

## Homework15

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### Problem1

$L_u = \{ \langle M, w \rangle \mid M \text{ accepts } w \}$  is RE

If there is a decider  $D_u$  for  $L_u$

Then input  $M, w$  to  $D_u$  will yield accept or reject;

So there is a decider  $D_1$  based on  $D_u$  that yields reject or accept if  $D_u$  yields accept or reject;

And there is a decider  $D'$  based on  $D_1$  that takes  $w$  as input and yields the result of  $D_1$ ;

Take  $D'$  as the input of  $D_1$ , if  $D'$  accepts  $w$  then  $D_1$  accepts  $w$  which means  $D'$  rejects  $w$ ;

So  $L_u$  is undecidable.

### Problem2

$L_{\text{halt}} = \{ \langle M, w \rangle \mid M \text{ halts on } w \}$  is RE

If there is a decider  $D_h$  for  $L_h$

Then input  $M, w$  to  $D_h$  will yield accept or reject if  $M$  halts on  $w$  or  $M$  loops on  $w$ ;

So there is a decider  $D_1$  based on  $D_h$  that yields halt or loop if  $D_h$  yields reject or accept;

And there is a decider  $D'$  based on  $D_1$  that takes  $w$  as input and yields the result of  $D_1$ ;

Take  $D'$  as the input of  $D_1$ , if  $D'$  halts on  $w$  then  $D_1$  halts on  $w$  which means  $D'$  loops on  $w$ ;

So  $L_{\text{halt}}$  is undecidable.