## Black Friday Project

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December 4, 2018

In this report I will be trying to construct a model that accurately predicts the amount (in dollars) of purchases a customer will make based on their individual characteristics. I will begin the process by first looking at the structure of the data and performing any cleaning and pre-processing. The data used in this project was gathered from Kaggle, and the purpose of this project was to submit the model as part of a contest.

First I check the structure of our data and determine whether or not there are any NAs in the data.

```
str(data)
```

##

```
'data.frame':
                    537577 obs. of
##
                                    12 variables:
##
    $ User_ID
                                 : int 1000001 1000001 1000001 1000001 1000002 1000003 1000004 1000004
##
    $ Product_ID
                                 : Factor w/ 3623 levels "P00000142", "P00000242", ...: 671 2375 851 827 27
##
    $ Gender
                                 : Factor w/ 2 levels "F", "M": 1 1 1 1 2 2 2 2 2 2 ...
##
    $ Age
                                 : Factor w/ 7 levels "0-17", "18-25", ...: 1 1 1 1 7 3 5 5 5 3 ....
##
    $ Occupation
                                       10 10 10 10 16 15 7 7 7 20 ...
                                 : Factor w/ 3 levels "A", "B", "C": 1 1 1 1 3 1 2 2 2 1 ...
    $ City_Category
##
    $ Stay_In_Current_City_Years: Factor w/ 5 levels "0","1","2","3",..: 3 3 3 5 4 3 3 3 2 ...
##
    $ Marital_Status
                                        0 0 0 0 0 0 1 1 1 1 ...
##
    $ Product_Category_1
                                        3 1 12 12 8 1 1 1 1 8 ...
##
                                   int
##
    $ Product_Category_2
                                 : int
                                        NA 6 NA 14 NA 2 8 15 16 NA ...
                                        NA 14 NA NA NA NA 17 NA NA NA ...
##
    $ Product Category 3
                                 : int
    $ Purchase
                                        8370 15200 1422 1057 7969 15227 19215 15854 15686 7871 ...
                                 : int
#The data is clearly cross-sectional
#checking which variables have NA's
colSums(is.na(data))
##
                      User_ID
                                                Product_ID
##
                                                         0
##
                        Gender
                                                       Age
##
##
                   Occupation
                                            City_Category
##
  Stay_In_Current_City_Years
##
                                           Marital_Status
##
##
           Product_Category_1
                                       Product_Category_2
##
                                                    166986
##
           Product_Category_3
                                                  Purchase
```

Since there are NAs in Product\_Category\_2 and Product\_Category\_3 i combined those into a dummy variable called "multi". Multi takes on a value of 1 if the product belongs to multiple categories and a value of 0 if the product belongs to only one category. Using this method i do not need to include all three dummy variables.

```
#combining product category 2 and 3 variable into dummy:
#with 1 if in more than one product category and 0 if not
data$multi = 1
data[is.na(data$Product_Category_2), "multi"] = 0
```

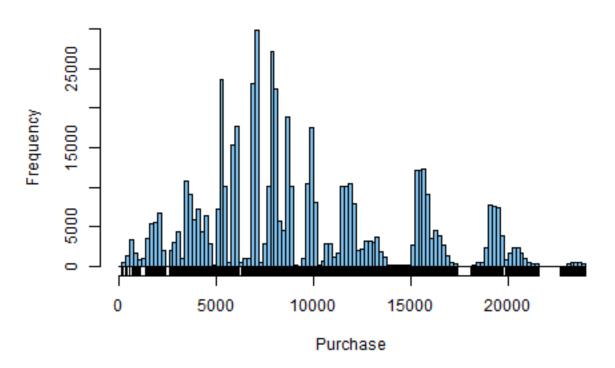
```
#removing product category 2 and 3 variables
data <- data[, -c(10:11)]
str(data)
   'data.frame':
                    537577 obs. of 11 variables:
##
    $ User ID
                                       1000001 1000001 1000001 1000001 1000002 1000003 1000004 1000004
    $ Product_ID
                                 : Factor w/ 3623 levels "P00000142", "P00000242", ...: 671 2375 851 827 27
##
##
    $ Gender
                                 : Factor w/ 2 levels "F", "M": 1 1 1 1 2 2 2 2 2 2 ...
##
    $ Age
                                 : Factor w/ 7 levels "0-17", "18-25", ...: 1 1 1 1 7 3 5 5 5 3 ....
##
    $ Occupation
                                 : int 10 10 10 10 16 15 7 7 7 20 ...
##
    $ City Category
                                 : Factor w/ 3 levels "A", "B", "C": 1 1 1 1 3 1 2 2 2 1 ...
##
    $ Stay_In_Current_City_Years: Factor w/ 5 levels "0","1","2","3",...: 3 3 3 3 5 4 3 3 3 2 ...
    $ Marital_Status
                                        0 0 0 0 0 0 1 1 1 1 ...
    $ Product_Category_1
                                        3 1 12 12 8 1 1 1 1 8 ...
                                   int
                                        8370 15200 1422 1057 7969 15227 19215 15854 15686 7871 ...
##
    $ Purchase
    $ multi
                                 : num 0 1 0 1 0 1 1 1 1 0 ...
colSums(is.na(data))
##
                      User_ID
                                                Product_ID
##
##
                        Gender
                                                       Age
##
##
                   Occupation
                                            City_Category
##
                                                         0
##
  Stay_In_Current_City_Years
                                           Marital_Status
##
           Product_Category_1
##
                                                  Purchase
##
                                                         0
                             0
##
                        multi
##
```

Now I will move on to the descriptive analysis. Notice that most of our variables are categorical and therefore I can only make histograms for Purchase and Occupation. It is important to note that purchases (total dollar amount of a persons transaction) is the dependent variable for this report.

I now conduct some data analysis on the variables to see if they are skewed, have outliers, or need to be transformed. I look at the Quantile-Quantile plots for Purchase in order to determine its normality.

```
#Histogram of Purchases
par(mfrow=c(1,1))
hist(Purchase, breaks = "FD", col = "skyblue2")
rug(Purchase)
```

# Histogram of Purchase

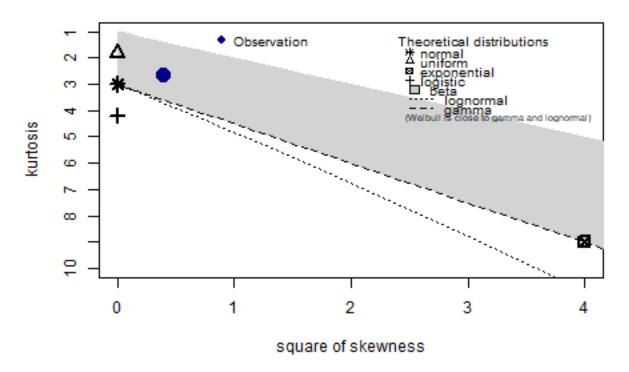


```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 185 5866 8062 9334 12073 23961

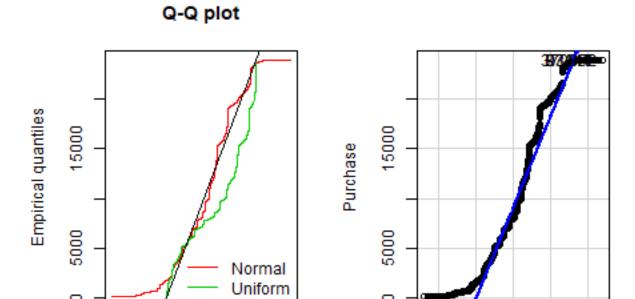
par(mfrow=c(1,1))

#Cullen-Frey graph of Purchases
descdist(Purchase)
```

## Cullen and Frey graph



```
## summary statistics
## -----
## min: 185
              max: 23961
## median: 8062
## mean: 9333.86
## estimated sd: 4981.022
## estimated skewness: 0.6242797
## estimated kurtosis: 2.656879
#Fitting Distributions to Purchases
fit.norm = fitdist(as.numeric(Purchase), "norm")
fit.unif = fitdist(as.numeric(Purchase),"unif")
plot.legend = c("Normal", "Uniform")
par(mfrow=c(1,2))
qqcomp(list(fit.norm, fit.unif), legendtext = plot.legend)
qqPlot(~ Purchase, data = data, id = list(n=3))
```



## [1] 87441 93017 370892

-10000

#I fit a gamma distribution to the inc data

10000

Theoretical quantiles

30000

Purchase looks fairly normal from the QQ-Plots but I log the data just to make sure there isn't a better transformation.

0

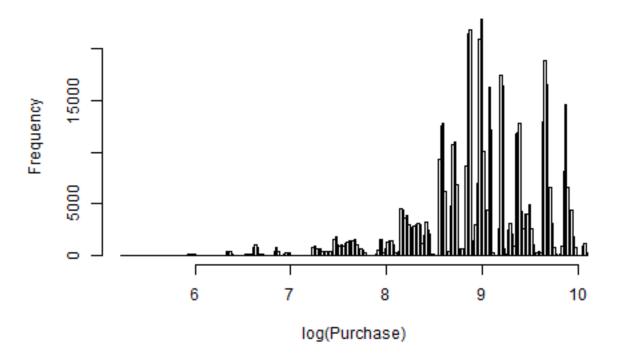
norm quantiles

2

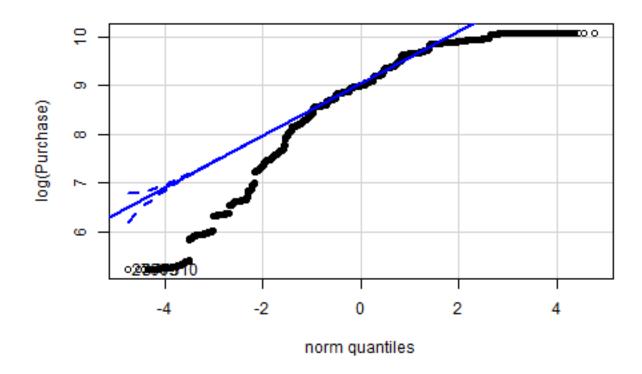
4

#Histogram of Log(Purchases)
hist(log(Purchase), breaks = "FD")

# Histogram of log(Purchase)



qqPlot(log(Purchase))

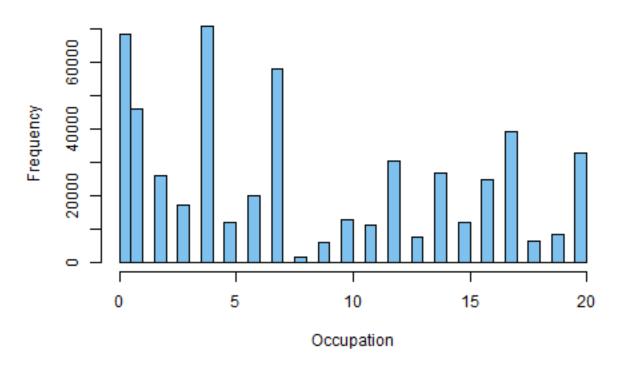


### ## [1] 27603 377310

Based on the QQ plot I can see that Purchase's should not be transformed as it makes the data less normal. Next, I looked at the histogram for Occupation.

```
#Histogram of occupation
par(mfrow=c(1,1))
hist(Occupation, breaks = "FD", col = "skyblue2")
```

## **Histogram of Occupation**

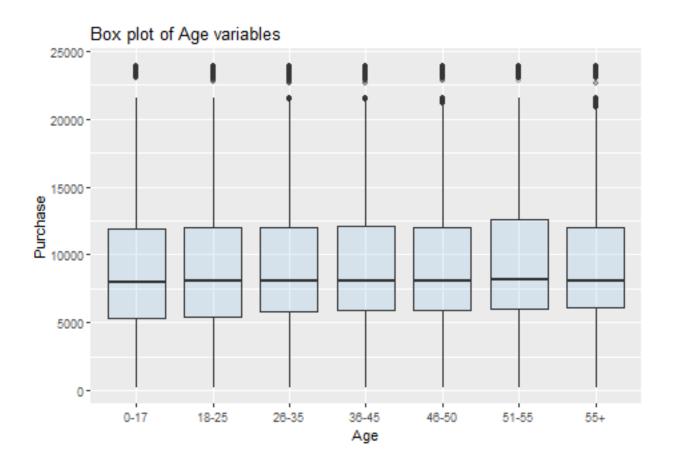


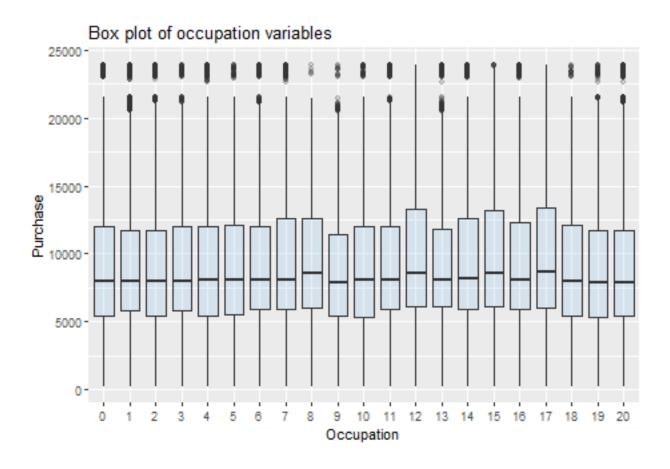
### S(Occupation)

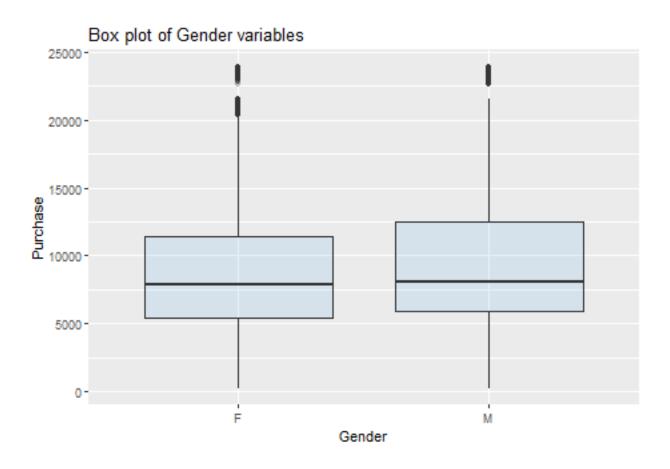
```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.000 2.000 7.000 8.083 14.000 20.000
```

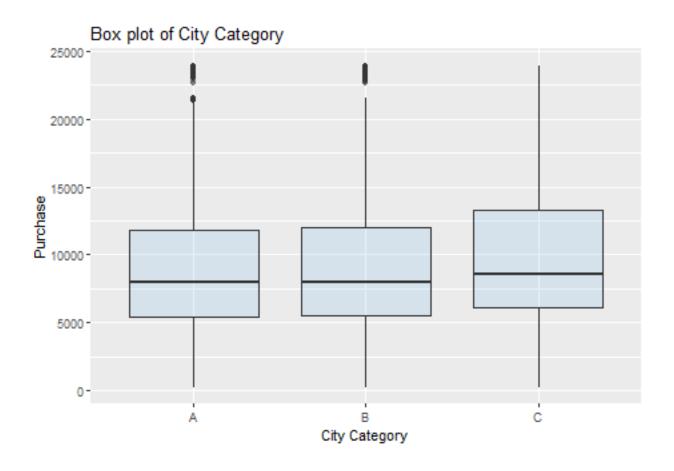
This plot illustrates how many observed individuals fall in specific Occupation categories. I can see from the histogram that the data is not skewed, does not contain any outliers, and does not need to be transformed. I confirmed these results using the Box-Cox transformation test.

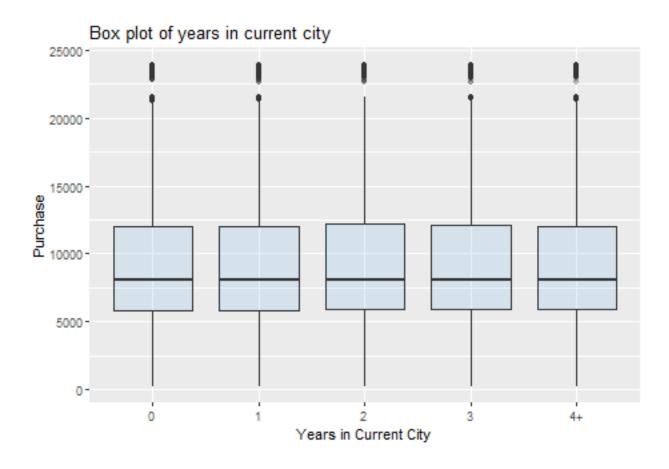
Next, I looked at the box plots to see what the spread of purchase amount looks like for each of the variables.

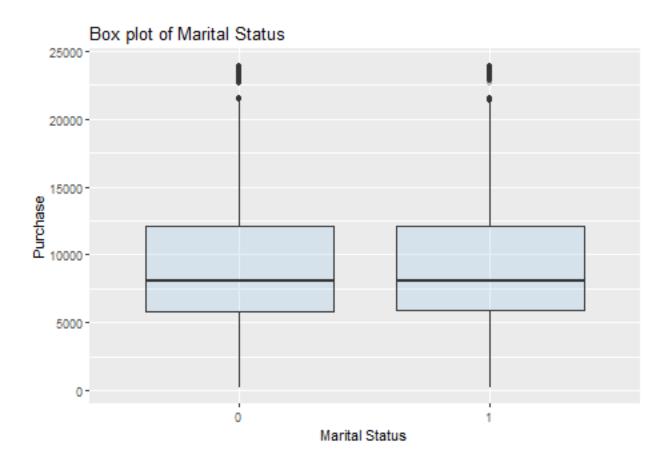


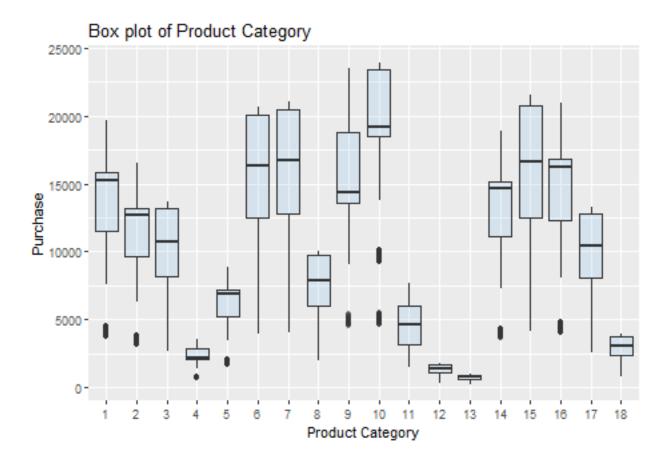


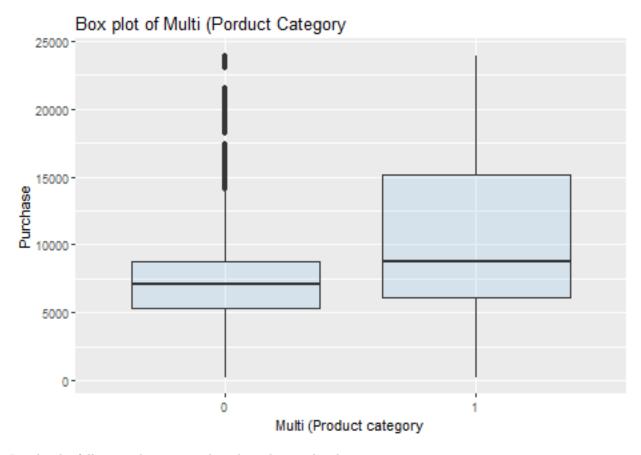












I make the following observations based on the graphs above:

- 1. The mean purchase amount is fairly evenly distributed across the specific category levels within each variable except for Product Category and multi.
- 2. I noticed that there is a larger spread in purchase amount when the product belongs to only one category.
- 3. Different product categories have different purchase amount means with different spreads.

Now that I have looked at some of the univariate and bivariate characteristics, I create a regression model with all of the additive terms.

```
#Model 1
mod.1 <- lm(Purchase ~ Gender + Age + Occupation + City_Category+Stay_In_Current_City_Years +
              Marital_Status+Product_Category_1 + multi, data)
S(mod.1)
## Call: lm(formula = Purchase ~ Gender + Age + Occupation + City_Category +
##
            Stay_In_Current_City_Years + Marital_Status + Product_Category_1 + multi,
##
            data = data)
##
## Coefficients:
                                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                9132.1573
                                             48.2767
                                                      189.163 < 2e-16 ***
## GenderM
                                 523.1621
                                             14.9960
                                                       34.887 < 2e-16 ***
## Age18-25
                                 349.5520
                                             41.7249
                                                        8.378 < 2e-16 ***
## Age26-35
                                 543.4284
                                             40.5208
                                                       13.411 < 2e-16 ***
## Age36-45
                                 633.9828
                                             41.6525
                                                       15.221 < 2e-16 ***
```

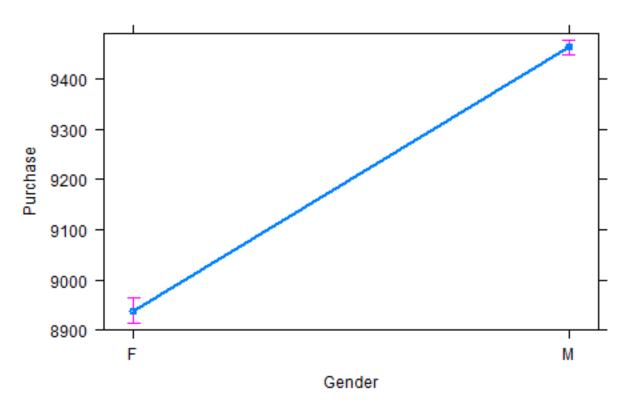
```
## Age46-50
                                  606.6089
                                              45.7437
                                                         13.261 < 2e-16 ***
                                                         19.995 < 2e-16 ***
## Age51-55
                                  934.5792
                                              46.7410
## Age55+
                                  739.0741
                                              51.2880
                                                         14.410 < 2e-16 ***
## Occupation
                                    6.1314
                                                          6.164 7.10e-10 ***
                                               0.9947
## City_CategoryB
                                  162.8656
                                              15.8793
                                                         10.256 < 2e-16 ***
## City CategoryC
                                  717.7012
                                              17.1714
                                                         41.796 < 2e-16 ***
## Stay In Current City Years1
                                   28.5154
                                              20.5123
                                                          1.390 0.16448
## Stay_In_Current_City_Years2
                                   62.9861
                                              22.8902
                                                          2.752 0.00593 **
## Stay_In_Current_City_Years3
                                   27.0766
                                              23.2618
                                                          1.164 0.24443
## Stay_In_Current_City_Years4+
                                   44.4407
                                              23.8489
                                                          1.863 0.06240 .
## Marital_Status
                                  -53.9095
                                              13.8472
                                                         -3.893 9.89e-05 ***
## Product_Category_1
                                               1.8840 -188.628 < 2e-16 ***
                                 -355.3684
## multi
                                 1139.8707
                                              15.2280
                                                         74.854 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard deviation: 4685 on 537559 degrees of freedom
## Multiple R-squared: 0.1153
                 4120 on 17 and 537559 DF, p-value: < 2.2e-16
## F-statistic:
##
        AIC
## 10612982 10613194
Since Stay_In_Current_City was not significant (except for Stay_In_Current_City_2) I used a Chow-Test
to determine if the estimated coefficient of any of the "Stay in Current City" variables are equal to zero.
hyp <- c("Stay_In_Current_City_Years1 = 0", "Stay_In_Current_City_Years2 = 0",</pre>
         "Stay_In_Current_City_Years3 = 0", "Stay_In_Current_City_Years4+ = 0")
linearHypothesis(mod.1, hyp)
## Linear hypothesis test
##
## Hypothesis:
## Stay_In_Current_City_Years1 = 0
## Stay_In_Current_City_Years2 = 0
## Stay_In_Current_City_Years3 = 0
## Stay_In_Current_City_Years4 + = 0
##
## Model 1: restricted model
## Model 2: Purchase ~ Gender + Age + Occupation + City_Category + Stay_In_Current_City_Years +
##
       Marital_Status + Product_Category_1 + multi
##
##
     Res.Df
                 RSS Df Sum of Sq
                                        F Pr(>F)
## 1 537563 1.18e+13
## 2 537559 1.18e+13 4 186223076 2.1209 0.07539 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Because the p-value is greater than 0.05, there is insufficient evidence to justify keeping "Stay in Current
City" in the model. I removed this in the following model.
#Model 2 (stay in city removed)
mod.2 <- lm(Purchase ~ Gender + Age + Occupation + City_Category +</pre>
              Marital_Status+Product_Category_1 + multi, data)
S(mod.2)
```

```
Marital_Status + Product_Category_1 + multi, data = data)
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      9164.473
                                   45.747
                                            200.330 < 2e-16 ***
## GenderM
                       523.371
                                   14.983
                                            34.932 < 2e-16 ***
## Age18-25
                       348.786
                                   41.709
                                             8.362 < 2e-16 ***
## Age26-35
                       543.423
                                   40.500
                                             13.418 < 2e-16 ***
## Age36-45
                       633.682
                                   41.641
                                            15.218 < 2e-16 ***
## Age46-50
                       605.493
                                   45.716
                                            13.245 < 2e-16 ***
## Age51-55
                       933.942
                                   46.696
                                            20.001 < 2e-16 ***
## Age55+
                       738.935
                                   51.273
                                            14.412 < 2e-16 ***
## Occupation
                         6.151
                                    0.994
                                             6.188 6.11e-10 ***
## City_CategoryB
                       163.903
                                   15.859
                                            10.335 < 2e-16 ***
## City_CategoryC
                       719.382
                                   17.154
                                             41.937 < 2e-16 ***
## Marital_Status
                       -53.926
                                   13.846
                                             -3.895 9.83e-05 ***
## Product_Category_1 -355.386
                                    1.884 -188.655 < 2e-16 ***
## multi
                      1140.011
                                   15.228
                                             74.863 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard deviation: 4685 on 537563 degrees of freedom
## Multiple R-squared: 0.1153
## F-statistic: 5387 on 13 and 537563 DF, p-value: < 2.2e-16
##
        AIC
                 BIC
## 10612982 10613150
Now that all the variables are statistically significant, I looked at the effects plots. Our \mathbb{R}^2 remains the same.
```

##

plot(effect(mod = mod.2, "Gender"), main="Marginal Effect of Gender on Purchases")

## Marginal Effect of Gender on Purchases

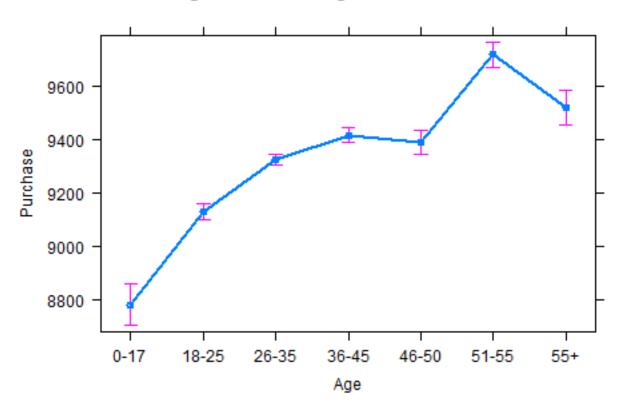


From the Gender effect plot, I can determine that males spent more on Black Friday than females. The spread on Purchases for males is also smaller than the spread on Purchases for females.

Intuitively, this may be a result of males buying more expensive/big-ticket items on Black Friday than females.

plot(effect(mod = mod.2, "Age"), main="Marginal Effect of Age on Purchases")

## Marginal Effect of Age on Purchases



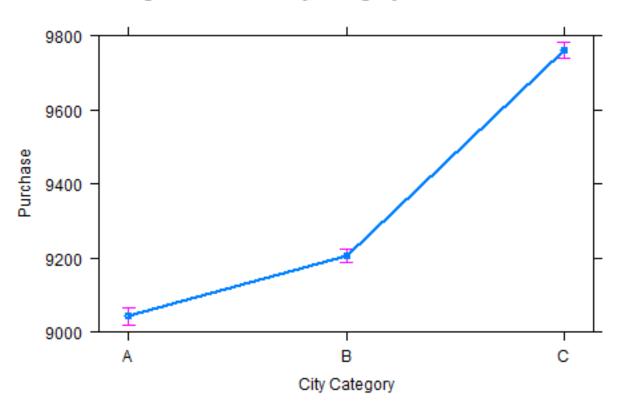
Here I see that in general, purchases go up as age increases, with more variability amongst the lower and higher age ranges.

However, I do see that purchases plateau between the age groups of 36-45 and 46-50.

Intuitively, I believe the variability is due to younger age groups because they could be spending either their money or their parents' money. For the older age groups the variability could be due to retirees in this group with lower disposable income.

#Marginal effect plot of City Category
plot(effect(mod = mod.2, "City\_Category"), main="Marginal Effect of City Category on Purchases", xlab=""

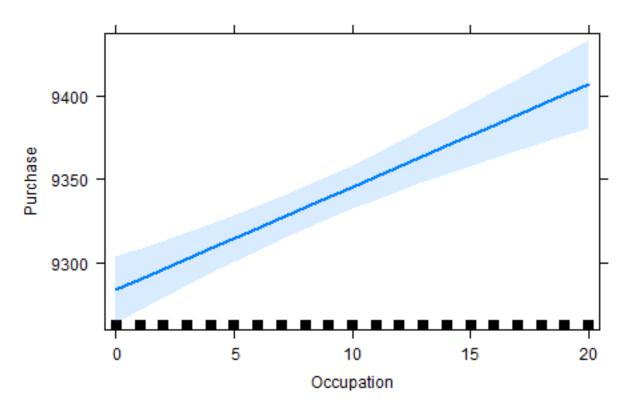
## Marginal Effect of City Category on Purchases



In City Category, I can see that the overall dollar value of purchases made in City C were much higher than B and C. This could mean that items are more expensive in city C or there is more variety (people shop more).

```
#Marginal effect plot of Occupation
plot(effect(mod = mod.2, "Occupation"), main="Marginal Effect of Occupation on Purchases", xlab="Occupation")
```

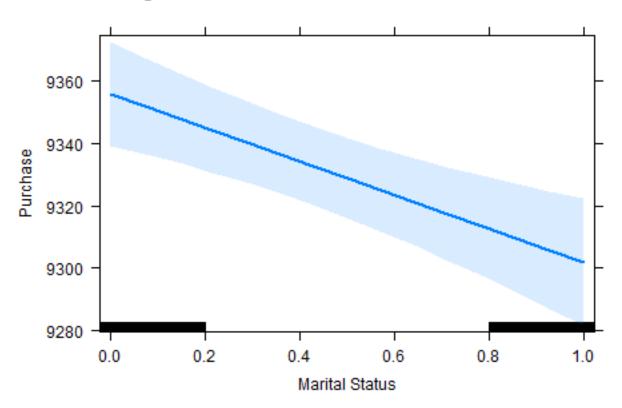
## Marginal Effect of Occupation on Purchases



The Occupation effect plot shows us that as the Occupation category increases, then purchases increase. This could indicate that the larger the occupation category, the higher the income. If this were the case, intuitively, it makes sense that there is a little more variation at the lower and higher occupation category values. This is because at lower levels of income, you are likely to have a different spending behavior than other people in the same income bracket.

```
#Marginal effect plot of Marital Status
plot(effect(mod = mod.2, "Marital_Status"), main="Marginal Effect of Marital Status on Purchases", xlab
```

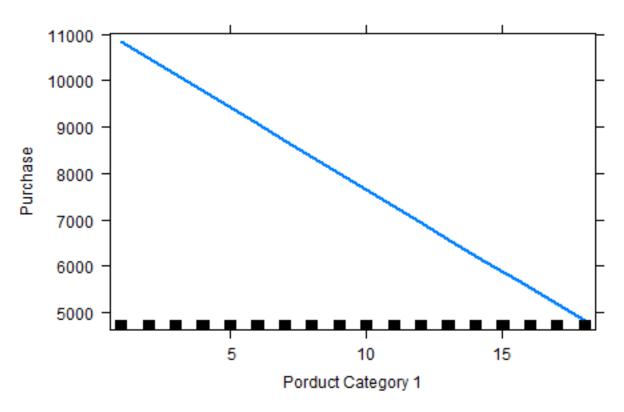
## Marginal Effect of Marital Status on Purchases



From this effects plot, it seems that purchases are lower for married individuals versus single individuals.

#Marginal effect plot of product category 1
plot(effect(mod = mod.2, "Product\_Category\_1"), main="Marginal Effect of Product Category 1 on Purchase

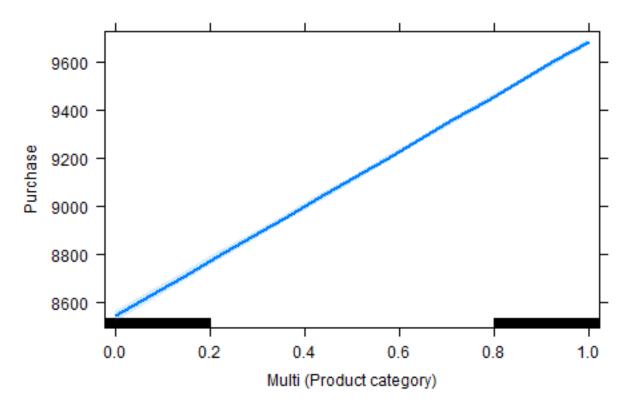
## Marginal Effect of Product Category 1 on Purchases



For Product Category\_1, I see that the higher the number of the category, the lower the purchase dollar amount. This could mean that higher category numbers are items that are cheaper or that less people buy them

#Marginal effect plot of product category
plot(effect(mod = mod.2, "multi"), main="Marginal Effect of Product Categories on Purchases", xlab="Multi")

### Marginal Effect of Product Categories on Purchases



This plot shows that if a product belongs to more than one category then, the dollar value of purchases increase. This could indicated that the items hold more value if they belong to multiple categories or they are items that are purchased more.

From the effects plots, I noticed that Gender and multi variables looked almost identical and wanted to test if there was any degree of collinearity between the two variables. In order to do this, I looked at their correlation.

```
#Correlation of product categories and gender
cor(multi, (as.numeric(Gender))-1)
```

### ## [1] 0.01197696

Because the result is so low I can safely assume that our multi and Gender variables are significantly different from each other.

Now that I have the effects plots, I use the Ramsey RESET test in order to determine whether or not our current model is mis-specified.

```
#Ramsey RESET test
resettest(mod.2, power=2, type="regressor")

##
## RESET test
##
## data: mod.2
## RESET = 24835, df1 = 4, df2 = 537560, p-value < 2.2e-16</pre>
```

Now I decided to look at interaction terms and possible variable transformations because I found from the Ramsey Reset Test that our model is mis-specified with just the additive terms.

I first try adding the interaction term of gender and age because spending at the different age groups might be different depending on gender.

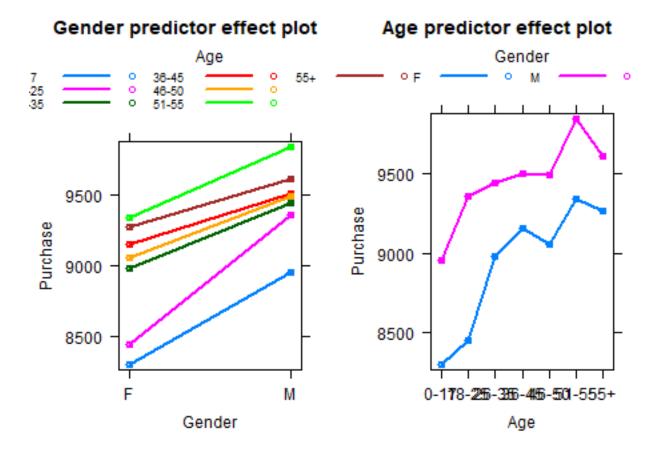
```
#Model 3 (Adding gender:age interaction term) BENCHMARK
mod.3 <- lm(Purchase ~ Gender + Age + Occupation + Marital_Status + Product_Category_1 +
              City_Category + multi + Gender:Age, data)
S(mod.3)
## Call: lm(formula = Purchase ~ Gender + Age + Occupation + Marital_Status +
            Product_Category_1 + City_Category + multi + Gender: Age, data = data)
##
##
## Coefficients:
##
                      Estimate Std. Error
                                           t value Pr(>|t|)
## (Intercept)
                      9073.021
                                    70.096
                                            129.438 < 2e-16 ***
## GenderM
                                    81.785
                                              8.016 1.10e-15 ***
                       655.554
## Age18-25
                                    73.252
                                              2.033 0.042015 *
                       148.948
## Age26-35
                                              9.629
                                                     < 2e-16 ***
                       675.167
                                    70.115
## Age36-45
                       849.590
                                    72.747
                                             11.679
                                                     < 2e-16 ***
## Age46-50
                       754.962
                                    79.139
                                              9.540
                                                     < 2e-16 ***
## Age51-55
                       1036.082
                                    82.424
                                             12.570
                                                     < 2e-16 ***
## Age55+
                       965.924
                                    94.756
                                             10.194
                                                     < 2e-16 ***
## Occupation
                         6.464
                                     0.995
                                              6.496 8.23e-11 ***
## Marital_Status
                       -50.459
                                    13.854
                                             -3.642 0.000270 ***
## Product_Category_1 -355.260
                                     1.884 -188.605
                                                     < 2e-16 ***
## City_CategoryB
                       166.108
                                    15.876
                                             10.463
                                                     < 2e-16 ***
## City_CategoryC
                       717.925
                                    17.172
                                             41.807
                                                     < 2e-16 ***
## multi
                       1140.442
                                    15.227
                                             74.898
                                                     < 2e-16 ***
## GenderM: Age18-25
                       248.626
                                              2.797 0.005157 **
                                    88.88
## GenderM: Age26-35
                      -191.445
                                    85.238
                                             -2.246 0.024704 *
## GenderM: Age36-45
                      -304.618
                                    88.249
                                             -3.452 0.000557 ***
## GenderM: Age46-50
                      -223.032
                                    95.419
                                             -2.337 0.019419 *
## GenderM: Age51-55
                      -155.584
                                             -1.575 0.115195
                                    98.767
## GenderM: Age55+
                      -317.237
                                             -2.834 0.004600 **
                                   111.948
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard deviation: 4685 on 537557 degrees of freedom
## Multiple R-squared: 0.1155
## F-statistic:
                 3695 on 19 and 537557 DF, p-value: < 2.2e-16
##
        AIC
                 BIC
```

After adding in the interaction term of Gender and Age, I see that the Adjusted R-Squared improves and the variable estimates do not vary by much. Additionally, the estimates remain statistically significant. The interaction terms of Gender on the different age groups have varying degrees of statistical significance. Going forward I use this model as a benchmark for comparison.

Next I show the predictor effects plots of the interaction between Gender and Age on Purchase.

## 10612829 10613064

```
#plotting the predictor effects of gender and age on purchase
plot(predictorEffects(mod.3, ~ Gender:Age), lines=list(multiline=TRUE))
```



I can see from the plots that males Purchases are higher at every age group. The difference in Purchases between males and females is large at the age group of "0-17" and decreases as the age group increases. So female spending increases faster than male spending as the age group increases and begins to converge with male spending. These two plots are showing us the same information.

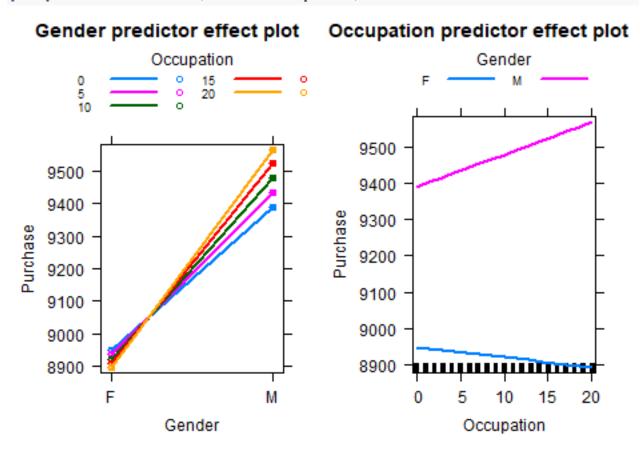
Next I try adding the interaction term of gender and occupation because the spending might be different in the occupation categories depending on the gender.

```
#Model 4 (Adding gender:occupation interaction term)
mod.4 <- lm(Purchase ~ Gender + Age + Occupation + Marital_Status + Product_Category_1 +</pre>
              City_Category + multi + Gender:Occupation, data)
S(mod.4)
## Call: lm(formula = Purchase ~ Gender + Age + Occupation + Marital_Status +
##
            Product_Category_1 + City_Category + multi + Gender:Occupation, data =
##
            data)
##
##
  Coefficients:
##
                       Estimate Std. Error
                                             t value Pr(>|t|)
## (Intercept)
                       9227.009
                                    47.473
                                             194.364
                                                     < 2e-16 ***
## GenderM
                        440.335
                                    22.546
                                              19.531
                                                      < 2e-16 ***
## Age18-25
                        345.953
                                    41.712
                                               8.294
                                                      < 2e-16 ***
## Age26-35
                        538.604
                                    40.511
                                              13.295
                                                      < 2e-16 ***
## Age36-45
                        629.584
                                    41.649
                                              15.117
                                                      < 2e-16 ***
## Age46-50
                        596.101
                                    45.755
                                              13.028
                                                      < 2e-16 ***
## Age51-55
                                    46.725
                                              19.812
                        925.705
                                                      < 2e-16 ***
## Age55+
                        730.781
                                    51.299
                                              14.246
                                                      < 2e-16 ***
```

```
## Occupation
                        -2.805
                                     2.071
                                             -1.354 0.175631
## Marital_Status
                        -50.301
                                             -3.628 0.000286 ***
                                    13.865
                                     1.884 -188.677
## Product Category 1 -355.423
                                                      < 2e-16 ***
## City_CategoryB
                        166.449
                                    15.867
                                             10.490
                                                      < 2e-16 ***
## City_CategoryC
                       721.500
                                    17.159
                                             42.048
                                                      < 2e-16 ***
## multi
                       1139.643
                                    15.228
                                             74.840
                                                      < 2e-16 ***
## GenderM:Occupation
                                     2.357
                                              4.929 8.28e-07 ***
                         11.617
##
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard deviation: 4685 on 537562 degrees of freedom
## Multiple R-squared: 0.1153
  F-statistic: 5004 on 14 and 537562 DF, p-value: < 2.2e-16
##
        AIC
                 BIC
## 10612960 10613139
```

The adjusted R-Squared does not change when I add this interaction term compared to the model with just interaction terms. Additionally, Occupation becomes insignificant, while the interaction of Occupation and Gender is significant.

```
#Marginal effect of Gender:occupation interaction (with occupation variable)
plot(predictorEffects(mod.4, ~ Gender:Occupation), lines=list(multiline=TRUE))
```



I can see from the plots that males spend more at every Occupation category. Females spend the least in occupation category 20 while males spend the most in occupation category 20. This is true for every occupation level.

I now try adding the gender occupation interaction term, but take out the occupation variable because it was

insignificant in the previous model with this interaction term.

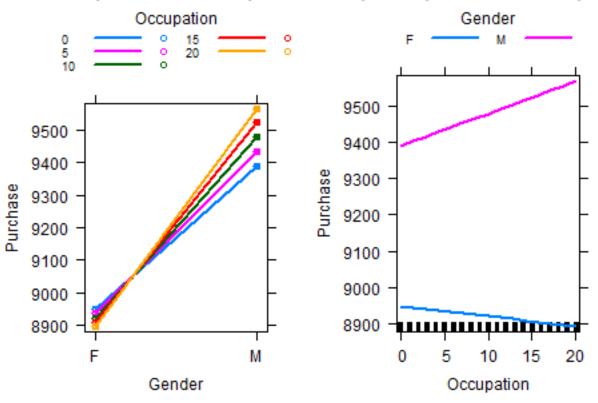
```
#Model 5 (adding gender:occupation interaction term, but without occupation term)
mod.5 <- lm(Purchase ~ Gender + Age + Marital_Status + Product_Category_1 +</pre>
              City_Category + multi + Gender:Occupation, data)
S(mod.5)
## Call: lm(formula = Purchase ~ Gender + Age + Marital_Status +
##
            Product_Category_1 + City_Category + multi + Gender:Occupation, data =
##
            data)
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      9227.009
                                   47.473
                                          194.364 < 2e-16 ***
## GenderM
                       440.335
                                   22.546
                                            19.531 < 2e-16 ***
## Age18-25
                       345.953
                                   41.712
                                             8.294
                                                    < 2e-16 ***
## Age26-35
                       538.604
                                   40.511
                                            13.295 < 2e-16 ***
## Age36-45
                       629.584
                                   41.649
                                            15.117
                                                    < 2e-16 ***
## Age46-50
                       596.101
                                   45.755
                                            13.028
                                                   < 2e-16 ***
## Age51-55
                       925.705
                                   46.725
                                            19.812
                                                    < 2e-16 ***
## Age55+
                       730.781
                                   51.299
                                            14.246 < 2e-16 ***
## Marital_Status
                       -50.301
                                   13.865
                                            -3.628 0.000286 ***
## Product_Category_1 -355.423
                                   1.884 -188.677
                                                    < 2e-16 ***
## City_CategoryB
                       166.449
                                   15.867
                                            10.490 < 2e-16 ***
## City_CategoryC
                       721.500
                                   17.159
                                            42.048
                                                   < 2e-16 ***
## multi
                      1139.643
                                   15.228
                                            74.840 < 2e-16 ***
## GenderF:Occupation
                        -2.805
                                    2.071
                                            -1.354 0.175631
## GenderM:Occupation
                         8.812
                                    1.131
                                             7.790 6.71e-15 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard deviation: 4685 on 537562 degrees of freedom
## Multiple R-squared: 0.1153
                5004 on 14 and 537562 DF, p-value: < 2.2e-16
## F-statistic:
##
        AIC
## 10612960 10613139
```

The Adjusted R-Squared does not change after I take out the occupation category and statistical significance do not change for the variables. However, the interaction of females with occupation becomes insignificant.

Next I show the predictor effects plots of the gender occupation interaction term in this model.

```
#Marginal effect of Gender:occupation interaction (without occupation variable)
plot(predictorEffects(mod.5, ~ Gender:Occupation), lines=list(multiline=TRUE))
```

## Gender predictor effect plot Occupation predictor effect plot



The predictor effects of spending based on gender and occupation does not change from the previous model.

After observing in the effects plots that the marginal effect of occupation on purchase is linear and strictly increasing, I think that the occupation category is separated based on purchasing power because the effect plot shows that as the occupation category increases the spending increases. Due to this, I think adding a quadratic term to occupation will improve the model as it will capture the decreasing marginal returns in spending to an increase in the occupation category.

```
#Model 7 (with quadratic occupation)
mod.6 <- lm(Purchase ~ Gender + Age + Occupation + I(Occupation^2) + City_Category +</pre>
              Marital_Status + Product_Category_1 + multi, data)
S(mod.6)
## Call: lm(formula = Purchase ~ Gender + Age + Occupation + I(Occupation^2)
##
            + City_Category + Marital_Status + Product_Category_1 + multi, data =
##
            data)
##
##
  Coefficients:
##
                                              t value Pr(>|t|)
                        Estimate Std. Error
## (Intercept)
                       8977.8279
                                    47.3348
                                              189.666
                                                      < 2e-16 ***
## GenderM
                        515.6934
                                    14.9878
                                               34.407
                                                       < 2e-16 ***
## Age18-25
                        411.0227
                                    41.8974
                                                9.810
                                                       < 2e-16 ***
## Age26-35
                                    40.7796
                        617.5623
                                               15.144
                                                       < 2e-16 ***
## Age36-45
                        698.8090
                                    41.8492
                                               16.698
                                                       < 2e-16 ***
## Age46-50
                        674.4405
                                    45.9280
                                               14.685
                                                       < 2e-16 ***
## Age51-55
                                    46.8925
                       1001.2764
                                               21.353
                                                       < 2e-16 ***
## Age55+
                        795.0995
                                    51.3931
                                               15.471 < 2e-16 ***
```

```
## Occupation
                        61.4957
                                    3.7502
                                             16.398 < 2e-16 ***
## I(Occupation^2)
                        -2.9421
                                    0.1922
                                            -15.305
                                                    < 2e-16 ***
                       155.3145
## City_CategoryB
                                   15.8653
                                              9.790
                                                     < 2e-16 ***
## City_CategoryC
                                             41.072
                                                    < 2e-16 ***
                       705.3858
                                   17.1746
## Marital_Status
                       -48.6963
                                   13.8471
                                             -3.517 0.000437 ***
## Product Category 1 -354.9086
                                    1.8836 -188.417
                                                    < 2e-16 ***
## multi
                      1138.9584
                                   15.2248
                                             74.809
                                                    < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard deviation: 4684 on 537562 degrees of freedom
## Multiple R-squared: 0.1156
## F-statistic: 5021 on 14 and 537562 DF, p-value: < 2.2e-16
##
        AIC
                 BIC
## 10612750 10612929
```

From the output I can see that the Adjusted R-Squared of 0.1156 has improved and all of the variables are statistically significant. I can see that the estimate of the quadratic occupation term is negative, which indicates that there is decreasing marginal returns to spending as the occupation category increases as I expected.

Next I try adding in the gender and age occupation interaction term with the quadratic occupation term in the model.

```
#model with quadratic occupation and gender:age
mod.7 <- lm(Purchase ~ Gender + Age + Occupation + I(Occupation^2) + Gender: Age + City_Category +
              Marital_Status + Product_Category_1 + multi, data)
S(mod.7)
## Call: lm(formula = Purchase ~ Gender + Age + Occupation + I(Occupation^2)
            + Gender: Age + City_Category + Marital_Status + Product_Category_1 +
            multi, data = data)
##
##
## Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
                                    71.2743
                                             124.523 < 2e-16 ***
## (Intercept)
                      8875.2704
## GenderM
                       666.1997
                                    81.7707
                                               8.147 3.73e-16 ***
## Age18-25
                                               3.098 0.001948 **
                       227.4473
                                    73.4173
## Age26-35
                       757.6103
                                    70.3087
                                              10.775
                                                      < 2e-16 ***
                                              12.725
                                                      < 2e-16 ***
## Age36-45
                       927.8264
                                    72.9123
## Age46-50
                                    79.3639
                                              10.699
                                                      < 2e-16 ***
                       849.1295
## Age51-55
                      1112.2854
                                    82.5587
                                              13.473 < 2e-16 ***
                                              10.802 < 2e-16 ***
## Age55+
                      1024.1485
                                    94.8131
## Occupation
                        61.5485
                                     3.7526
                                              16.402
                                                      < 2e-16 ***
## I(Occupation^2)
                                     0.1923
                                             -15.224
                                                     < 2e-16 ***
                        -2.9279
## City_CategoryB
                                    15.8831
                                               9.903 < 2e-16 ***
                       157.2922
## City_CategoryC
                       703.7400
                                              40.930 < 2e-16 ***
                                    17.1938
## Marital_Status
                       -45.3900
                                    13.8553
                                              -3.276 0.001053 **
                                                      < 2e-16 ***
## Product_Category_1 -354.7798
                                     1.8835 -188.364
## multi
                      1139.4141
                                    15.2235
                                              74.846 < 2e-16 ***
## GenderM: Age18-25
                                    88.8835
                                               2.526 0.011553 *
                       224.4765
## GenderM: Age26-35
                      -205.2082
                                    85.2244
                                              -2.408 0.016047 *
## GenderM: Age36-45
                      -324.5758
                                    88.2401
                                              -3.678 0.000235 ***
## GenderM: Age46-50
                      -260.0536
                                    95.4294
                                              -2.725 0.006429 **
## GenderM: Age51-55
                      -169.7914
                                    98.7500
                                              -1.719 0.085541
## GenderM: Age55+
                      -322.6017
                                   111.9247
                                              -2.882 0.003948 **
```

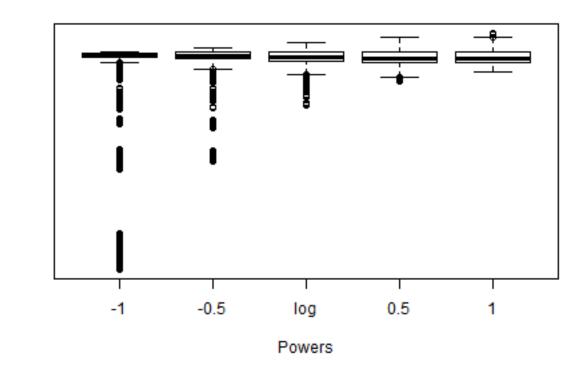
```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard deviation: 4684 on 537556 degrees of freedom
## Multiple R-squared: 0.1159
## F-statistic: 3524 on 20 and 537556 DF, p-value: < 2.2e-16
       AIC
                BIC
## 10612600 10612846
```

The Adjusted R-Squared increases after I add the interaction term. The variables significance do not change. However, the different interactions between age and gender have varying degrees of significance.

```
\#Box\text{-}Cox\ transformation\ test
powerTransform((Occupation+1)~1,data, family = "bcPower")
```

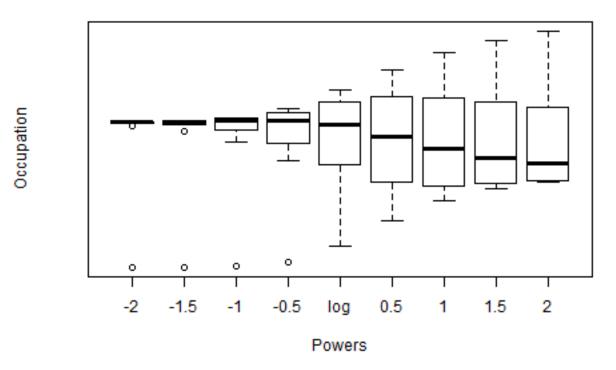
- ## Estimated transformation parameter
- ## Y1
- ## 0.3784342

## Symbox Plot of Purchases



```
## Warning in symbox.default(Occupation, powers = c(-2, -1.5, -1, -0.5, 0, :
## start set to 0.2
```

### Symbox Plot of Occupation



The output above from the power transform function suggests that I should perform a square root transformation to the occupation variable (I rounded the transformation parameter to the nearest tenth). I can confirm the output of the power transform function by looking at the symbox transformation plot of the occupational variable. The symbox plot also suggests that I should perform a square root transformation.

```
#Model 8 (with sqrt(occupation) and gender:age terms)
mod.8 <- lm(Purchase ~ Gender + Age + I(sqrt(Occupation)) + Gender:Age +</pre>
              Marital_Status + Product_Category_1 + City_Category, data)
S(mod.8)
## Call: lm(formula = Purchase ~ Gender + Age + I(sqrt(Occupation)) +
##
            Gender:Age + Marital_Status + Product_Category_1 + City_Category, data =
##
            data)
##
##
   Coefficients:
##
                         Estimate Std. Error
                                              t value Pr(>|t|)
##
   (Intercept)
                        10128.975
                                      69.439
                                              145.868 < 2e-16 ***
                                      82.204
## GenderM
                          607.469
                                                 7.390 1.47e-13 ***
## Age18-25
                          131.060
                                      73.627
                                                 1.780
                                                        0.07507 .
                                      70.489
                                                9.282
## Age26-35
                          654.290
                                                        < 2e-16 ***
## Age36-45
                          846.198
                                      73.126
                                                11.572
                                                        < 2e-16 ***
## Age46-50
                          747.610
                                      79.563
                                                9.396
                                                        < 2e-16 ***
## Age51-55
                                      82.855
                                                12.245
                         1014.595
                                                        < 2e-16 ***
## Age55+
                          957.554
                                      95.249
                                                10.053
                                                        < 2e-16 ***
## I(sqrt(Occupation))
                           43.621
                                       4.673
                                                9.334
                                                        < 2e-16 ***
## Marital Status
                          -56.063
                                      13.926
                                                -4.026 5.68e-05 ***
## Product_Category_1
                         -414.372
                                       1.719 -241.096 < 2e-16 ***
```

```
## City_CategoryB
                          175.324
                                       15.958
                                                10.987
                                                        < 2e-16 ***
## City_CategoryC
                          748.749
                                       17.256
                                                43.391
                                                        < 2e-16 ***
                                                        0.00183 **
## GenderM: Age18-25
                          278.463
                                       89.347
                                                 3.117
                                                -1.747
                                                        0.08067 .
## GenderM: Age26-35
                         -149.657
                                       85.675
## GenderM: Age36-45
                         -277.930
                                       88.704
                                                -3.133
                                                        0.00173 **
## GenderM: Age46-50
                         -181.617
                                       95.916
                                                -1.894
                                                        0.05829 .
## GenderM: Age51-55
                          -96.017
                                       99.269
                                                -0.967
                                                         0.33343
  GenderM: Age55+
                         -294.042
                                      112.523
                                                -2.613
                                                        0.00897 **
##
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard deviation: 4709 on 537558 degrees of freedom
## Multiple R-squared: 0.1064
##
  F-statistic:
                 3555 on 18 and 537558 DF, p-value: < 2.2e-16
##
        AIC
                  BIC
## 10618368 10618592
```

After adding the square root occupation term I can see that the significance for the Age18-25, GenderM:Age26-35, GenderM:Age46-50, and GenderM:Age51-55 variables dropped, when compared to model 7. the GenderM:Age51-55 variable became completely insignificant, while the other terms dropped to a significance level of 10%. The R\_squared for model 8 is also lower than 7, which suggests that the model is worse at explaining the variation in the data. In order to confirm which model is better I looked at the BIC and AIC for each regression.

```
#comparing AIC and BIC of Model 7 and 8
AIC(mod.8, mod.7)

## df AIC

## mod.8 20 10618368

## mod.7 22 10612600

BIC(mod.8, mod.7)

## df BIC

## mod.8 20 10618592

## mod.7 22 10612846
```

From the output above I can see that model 7 has a lower AIC and BIC compared to model 8, which includes the square root occupation term. Since AIC and BIC are used for model comparison I can conclude that model 7 fits and explains the data better than model 8.

```
#Variance Inflation Factor for Model 7
vif(mod.7)
```

```
##
               GenderM
                                   Age18-25
                                                        Age26-35
##
               30.3870
                                    19.6340
                                                         29.0600
##
              Age36-45
                                   Age46-50
                                                        Age51-55
##
               20.8430
                                    11.7260
                                                         10.8710
                                                I(Occupation^2)
##
                Age55+
                                Occupation
##
                8.2332
                                    14.6890
                                                         14.6230
##
                            City_CategoryC
                                                 Marital_Status
       City_CategoryB
##
                1.5073
                                     1.5486
                                                          1.1370
##
   Product_Category_1
                                      multi
                                               GenderM: Age18-25
##
                                                         22.8720
                1.2230
                                     1.2162
##
     GenderM:Age26-35
                          GenderM: Age36-45
                                               GenderM: Age46-50
##
               37.9090
                                    24.4390
                                                         12.3730
##
     GenderM: Age51-55
                            GenderM: Age55+
```

```
## 11.7930 8.8515
```

##

Evaluating the variance inflating factor suggests there is a high degree of colinearity between most of our variables. However, this is to be expected. Since our variables are almost entirely categorical, there is not a wide range of variation and therefore little opportunity for the values of each variable to not be colinear. While I will not use these results to change our model decision, it is worth noting for the sake of completeness.

```
#Creating Stepwise model
step.model <- stepAIC(mod.2, direction = "backward", trace = FALSE)</pre>
summary(step.model)
##
## Call:
  lm(formula = Purchase ~ Gender + Age + Occupation + City_Category +
       Marital_Status + Product_Category_1 + multi, data = data)
##
##
##
  Residuals:
##
        Min
                  1Q
                       Median
                       -717.7
                                        17913.0
##
  -10403.1 -3152.7
                                 2423.4
##
## Coefficients:
##
                      Estimate Std. Error
                                            t value Pr(>|t|)
                                            200.330 < 2e-16 ***
## (Intercept)
                      9164.473
                                    45.747
## GenderM
                       523.371
                                    14.983
                                             34.932
                                                     < 2e-16 ***
## Age18-25
                       348.786
                                    41.709
                                              8.362
                                                     < 2e-16 ***
## Age26-35
                       543.423
                                    40.500
                                             13.418
                                                     < 2e-16 ***
## Age36-45
                       633.682
                                    41.641
                                             15.218
                                                     < 2e-16 ***
## Age46-50
                       605.493
                                    45.716
                                             13.245
                                                     < 2e-16 ***
## Age51-55
                       933.942
                                    46.696
                                             20.001
                                                     < 2e-16 ***
## Age55+
                       738.935
                                    51.273
                                             14.412 < 2e-16 ***
## Occupation
                         6.151
                                     0.994
                                              6.188 6.11e-10 ***
## City_CategoryB
                                             10.335
                       163.903
                                    15.859
                                                    < 2e-16 ***
## City_CategoryC
                       719.382
                                    17.154
                                             41.937
                                                     < 2e-16 ***
## Marital_Status
                                    13.846
                                             -3.895 9.83e-05 ***
                       -53.926
## Product_Category_1 -355.386
                                     1.884 -188.655
                                                     < 2e-16 ***
## multi
                      1140.011
                                    15.228
                                             74.863 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4685 on 537563 degrees of freedom
## Multiple R-squared: 0.1153, Adjusted R-squared: 0.1152
## F-statistic: 5387 on 13 and 537563 DF, p-value: < 2.2e-16
```

When I do a backwards selection on the baseline model (only additive terms), the results suggest to use all the additive terms. These results will be used to compare the results of applying the same process to our selected model.

```
#Creating Stepwise Model
step.model2 <- stepAIC(mod.7, direction = "backward", trace = FALSE)
summary(step.model2)

##
## Call:
## lm(formula = Purchase ~ Gender + Age + Occupation + I(Occupation^2) +
## Gender:Age + City_Category + Marital_Status + Product_Category_1 +
## multi, data = data)</pre>
```

```
## Residuals:
##
        Min
                  10
                       Median
                                    3Q
                                             Max
  -10409.4 -3154.2
                       -702.8
                                2426.3
                                        18160.2
##
## Coefficients:
                                            t value Pr(>|t|)
##
                       Estimate Std. Error
## (Intercept)
                      8875.2704
                                   71.2743
                                             124.523 < 2e-16 ***
## GenderM
                       666.1997
                                   81.7707
                                               8.147 3.73e-16 ***
## Age18-25
                       227.4473
                                   73.4173
                                               3.098 0.001948 **
## Age26-35
                       757.6103
                                   70.3087
                                              10.775
                                                     < 2e-16 ***
## Age36-45
                       927.8264
                                   72.9123
                                              12.725
                                                      < 2e-16 ***
## Age46-50
                       849.1295
                                   79.3639
                                              10.699
                                                     < 2e-16 ***
## Age51-55
                      1112.2854
                                   82.5587
                                              13.473 < 2e-16 ***
## Age55+
                      1024.1485
                                   94.8131
                                              10.802 < 2e-16 ***
                                    3.7526
                                              16.402 < 2e-16 ***
## Occupation
                        61.5485
## I(Occupation^2)
                        -2.9279
                                    0.1923
                                             -15.224
                                                      < 2e-16 ***
## City_CategoryB
                                   15.8831
                                               9.903 < 2e-16 ***
                       157.2922
## City CategoryC
                       703.7400
                                   17.1938
                                              40.930 < 2e-16 ***
                                   13.8553
                                              -3.276 0.001053 **
## Marital_Status
                       -45.3900
## Product_Category_1 -354.7798
                                    1.8835 -188.364 < 2e-16 ***
## multi
                      1139.4141
                                   15.2235
                                             74.846 < 2e-16 ***
## GenderM: Age18-25
                                   88.8835
                                               2.526 0.011553 *
                       224.4765
## GenderM: Age26-35
                      -205.2082
                                   85.2244
                                              -2.408 0.016047 *
## GenderM: Age36-45
                      -324.5758
                                   88.2401
                                              -3.678 0.000235 ***
## GenderM: Age46-50
                      -260.0536
                                   95.4294
                                              -2.725 0.006429 **
## GenderM: Age51-55
                      -169.7914
                                   98.7500
                                              -1.719 0.085541 .
## GenderM: Age55+
                      -322.6017
                                  111.9247
                                             -2.882 0.003948 **
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4684 on 537556 degrees of freedom
## Multiple R-squared: 0.1159, Adjusted R-squared: 0.1159
## F-statistic: 3524 on 20 and 537556 DF, p-value: < 2.2e-16
```

In performing the backward selection, I see that all but the interaction between gender and the 51 to 55 age range and also the 18 to 25 age range are significant. Next I will repeat the process using a stepwise selection process.

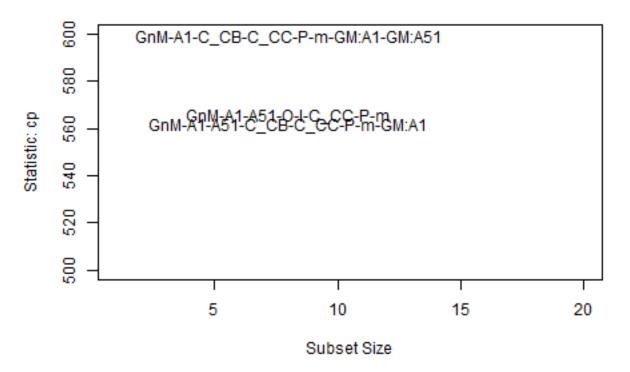
```
step.model3 <- stepAIC(mod.7, direction = "both", trace = FALSE)</pre>
summary(step.model3)
##
## Call:
  lm(formula = Purchase ~ Gender + Age + Occupation + I(Occupation^2) +
       Gender:Age + City_Category + Marital_Status + Product_Category_1 +
##
##
       multi, data = data)
##
## Residuals:
        Min
                  1Q
                        Median
                                     3Q
##
                        -702.8
  -10409.4 -3154.2
                                 2426.3
                                        18160.2
##
## Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      8875.2704
                                    71.2743
                                             124.523 < 2e-16 ***
```

#Creating Stepwise Model

```
## GenderM
                       666.1997
                                   81.7707
                                              8.147 3.73e-16 ***
                                              3.098 0.001948 **
## Age18-25
                       227.4473
                                   73.4173
                                   70.3087
## Age26-35
                       757.6103
                                             10.775 < 2e-16 ***
## Age36-45
                                   72.9123
                                             12.725
                                                    < 2e-16 ***
                       927.8264
## Age46-50
                       849.1295
                                   79.3639
                                             10.699
                                                     < 2e-16 ***
## Age51-55
                      1112.2854
                                   82.5587
                                             13.473 < 2e-16 ***
## Age55+
                      1024.1485
                                   94.8131
                                             10.802 < 2e-16 ***
## Occupation
                                             16.402 < 2e-16 ***
                        61.5485
                                    3.7526
## I(Occupation^2)
                        -2.9279
                                    0.1923
                                            -15.224 < 2e-16 ***
## City_CategoryB
                       157.2922
                                   15.8831
                                              9.903 < 2e-16 ***
## City_CategoryC
                       703.7400
                                   17.1938
                                             40.930 < 2e-16 ***
## Marital_Status
                       -45.3900
                                   13.8553
                                             -3.276 0.001053 **
## Product_Category_1 -354.7798
                                    1.8835 -188.364 < 2e-16 ***
## multi
                      1139.4141
                                   15.2235
                                             74.846 < 2e-16 ***
## GenderM: Age18-25
                                   88.8835
                                              2.526 0.011553 *
                       224.4765
## GenderM: Age26-35
                      -205.2082
                                   85.2244
                                             -2.408 0.016047 *
## GenderM: Age36-45
                      -324.5758
                                   88.2401
                                             -3.678 0.000235 ***
## GenderM: Age46-50
                      -260.0536
                                   95.4294
                                             -2.725 0.006429 **
## GenderM: Age51-55
                                   98.7500
                      -169.7914
                                             -1.719 0.085541 .
## GenderM: Age55+
                      -322.6017
                                  111.9247
                                             -2.882 0.003948 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4684 on 537556 degrees of freedom
## Multiple R-squared: 0.1159, Adjusted R-squared: 0.1159
## F-statistic: 3524 on 20 and 537556 DF, p-value: < 2.2e-16
```

In terms of significance, the results of backward selection and stepwise selection on our model are identical. The only terms that may possibly be desirable to remove is the previously mentioned interaction term and the 18 to 25 age range. I will continue the model evaluation with a Mallow CP.

### Mallows CP



```
##
                       Abbreviation
## GenderM
                                 GnM
## Age18-25
                                  A1
## Age26-35
                                  A2
## Age36-45
                                  AЗ
## Age46-50
                                  A4
## Age51-55
                                 A51
## Age55+
                                 A55
## Occupation
                                   0
## I(Occupation^2)
                                   Ι
## City_CategoryB
                                C_CB
## City_CategoryC
                                C\_CC
## Marital_Status
                                   М
## Product_Category_1
                                   Р
## multi
                                   m
## GenderM: Age18-25
                               GM:A1
## GenderM: Age26-35
                               GM:A2
## GenderM: Age36-45
                               GM:A3
## GenderM: Age46-50
                               GM:A4
## GenderM: Age51-55
                              GM: A51
## GenderM: Age55+
                              GM: A55
data\$A1 = 0
data[(data\$Age=="18-25"), "A1"] = 1
data\$A51 = 0
data[(data\$Age=="51-55"), "A51"] = 1
```

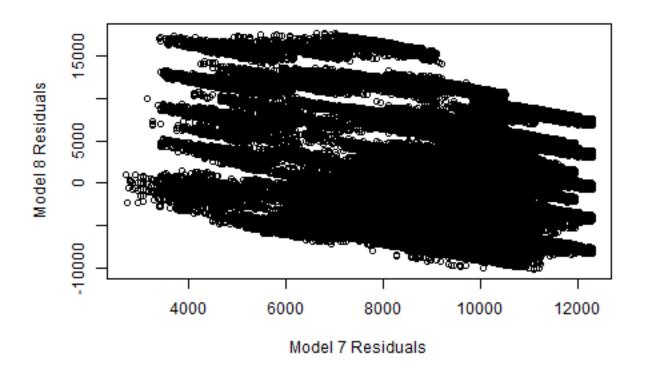
```
data$City_C = 0
data[data$City_C == "C", "City_C"] = 1
test1 = lm(Purchase ~ Gender + A1 + A51 + Occupation + I(Occupation^2) + City_C + Product_Category_1 + 1
test2 = lm(Purchase ~ Gender + A1 + A51 + City_Category + Product_Category_1 + multi + Gender:A1, data)
AIC(test1, mod.7, test2)
##
         df
                 AIC
## test1 9 10615065
## mod.7 22 10612600
## test2 10 10613140
BIC(test1, mod.7, test2)
##
         df
                 BIC
## test1 9 10615166
## mod.7 22 10612846
## test2 10 10613251
```

For the Mallow CP, the resulting graph has been rescaled to exclude all the results that are well above the models of interest so as to see the suggested models more clearly. Interestingly enough, when I compare the two best suggestions from Mallow C with our original model using AIC and BIC, our original model scores better. As a result, I will use the following model:

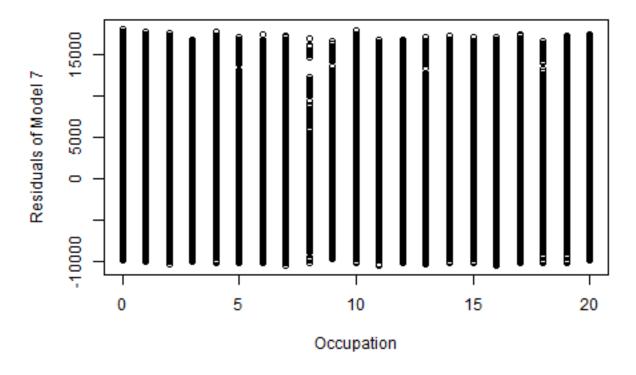
 $Purchases = \beta_o + \beta_1 Male + \beta_2 Occupation + \beta_3 Occupation^2 + \beta_4 Marital Status + \beta_5 Multi + \beta_6 Age + \beta_7 Male \times AGE + \beta_8 City$ 

Now that I have come to our model, I will plot the residuals, plot the fitted values, and perform a 5-fold cross-validation as a robustness check.

```
#Plot of Residuals from models
plot(mod.7$fitted.values, mod.8$residuals, ylab="Model 8 Residuals", xlab="Model 7 Residuals")
```



#Plot of occupation variable and Model 7 residuals
plot(Occupation, mod.7\$residuals, ylab="Residuals of Model 7")



#### #Model 7 is preferred

The residual plot and fitted values plot do not seem to show us very much. This is likely because most of the values are categorical. I can say that the residual plot seems to suggest that the errors are random about zero, which is good. I now move on to cross-validation.

It is important to note that I did not test for heteroskedasticity since the majority of our data is categorical.

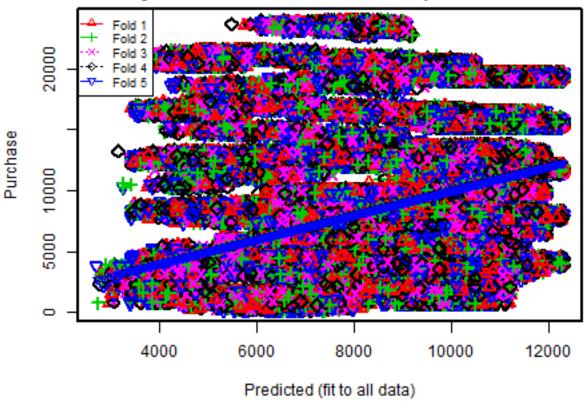
```
cv.lm(data = data, form.lm = mod.7, m = 5, plotit = TRUE, printit = FALSE)
## Warning in cv.lm(data = data, form.lm = mod.7, m = 5, plotit = TRUE, printit = FALSE):
##
##
   As there is >1 explanatory variable, cross-validation
```

predicted values for a fold are not a linear function ##

of corresponding overall predicted values. Lines that ##

are shown for the different folds are approximate ##

## Small symbols show cross-validation predicted values



From the 5-fold cross validation test, I can see that there is a high level of agreement across the different folds. This indicates that our model does reasonably well at predicting purchases for out of model observations. The five-fold cross validation test seaperates the data into five segments and uses 4/5 of those segments to predict the other 1/5.

### summary(mod.7)

```
##
## Call:
  lm(formula = Purchase ~ Gender + Age + Occupation + I(Occupation^2) +
       Gender:Age + City_Category + Marital_Status + Product_Category_1 +
##
       multi, data = data)
##
##
##
  Residuals:
##
        Min
                  1Q
                        Median
                                     3Q
   -10409.4
                        -702.8
                                 2426.3
                                         18160.2
##
             -3154.2
##
## Coefficients:
##
                        Estimate Std. Error
                                             t value Pr(>|t|)
                       8875.2704
## (Intercept)
                                    71.2743
                                             124.523 < 2e-16 ***
## GenderM
                        666.1997
                                    81.7707
                                               8.147 3.73e-16 ***
                                    73.4173
## Age18-25
                        227.4473
                                               3.098 0.001948 **
## Age26-35
                       757.6103
                                    70.3087
                                              10.775
                                                      < 2e-16 ***
                                              12.725
## Age36-45
                        927.8264
                                    72.9123
                                                      < 2e-16 ***
## Age46-50
                       849.1295
                                    79.3639
                                              10.699
                                                      < 2e-16 ***
## Age51-55
                       1112.2854
                                    82.5587
                                              13.473 < 2e-16 ***
## Age55+
                       1024.1485
                                    94.8131
                                              10.802 < 2e-16 ***
```

```
## Occupation
                        61.5485
                                     3.7526
                                              16.402
                                                      < 2e-16 ***
                                             -15.224
## I(Occupation^2)
                        -2.9279
                                    0.1923
                                                      < 2e-16 ***
## City_CategoryB
                                               9.903
                       157.2922
                                    15.8831
                                                      < 2e-16 ***
## City_CategoryC
                       703.7400
                                    17.1938
                                              40.930
                                                      < 2e-16 ***
## Marital_Status
                       -45.3900
                                    13.8553
                                              -3.276 0.001053 **
## Product_Category_1 -354.7798
                                            -188.364
                                     1.8835
                                                      < 2e-16 ***
## multi
                      1139.4141
                                    15.2235
                                              74.846 < 2e-16 ***
## GenderM: Age18-25
                       224.4765
                                    88.8835
                                               2.526 0.011553 *
  GenderM: Age26-35
                      -205.2082
                                    85.2244
                                              -2.408 0.016047 *
  GenderM: Age36-45
                      -324.5758
                                    88.2401
                                              -3.678 0.000235 ***
## GenderM: Age46-50
                      -260.0536
                                    95.4294
                                              -2.725 0.006429 **
  GenderM: Age51-55
                      -169.7914
                                    98.7500
                                              -1.719 0.085541
##
  GenderM: Age55+
                      -322.6017
                                   111.9247
                                              -2.882 0.003948 **
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4684 on 537556 degrees of freedom
## Multiple R-squared: 0.1159, Adjusted R-squared:
## F-statistic: 3524 on 20 and 537556 DF, p-value: < 2.2e-16
```

Reviewing the results of our model, I see that males have consistently higher purchases relative to females across all age groups. Also, while purchases generally increase with age, there are dips in purchases for age group 46 to 50 and group 55 and older. Also, for each increase in the occupation value I see a 25.88 reduction in purchases plus 157.75 for each additional occupation value, on average. For city categories, I see that city category B and C are associated with 165.14 and 716.71 more purchases respectively, all else equal. Being married is associated with a 47.87 reduction in purchases, all else constant. For product category, an increase of the product category number by 1 is associated with a 355.1 reduction in purchases, all else constant. A product having multiple categories, however, is associated with a 1140.35 increase in purchases, all else constant.