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Date		Student Name	

Experiment Title: Performance analysis of Time and Space Complexity

Aim/Objective: Analysis of Time and Space Complexity of Algorithms

Description: The students will understand and find the Time and Space Complexity of Algorithms

Pre-Requisites

Knowledge: Basics of Data Structures and C Programming, Basic knowledge about algorithms in C and Data Structures.

Tools: Code Blocks / Eclipse IDE

Pre-Lab:

1. During lockdown Mothi gets bored by his daily routine while scrolling YouTube and he found an algorithm that looks different. Mothi is very crazy about algorithms, but as he cannot solve algorithms of multiple loops, he got struck and need your help to find the time complexity of that algorithm

```

Algorithm KLU(int n) {
    int count=0;
    for(int i=0;i<n;i=i*2) {
        for(int j=n;j>0;j=j/3) {
            for(int k=0;k<n;k++) {
                Count++;
            }
        }
    }
}

```

• **Procedure/Program:**

```

void KLU(int n)
{
    int count = 0;
    for(int i=0; i<n; i=i*2)
    {
        for(int j=n; j>0; j=j/3)
        {
            for(int k=0; k<n; k++)
            {
                count ++;
            }
        }
    }
}

```

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- Data and Results: $\text{for}(\text{int } i=0; i < n; i = i * 2)$ ———
 if multiplied by 2 after each iteration, i is doubled
 $\text{for}(\text{int } i=1; i < n; i = i * 2)$ the i is doubled
 each time which means $\log_2(n)$ to reach n
 $\text{for}(\text{int } j=n; j > 0; j = j / 3)$ dividing 3 after each
 iteration $j > 0$ and the number $\log_3(n)$
 $\text{for}(\text{int } k=0; k < n; k++)$ starts at 0 and
 increments by 1 up to $n-1$

- Analysis and Inferences:
 , The outer loop runs $\log_2(n)$ times
 , The middle loop runs $\log_3(n)$
 , The inner loop runs n times
 $T(n) = (\log_2(n)) * (\log_3(n)) * n$

2. Suresh provided the following recursive algorithm to the students:

recursive algorithm:

```
int custom_recursive_function(int n)
{
    if (n <= 1)
        return 1;
    else
        return 3 * custom_recursive_function(n-1);
}
```

Determine the time complexity of the custom_recursive_function function.

- Procedure/Program:

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```

int custom-recursive-function(int n)
{
    if(n == 1)
        return 1;
    else
        return n * custom-recursive-function(n-1);
}

```

• Data and Results:

when $n \leq 1$ the function returns 1
 In recursive case $n > 1$ the function calls
 recursive call to custom-recursive-function($n-1$)
 and multiplies

• Analysis and Inferences:

$$\begin{aligned}
 T(n) &= T(n-1) + O(1) \\
 T(n-1) &= T(n-2) + O(1) \\
 T(n-2) &= T(n-3) + O(1) \\
 T(n) &= T(1) + O(n) = O(n)
 \end{aligned}$$

The recursive call to custom recursive function ($n-1$)
 recursive relation $T(n) = T(n-1) + O(1)$

In-Lab:

1. During the final skill exam, the teacher gave the students a problem to calculate the factorial of a given number n . One student, Ravi, decided to write a recursive algorithm that is intentionally inefficient to ensure his approach is unique. Your task is to determine whether Ravi's algorithm for calculating the factorial is correct and to analyze its time complexity.

Here is Ravi's recursive algorithm:

```

int inefficient_factorial(int n) {
    if(n == 0)
        return 1;
    else if(n == 1)
        return 1;
    else

```

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```
return n * inefficient_factorial(n-1) * inefficient_factorial(n-1);
```

}
Question: Determine if Ravi's algorithm for calculating the factorial is correct and analyze its time complexity.

• Procedure/Program:

```
int inefficient_factorial(int n) {
    if (n == 0)
        return 1;
    else if (n == 1)
        return 1;
    else
        return inefficient_factorial(n-1) *
               inefficient_factorial(n-1);
}
```

• Data and Results:

The result of correctness and time complexity analysis

correctness is correct

Time complexity $O(2^n)$

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- **Analysis and Inferences:** Instead of multiplying n by the factorial of $(n-1)$ once. Additionally, the time complexity $O(n)$ makes the algorithm inefficient for moderately large values of n .

Post-Lab:

- 1) In the city of KLU, there are numerous street lamps arranged in a straight line. These street lamps are equipped with sensors that can detect their respective positions. Professor Stefan has asked Mothi to find the street lamp that has a specific height using a recursive search algorithm. Mothi has written a recursive algorithm to find the height but needs help in determining the time complexity. Given an array of street lamp heights a , which is sorted in ascending order, write an algorithm to find the position of a lamp with a specific height using a recursive linear search.

```
int recursiveLinearSearch(int a[], int low, int high, int tar)
{
    if (low > high)
        return -1;
    if (a[low] == tar)
        return low;
    return recursiveLinearSearch(a, low + 1, high, tar);
}
```

Question: Determine the time complexity of the recursiveLinearSearch function in the best, worst, and average cases.

- **Procedure/Program:**

```
int recursive linear search(int a[], int low, int high, int tar)
{
    if (low > high)
        return -1;
    }
    if (a[low] == tar)
    {
        return low;
    }
    return recursive linear search(a, low + 1, high, tar);
}
```

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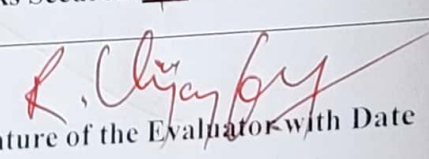
• Data and Results:

The result of the time complexity of analysis
 Best case $O(1)$
 Worst case $O(n)$
 Average case $O(n)$

• Analysis and Inferences: ~~*The successive linear search function has a time complexity of $O(n)$ the function reads from best case $O(1)$~~

• Sample VIVA-VOCE Questions (In-Lab):

1. Define time complexity in the context of algorithms. How does time complexity influence the efficiency of an algorithm?
2. Explain the concept of space complexity. Why is it important to consider space complexity along with time complexity when analyzing algorithms?
3. Differentiate between worst-case, best-case, and average-case time complexity. How do each scenario impact the performance of an algorithm?
4. What is Big-O notation? How is it used to express the time complexity of algorithms? Provide an example to illustrate.
5. Explain the process of Merge Sort with a detailed step-by-step example. How does Merge Sort ensure its time complexity of $O(n \log n)$?

Evaluator Remark (if Any):	Marks Secured: <u>47</u> out of 50
	Signature of the Evaluator with Date 

Evaluator MUST ask Viva-voce prior to signing and posting marks for each experiment.

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Complexity of analysis
 $O(1)$
 $O(n)$
 $O(n^2)$

Linear search function
 The function reads

How does time complexity influence

important to consider space complexity

average-case time complexity. How does

time complexity of algorithms?

by-step example. How does Merge

ed: 4 out of 50

by
 e Evaluator with Date

marks for each experiment.

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- ① The two amount of time it tak for each statement to complete
- ② The function that describes how much memory (space) algorithm requires to the quantity.
- ③ The Best case the minimum no. of step of an algorithm.
 The function a specifies the minimum of an n size of a n.
- ④ The describes the worst - case to Provide an upper bound on the algorithm.
- ⑤ Divide the array int two (nearby) equal hot using merge sort only (mid) using with help of sid.