Homework 1

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1 Chapter 1

1.1 1.1

2. Which of these are propositions? What are the truth values of those that are propositions?

   a. Do not pass go.

   b. What time is it?

   c. There are no black flies in Maine.

   d. 4 + x = 5.

   e. The moon is made of green cheese.

   f. 2n $\geq$ 100.

   Answer: c and e are both propositions, and both of their truth values are false.

4. What is the negation of each of these propositions?

   a. Jennifer and Teja are friends.

   b. There are 13 items in a baker's dozen.

   c. Abby sent more than 100 text messages every day.

   d. 121 is a perfect square.

   Answer:

   a. Jennifer and Teja are not friends.

   b. There aren't 13 items in a baker's dozen.

   c. Abby sent less than or equal to 100 text messages every day.

   d. 121 is not a perfect square.

6. Suppose that Smartphone A has 256 MB RAM and 32 GB ROM, and the resolution of its camera is 8 MP; Smartphone B has 288 MB RAM and 64 GB ROM, and the resolution of its camera is 4 MP; and Smartphone C has 128 MB RAM and 32 GB ROM, and the resolution of its camera is 5 MP. Determine the truth value of each of these propositions.

   a. Smartphone B has the most RAM of these three smartphones.

   b. Smartphone C has more ROM or a higher resolution camera than Smartphone B.

   c. Smartphone B has more RAM, more ROM, and a higher resolution camera than Smartphone A.

   d. If Smartphone B has more RAM and more ROM than Smartphone C, then it also has a higher resolution camera.

e. Smartphone A has more RAM than Smartphone B if and only if Smartphone B has more RAM than Smartphone A.

Answer:

a. True

b. True

c. False

d. False

e. False

1.2 1.2

For exercises 2 & 4, translate into propositional logic.

2. You can see the movie only if you are over 18 years old or you have the permission of a parent. Express your answer in terms of m: "You can see the movie," e: "You are over 18 years old," and p: "You have the permission of a parent."

   Answer: $m \rightarrow (e \vee p)$

4. To use the wireless network in the airport you must pay the daily fee unless you are a subscriber to the service. Express your answer in terms of w: "You can use the wire- less network in the airport," d: "You pay the daily fee," and s: "You are a subscriber to the service."

   Answer: $w \rightarrow (d \vee s)$

1.3 1.3

6. Use a truth table to verify the first De Morgan law

$$\neg(p \wedge q) \equiv \neg p \vee \neg q$$

   Answer:

p	q	$\neg p$	$\neg q$	$\neg(p \wedge q)$	$\neg p \vee \neg q$
T	T	F	F	F	F
T	F	F	T	T	T
F	T	T	F	T	T
F	F	T	T	T	T

8. Use De Morgan's laws to find the negation of each of the following statements

   a. Kwame will take a job in industry or go to graduate school.

b. Yoshiko knows Java and calculus.

c. James is young and strong.

d. Rita will move to Oregon or Washington.