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Working Draft, C++ Extensions for Numerics

Note: this is an early draft. It's known to be incomplet and incorrekt, and it has lots of bad formatting.

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1 Scope [scope]

¹ This document describes extensions to the C++ Standard Library. This document specifies requirements for implementations of an interface that computer programs written in the C++ programming language may use to perform operations related to numbers, such as work with unbounded numbers. This document is applicable to information technology systems that can perform operations with big numbers. This document is applicable only to vendors who wish to provide the interface it describes.

2 Normative references

[references]

- ¹ The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.
- (1.1) ISO/IEC 14882:2017, Programming languages C++
 - ² The programming language and library described in ISO/IEC 14882 is herein called the C++ Standard. References to clauses within the C++ Standard are written as "C++ 2017 [library]".
 - ³ Unless otherwise specified, the whole of the C++ Standard's Library introduction (C++ 2017 [library]) is included into this document by reference.

3 Feature test macros (Informative) [feature.test]

- ¹ These macros allow users to determine which version of this document is supported by the headers defined by the specification. All headers in this document shall define the __cpp_lib_experimental_net feature test macro in Table 1.
- ² If an implementation supplies all of the conditionally-supported features specified in ??, <wide_integer> header in this document shall additionally define the __cpp_lib_wide_integer feature test macro.

Table 1 — Feature-test macro(s)

Macro name	Value
cpp_lib_wide_integer	201909

4 Wide_integer

[wide_integer]

4.1 Class template numeric_limits

[numeric.limits]

[Note to editor: Add the following sentence after the sentence "Specializations shall be provided for each arithmetic type, both floating-point and integer, including bool." (first sentence in fourth paragraph in [numeric.limits]) - end note]

Specializations shall be also provided for wide_integer type.

[Note: If there is a built-in integral type Integral that has the same signedness and width as wide_-integer<Bits, S>, then numeric_limits<wide_integer<Bits, S>> specialized in the same way as numeric_-limits<Integral> — end note]

4.2 Header <wide_integer> synopsis

[numeric.wide_integer.syn]

```
namespace std {
  // 26.??.2 class template wide_integer
  template<size_t Bits, typename S> class wide_integer;
  // 26.??.?? type traits specializations
  template<size_t Bits, typename S, size_t Bits2, typename S2>
    struct common_type<wide_integer<Bits, S>, wide_integer<Bits2, S2>>;
 template<size_t Bits, typename S, typename Arithmetic>
    struct common_type<wide_integer<Bits, S>, Arithmetic>;
  template<typename Arithmetic, size_t Bits, typename S>
    struct common_type<Arithmetic, wide_integer<Bits, S>>
  : common_type<wide_integer<Bits, S>, Arithmetic>
  // 26.??.?? unary operations
  template<size_t Bits, typename S>
    constexpr wide_integer<Bits, S> operator~(const wide_integer<Bits, S>& val) noexcept;
  template<size_t Bits, typename S>
    constexpr wide_integer<Bits, S> operator-(const wide_integer<Bits, S>& val) noexcept(is_unsigned_v<S>);
 template<size_t Bits, typename S>
    constexpr wide_integer<Bits, S> operator+(const wide_integer<Bits, S>& val) noexcept(is_unsigned_v<S>);
  // 26.??.?? binary operations
  template<size_t Bits, typename S, size_t Bits2, typename S2>
  common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
    constexpr operator*(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs);
  template<size_t Bits, typename S, size_t Bits2, typename S2>
  common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
    constexpr operator/(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs);
  template<size_t Bits, typename S, size_t Bits2, typename S2>
  common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
    constexpr operator+(const wide_integer<Bits, S>& lhs,
```

```
const wide_integer<Bits2, S2>& rhs) noexcept(is_unsigned_v<S>);
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator-(const wide_integer<Bits, S>& lhs,
                      const wide_integer<Bits2, S2>& rhs) noexcept(is_unsigned_v<S>);
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator%(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs);
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator&(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator|(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator^(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
template<size_t Bits, typename S>
common_type_t<wide_integer<Bits, S>, size_t>
  constexpr operator<<(const wide_integer<Bits, S>& lhs, size_t rhs);
template<size_t Bits, typename S>
common_type_t<wide_integer<Bits, S>, size_t>
  constexpr operator>>(const wide_integer<Bits, S>& lhs, size_t rhs);
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator<(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator>(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator<=(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator>=(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator==(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator!=(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
// 26.??.?? numeric conversions
template<size_t Bits, typename S> std::string to_string(const wide_integer<Bits, S>& val);
template<size_t Bits, typename S> std::wstring to_wstring(const wide_integer<Bits, S>& val);
// 26.??.?? iostream specializations
template<class Char, class Traits, size_t Bits, typename S>
```

```
basic_ostream<Char, Traits>& operator<<(basic_ostream<Char, Traits>& os,
                                             const wide_integer<Bits, S>& val);
  template<class Char, class Traits, size_t Bits, typename S>
    basic_istream<Char, Traits>& operator>>(basic_istream<Char, Traits>& is,
                                             wide_integer<Bits, S>& val) noexcept;
  // 26.??.?? hash support
  template<class T> struct hash;
  template<size_t Bits, typename S> struct hash<wide_integer<Bits, S>>;
  template <size_t Bits, typename S>
    to_chars_result to_chars(char* first, char* last, const wide_integer<Bits, S>& value,
                             int base = 10);
  template <size_t Bits, typename S>
    from_chars_result from_chars(const char* first, const char* last, wide_integer<Bits, S>& value,
                                 int base = 10);
  template <size_t Bits>
  using wide_int = wide_integer<Bits, signed>;
 template <size_t Bits>
  using wide_uint = wide_integer < Bits, unsigned >
  // optional literals
  inline namespace literals {
 inline namespace wide_int_literals {
  constexpr wide_int<128> operator "" _int128(const char*);
  constexpr wide_int<256> operator "" _int256(const char*);
  constexpr wide_int<512> operator "" _int512(const char*);
 constexpr wide_uint<128> operator "" _uint128(const char*);
  constexpr wide_uint<256> operator "" _uint256(const char*);
  constexpr wide_uint<512> operator "" _uint512(const char*);
  } // namespace wide_int_literals
  } // namespace literals
} // namespace std
```

The header <wide_integer> defines class template wide_integer and a set of operators for representing and manipulating integers of specified width.

Example:

4.3 Template class wide_integer overview

[numeric.wide_integer.overview]

```
namespace std {
 template<size_t Bits, typename S>
  class wide_integer {
  public:
    // 26.??.2.?? construct:
    constexpr wide_integer() noexcept = default;
    constexpr wide_integer(const wide_integer<Bits, S>& ) noexcept = default;
    template<typename Arithmetic> constexpr wide_integer(const Arithmetic& other) noexcept;
    template<size_t Bits2, typename S2> constexpr wide_integer(const wide_integer<Bits2, S2>& other) noexcept;
    // 26.??.2.?? assignment:
    constexpr wide_integer<Bits, S>& operator=(const wide_integer<Bits, S>& ) noexcept = default;
    template<typename Arithmetic>
      constexpr wide_integer<Bits, S>& operator=(const Arithmetic& other) noexcept;
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator=(const wide_integer<Bits2, S2>& other) noexcept;
    // 26.??.2.?? compound assignment:
    template<typename Arithmetic>
      constexpr wide_integer<Bits, S>& operator*=(const Arithmetic&);
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator*=(const wide_integer<Bits2, S2>&);
    template<typename Arithmetic>
      constexpr wide_integer<Bits, S>& operator/=(const Arithmetic&);
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator/=(const wide_integer<Bits2, S2>&);
    template<typename Arithmetic>
      constexpr wide_integer<Bits, S>& operator+=(const Arithmetic&) noexcept(is_unsigned_v<S>);
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator+=(const wide_integer<Bits2, S2>&) noexcept(is_unsigned_v<S>);
    template<typename Arithmetic>
      constexpr wide_integer<Bits, S>& operator-=(const Arithmetic&) noexcept(is_unsigned_v<S>);
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator-=(const wide_integer<Bits2, S2>&) noexcept(is_unsigned_v<S>);
    template<typename Integral>
      constexpr wide_integer<Bits, S>& operator%=(const Integral&);
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator%=(const wide_integer<Bits2, S2>&);
    template<typename Integral>
      constexpr wide_integer<Bits, S>& operator&=(const Integral&) noexcept;
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator&=(const wide_integer<Bits2, S2>&) noexcept;
    template<typename Integral>
      constexpr wide_integer<Bits, S>& operator|=(const Integral&) noexcept;
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator|=(const wide_integer<Bits2, S2>&) noexcept;
    template<typename Integral>
```

```
constexpr wide_integer<Bits, S>& operator^=(const Integral&) noexcept;
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator^=(const wide_integer<Bits2, S2>&) noexcept;
    template<typename Integral>
      constexpr wide_integer<Bits, S>& operator<<=(const Integral&);</pre>
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator<<=(const wide_integer<Bits2, S2>&);
    template<typename Integral>
      constexpr wide_integer<Bits, S>& operator>>=(const Integral&) noexcept;
    template<size_t Bits2, typename S2>
      constexpr wide_integer<Bits, S>& operator>>=(const wide_integer<Bits2, S2>&) noexcept;
    constexpr wide_integer<Bits, S>& operator++() noexcept(is_unsigned_v<S>);
    constexpr wide_integer<Bits, S> operator++(int) noexcept(is_unsigned_v<S>);
    constexpr wide_integer<Bits, S>& operator--() noexcept(is_unsigned_v<S>);
    constexpr wide_integer<Bits, S> operator--(int) noexcept(is_unsigned_v<S>);
    // 26.??.2.?? observers:
    template <typename Arithmetic> constexpr operator Arithmetic() const noexcept;
      constexpr explicit operator bool() const noexcept;
  private:
    byte data[Bits / CHAR_BITS]; // exposition only
} // namespace std
```

The class template wide_integer<size_t Bits, typename S> is a trivial standard layout class that behaves as an integer type of a compile time specified bitness.

Template parameter Bits specifies exact bits count to store the integer value. Bits

When size of wide_integer is equal to a size of builtin integral type then the alignment and layout of that wide integer is equal to the alignment and layout of the builtin type.

Template parameter S specifies signedness of the stored integer value and is either signed or unsigned.

Implementations are permitted to add explicit conversion operators and explicit or implicit constructors for Arithmetic and for Integral types.

Example:

```
template<size t Bits2, typename S2>
  constexpr wide_integer(const wide_integer<Bits2, S2>& other) noexcept;
     Effects: Constructs an object from other using the integral conversion rules [conv.integral].
4.3.2 wide_integer assignments
                                                                 [numeric.wide integer.assign]
template<typename Arithmetic>
  constexpr wide_integer<Bits, S>& operator=(const Arithmetic& other) noexcept;
     Effects: Constructs an object from other using the integral conversion rules [conv.integral].
template<size_t Bits2, typename S2>
  constexpr wide_integer<Bits, S>& operator=(const wide_integer<Bits2, S2>& other) noexcept;
     Effects: Constructs an object from other using the integral conversion rules [conv.integral].
4.3.3 wide_integer compound assignments
                                                                [numeric.wide_integer.cassign]
template<size_t Bits2, typename S2>
 constexpr wide_integer<Bits, S>& operator*=(const wide_integer<Bits2, S2>&);
template<size_t Bits2, typename S2>
  constexpr wide_integer<Bits, S>& operator/=(const wide_integer<Bits2, S2>&);
template<size_t Bits2, typename S2>
  constexpr wide_integer<Bits, S>& operator+=(const wide_integer<Bits2, S2>&) noexcept(is_unsigned_v<S>);
template<size_t Bits2, typename S2>
  constexpr wide_integer<Bits, S>& operator-=(const wide_integer<Bits2, S2>&) noexcept(is_unsigned_v<S>);
template<size_t Bits2, typename S2>
  constexpr wide_integer<Bits, S>& operator%=(const wide_integer<Bits2, S2>&);
template<size_t Bits2, typename S2>
  constexpr wide_integer<Bits, S>& operator&=(const wide_integer<Bits2, S2>&) noexcept;
template<size_t Bits2, typename S2>
 constexpr wide integer < Bits, S > & operator | = (const wide integer < Bits2, S2 > &) noexcept;
template<size_t Bits2, typename S2>
 constexpr wide_integer<Bits, S>& operator^=(const wide_integer<Bits2, S2>&) noexcept;
template<size_t Bits2, typename S2>
 constexpr wide_integer<Bits, S>& operator<<=(const wide_integer<Bits2, S2>&);
template<size_t Bits2, typename S2>
 constexpr wide_integer<Bits, S>& operator>>=(const wide_integer<Bits2, S2>&) noexcept;
constexpr wide_integer<Bits, S>& operator++() noexcept(is_unsigned_v<S>);
constexpr wide_integer<Bits, S> operator++(int) noexcept(is_unsigned_v<S>);
constexpr wide_integer<Bits, S>& operator--() noexcept(is_unsigned_v<S>);
constexpr wide_integer<Bits, S> operator--(int) noexcept(is_unsigned_v<S>);
     Effects: Behavior of the above operators is similar to operators for built-in integral types.
template<typename Arithmetic>
  constexpr wide_integer<Bits, S>& operator*=(const Arithmetic&);
template<typename Arithmetic>
 constexpr wide_integer<Bits, S>& operator/=(const Arithmetic&);
template<typename Arithmetic>
 constexpr wide_integer<Bits, S>& operator+=(const Arithmetic&) noexcept(is_unsigned_v<S>);
template<typename Arithmetic>
  constexpr wide_integer<Bits, S>& operator-=(const Arithmetic&) noexcept(is_unsigned_v<S>);
     Effects: As if an object wi of type wide_integer Bits, S> was created from input value and the
     corresponding operator was called for *this and the wi.
```

```
template<typename Integral>
  constexpr wide_integer<Bits, S>& operator%=(const Integral&);
template<typename Integral>
  constexpr wide_integer<Bits, S>& operator&=(const Integral&) noexcept;
template<typename Integral>
  constexpr wide_integer<Bits, S>& operator|=(const Integral&) noexcept;
template<typename Integral>
  constexpr wide_integer<Bits, S>& operator^=(const Integral&) noexcept;
template<typename Integral>
  constexpr wide_integer<Bits, S>& operator<==(const Integral&);
template<typename Integral>
  constexpr wide_integer<Bits, S>& operator<>=(const Integral&);
template<typename Integral>
  constexpr wide_integer<Bits, S>& operator>>=(const Integral&) noexcept;
```

Effects: As if an object wi of type wide_integer<Bits, S> was created from input value and the corresponding operator was called for *this and the wi.

4.3.4 wide_integer observers

[numeric.wide_integer.observers]

template <typename Arithmetic> constexpr operator Arithmetic() const noexcept;

Returns: If is_integral_v<Arithmetic> then Arithmetic is constructed from *this using the integral conversion rules [conv.integral]. If is_floating_point_v<Arithmetic>, then Arithmetic is constructed from *this using the floating-integral conversion rules [conv.fpint]. Otherwise the operator shall not participate in overload resolution.

4.4 Specializations of common_type [numeric.wide_integer.traits.specializations]

```
template<size_t Bits, typename S, size_t Bits2, typename S2>
struct common_type<wide_integer<Bits, S>, wide_integer<Bits2, S2>> {
   using type = wide_integer<max(Bits, Bits2), see below>;
};
```

The signed template parameter indicated by this specialization is following:

- (is_signed_v<S> && is_signed_v<S2> ? signed : unsigned) if Bits == Bits2
- S if Bits > Bits2
- S2 otherwise

[Note: common type follows the usual arithmetic conversions design. - end note]

[Note: common_type attempts to follow the usual arithmetic conversions design here for interoperability between different numeric types. Following two specializations must be moved to a more generic place and enriched with usual arithmetic conversion rules for all the other numeric classes that specialize std::numeric_-limits- end note]

```
template<size_t Bits, typename S, typename Arithmetic>
struct common_type<wide_integer<Bits, S>, Arithmetic> {
    using type = see below;
};

template<typename Arithmetic, size_t Bits, typename S>
struct common_type<Arithmetic, wide_integer<Bits, S>>
: common_type<wide_integer<Bits, S>, Arithmetic>;

The member typedef type is following:
```

— Arithmetic if numeric limits<Arithmetic>::is integer is false

```
— wide_integer<Bits, S> if sizeof(wide_integer<Bits, S>) > sizeof(Arithmetic)
  — Arithmetic if sizeof(wide_integer<Bits, S>) < sizeof(Arithmetic)</pre>
  — Arithmetic if sizeof(wide_integer<Bits, S>) == sizeof(Arithmetic) && is_signed_v<S>
  — Arithmetic if sizeof(wide integer<Bits, S>) == sizeof(Arithmetic) && numeric limits<wide -</pre>
     integer<Bits, S>>::is signed == numeric limits<Arithmetic>::is signed
  — wide_integer<Bits, S> otherwise
4.5 Unary operators
                                                          [numeric.wide_integer.unary_ops]
template<size_t Bits, typename S>
  constexpr wide_integer<Bits, S> operator~(const wide_integer<Bits, S>& val) noexcept;
     Returns: value with inverted significant bits of val.
template<size_t Bits, typename S>
  constexpr wide_integer<Bits, S> operator-(const wide_integer<Bits, S>& val) noexcept(is_unsigned_v<S>);
     Returns: val *= -1 if S is true, otherwise the result is unspecified.
template<size_t Bits, typename S>
  \verb|constexpr wide_integer<Bits, S> operator + (\verb|const wide_integer<Bits, S> \& val) no except(is_unsigned_v<S>); \\
     Returns: val.
                                                          [numeric.wide_integer.binary_ops]
4.6 Binary operators
In the function descriptions that follow, CT represents common_type_t<A, B>, where A and B are the types
of the two arguments to the function.
template<size_t Bits, typename S, size_t Bits2, typename S2>
  common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator*(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs);
     Returns: CT(lhs) *= rhs.
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator/(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs);
     Returns: CT(lhs) /= rhs.
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
 constexpr operator+(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs)
                     noexcept(is_unsigned_v<S>);
     Returns: CT(lhs) += rhs.
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator-(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs)
                     noexcept(is_unsigned_v<S>);
     Returns: CT(lhs) -= rhs.
```

```
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator%(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs);
     Returns: CT(lhs) %= rhs.
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator&(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
     Returns: CT(lhs) \&= rhs.
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator|(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
     Returns: CT(lhs) \mid = rhs.
template<size_t Bits, typename S, size_t Bits2, typename S2>
common_type_t<wide_integer<Bits, S>, wide_integer<Bits2, S2>>
  constexpr operator^(const wide_integer<Bits, S>& lhs, const wide_integer<Bits2, S2>& rhs) noexcept;
     Returns: CT(lhs) ^= rhs.
template<size_t Bits, typename S>
common_type_t<wide_integer<Bits, S>, size_t>
  constexpr operator<<(const wide_integer<Bits, S>& lhs, size_t rhs);
     Returns: CT(lhs) <<= rhs.
template<size_t Bits, typename S>
common_type_t<wide_integer<Bits, S>, size_t>
  constexpr operator>>(const wide_integer<Bits, S>& lhs, size_t rhs) noexcept;
     Returns: CT(lhs) >>= rhs.
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator<(const wide_integer<Bits, S>& lhs,
                           const wide_integer<Bits2, S2>& rhs) noexcept;
     Returns: true if value of CT(lhs) is less than the value of CT(rhs).
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator>(const wide_integer<Bits, S>& lhs,
                           const wide_integer<Bits2, S2>& rhs) noexcept;
     Returns: true if value of CT(lhs) is greater than the value of CT(rhs).
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator<=(const wide_integer<Bits, S>& lhs,
                            const wide_integer<Bits2, S2>& rhs) noexcept;
     Returns: true if value of CT(lhs) is equal or less than the value of CT(rhs).
template<size_t Bits, typename S, size_t Bits2, typename S2>
  constexpr bool operator>=(const wide_integer<Bits, S>& lhs,
                            const wide_integer<Bits2, S2>& rhs) noexcept;
     Returns: true if value of CT(lhs) is equal or greater than the value of CT(rhs).
```

4.7 Numeric conversions

[numeric.wide_integer.conversions]

```
template<size_t Bits, typename S> std::string to_string(const wide_integer<Bits, S>& val);
template<size_t Bits, typename S> std::wstring to_wstring(const wide_integer<Bits, S>& val);
```

Returns: Each function returns an object holding the character representation of the value of its argument. All the significant bits of the argument are outputed as a signed decimal in the style [-]dddd.

Behavior of wide_integer overload is subject to the usual rules of primitive numeric output conversion functions [utility.to.chars].

Behavior of wide_integer overload is subject to the usual rules of primitive numeric input conversion functions [utility.from.chars].

4.8 iostream specializations

[numeric.wide integer.io]

template<class Char, class Traits, size_t Bits, typename S>

- Effects: Extracts a wide_integer that is represented as a decimal number in the is. If bad input is encountered, calls is.setstate(ios_base::failbit) (which may throw ios::failure ([iostate.flags])).
- 4 Returns: is.

4.9 Hash support

[numeric.wide_integer.hash]

```
template<size_t Bits, typename S> struct hash<wide_integer<Bits, S>>;
```

The specialization is enabled (20.14.14). If there is a built-in integral type Integral that has the same typename and width as wide_integer<Bits, S>, and wi is an object of type wide_integer<Bits, S>, then hash<wide_integer<MachineWords, S>>()(wi) == hash<Integral>()(Integral(wi)).

2

5 Unbounded Types

[unbounded_types]

5.1 Class integer_data_proxy

[numeric.integer_data_proxy.syn]

```
namespace std {
  class integer_data_proxy {
        // type names
        typedef unspecified data_type;
        typedef unspecified arithmetic_type;
        typedef unspecified uarithmetic_type;
        typedef unspecified iterator;
        typedef unspecified const_iterator;
        typedef unspecified reverse_iterator;
        typedef unspecified const_reverse_iterator;
        // constructors
        integer_data_proxy(const integer_data_proxy& rhs) = delete;
        integer_data_proxy(integer_data_proxy&& rhs);
        integer_data_proxy& operator=(const integer_data_proxy& rhs) = delete;
        integer_data_proxy& operator=(integer_data_proxy&& rhs) = delete;
        // iterators
        iterator begin() noexcept;
        iterator end() noexcept;
        reverse_iterator rbegin() noexcept;
        reverse_iterator rend() noexcept;
        const_iterator cbegin() const noexcept;
        const_iterator cend() const noexcept;
        const_reverse_iterator crbegin() const noexcept;
        const_reverse_iterator crend() const noexcept;
        // element access
        data_type operator[](size_t pos) const;
        data_type& operator[](size_t pos);
        // capacity
        size_t size() const noexcept;
        size_t capacity() const noexcept;
        void reserve(size_t digits);
        void shrink_to_fit();
  };
} // namespace std
```

The class describes an object that can be used to examine and modify the internal representation of an object of type integer. This allows advanced users to portably implement algorithms that are not provided natively.

There can be only one integer_data_proxy object associated with a particular integer object at any given time; that object is obtained by calling the get_data_proxy member function on the integer object. The

resulting object can be moved but not copied.

typedef unspecified arithmetic_type;

The typedef defines a synonym for a signed arithmetic type that is large enough to hold the product of the largest values that the implementation will store in an object of type data_type.

iterator begin();

Returns: An iterator object such that the iterators [begin(), end()) point to the internal data elements of the integer object.

size_t capacity() const noexcept;

Returns: The number of decimal digits that the integer object can represent without reallocating its internal storage.

const_iterator cbegin() const;

Returns: An iterator object such that the iterator range [cbegin(), cend()) points to the internal data elements of the integer object.

const_iterator cend() const;

Returns: An iterator object such that the iterator range [cbegin(), cend()) points to the internal data elements of the integer object.

typedef unspecified const_iterator;

The typedef defines a synonym for an iterator that can be used to access but not modify internal data elements of the integer object.

typedef unspecified const_reverse_iterator;

The typedef defines a synonym for a reverse iterator that can be used to access but not modify internal data elements of the integer object.

const_reverse_iterator crbegin() const;

Returns: The member function returns a reverse iterator object such that the iterator range [crbegin(), crend()) points to the internal data elements of the integer object in reverse order.

const_reverse_iterator crend() const;

Returns: A reverse iterator object such that the iterator range [crbegin(), crend()) points to the internal data elements of the integer object in reverse order.

typedef unspecified data_type;

The typedef defines a synonym for the type of the integer object's internal data elements.

iterator end();

Returns: An iterator object such that the iterator range [begin(), end()) points to the internal data elements of the integer object.

integer_data_proxy(const integer_data_proxy&) = delete;

The copy constructor is deleted.

```
integer_data_proxy(integer_data_proxy&& rhs);
```

Effects: Copies the contents of rhs and leaves rhs in an unspecified valid state.

```
typedef unspecified iterator;
```

The typedef defines a synonym for an iterator that can be used to access internal data elements of the integer object.

```
integer& operator=(const integer_data_proxy&) = delete;
integer& operator=(integer_data_proxy&&) = delete;
```

The copy assignment and move assignment operators are deleted.

```
data_type operator[](size_t pos) const;
```

Returns: The value of the internal data element at index pos.

```
data_type& operator[](size_t pos);
```

Returns: A reference to the internal data element at index pos.

```
reverse_iterator rbegin();
```

Returns: A reverse iterator object such that the iterator range [crbegin(), crend()) points to the internal data elements of the integer object in reverse order.

```
reverse_iterator rend();
```

Returns: A reverse iterator object such that the iterator range [crbegin(), crend()) points to the internal data elements of the integer object in reverse order.

```
void reserve(size_t digits);
```

Effects: Ensures that capacity() >= digits.

```
typedef unspecified reverse_iterator;
```

The typedef defines a synonym for a reverse iterator that can be used to access internal data elements of the integer object.

```
void shrink_to_fit();
```

Effect on original feature: Is a non-binding request to reduce capacity() to hold the integer object's current stored value without wasted space.

```
size_t size() const;
```

Returns: capacity().

```
typedef unspecified uarithmetic_type;
```

The typedef defines a synonym for an unsigned arithmetic type that is large enough to hold the product of the largest values that the implementation will store in an object of type data_type.

5.2 Bits [numeric.bits.syn]

```
namespace std {
  // 26.??.?? binary operations
 bits operator&(const bits& lhs, const bits& rhs);
  bits operator|(const bits& lhs, const bits& rhs);
  bits operator (const bits& lhs, const bits& rhs);
  // 26.??.?? iostream specializations
  template < class CharT, class Traits >
    basic_ostream<CharT, Traits>& operator<<(basic_ostream<CharT, Traits>& os,
                                              const bits& val);
  template < class CharT, class Traits>
    basic_ostream<CharT, Traits>& operator>>(basic_ostream<CharT, Traits>& os,
                                              bits& val);
} // namespace std
namespace std {
  class bits {
  public:
    class reference;
    // constructors
    bits() noexcept;
    template <class Ty>
      bits(Ty rhs) noexcept;
                                // integral types only
    bits(initializer_list<uint_least32_t> list);
    template <class CharT, class Traits, class Alloc>
      explicit bits(const basic_string<CharT, Traits, Alloc>& str,
                    typename basic_string<CharT, Traits, Alloc>::size_t pos = 0,
                    typename basic_string<CharT, Traits, Alloc>::size_t count = std::basic_string<CharT>::npos,
                    CharT zero = CharT('0'),
                    CharT one = CharT('1'));
        template <class CharT>
          explicit bits(const CharT *ptr,
                        typename basic_string<CharT>::size_t count = std::basic_string<CharT>::npos,
                        CharT zero = CharT('0'),
                        CharT one = CharT('1'));
        explicit bits(const integer& val);
        explicit bits(integer&& val);
        bits(const bits& rhs);
        bits(bits&& rhs) noexcept;
    // assign and swap
    template <class Ty>
      bits& operator=(Ty rhs); // integral types only
```

```
bits& operator=(const integer& rhs);
    bits& operator=(integer&& rhs);
    bits& operator=(const bits& rhs);
    bits& operator=(bits&& rhs);
    void swap(bits& rhs) noexcept;
    // conversions
    unsigned long to_ulong() const;
    unsigned long long to_ullong() const;
    template <class CharT = char, class Traits = char_traits<CharT>, class Alloc = allocator<CharT>>
      basic_string<CharT, Traits, Alloc> to_string(CharT zero = CharT('0'), CharT one = CharT('1')) const;
    // logical operations
    bits& operator&=(const bits& rhs);
    bits& operator|=(const bits& rhs);
    bits& operator^=(const bits& rhs);
    bits operator~() const;
    bits& operator<<=(size_t rhs);</pre>
    bits& operator>>=(size_t rhs);
    bits& operator<<(size_t rhs) const;</pre>
    bits& operator>>(size_t rhs) const;
    // element access and modification
    bits& set() noexcept;
    bits& set(size_t pos, bool val = true);
    bits& reset() noexcept;
    bits& reset(size_t pos);
    bits& flip() noexcept;
    bits& flip(size_t pos);
    bool operator[](size_t pos) const;
    reference operator[](size_t pos);
    bool test(size_t pos) const noexcept;
    bool all() const noexcept;
    bool any() const noexcept;
    bool none() const noexcept;
    size_t count() const noexcept;
    size_t count_not_set() const noexcept;
    // comparison
    bool operator==(const bits& rhs) const noexcept;
    bool operator!=(const bits& rhs) const noexcept;
    // capacity
    size_t size() const noexcept;
    size_t capacity() const noexcept;
    void reserve(size_t bit_count);
    void shrink_to_fit();
  };
} // namespace std
```

The class describes an object that represents an unbounded set of bits.

5.2.1 Constructors

[numeric.bits.cons]

bits() noexcept;

```
Effects: Constructs an object whose value is 0.
template <class Ty>
                             // integral types only
  bits(Ty rhs) noexcept;
     Effects: Constructs an object whose value is the ones-complement representation of rhs. Shall not take
     part in overload resolution unless the type Ty is an integral type.
bits(initializer_list<uint_least32_t> list);
     Effects: Constructs an object whose stored value is equal to the elements of the initializer_list
     treated as a series of unsigned 32-bit digits with the leftmost digit being most significant. For example,
     the initializer_list 0xFE, 0xFO, 0xAA, 0x31 represents the value 0xFE * 323 + 0xFO * 322
     + 0xAA * 321 + 0x31 * 320.
template <class CharT, class Traits, class Alloc>
  explicit bits::bits(const basic_string<CharT, Traits, Alloc>& str,
                       typename basic_string<CharT, Traits, Alloc>::size_t pos = 0,
                       typename basic_string<CharT, Traits, Alloc>::size_t count = basic_string<CharT>::npos,
                       CharT zero = CharT('0'),
                       CharT one = CharT('1'));
template <class CharT>
  explicit bits::bits(const CharT *ptr,
                       typename basic_string<CharT>::size_t count = basic_string<CharT>::npos,
                       CharT zero = CharT('0'),
                       CharT one = CharT('1'));
     Effects: Construct an object whose value is the value represented by their argument, treating zero as 0
     and one as 1.
explicit bits(const integer& rhs);
explicit bits(integer&& rhs);
     Effects: Construct objects whose value is the ones-complement representation of rhs.
bits(const bits& rhs);
bits(bits&& rhs) noexcept;
     Effects: Construct objects with the same value as rhs. The move constructor leaves rhs in an unspecified
     valid state.
5.2.2 Operations
                                                                                  [numeric.bits.ops]
size_t capacity() const noexcept;
     Returns: The number of bits that the object can represent without reallocating its internal storage.
size_t count() const noexcept;
     Returns: The number of bits in *this that are set, or static_cast<size_t>(-1) if the number of
     bits that are set is too large to fit in an object of type size_t.
size_t count_not_set() const noexcept;
     Returns: The number of bits in *this that are not set, or static_cast<size_t>(-1) if the number
     of bits that are not set is too large to fit in an object of type size_t.
void flip() const noexcept;
```

Effects: Toggles all the bits in the stored value.

```
void flip(size_t pos);
     Effects: Toggles the bit at position pos in the stored value.
bool none() const noexcept;
     Returns: True only if none of the bits in *this is set.
void reserve(size_t bit_count);
     Effects: Ensures that capacity() >= bit_count.
bits& reset() noexcept;
     Effects: Clears all the bits of *this.
     Returns: *this.
bits& reset(size_t pos);
     Effects: Clears the bit as position pos.
     Returns: *this.
void set() noexcept;
     Effects: Sets all the bits of *this.
     Returns:*this.
void set(size_t pos, bool val = true);
     Effects: Sets the bit at position pos in the stored value to val.
     Returns: *this.
void shrink_to_fit();
     Effects: Is a non-binding request to reduce capacity() to hold the current stored value without wasted
     space.
size_t size() const noexcept;
     Returns: capacity().
bool test(size_t pos) const noexcept;
     Returns: True only if the bit at position pos in the stored value is non-zero.
5.2.3 Bits conversion
                                                                                 [numeric.bits.conv]
template <class CharT = char, class Traits = char_traits<CharT>, class Alloc = allocator<CharT>>
  basic_string<CharT, Traits, Alloc> to_string(CharT zero = CharT('0'),
                                                 CharT one = CharT('1'));
     Returns: A string representation of the bits in the value stored in *this, using zero to represent 0 and
     one to represent 1.
unsigned long long to_ullong() const;
     Returns: A value equal to the stored value of *this. It throws an exception of type range_error if
     the value cannot be represented as an unsigned long long.
unsigned long to_ulong() const;
     Returns: A value equal to the stored value of *this. It throws an exception of type range_error if
     the value cannot be represented as a long long.
```

```
5.2.4 Bits operators
```

```
template <class Ty>
  bits& operator=(Ty rhs); // integral types only
     Effects: Shall not take part in overload resolution unless the type Ty is an arithmetic type. The operator
     effectively executes *this = integer(rhs).
     Returns: *this.
bits& operator=(const bits& rhs);
bits& operator=(bits&& rhs);
     Effects: Store the value of rhs into *this.
     Returns: *this.
bits& operator=(const integer& rhs);
bits& operator=(integer&& rhs);
     Effects: Store the ones-complement representation of rhs into *this.
     Returns: *this.
bool operator==(const bits& rhs) const noexcept;
     Returns: True only if the stored value in *this is the same as the stored value in rhs.
bool operator!=(const bits& rhs) const noexcept;
     Returns: !(*this == rhs).
bits operator&(const bits& lhs, const bits& rhs);
     Returns: An object whose value is the bitwise AND of the values of 1hs and rhs.
bits& operator&=(const bits& rhs);
     Effects: Sets the value of *this to the bitwise AND of the values of *this and rhs.
     Returns: A reference to *this.
bits operator|(const bits& lhs, const bits& rhs);
     Returns: An object whose value is the bitwise inclusive OR of the values of lhs and rhs.
bits& operator|=(const bits& rhs);
     Effects: Sets the value of *this to the bitwise inclusive OR of the values of *this and rhs.
     Returns: *this.
bits operator^(const bits& lhs, const bits& rhs);
     Returns: An object whose value is the bitwise exclusive OR of the values of 1hs and rhs.
bits& operator^=(const bits& rhs);
     Effects: Sets the value of *this to the bitwise exclusive OR of the values of *this and rhs.
     Returns: *this.
bits operator~() const;
     Returns: An object that holds the complement of the set of bits held by *this.
```

```
bits operator>>(const bits& lhs, size_t rhs);
     Returns: An object whose stored value is the value of the bits in 1hs shifted right rhs positions.
bits& operator>>=(size_t rhs);
     Effects: Sets the stored value in *this to the value of the bits in *this shifted right rhs positions.
     Returns: *this.
template <class CharT, class Traits>
  basic_istream<CharT, Traits>& operator>>(basic_istream<CharT, Traits>& is,
                                             bits& val);
     Effects: Has the effect of std::string temp; is >> temp; val = temp; .
     Returns: is.
bits operator<<(const bits& lhs, size_t rhs);</pre>
     Returns: An object whose stored value is the value of the bits in lhs shifted left rhs positions.
bits& operator<<=(size_t rhs);</pre>
     Effects: Sets the stored value in *this to the value of the bits in *this shifted left rhs positions.
     Returns: *this.
template <class CharT, class Traits>
  basic_ostream<CharT, Traits>& operator<<(basic_ostream<CharT, Traits>& os,
                                             const bits& val);
     Effects: Has the effect of os << val.to string().
     Returns: os.
bool operator[](size_t pos) const;
     Returns: The value of the bit at position pos.
reference operator[](size_t pos);
     Returns: An object of type bits::reference that refers to the bit at position pos.
5.2.5 bits::reference class
                                                                            [numeric.bits.reference]
  namespace std {
    class bits {
      class reference {
      public:
        reference& operator=(bool val) noexcept;
        reference& operator=(const reference& rhs) noexcept;
        bool operator~() const noexcept;
        operator bool() const noexcept;
        reference& flip() noexcept;
      };
    }:
  } // namespace std
```

The nested class bits::reference describes an object that can be used to manage a particular bit in an object of type bits.

```
reference& flip() noexcept;
     Effects: Toggles the bit that the object manages.
reference& operator=(bool rhs) noexcept;
     Effects: Sets the bit that the object manages to the value of rhs.
reference& operator=(const reference& rhs) noexcept;
     Effects: Sets the bit that the object manages to the value managed by rhs.
bool operator~() const noexcept;
     Returns: True if the bit managed by the object is set, otherwise false.
operator bool() const noexcept;
     Returns: True if the bit that the object manages is set.
5.3 Integer
                                                                             [numeric.integer.syn]
 namespace std {
    class integer {
    public:
      // constructors
      integer() noexcept;
      template <class Ty>
        integer(Ty rhs) noexcept; // arithmetic types only
      integer(initializer_list<uint_least32_t> init);
      template <class CharT, class Traits, class Alloc>
        explicit integer(const basic_string<CharT, Traits, Alloc>& str);
      explicit integer(const bits& rhs);
      explicit integer(bits&& rhs);
      integer(const integer& rhs);
      integer(integer&& rhs) noexcept;
      // assign and swap
      template <class Ty>
        integer& operator=(Ty rhs); // arithmetic types only
      integer& operator=(const bits& rhs);
      integer& operator=(bits&& rhs);
      integer& operator=(const integer& rhs);
      integer& operator=(integer&& rhs);
      void swap(integer& rhs) noexcept;
      // conversions
      explicit operator long long() const;
      explicit operator unsigned long long() const;
      explicit operator long double() const noexcept;
      explicit operator bool() const noexcept;
      // comparisons
```

```
int compare(const integer& rhs) const noexcept;
    // arithmetic operations
    integer& operator+=(const integer& rhs);
    integer& operator-=(const integer& rhs);
    integer& operator*=(const integer& rhs);
    integer& operator/=(const integer& rhs);
    integer& operator%=(const integer& rhs);
    integer& operator++();
    integer operator++(int);
    integer& operator--();
    integer operator--(int);
    integer div(const integer& rhs);
    integer& abs() noexcept;
    integer& negate() noexcept;
    integer operator+() const noexcept;
    integer operator-() const noexcept;
    integer& operator<<=(size_t rhs);</pre>
    integer& operator>>=(size_t rhs);
    // numeric operations
    integer& sqr();
    integer& sqrt();
    integer& pow(const integer& exp);
    integer& mod(const integer& rhs);
    integer& mulmod(const integer& rhs, const integer& m);
    integer& powmod(const integer& exp, const integer& m);
    // observers
    bool is_zero() const noexcept;
    bool is_odd() const noexcept;
    // accessors
    integer_data_proxy get_data_proxy();
    // capacity
    size_t size() const noexcept;
    size_t capacity() const noexcept;
    void reserve(size_t digits);
    void shrink_to_fit();
  };
} // namespace std
void swap(integer& lhs, integer& rhs) noexcept;
// comparisons
bool operator==(const integer& lhs, const integer& rhs) noexcept;
bool operator!=(const integer& lhs, const integer& rhs) noexcept;
bool operator<(const integer& lhs, const integer& rhs) noexcept;</pre>
bool operator<=(const integer& lhs, const integer& rhs) noexcept;</pre>
bool operator>(const integer& lhs, const integer& rhs) noexcept;
```

```
// arithmetic operations
  integer operator+(const integer& lhs, const integer& rhs);
  integer operator-(const integer& lhs, const integer& rhs);
  integer operator*(const integer& lhs, const integer& rhs);
  integer operator/(const integer& lhs, const integer& rhs);
  integer operator%(const integer& lhs, const integer& rhs);
 pair<integer, integer> div(const integer& lhs, const integer& rhs);
  integer abs(const integer& val);
  integer operator<<(const integer& lhs, size_t rhs);</pre>
  integer operator>>(const integer& lhs, size_t rhs);
  // numeric operations
  integer sqr(const integer& val);
  integer sqrt(const integer& val);
  integer pow(const integer& val, const integer& exp);
  integer mod(const integer& lhs, const integer& rhs);
  integer mulmod(const integer& lhs, const integer& rhs, const integer& m);
  integer powmod(const integer& lhs, const integer& rhs, const integer& m);
  integer gcd(const integer& a, const integer& b);
  integer lcm(const integer& a, const integer& b);
  // conversions
  string to_string(const integer& val, int radix = 10);
  // I/O operations
  template <class CharT, class Traits>
    basic_ostream<CharT, Traits>& operator<<(basic_ostream<CharT, Traits>& str,
                                              const integer& val);
  template <class CharT, class Traits>
    basic_istream<CharT, Traits>& operator>>(basic_istream<CharT, Traits>& str,
                                              integer& val);
The class describes an object that manages an unbounded-precision signed integral type that can be used in
most contexts where an int could be used.
Any function specified to return an object of type integer may return an object of another type, provided
all the const member functions of the class integer are also applicable to that type.
integer abs(const integer& other);
     Returns: An object that holds the absolute value of other.
integer& abs() noexcept;
     Effects: Sets the stored value of *this to its absolute value and returns *this.
size_t capacity() const noexcept;
     Returns: The number of decimal digits that the object can represent without reallocating its internal
     storage.
int compare(const integer& rhs) const noexcept;
```

bool operator>=(const integer& lhs, const integer& rhs) noexcept;

Returns: A value less than 0 if *this is less than rhs, 0 if *this is equal to rhs, and greater than 0 if *this is greater than rhs.

```
pair<integer, integer> div(const integer& lhs, const integer& rhs);
```

Returns: An object that is an instantiation of pair; its first field holds the quotient, lhs / rhs, and its second field holds the remainder, lhs % rhs.

```
integer div(const integer& rhs) const;
```

Returns: The remainder, *this % rhs, and stores the quotient, *this / rhs, into *this.

```
integer gcd(const integer& a, const integer& b);
```

Returns: An object whose value is the greatest common denominator of a and b.

```
integer_data_proxy get_data_proxy();
```

Returns: An object of type integer_data_proxy that can be used to examine and modify the internal storage of *this. If an object of type integer_data_proxy that refers to *this exists at the time of a call to this function, the function throws an exception object of type std::runtime_error.

5.3.1 Constructors

[numeric.integer.ctors]

integer() noexcept;

Effects: Constructs an object whose value is 0.

```
template <class Ty>
  integer(Ty val) noexcept; // arithmetic types only
```

Effects: For integral types the constructor constructs an object whose value is val. For floating-point types the constructor constructs an object whose value is the value of val with any fractional part discarded. Shall not take part in overload resolution unless the type Ty is an arithmetic type.

```
integer(initializer_list<unspecified> list);
```

Effects: Constructs an object whose stored value is equal to the elements of the initializer_list treated as a series of unsigned 32-bit digits with the leftmost digit being most significant. For example, the initializer list 0xFE, 0xFO, 0xAA, 0x31 represents the value 0xFE * 323 + 0xFO * 322 + 0xAA * 321 + 0x31 * 320.

```
template<class CharT, class Traits, class Alloc>
  explicit integer(const basic_string<CharT, Traits, Alloc>& str);
```

Effects: Constructs an object whose value is the value represented by the string object. The string object shall have the form required for the string argument to the function strtol with a radix of base, and shall be interpreted as if by strtol(str.c_str(), 0, base), except that the resulting value can never be outside the range of representable values.

```
integer(const bits& rhs);
integer(bits&& rhs);
```

Effects: Construct an object whose stored value is the value in the bit pattern in **rhs** interpreted as a ones-complement representation of an integer value.

```
integer(const integer& rhs);
integer(integer&& rhs) noexcept;
```

Effects: Construct objects with the same value as rhs. The move constructor leaves rhs in an unspecified valid state.

```
bool is_odd() const noexcept;
     Returns: True only if the stored value represents an odd number.
bool is_zero() const noexcept;
     Returns: True only if the stored value is zero.
integer lcm(const integer& a, const integer& b);
     Returns: An object whose value is the least common multiple of a and b.
integer mod(const integer& lhs, const integer& rhs);
     Returns: An object whose value is 1hs mod rhs.
integer& mod(const integer& rhs);
     Effects: Sets the stored value in *this to *this mod rhs.
     Returns: *this.
integer mulmod(const integer& lhs, const integer& rhs, const integer& m);
     Returns: An object whose value is (lhs * rhs) mod m.
integer& mulmod(const integer& rhs, const integer& m);
     Effects: Sets the value of *this to (*this * rhs) mod m.
     Returns: *this.
integer& negate() noexcept;
     Effects: Sets the stored value of *this to the negation of its previous value.
     Returns: this.
integer pow(const integer& val, const integer& exp);
     Requires: 0 \le exp.
     Returns: An object whose value is val^{exp}.
integer& pow(const integer& exp);
     Requires: 0 \le exp.
     Effects: Sets the value of *this to *this e^{xp}.
     Returns: *this.
integer powmod(const integer& val, const integer& exp, const integer& m);
     Requires: 0 \le \exp and m != 0.
     Returns: An object whose value is val^{exp} \mod m.
integer& powmod(const integer& exp, const integer& m);
     Requires: 0 \le \exp and m != 0.
     Effects: Sets the value of *this to *this^{exp} \mod m.
     Returns: *this.
```

```
void reserve(size_t digits);
     Effects: Ensures that capacity() >= digits.
void shrink_to_fit();
     Effects: A non-binding request to reduce capacity() to hold the current stored value without wasted
size_t size() const noexcept;
     Returns: capacity().
integer sqr(const integer& val);
     Returns: An object whose value is val * val.
integer& sqr();
     Effects: Sets the value of *this to *this * *this.
     Returns: *this.
integer sqrt(const integer& val);
     Requires: 0 <= val.
     Returns: An object whose value is the square root of the value held by val, discarding any fractional
integer& sqrt();
     Requires: 0 \le *this.
     Effects: Sets the value of *this to the square root of the value held by *this, discarding any fractional
     Returns: *this.
void swap(integer& lhs, integer& rhs) noexcept;
     Effects: Swaps the stored values of lhs and rhs.
void swap(integer& rhs) noexcept;
     Effects: Swaps the stored values of *this and rhs.
string to_string(const integer& val, int radix = 10) const;
     Returns: A string representation of the value stored in val, using radix as the radix.
5.3.3 Conversion
                                                                             [numeric.integer.conv]
explicit operator bool() const noexcept;
     Returns: False only if *this is equal to 0.
explicit operator long double() const noexcept;
     Returns: A value equal to the stored value of *this. If the stored value is outside the range that can
     be represented by an object of type long double the returned value is positive or negative infinity, as
     appropriate.
```

```
explicit operator long long() const;
     Returns: A value equal to the stored value of *this. If the stored value cannot be represented as a
     long long it throws an exception of type range_error.
explicit operator unsigned long long() const;
     Returns: A value equal to the stored value of *this. If the stored value cannot be represented as an
     unsigned long it throws an exception of type range_error.
5.3.4 Comparison
                                                                          [numeric.integer.comp]
bool operator==(const integer& lhs, const integer& rhs) noexcept;
     Returns: True only if the value stored in 1hs is equal to the value stored in rhs.
bool operator!=(const integer& lhs, const integer& rhs) noexcept;
     Returns: !(lhs == rhs).
bool operator>(const integer& lhs, const integer& rhs) noexcept;
     Returns: rhs < lhs.
bool operator>=(const integer& lhs, const integer& rhs) noexcept;
     Returns: !(lhs < rhs).
bool operator<(const integer& lhs, const integer& rhs) noexcept;
     Returns: True only if lhs.compare(rhs) returns -1.
bool operator <= (const integer & lhs, const integer & rhs) noexcept;
     Returns: !(rhs < lhs).
5.3.5 Assignment
                                                                          [numeric.integer.assign]
template <class Ty>
  integer& operator=(Ty rhs); // arithmetic types only
     Effects: Shall not take part in overload resolution unless the type Ty is an arithmetic type. The operator
     effectively executes *this = integer(rhs).
     Returns: *this.
integer& operator=(const integer& rhs);
integer& operator=(integer&& rhs);
     Effects: Store the value of rhs into *this.
     Returns: *this.
integer& operator=(const bits& rhs);
integer& operator=(bits&& rhs);
     Effects: Store the value of rhs, interpreted as a ones-complement representation of an integer value,
     into *this.
     Returns: *this.
```

5.3.6

Arithmetic operations

integer operator+(const integer& lhs, const integer& rhs); Returns: An object whose value is the sum of the values of lhs and rhs. integer operator+() const noexcept; Returns: A copy of *this. integer& operator+=(const integer& rhs); Effects: Sets the stored value of *this to the sum of the values of *this and rhs. Returns: A reference to *this. integer& operator++(); Effects: Set the value stored in *this to *this + 1. Returns: *this. integer operator++(int); Returns: An object whose value is the value stored in *this prior to the increment. integer operator-(const integer& lhs, const integer& rhs) Returns: An object whose value is the difference between the values of 1hs and rhs. integer operator-() noexcept; Returns: An object whose value is the negation of the value of *this. integer& operator-=(const integer&); Effects: Sets the stored value of *this to the difference between the values of *this and rhs. Returns: *this. integer& operator--(); Effects: Set the value stored in *this to *this - 1. Returns: *this. integer operator--(int); Effects: Set the value stored in *this to *this - 1. Returns: An object whose value is the value stored in *this prior to the decrement. integer operator*(const integer& lhs, const integer& rhs); Returns: An object whose value is the product of the values of lhs and rhs. integer& operator*=(const integer& rhs); Effects: Sets the stored value of *this to the product of the values of *this and rhs. Returns: A reference to *this. integer operator/(const integer& lhs, const integer& rhs);

discarding any fractional part. integer& operator/=(const integer& rhs); Effects: Sets the stored value of *this to the quotient of the value of *this divided by the value of rhs, discarding any fractional part. Returns: *this. integer operator%(const integer&, const integer&); Returns: An object whose value is the remainder of the value of lns divided by the value of rns. The remainder is the value such that (lhs / rhs) * rhs + lhs % rhs is equal to lhs. integer& integer::operator%=(const integer&); Effects: Sets the stored value of *this to the remainder of *this divided by the value of rhs. Returns: *this. integer operator>>(const integer& val, size_t rhs); Returns: An object whose value is val / 2^{rhs} . integer& operator>>=(size_t rhs); Effects: Sets the value of *this to *this / 2^{rhs} . Returns: *this. 5.3.7 I/O [numeric.integer.io] template <class Elem, class Traits> basic_istream<Elem, Traits>& operator>>(basic_istream<Elem, Traits>& is, integer& val); Effects: Has the effect of std::string temp; is >> temp; val = integer(temp); . Returns: is. integer operator<<(const integer& val, size_t rhs);</pre> Returns: An object whose value is val * 2^{rhs} . integer& integer::operator<<=(size_t rhs);</pre> Effects: Sets the value of *this to *this * 2^{rhs} . Returns: *this. template <class Elem, class Traits> basic_ostream<Elem, Traits>& operator<<(basic_ostream<Elem, Traits>& os, const integer& val);

Returns: An object whose value is the quotient of the value of 1hs divided by the value of rhs,

Effects: Has the effect of os << to string(val).

Returns: os.