c	d
b	e	d	g
b	f	d	j

b	e	d	g
b	e	d	g
c	i	e	m

جیب

Key length the same as the message length.

Vigenere cipher \rightarrow One-Time-Pad

So this perfectly secret

because that the two passwords cannot be distinguished based on the ciphertext.

Q10:

Results:

The method is through letter ratios, The largest number of letters in a word, the letter is its highest ratio, and so on.

```
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Q10:
Character Counts in the Ciphertext:
Char: R Count: 7
Char: J Count: 9
Char: O Count: 16
Char: G Count: 19
Char: M Count: 4
Char: Y Count: 3
Char: Q Count: 26
Char: H Count: 14
Char: V Count: 15
Char: B Count: 12
Char: W Count: 21
Char: F Count: 37
Char: P Count: 10
Char: D Count: 2
Char: Z Count: 7
Char: K Count: 3
Char: E Count: 4
Char: I Count: 9
Char: C Count: 3
Char: L Count: 17
Char: A Count: 3
Char: S Count: 2
Char: X Count: 1

Char: F Frequency: 0.151639 Expected: E
Char: Q Frequency: 0.106557 Expected: T
```

```
Char: F Frequency: 0.151639 Expected: E
Char: Q Frequency: 0.106557 Expected: T
Char: W Frequency: 0.0860656 Expected: A
Char: G Frequency: 0.0778689 Expected: O
Char: L Frequency: 0.0696721 Expected: I
Char: O Frequency: 0.0655738 Expected: N
Char: V Frequency: 0.0614754 Expected: S
Char: H Frequency: 0.057377 Expected: H
Char: B Frequency: 0.0491803 Expected: R
Char: P Frequency: 0.0409836 Expected: D
Char: J Frequency: 0.0368852 Expected: L
Characters with similar frequencies found:
11. Char: J Frequency: 0.0368852
12. Char: I Frequency: 0.0368852
Enter the number of your choice for decryption (or press Enter to use the default): 12
Char: R Frequency: 0.0286885 Expected: U
Characters with similar frequencies found:
13. Char: R Frequency: 0.0286885
14. Char: Z Frequency: 0.0286885
Enter the number of your choice for decryption (or press Enter to use the default): 13
Char: M Frequency: 0.0163934 Expected: W
Characters with similar frequencies found:
15. Char: M Frequency: 0.0163934
16. Char: E Frequency: 0.0163934
Enter the number of your choice for decryption (or press Enter to use the default): 15
Char: Y Frequency: 0.0122951 Expected: G
```



```

15. Char: M      Frequency: 0.0163934
16. Char: E      Frequency: 0.0163934
Enter the number of your choice for decryption (or press Enter to use the default): 15
Char: Y Frequency: 0.0122951      Expected: G
Characters with similar frequencies found:
17. Char: Y      Frequency: 0.0122951
18. Char: K      Frequency: 0.0122951
19. Char: C      Frequency: 0.0122951
20. Char: A      Frequency: 0.0122951
Enter the number of your choice for decryption (or press Enter to use the default): 20
Char: D Frequency: 0.00819672      Expected: V
Characters with similar frequencies found:
21. Char: D      Frequency: 0.00819672
22. Char: S      Frequency: 0.00819672
Enter the number of your choice for decryption (or press Enter to use the default): 22
Char: X Frequency: 0.00409836      Expected: J
Character Frequencies and Decrypted Letters:
Char: J Frequency: 0.0368852      Decrypted: I
Char: R Frequency: 0.0286885      Decrypted: R
Char: G Frequency: 0.0778689      Decrypted: O
Char: O Frequency: 0.0655738      Decrypted: N
Char: M Frequency: 0.0163934      Decrypted: M
Char: Q Frequency: 0.106557       Decrypted: T
Char: Y Frequency: 0.0122951      Decrypted: A
Char: H Frequency: 0.057377       Decrypted: H
Char: V Frequency: 0.0614754      Decrypted: S
Char: B Frequency: 0.0491803      Decrypted: R
Char: W Frequency: 0.0860656      Decrypted: A
Char: F Frequency: 0.151639       Decrypted: E
Char: P Frequency: 0.0409836      Decrypted: D

```

```

Char: Y Frequency: 0.0122951      Decrypted: A
Char: H Frequency: 0.057377       Decrypted: H
Char: V Frequency: 0.0614754      Decrypted: S
Char: B Frequency: 0.0491803      Decrypted: R
Char: W Frequency: 0.0860656      Decrypted: A
Char: F Frequency: 0.151639       Decrypted: E
Char: P Frequency: 0.0409836      Decrypted: D
Char: D Frequency: 0.00819672      Decrypted: S
Char: Z Frequency: 0.0286885      Decrypted: Z
Char: K Frequency: 0.0122951      Decrypted: K
Char: E Frequency: 0.0163934      Decrypted: E
Char: I Frequency: 0.0368852      Decrypted: I
Char: C Frequency: 0.0122951      Decrypted: C
Char: L Frequency: 0.0696721      Decrypted: I
Char: A Frequency: 0.0122951      Decrypted: A
Char: S Frequency: 0.00819672      Decrypted: S
Char: X Frequency: 0.00409836      Decrypted: J

```

The ciphertext:
JGRMQOYGHMVB JW RWQFPWHGFFDQGF PFZ RKBEEBJIZQQOCIBZKLF
AFGQVFZF W WEOGWOPFGFHWOLPHLRLOLFDMFGQWBLWBWQOLKF
WBYLBYLFLSFLJGRMQBOLWJVFPFWQVHQWFFPQOQVFPQOCFPOGFW
FJIGFQVHLHLROQVFGWJVFPFOLF H GQVQVFILEOGQILHQFQGIQVVS
FAFGBWQVHQWQWJWJVFPFWHGF IWHZZRQGBABHZQOCGFHX

Decrypted Text:
IORMTNAOHMSRIARATEDAHOEESTOEDEZRKREERIIZTTNCIRZKIEAEO
TSEZEAAENOANDEOEHANIDHIRINIESMEOTARIARATNIKEARAIRIAIESE
IORMTRNIAISEDEATSHTAEDTNTSEDNTCEDNOEAEIHOETSHIHIRTSE
OAISEDENIEHOTSTSEIENOTIHTTETOITSSNSEAEORATSHTAIISAISEDEA
HOEIAIHZZRTORARHZTNCOEHJ

C:\Users\Lenovo\Desktop\ConsoleApplication2\x64\Debug\ConsoleApplication2.exe (process 22592) exited with code 0.

The ciphertext:

JGRMQOYGHMVB JW RWQFPWHGFFDQGF PFZ RKBEEBJIZQQOCIBZKLF
AFGQVFZF W WEOGWOPFGFHWOLPHLRLOLFDMFGQWBLWBWQOLKF
WBYLBYLFLSFLJGRMQBOLWJVFPFWQVHQWFFPQOQVFPQOCFPOGFW
FJIGFQVHLHLROQVFGWJVFPFOLF H GQVQVFILEOGQILHQFQGIQVVS
FAFGBWQVHQWQWJWJVFPFWHGF IWHZZRQGBABHZQOCGFHX

Decrypted Text:

IORMTNAOHMSRIARATEDAHOEESTOEDEZRKREERIIZTTNCIRZKIEAEO
TSEZEAAENOANDEOEHANIDHIRINIESMEOTARIARATNIKEARAIRIAIESE
IORMTRNIAISEDEATSHTAEDTNTSEDNTCEDNOEAEIHOETSHIHIRTSE
OAISEDENIEHOTSTSEIENOTIHTTETOITSSNSEAEORATSHTAIISAISEDEA
HOEIAIHZZRTORARHZTNCOEHJ

❖ The code is in another file that was delivered with PDF