

Digital Communication 22EC2208A

Digital Carrier Modulation

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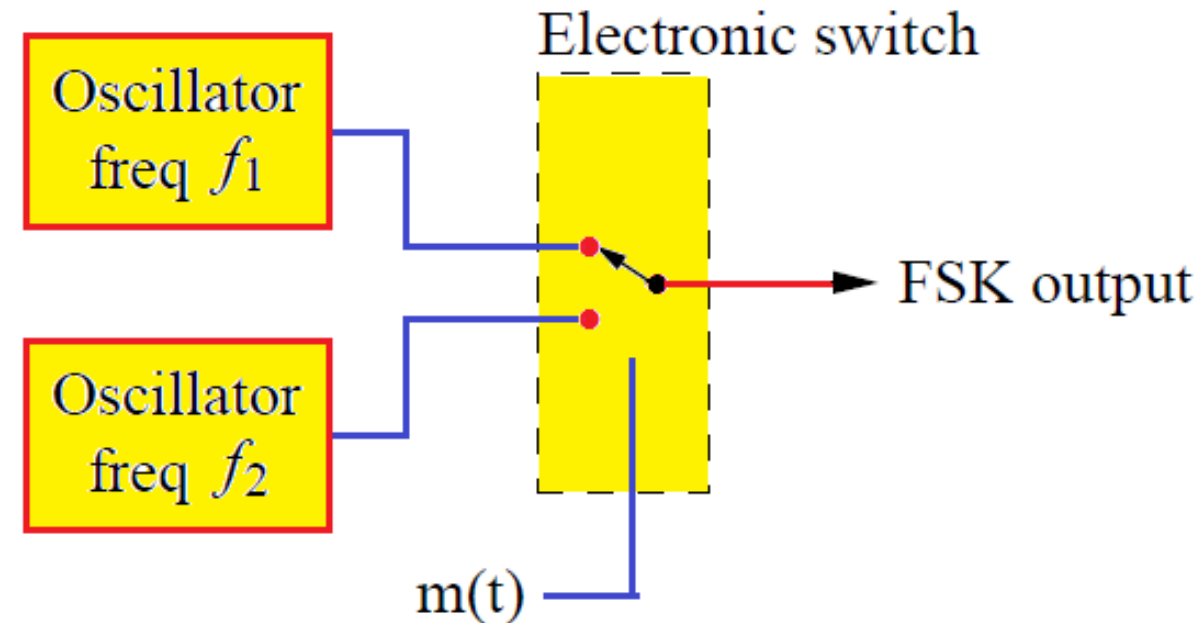
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Binary Frequency Shift Keying (BFSK)

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- Frequency Shift Keying is analogous to Frequency Modulation (FM) in analog domain, where the slope of the **time varying angle of the signal, i.e., instantaneous frequency of the carrier signal** varies with respect to the baseband signal.
- In the digital symbol, there exist two amplitude levels defined for two logic values one and zero.
- Therefore, two sinusoidal carrier waves of the same amplitude A_c but different frequencies f_1 and f_2 are used to represent the two symbol



Mathematical Model

$$s_i(t) = \begin{cases} \sqrt{\frac{2E_b}{T_b}} \cos 2\pi f_1 t, & \text{for symbol 1, corresponds to } i = 1 \text{ (mark)} \\ \sqrt{\frac{2E_b}{T_b}} \cos 2\pi f_2 t, & \text{for symbol 0, corresponds to } i = 2 \text{ (space)} \end{cases} \Rightarrow 0 \leq t \leq T_b$$

f_m Mark frequency
 f_s Space frequency

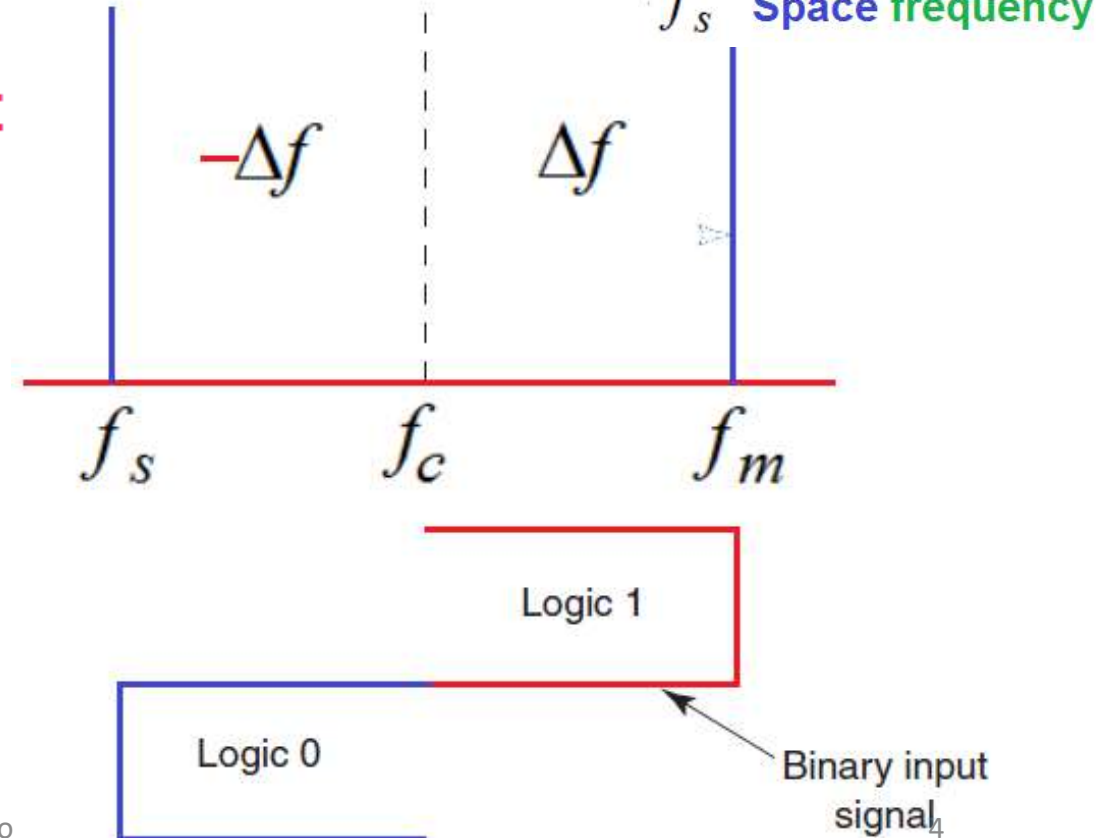
where E_b transmitted signal energy per bit

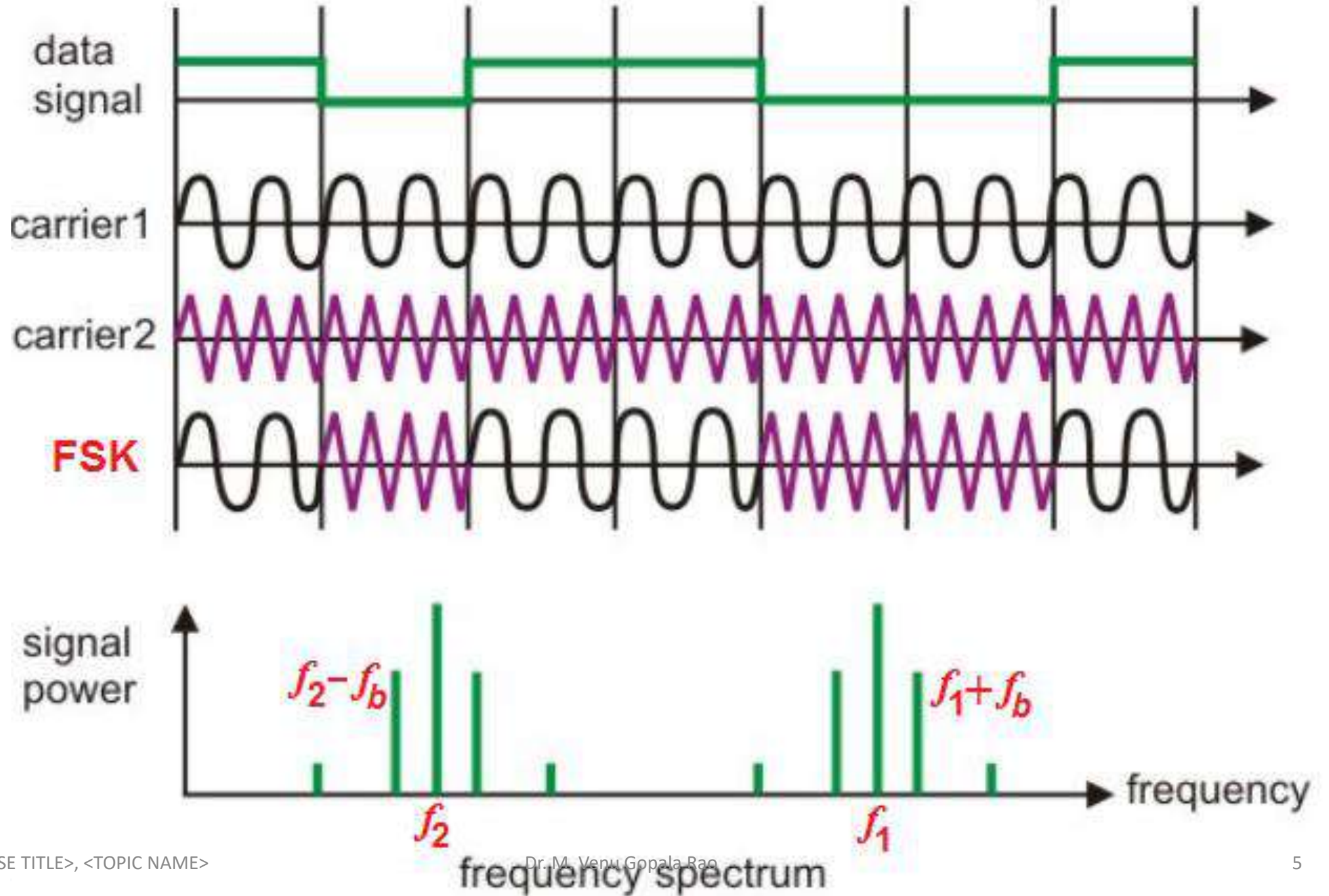
The transmitted frequency with separation

$$\Delta f = \frac{|f_m - f_s|}{2}$$

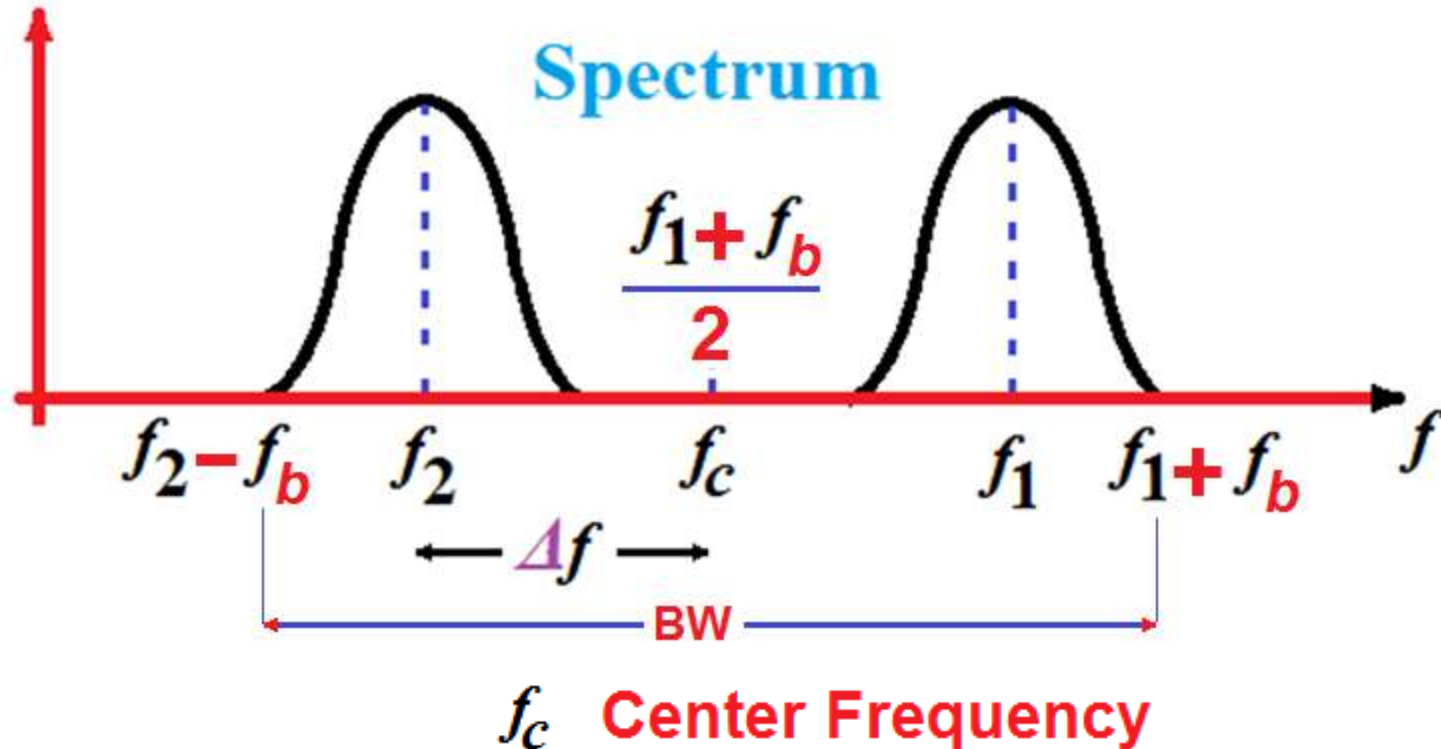
The Δf is selected such that $s_1(t)$ and $s_2(t)$ are orthogonal

$$\int_0^{T_b} s_1(t) s_2(t) dt = 0$$





Bandwidth of FSK



Bandwidth =

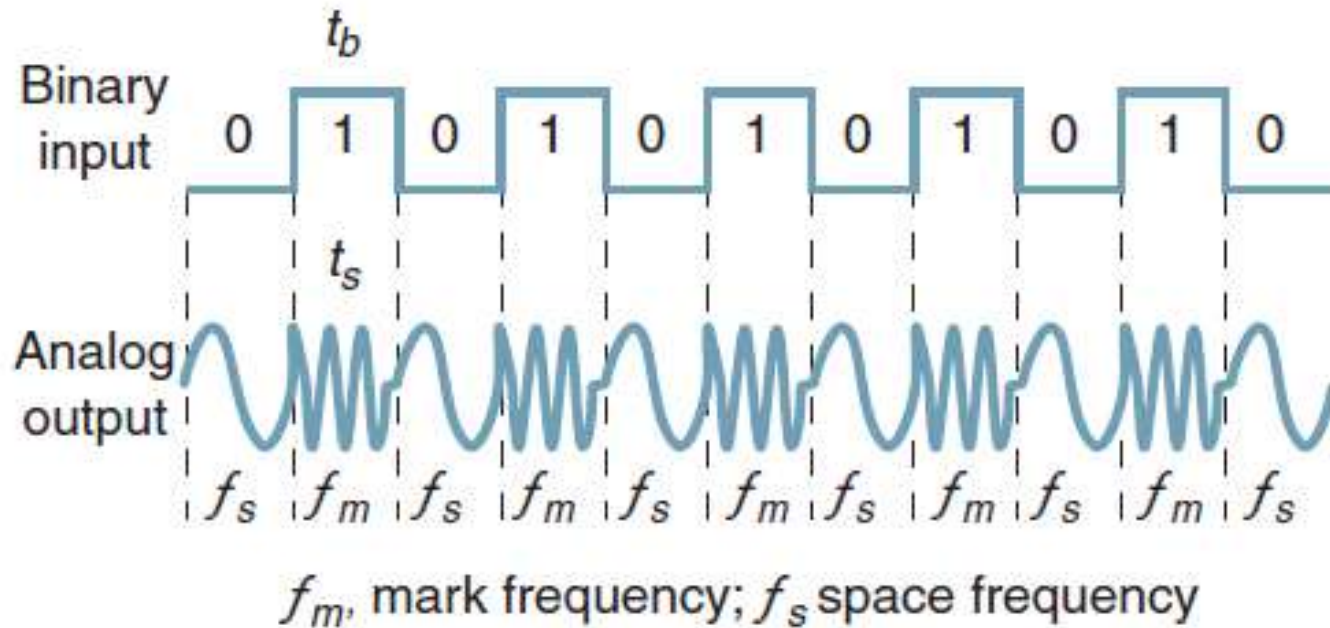
$$B = (f_1 + f_b) - (f_2 - f_b) = (f_1 - f_2) + 2f_b$$

$$= 2\Delta f + 2f_b = 2(\Delta f + f_b) \quad \text{Carson's rule}$$

Baud, Bit rate and Bandwidth of FSK

In Fig (a), it can be seen that the time of one bit (t_b) is the same as the time the FSK output is a mark or space frequency (t_s).

Thus, the bit time equals the time of an FSK signaling element, and the bit rate equals the baud.

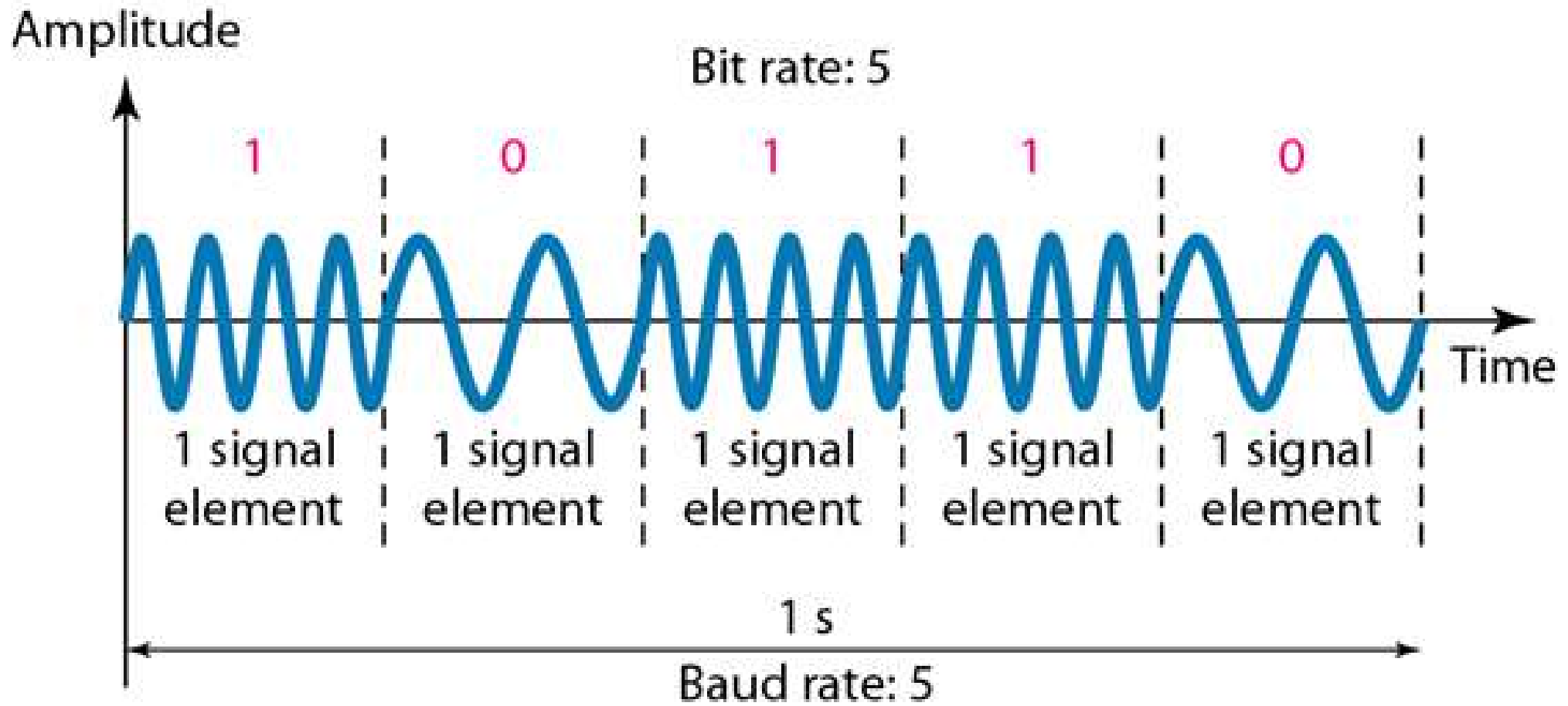


(a)

$$\text{baud} = \frac{f_b}{1} = f_b$$

binary input	frequency output
0	space (f_s)
1	mark (f_m)

(b)



Ex1: Determine (a) the peak frequency deviation, (b) minimum bandwidth, and (c) baud for a binary FSK signal with a mark frequency of 49 kHz, a space frequency of 51 kHz, and an input bit rate of 2 kbps.

Solution a. The peak frequency deviation is determined from Equation

$$\Delta f = \frac{|49\text{kHz} - 51\text{kHz}|}{2} = 1 \text{ kHz}$$

b. The minimum bandwidth is determined from Equation

$$B = 2(1000 + 2000) = 6 \text{ kHz}$$

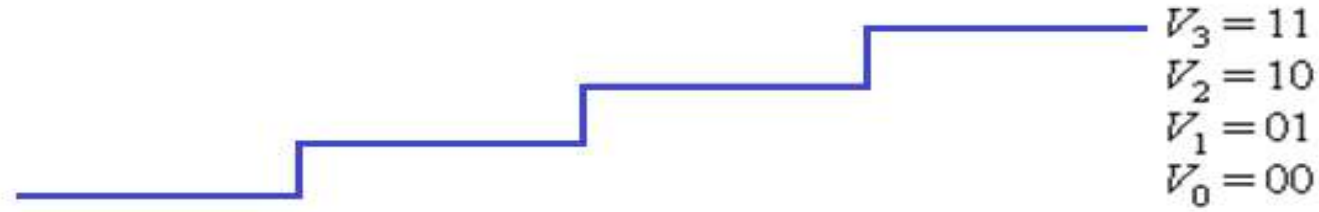
c. For FSK, $n = 1$, and the baud is determined from Equation

$$\text{baud} = \frac{2000}{1} = 2000$$

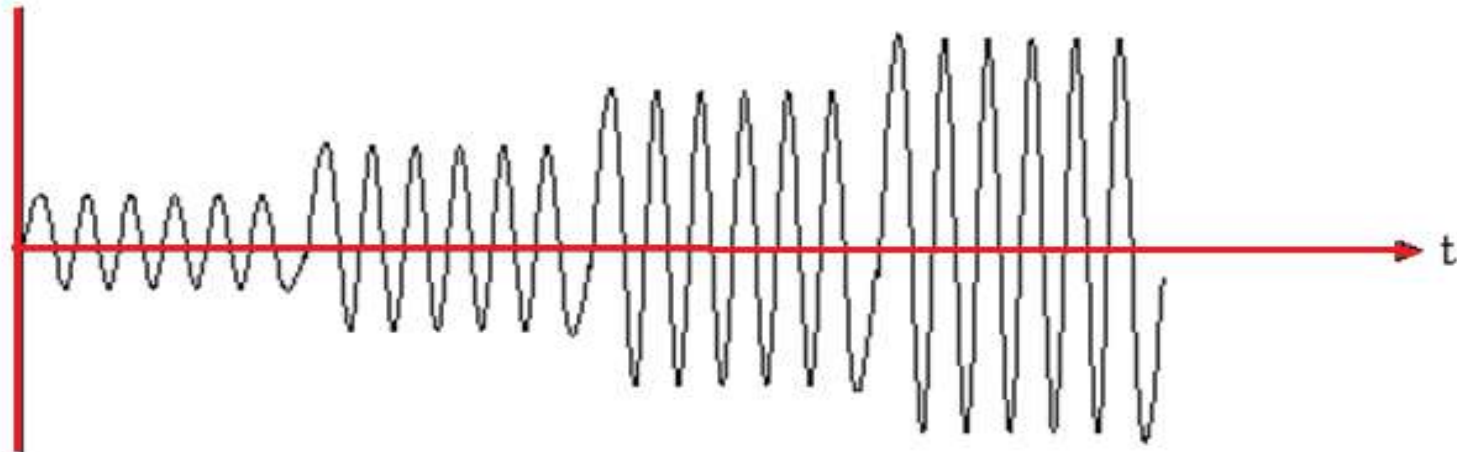
Information



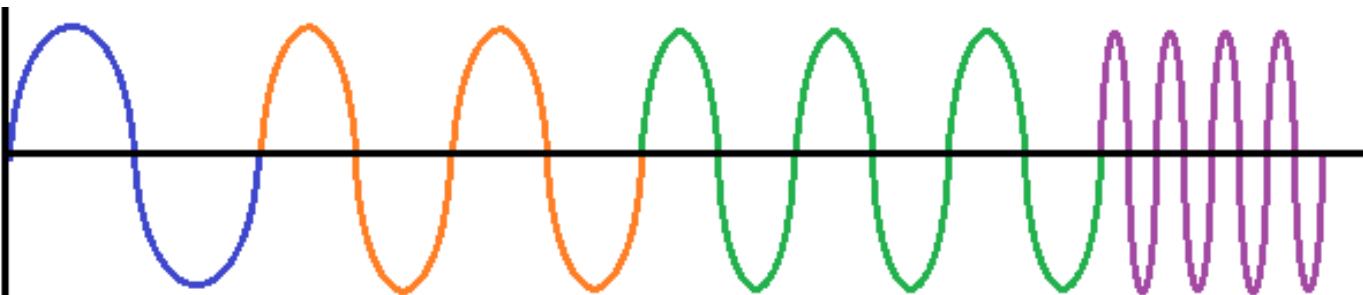
m levels
 $m = 4$



4 level
ASK



4 level FSK



Bandwidth for M-ary FSK

$$\text{Bandwidth} = 2 \frac{f_b}{N} + (M - 1)2\Delta f, \quad N = \log_2 M$$

$$\text{For Coherent M-ary FSK; } 2\Delta f = \frac{f_b}{2N}$$

$$\text{Thus } BW = (M + 3) \frac{f_b}{2N}$$

Signal Space Representation

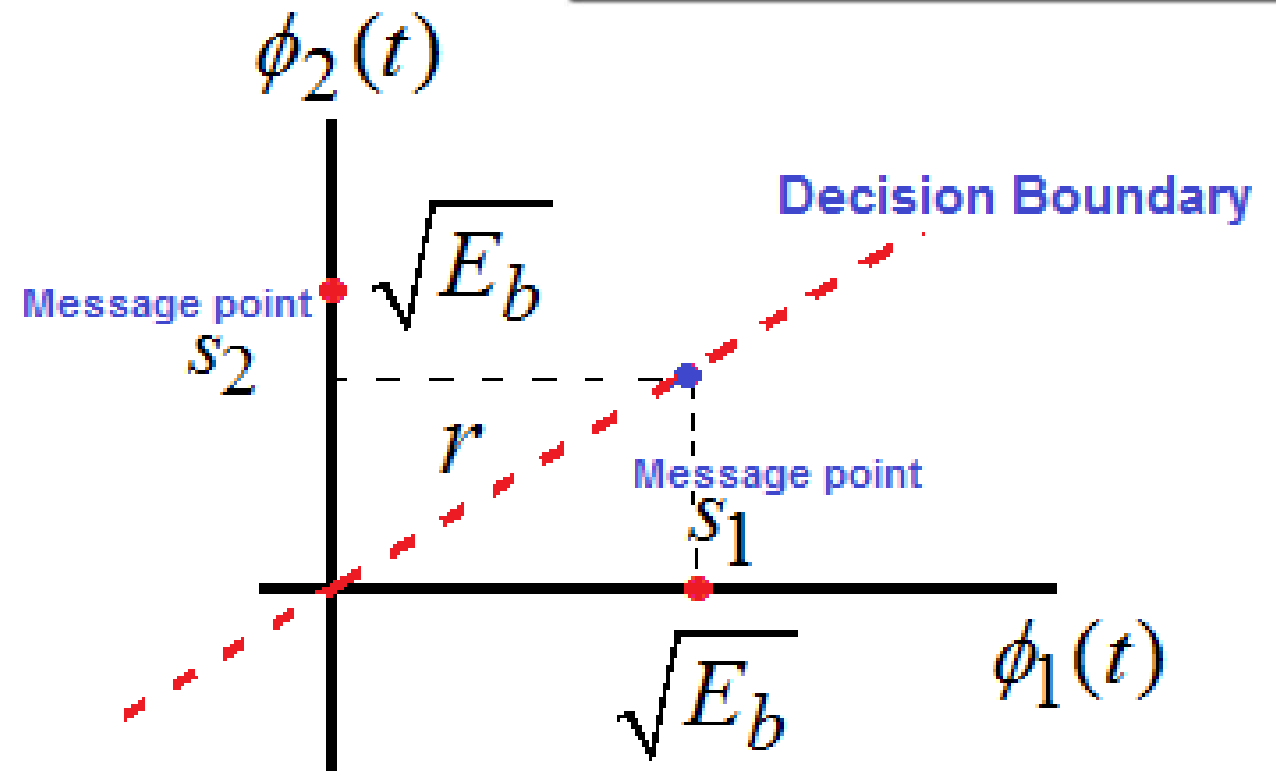
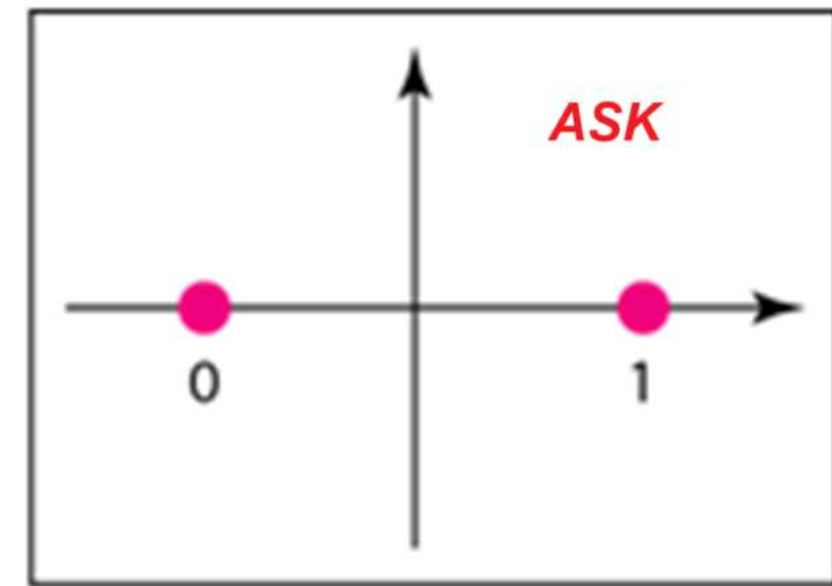
$$s_1(t) = \begin{bmatrix} \sqrt{E_b} & 0 \end{bmatrix}$$

$$s_2(t) = \begin{bmatrix} 0 & \sqrt{E_b} \end{bmatrix}$$

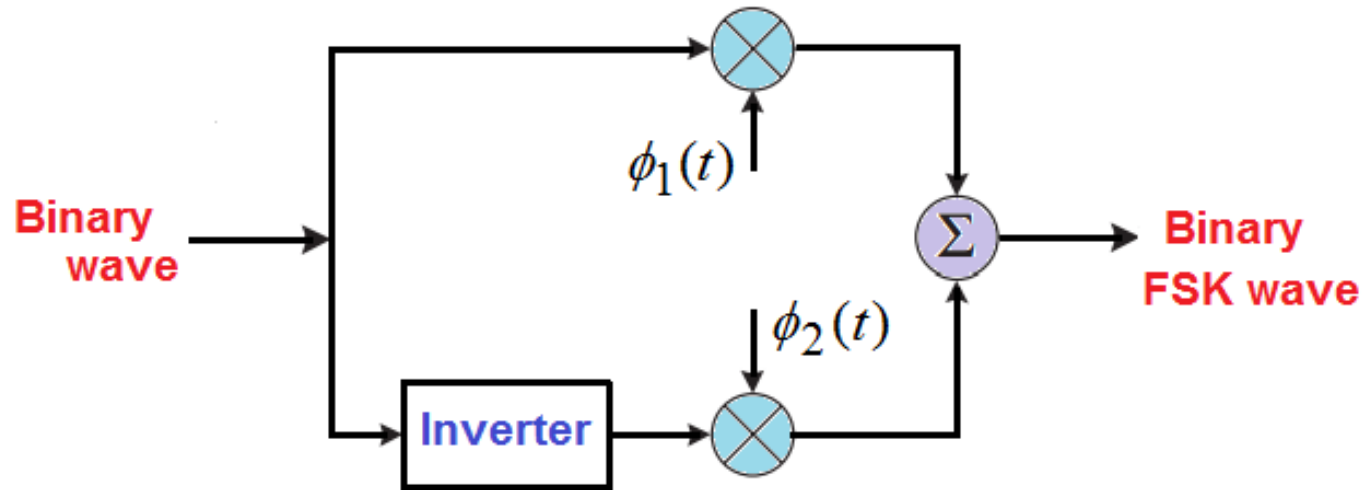
$$r = [r_1 \quad r_2]$$

$$r_1 = \int_0^{T_b} r(t) \phi_1(t) dt$$

$$r_2 = \int_0^{T_b} r(t) \phi_2(t) dt$$



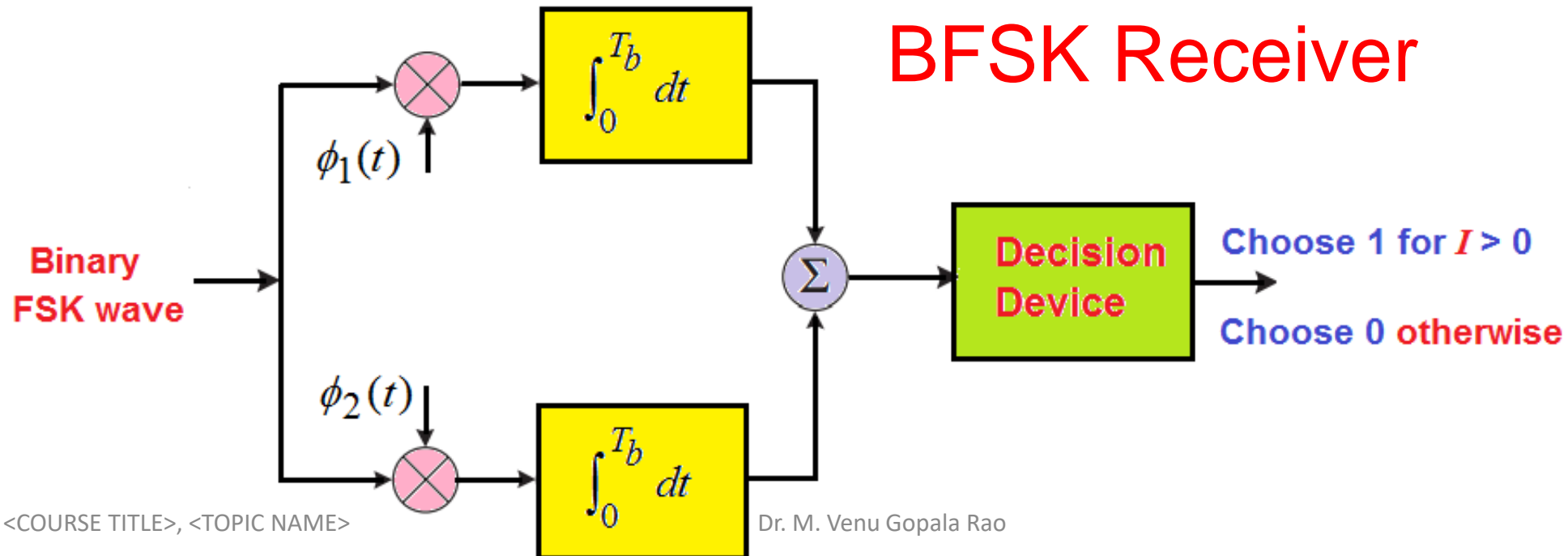
BFSK Transmitter



$$\phi_1(t) = \sqrt{\frac{2}{T_b}} \cos 2\pi f_1 t$$

$$\phi_2(t) = \sqrt{\frac{2}{T_b}} \cos 2\pi f_2 t$$

BFSK Receiver



Bit Error Rate for BFSK

The average probability of error

$$\text{BER}_{\text{ASK}} = Q\left(\sqrt{\frac{E_b}{N_0}}\right)$$

$$\text{BER}_{\text{FSK}} = Q\left(\sqrt{\frac{E_b}{N_0}}\right) \Rightarrow 3 \text{ dB worse than BPSK}$$

Find the SNR / bit and average power required at the demodulator to maintain a $BER = 10^{-6}$ using BFSK for data transmission over a radio channel at 56 kbps. Assume that the channel adds white Gaussian noise with power spectral density $N_0 = 10^{-10}$.

Use $Q(x) = 10^{-6} \Rightarrow x = 4.75$

$$BER_{BFSK} = Q\left(\sqrt{\frac{E_b}{N_0}}\right) \Rightarrow \sqrt{\frac{E_b}{N_0}} = 4.75 \Rightarrow E_b = 2.256 \times 10^{-9}$$

$$P_{av} = \frac{E_b}{T_b} = E_b R_b = 2.256 \times 10^{-9} \times 56 \times 10^3 = 126.34 \mu W = -9 \text{ dBm}$$

Digital data **80 kbps** is transmitted over an AWGN channel with PSD

$\frac{N_o}{2} = 10^{-10}$ W/Hz. Calculate the averaged receiver power level to achieve a

BER = 10^{-6} for coherent FSK. Use $Q(x) = 10^{-6} \Rightarrow x = 4.75$

Advantages of FSK:

- FSK is ideally a constant envelope modulation; hence, more power-efficient class-C non-linear Power Amplifiers can be used in the transmitter.
- FSK is more bandwidth efficient than ASK.
- Reasonably simple modulation and demodulation schemes.

Disadvantages of FSK:

- The difference between coherent FSK detection and non-coherent FSK detection is not significant for higher FSK levels.
- The extra hardware required for coherent FSK detection is hence hard to justify.
- Coherent FSK is not often used in practice due to the difficulty (and cost) in generating two reference frequencies close together at the receiver.

End