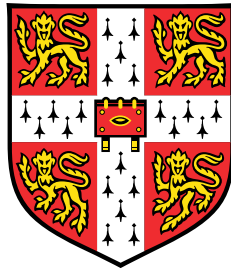


# How to use CUED L<sup>A</sup>T<sub>E</sub>X template

## Using the CUED template



CSSA

Department of Engineering  
University of Cambridge

This work is submitted for the requirements of the  
*First year report*



## Declaration

This report is the result of my own work whilst at Ph.D. candidate at the University of Cambridge and includes nothing which is the outcome of work done in collaboration. No part of this report has been submitted for full or partial fulfilment of the requirements any other degree or diploma at this or any other university or institute of learning.

CSSA

April 2019



## Acknowledgements

I would like to thank CSSA of the University of Cambridge for their “academic supervision and guidance” throughout this Ph.D.

Blah blah blah



## Abstract

This paper .... Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, consectetur id, vulputate a, magna. Donec vehicula augue eu neque. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Mauris ut leo. Cras viverra metus rhoncus sem. Nulla et lectus vestibulum urna fringilla ultrices. Phasellus eu tellus sit amet tortor gravida placerat. Integer sapien est, iaculis in, pretium quis, viverra ac, nunc. Praesent eget sem vel leo ultrices bibendum. Aenean faucibus. Morbi dolor nulla, malesuada eu, pulvinar at, mollis ac, nulla. Curabitur auctor semper nulla. Donec varius orci eget risus. Duis nibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.





# Table of contents

List of figures	xii
List of tables	xiii
<b>1 Introduction</b>	<b>1</b>
1.1 Heading 1 . . . . .	1
1.1.1 Heading 2 . . . . .	1
1.2 Heading 1 with references . . . . .	1
<b>2 Equations, images and algorithms</b>	<b>3</b>
2.1 Image with tikz label . . . . .	3
2.1.1 Equation 1 . . . . .	3
2.1.2 Cross reference equations and images . . . . .	4
2.2 Two images in the same row . . . . .	5
2.3 3 images in the same row . . . . .	5
2.4 Algortihm . . . . .	6
<b>3 Tables and more equations</b>	<b>7</b>
3.1 Simple table . . . . .	7
3.2 Equation with bracket . . . . .	7
3.3 Aligning equations . . . . .	7
3.4 Another table . . . . .	8
<b>References</b>	<b>9</b>
<b>Appendix A Project plan</b>	<b>11</b>
<b>Appendix B Title</b>	<b>13</b>



# List of figures

2.1	The coordinate system for analyzing different diffraction regimes . . . .	3
2.3	Example of position 3 figures . . . . .	5



# List of tables

3.1	General comparison among CPU, GPU and FPGA . . . . .	7
3.2	Comparison of computation time . . . . .	8
3.3	Result comparison between Verilog and MATLAB fft function . . . . .	8



# Chapter 1

## Introduction

This chapter ..... 我来写写中文， 这个中文环境有点傻逼啊，不推荐使用。

### 1.1 Heading 1

Big section

#### 1.1.1 Heading 2

##### Heading 3

List:

- aa
- bb
  - sub list

Numbered list:

1. aa
2. bb
  - (a) sub enumerate list

### 1.2 Heading 1 with references

aa [1][2]





# Chapter 2

## Equations, images and algorithms

This chapter shows you how to write complex equation and position complicated images.

### 2.1 Image with tikz label

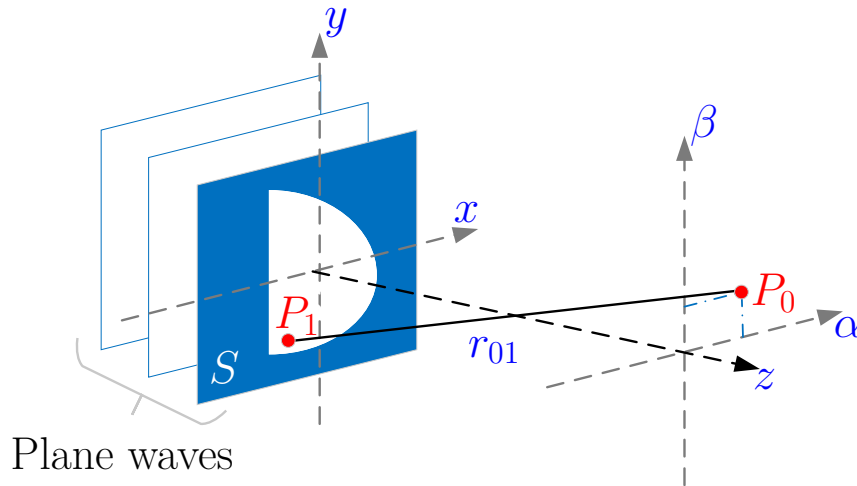


Figure 2.1: The coordinate system for analyzing different diffraction regimes

#### 2.1.1 Equation 1

Consider the geometry shown in Figure. 2.1, coordinates  $(x, y)$  and  $(\alpha, \beta)$  locates at the aperture plane and the observation plane respectively. Setting  $r_{01}$  as the distance

between  $P_0$  and  $P_1$ , the Rayleigh-Sommerfeld relationship becomes:

$$U(\alpha, \beta) = \frac{z}{j\lambda} \iint_{\Sigma} U(x, y) \frac{\exp jkr_{01}}{r_{01}^2} dx dy \quad (2.1-1)$$

where,  $r_{01} = \sqrt{z^2 + (\alpha - x)^2 + (\beta - y)^2}$ . The complexity of  $r_{01}$  suggests further assumptions to simplify Equation. 2.1-1. Assume  $P_0$  and  $P_1$  are reasonably coaxial, then  $r_{01}$  in the denominator approximates to  $z$ . However, it is the fact that small perturbation in the exponential function might lead to huge changes. The simplification of the distance term requires other approach. Binomial expansion is therefore adopted on  $r_{01}$  to eliminate the square root.

$$r_{01} \approx z \left\{ 1 + \frac{1}{2} \left[ \left( \frac{\alpha - x}{z} \right)^2 + \left( \frac{\beta - y}{z} \right)^2 \right] \right\} \quad (2.1-2)$$

Substitution Equation.2.1-2 into Equation.2.1-1 yields the Fresnel diffraction integral:

$$U(\alpha, \beta) = \frac{e^{jkz}}{j\lambda z} e^{j\frac{k(\alpha^2 + \beta^2)}{2z}} \iint \left\{ U(x, y) e^{j\frac{k(x^2 + y^2)}{2z}} \right\} e^{-j\frac{2\pi}{\lambda z}(\alpha x + \beta y)} dx dy \quad (2.1-3)$$

The above equation suggests a significant conclusion: the diffraction pattern is the Fourier transform of a quadratic phase modulated aperture, multiplied with a scaling factor.

### 2.1.2 Cross reference equations and images

Fraunhofer diffraction deals with light propagation in the far field. In this regime, the quadratic phase term in Equation.2.1-3 can be dropped to make the whole equation even simpler:

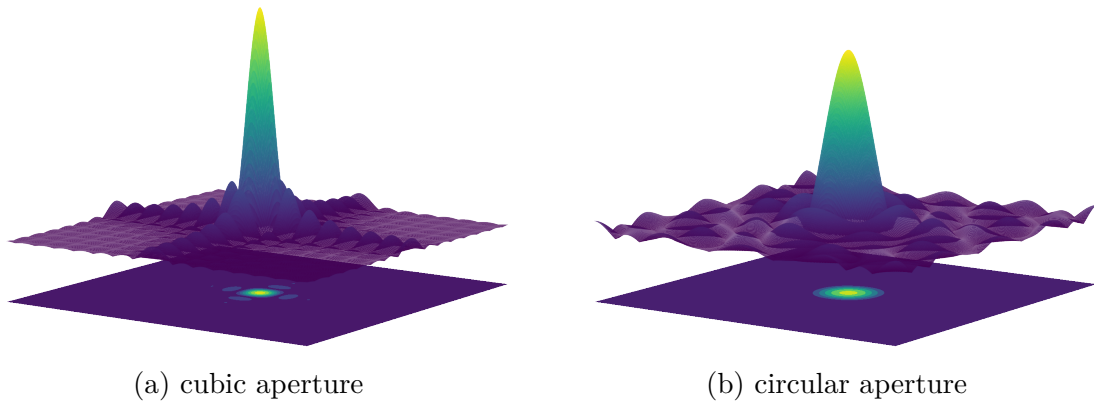
$$U(\alpha, \beta) = \frac{e^{jkz}}{j\lambda z} e^{j\frac{k(\alpha^2 + \beta^2)}{2z}} \iint U(x, y) e^{-j\frac{2\pi}{\lambda z}(\alpha x + \beta y)} dx dy \quad (2.1-4)$$

Normalizing above equation, and letting  $u = \frac{k\alpha}{2\pi z}$ ,  $v = \frac{k\beta}{2\pi z}$  [3], the final relationship becomes:

$$U(u, v) = \iint U(x, y) e^{-j2\pi(ux + vy)} dx dy \quad (2.1-5)$$

Figure 2.2a and 2.2b visualized a plane wave traversing a cubic or a circular aperture respectively.

## 2.2 Two images in the same row



## 2.3 3 images in the same row

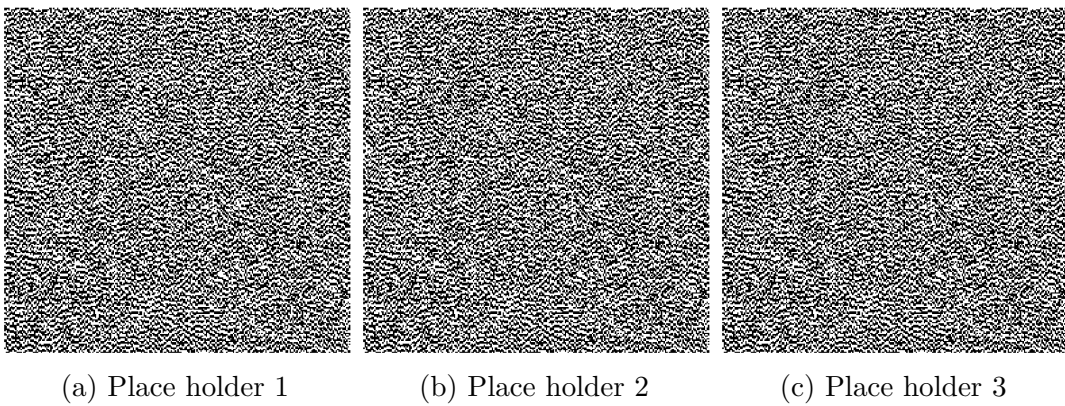


Figure 2.3: Example of position 3 figures

## 2.4 Algortihm

---

**Algorithm 1:** Direct binary search
 

---

**Data:**

$\mathbf{T}$ : Target replay field

$\mathbf{C}_{0,1}$ : Cost function

$\mathbf{H}_{0,1}$ : Replay field after flipping one pixel

**Input:**

$N$ : Number of iterations

**Output:** Optimized phase

- 1 Define the target replay field,  $\mathbf{T}$  Random flip one pixel, and calculate its replay field,  $\mathbf{H}_0$
  - 2 **for**  $k < N$  **do**
  - 3   Take the difference between  $\mathbf{T}$  and  $\mathbf{H}_0$ , calculate the first cost function  $\mathbf{C}_0$ ;
  - 4   Random flip one pixel, then calculate its replay field,  $\mathbf{H}_1$ ;
  - 5   Take the difference between  $\mathbf{T}$  and  $\mathbf{H}_1$ , then find the second cost function  $\mathbf{C}_1$ ;
  - 6   **if**  $C_0 < C_1$  **then**
  - 7     Reject the flip and turn it back;
  - 8   **else if**  $C_0 > C_1$  **then**
  - 9     Accept the flip and update the old cost function  $C_0$  with the new one  $C_1$ ;
  - 10    $\mathbf{k} = \mathbf{k} + 1$
  - 11 **end**
-

# Chapter 3

## Tables and more equations

This chapter ..... table

### 3.1 Simple table

Table 3.1: General comparison among CPU, GPU and FPGA [4]

	Number of cores	Development time	Clock frequency	Power consumption
CPU	Low	Short	High	Average
FPGA	High	Long	Low	Low
GPU	High	Average	High	High

### 3.2 Equation with bracket

$$\theta_H(x_{\alpha j}, y_{\alpha j}, z_j) = kR_{\alpha j} = 2\pi \left( \underbrace{\frac{z_j}{\lambda}}_{\theta_Z} + \underbrace{\frac{p^2}{2\lambda z_j}(x_{\alpha j}^2 + y_{\alpha j}^2)}_{\theta_{XY}} \right) \tag{3.2-1}$$

### 3.3 Aligning equations

$$\theta_{XY}(x_{\alpha j} + d, y_{\alpha j}, z_j) = \text{mod}[\frac{p^2}{2\lambda z_j}(x_{(\alpha j} + d)^2 + y_{\alpha j}^2)] \tag{3.3-1}$$

$$= \text{mod}[\theta_{XY}(x_{\alpha j}, y_{\alpha j}, z_j) + \Gamma_d] \tag{3.3-2}$$

Table 3.2: Comparison of computation time [5]

	Direct computes	Fresnel approximation	Recurrence algorithm
Time(s)	603	118	25

### 3.4 Another table

Table 3.3: Result comparison between Verilog and MATLAB fft function

Input data (s)	Verilog		MATLAB	
	Binary real part	Binary imaginary part	Decimal	Decimal
1	9'b011111111	9'b000000000	255	255
2	9'b000110000	9'b010100101	48+j165	48.6396 + j166.0660
4	9'b111001101	9'b001100110	-51+j102	-51 + j102
8	9'b110110010	9'b000101101	-78+j45	-78.6396 + j46.0660
16	9'110101011	9'b000000000	-85	-85
32	9'b110110010	9'b111010011	-78-j45	-78.6396 - j46.0660
64	9'b111001101	9'b110011010	-51-j102	-51 - j102
128	9'b000110000	9'b101011011	48-j165	48.6396 -j166.066

# References

- [1] D. Gabor. A new microscopic principle. *Nature*, 161(161):777–778, May 1948.
- [2] H. Kim, Y. Kim, H. Ji, H. Park, J. An, H. Song, Y. T. Kim, H. Lee, and K. Kim. A single-chip fpga holographic video processor. *IEEE Transactions on Industrial Electronics*, 66(3):2066–2073, March 2019.
- [3] T. Wilkinson. Lecture notes 4B11 photonics systems, October 2015.
- [4] T. Shimobaba, T. Kakue, and T. Ito. Review of fast algorithms and hardware implementations on computer holography. *IEEE TRANSACTIONS ON INDUSTRIAL INFORMATICS*, 12(4):1611–1622, 2016.
- [5] T. Shimobaba and T. Ito. An efficient computational method suitable for hardware of computer-generated hologram with phase computation by addition. *Computer physics communications*, 138:44–52, July 2001.





# Appendix A

## Project plan

aaaaaaa



# Appendix B

## Title

bbbbbb