

Course outline

- Session 1. Simple Regression; Individual Difference; Intro to Linear mixed-effect models (LMMs)
- Session 2. LMMs (lmer); Generalised LMMs (glmer)
- Session 3. Practical
- Session 4. Ggeneralised LMMs continued; Model assumptions and diagnostics
- Session 5. Practical



Session 3 Roadmap (today)

- Model Comparison & Selection
- Generalised LMMs
- Model Assumptions
- Exercise and Q&A





Model Comparison and Selection

Recall: Structure of LMMS

• R code: $|mer(y \sim x1 * x2 + (1 + x1 * x2 | Grouping_1) + (1 + x1 | Grouping_2) ,$ |data = datafilename|

Recall: Model Fit

- No *R*²
- Use Maximum likelihood Ratio test to compare models
- R code: anova(model1, modle2)

NB: when using it to test random structures, make sure to set REML = T

Model Comparison & Selection

In what order should you build your models?

- Which model should you select as final model?
 - > Barr, Levy, Scheepers, & Tily, (2013): keep it maximal
 - ➤ Matuschek, Kliegl, Vasishth, Baayen & Bates (2017): make it parsimonious to balance Type1 error and power

Common Issues

Convergence

```
Warning message:
In checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, :

Model failed to converge with max|grad| = 0.0206805 (tol = 0.002, component 1)
```

Overfitting

```
boundary (singular) fit: see ?isSingular
```

Deal with Convergence Issue

```
Warning message:
In checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, :

Model failed to converge with max|grad| = 0.0206805 (tol = 0.002, component 1)
```

Solutions:

- Adjust stopping (convergence) tolerances for the nonlinear optimizer, using the optCtrl() argument to ImerControl.
- Centre and standardise continuous predictor variables
 - the scale() function

Deal with Overfitting Issue

boundary (singular) fit: see ?isSingular

Solutions:

- Remove the most complex part of the random effects structure (i.e. random slopes)
- Maybe acceptable to remove a specific random effect term when its variance estimates are very low

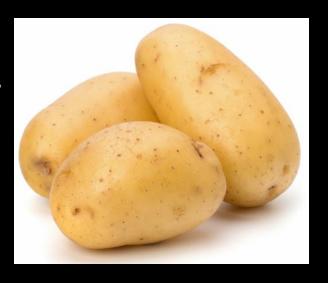


Generalised Linear Mixed-effects Models

Binary Outcome

- Pass or Fail
- Invest or Not
- Vote 'Yes' or 'No'
- 'Correct' or 'incorrect' answer
- Fixation on the target image or not
- Align with partner or not
 - Lexical choice
 - Grammatical choice

'potato' or 'tattie'





- (a) Gromit gave Wallace some cheese.
- (b) Gromit gave some cheese to Wallace.

Generalised Linear Mixed-effects Models

• glmer () for binary outcome

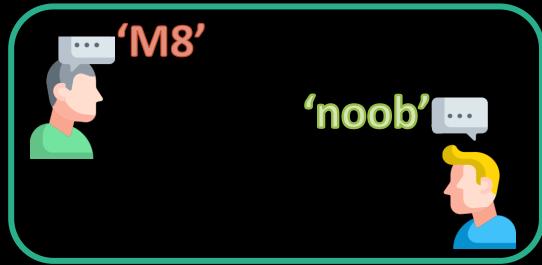
• *R* code:

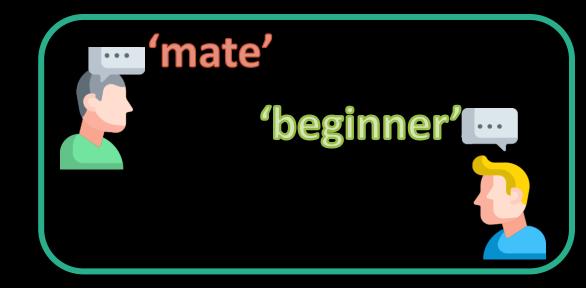
Example: Lexical Choice Study

'Noob' or 'Beginner'?

Internet slang data (simulated data)

• Hypothesis: People were more likely to use internet slang words (as relative to alternative expressions) after seeing their conversational partner uses a slang rather than a stand word.



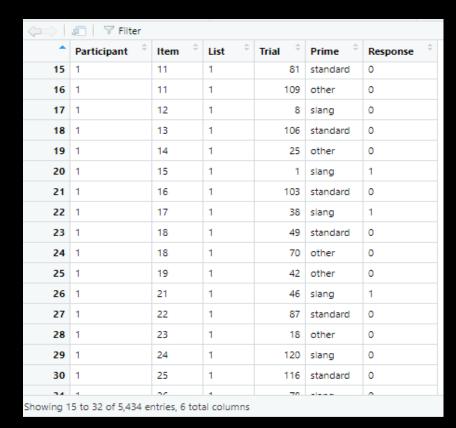


Example: Lexical Choice Study

Repeated measure (36 items/participant)

One predictor (3 conditions):
 'prime' = slang / standard words / other

Two sources of random variance



```
summary(data_ISD)
                     Item
                                     List
                                                                                    Response
                       : 248
                                       : 457
                                                                           :1787
                                                                                        :2874
                       : 234
                                                                  standard: 1833
                                                                                        :2512
                       : 215
                                       : 401
                                                Median : 63.00
                                                                           :1814
                                                                                    NA's: 48
                                                                  sland
                       : 208
                                       : 377
                                                3rd Qu.: 95.00
                                       : 374
                                                        :123.00
(Other):5218
                (Other):4120
                                (Other):3029
```

Build a Glmer Model

Interpret Coefficients

```
Generalized linear mixed model fit by maximum likelihood (Laplace Approximation) ['glmerMod']
 Family: binomial (logit)
Formula: Response ~ Prime + (1 | Participant) + (1 | Item)
   Data: data_ISD
Control: glmerControl(optimizer = "bobyqa", optCtrl = list(maxfun = 2e+05))
              BIC logLik deviance df.resid
Scaled residuals:
             1Q Median
-4.9925 -0.5758 -0.2008 0.6024 4.8213
Random effects:
 Groups
                         Variance Std.Dev.
 Participant (Intercept) 2.4345 1.5603
             (Intercept) 0.1262 0.3552
Number of obs: 5386, groups: Participant, 160; Item, 30
Fixed effects:
              <u>Estimate S</u>td, Error z value Pr(>|z|)
             -0.27907 0.15230 -1.832
Primestandar -0.93888
                        0.08594 -10.925
              1.12819
                         0.08583 13.145
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Correlation of Fixed Effects:
            (Intr) Prmstn
Primestndrd -0.266
Primeslang -0.277 0.441
```

Use β 0 to calculate the probability of the intercept:

$$\frac{e^{-0.28}}{1+e^{-0.28}}=0.43$$

Use $\beta 1$ to get the probability of using standard form (slope 1):

$$\frac{e^{(-0.28+(-0.94))}}{1+e^{(-0.28+(-0.94))}}=0.23$$

Use β 2 to get the probability of using slang (slope 2):

• Can be transformed to probabilities:
$$prob(x) = \frac{e^x}{1+e^x}$$

$$\frac{e^{(-0.28+1.13)}}{1+e^{(-0.28+1.13)}}=0.70$$



Model Assumptions

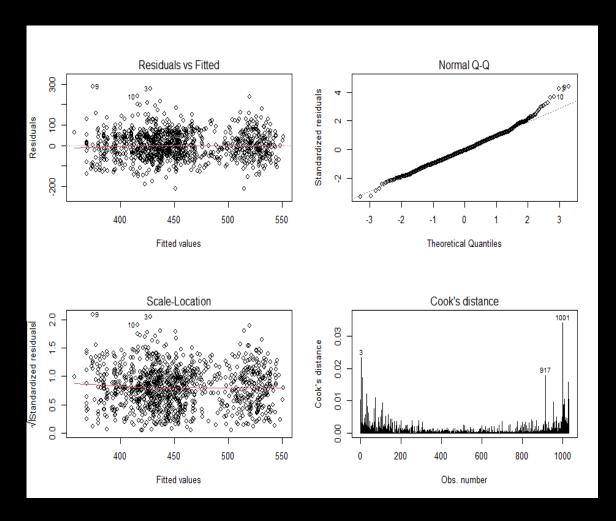
Model Assumptions: Linear regression

- Nature of the model
 - the relation between predictor and outcome has to be linear

- Nature of the errors (i.e., residuals)
 - normal and independent of each other

Model Assumptions: Simple regression Im()

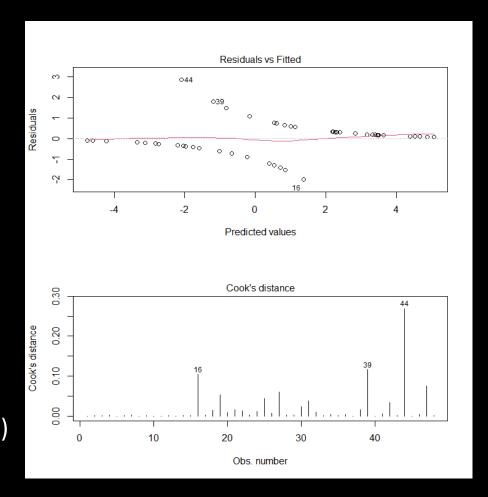
- Required(LINE):
 - Linearity of relationships
 - Independence of residuals
 - Normality of residuals
 - Equal variances for residuals
- Desirable:
 - uncorrelated predictors (no collinearity)
 - no outliers



Model Assumptions: Simple regression glm()

For binomial DVs, (logistic regression)

- Required:
 - LINEAR relationships between IVs and log-odds
 - Normality of residuals
 - homogeneity of variance
 - Independence of residuals
- Desirable:
 - uncorrelated predictors (no collinearity)
 - no "bad" (overly influential) observations
 - large samples (due to maximum likelihood fitting)



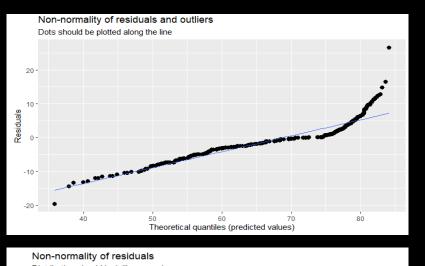
Model Assumptions: Mixed-effects Models

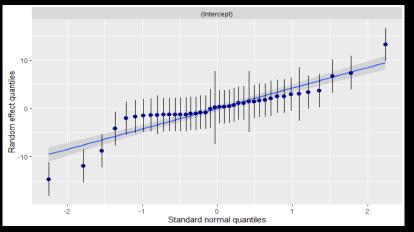
Similar to simple linear regressions model

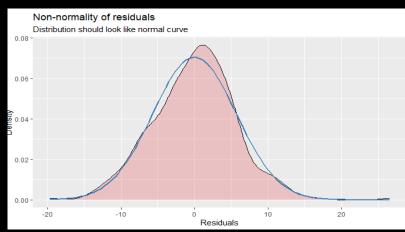
- Error is random
- Residuals at multiple levels
 - Level1 residuals: mean = 0, variance constant (R code: residual())
 - Level2+ residuals: mean = 0, variance constant (R code: ranef())

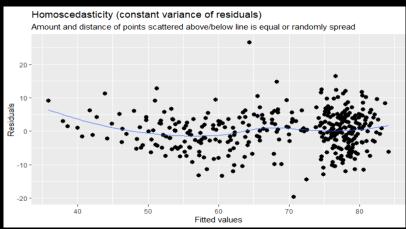
Model Assumptions: Mixed Models – Imer()

plot_model(mMixed_reduced , type = "diag")



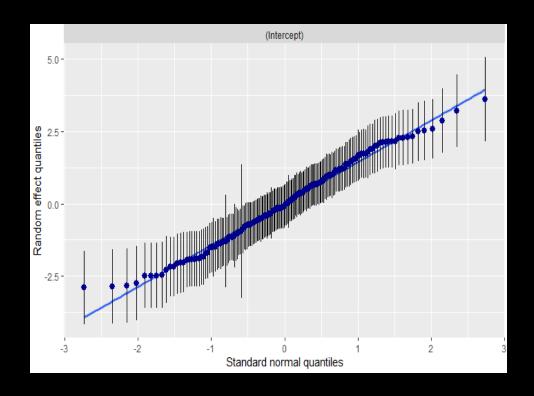


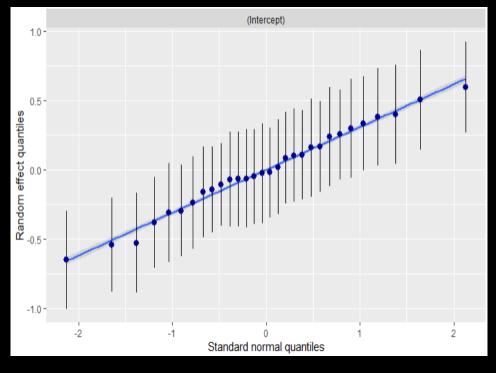




Model Assumptions: Mixed Models – glmer()

plot_model(m3_dataISD, type = "diag")





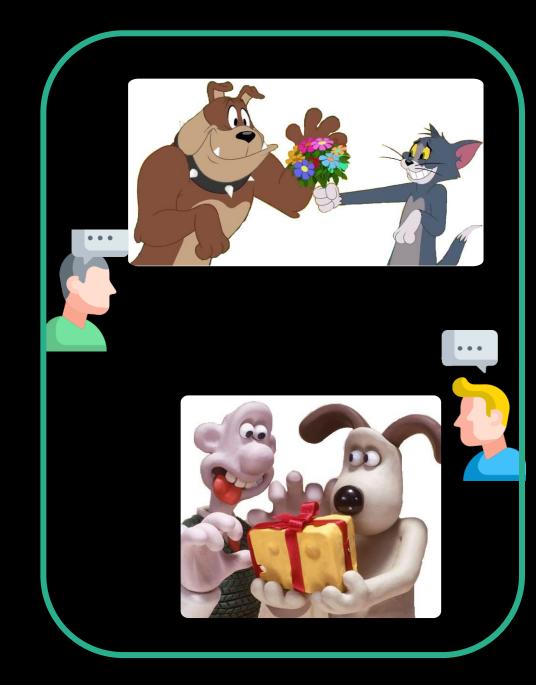


Exercise & Q&A

Exercise for Friday

The 'cheese data': Simulated data based on real psycholinguistic findings on structural priming.

- Two Predictors :
 - 2-level factor "Prime"
 - (a): Tom gave Spike some flowers.
 - (b): Tom gave some flowers to Spike.
 - 2-level factor "communication" (video- vs audio-call)
- Binary outcome: (a) or (b)?
 - (a) Gromit gave ... (Wallace some cheese)
 - (b) Gromit gave ... (some cheese to Wallace).



Exercise



Can you investigate the priming effect in the 'cheese data'?

• R code:

```
glmer (y \sim x1 * x2 +
	(1 + x1 * x2 | Grouping_1) +
	(1 + x1 | Grouping_2),
	data = datafilename,
	family = 'binomial'
)
```

Further Reading

Paper

Brown, VA. (2021). An Introduction to Linear Mixed-Effects Modeling in R. *Advances in Methods and Practices in Psychological Science*. 4(1). doi:10.1177/2515245920960351

Advances in Methods and Practices in Psychological Science

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An Introduction to Linear Mixed-Effects Modeling in R

Violet A. Brown Description Wiew all authors and affiliations

All Articles https://doi.org/10.1177/2515245920960351

E-Book

https://vasishth.github.io/Freq CogSci/

Shravan Vasishth, Daniel Schad, Audrey Bürki, Reinhold Kliegl

Linear Mixed Models in Linguistics and Psychology: A Comprehensive Introduction

THANK YOU

