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Alrifa'a

Introduce New Non-terminals: For terminal symbols in longer productions, introduce new non-terminals to ensure all rules fit the binary or terminal production form.

### Pre-Tutorial (To be completed by student before attending tutorial session)

1. Remove unit productions from the following grammar

$$S \rightarrow AC, A \rightarrow a, C \rightarrow X|b, X \rightarrow Y, Y \rightarrow Z, Z \rightarrow a$$

Solution:

$$C \rightarrow X$$

$$X \rightarrow Y$$

$$Y \rightarrow Z$$

Dependency graph:



$$C \rightarrow Y$$

$$X \rightarrow Z$$

$$C \rightarrow X$$

$$X \rightarrow Y$$

$$Y \rightarrow Z$$

$$C \rightarrow Y$$

$$C \rightarrow Y$$

$$\rightarrow Z$$

$$Y \rightarrow a$$

$$C \rightarrow Z$$

$$\rightarrow Z$$

$$\rightarrow a$$

$$C \rightarrow a$$

$$X \rightarrow a$$

$$C \rightarrow a$$

$$X \rightarrow Z$$

$$X \rightarrow a$$

$$\therefore \{ S \rightarrow AC$$

$$A \rightarrow a$$

$$C \rightarrow a|b$$

$$X \rightarrow a$$

$$Y \rightarrow a \quad Z \rightarrow a^y$$

Course Title	AUTOMATA THEORY AND FORMAL LANGUAGES	ACADEMIC YEAR: 2023-24
Course Code(s)	22CS2002A	123

Remove useless productions and symbols from the following CFG:

$S \rightarrow AB \mid CA, B \rightarrow BC \mid AB, A \rightarrow a, C \rightarrow aB \mid b$

ion:

1)  $S \rightarrow AB$      $S \rightarrow CA$      $B \rightarrow BC$      $C \rightarrow aB$   
 $\rightarrow aB$      $\rightarrow bA$      $\otimes$      $\otimes$   
 $\rightarrow aBC$      $\rightarrow ba$   
 $\rightarrow aBb$   
 $\otimes$

2)  $S \rightarrow AB$      $S \rightarrow CA$   
 $\otimes$      $\rightarrow ba$

$\therefore [S \rightarrow CA$   
 $A \rightarrow a$   
 $C \rightarrow ab$

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3. Remove unit production from the following CFG:

$$S \rightarrow 0A \mid 1B \mid C, A \rightarrow 0S \mid 00, B \rightarrow 1 \mid A, C \rightarrow 01$$

Solution:

$$S \rightarrow C$$

$$B \rightarrow A$$

$$S \rightarrow C$$

$$B \rightarrow A$$

$$C \mid B \rightarrow 0S \rightarrow 0 \mid A \rightarrow 00A$$

$$\boxed{S \rightarrow 0}$$

$$\boxed{B \rightarrow 00}$$

B → 00

$$\therefore S \rightarrow 0A \mid 1B \mid 0$$

$$A \rightarrow 0S \mid 00$$

$$B \rightarrow 1 \mid 00$$

$$C \rightarrow 01$$

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TUTORIAL (To be carried out in presence of faculty in classroom)

Convert the given grammar to CNF

$$S \rightarrow aAD, A \rightarrow aB \mid bAB, B \rightarrow b, D \rightarrow d$$

Solution:

1) Simplification of CNF: NIL

2) Already in CNF

$$B \rightarrow b$$

$$D \rightarrow d$$

Introduce two new variables  $C_a \rightarrow a$   
 $C_b \rightarrow b$ 

$$\begin{aligned} S &\rightarrow aAD & A &\rightarrow aB & A &\rightarrow bAB \\ &\rightarrow C_aAD & &\rightarrow C_aB & &\rightarrow C_bAB \end{aligned}$$

(CNF)

introduce (n-2) variable  $D_1$ ,

$$S \rightarrow C_aD_1$$

$$D_1 \rightarrow AD$$

introduce (n-2) variable  $D_2$ ,

$$A \rightarrow C_bD_2$$

$$D_2 \rightarrow AB$$

$$P = \{ S \rightarrow C_aD_1$$

$$A \rightarrow C_aB \mid C_bD_2$$

$$B \rightarrow b$$

$$C_a \rightarrow a$$

$$C_b \rightarrow b$$

$$D \rightarrow d$$

$$D_1 \rightarrow AD$$

$$D_2 \rightarrow AB$$

$$G = (\{S, A, B, C_a, C_b, D, D_1, D_2\}, \{a, b\}, P, S)$$

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2. Convert the following CFG to CNF

$$S \rightarrow XSY, X \rightarrow aXS \mid a \mid \epsilon, Y \rightarrow SbS \mid X \mid bb.$$

Solution:

Step 1: $\epsilon$ -productions:

$$X \rightarrow \epsilon$$

$$S \rightarrow XSY$$

$$X \rightarrow aXS$$

$$S \rightarrow SY$$

$$X \rightarrow aS$$

unit-productions:

$$Y \rightarrow X$$

$$Y \rightarrow a$$

$$Y \rightarrow a$$

$$Y \rightarrow aXS$$

$$aXS$$

$$aXS$$

cycle productions:

$$1) S \rightarrow XSY$$

$$X \rightarrow aXS$$

$$Y \rightarrow SbS$$

$$Y \rightarrow X$$

$$\rightarrow aSbb$$

$$\downarrow$$

$$\rightarrow \textcircled{X}$$

$$\rightarrow a$$

$$\textcircled{X}$$

$$S \rightarrow SY \text{ (CNF)}$$

$$\text{widen: } \{S\}$$

$$P = \{X \rightarrow a/aS\}$$

$$2) S \rightarrow XSY$$

$$Y \rightarrow SbS/aS$$

$$\textcircled{X}$$

$$\text{let } C_a \rightarrow a, C_b \rightarrow b$$

$$X \rightarrow aS$$

$$Y \rightarrow bb$$

$$\rightarrow C_a S$$

$$\rightarrow C_b C_b$$

$$G = (\{S, X, Y, Z, C_a, C_b\}, \{a, b\}, P, S)$$

$$C_a, C_b$$

$$P = \{S \rightarrow SY\}$$

$$X \rightarrow a/aS$$

$$Y \rightarrow a/C_b C_b$$

$$C_a \rightarrow a$$

$$C_b \rightarrow b$$



3. Convert the following grammar into CNF.

$S \rightarrow aAB, A \rightarrow aB \mid bAB, B \rightarrow aBB \mid bS \mid b.$

Solution:

Step 1: Simplification: NIL

Step 2:  $B \rightarrow b$  already CNF

introduce two new variables  $C_a \rightarrow a, C_b \rightarrow b$

$S \rightarrow C_a AB$

$A \rightarrow C_a B$  (CNF)

$A \rightarrow C_b AB$

$B \rightarrow C_a BB$

$B \rightarrow C_b S$  (CNF)

introduce (n-2) variables  $D_1, D_2$

$S \rightarrow C_a D_1$

$B \rightarrow C_a D_2$

$A \rightarrow C_b D_1$

$D_2 \rightarrow BB$

$D_1 \rightarrow AB$

$G_2 = (\{S, A, B, C_a, C_b, D_1, D_2\}, \{a, b\}, P, S)$

$P = \{ S \rightarrow C_a D_1$

$A \rightarrow C_a B \mid C_b D_1$

$B \rightarrow C_a D_2 \mid C_b S \mid b$

$C_a \rightarrow a$

$C_b \rightarrow b$

$D_1 \rightarrow AB$

$D_2 \rightarrow BB$

Post-Tutorial (To be carried out by student after attending tutorial session)

1. Convert the following CFG to CNF:  $S \rightarrow AOB$ ,  $A \rightarrow AA \mid OS \mid O$ ,  $B \rightarrow OBB \mid 1S \mid 1$

Solution:

$$\begin{aligned} A &\rightarrow AA \\ B &\rightarrow 1 \\ A &\rightarrow O \\ S &\rightarrow AOB \end{aligned} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \text{already CNF}$$

$$\text{let } C_a \rightarrow AO$$

$$C_b \rightarrow 1$$

$$\begin{aligned} \Rightarrow S &\rightarrow A C_a B \\ A &\rightarrow C_a S \text{ (CNF)} \\ B &\rightarrow C_b B \\ B &\rightarrow C_b S \text{ (CNF)} \end{aligned}$$

let  $D_1, D_2$  (non-terminal) variable

$$\begin{aligned} S &\rightarrow A D_1 & B &\rightarrow C_a D_2 \\ D_1 &\rightarrow C_a B & D_2 &\rightarrow B B \end{aligned}$$

$$G = (\{S, A, B, C_a, C_b, D_1, D_2\}, \{a, 1\}, P, S)$$

$$P = \left\{ \begin{array}{l} S \rightarrow A D_1 \\ A \rightarrow AA \mid C_a S \mid O \\ B \rightarrow C_a D_2 \mid C_b S \mid 1 \\ C_a \rightarrow O \\ C_b \rightarrow 1 \end{array} \right\}$$

$$D_1 \rightarrow C_a B$$

$$D_2 \rightarrow B B$$

2. Convert the following CFG to CNF:  $S \rightarrow AB$ ,  $A \rightarrow aab$ ,  $B \rightarrow aAc$

Solution:

$$S \rightarrow AB \text{ (already CNF)}$$

$$\text{let } C_a \rightarrow a, C_b \rightarrow b, C_c \rightarrow c$$

$$B \rightarrow aAc \quad A \rightarrow C_a C_a C_b$$

$$C_a A C_c$$

let  $D_1, D_2$  (non-terminal) variable

$$B \rightarrow C_a D_1 \quad A \rightarrow C_a D_2$$

$$D_1 \rightarrow A C_c \quad D_2 \rightarrow C_a C_b$$

$$G = (\{S, A, B, C_a, C_b, C_c, D_1, D_2\}, \{a, b, c\}, P, S)$$

$$P = \left\{ \begin{array}{l} S \rightarrow AB \\ A \rightarrow C_a D_2 \\ B \rightarrow C_a D_1 \\ C_a \rightarrow a \\ C_b \rightarrow b \\ C_c \rightarrow c \end{array} \right\}$$

$$D_1 \rightarrow A C_c$$

$$D_2 \rightarrow C_a C_b$$

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Convert the following CFG into CNF:  $S \rightarrow ASA \mid aB, A \rightarrow B \mid S, B \rightarrow b \mid \epsilon$

Solution:

(i)  $B \rightarrow \epsilon$

$S \rightarrow aB$

$S \rightarrow a$

~~$A \rightarrow B$~~

(ii)

$A \rightarrow B$

$A \rightarrow S$

$A \rightarrow b$

$A \rightarrow aB$

$A \rightarrow ab$

(iii)  $S \rightarrow ASA$

$\rightarrow BABB$

$\rightarrow babb$

$S \rightarrow aB$

$\rightarrow ab$

$A \rightarrow B$

$\rightarrow b$

$A \rightarrow S$

$\rightarrow aB$

$\rightarrow ab$

2)  $S \rightarrow ASA$  (i)  $S \rightarrow aB$   
 $\checkmark$   $\checkmark$

$P = \{ S \rightarrow ASA \mid aB \mid a$

$A \rightarrow b \mid ab$

$B \rightarrow b \}$

$S \rightarrow a$

$A \rightarrow b$

$B \rightarrow b$

} already CNF

let  $C_a \rightarrow a, C_b \rightarrow b$

$S \rightarrow CAB$

$A \rightarrow C_a C_b$

$S \rightarrow ASA$

(let  $D_1$  (non-terminal) variable

$S \rightarrow AD_1$

$D_1 \rightarrow SA$

$P' = \{ S \rightarrow AD_1 \mid a \mid CAB \}$

$A \rightarrow C_a C_b \mid b$

$B \rightarrow b$

$C_a \rightarrow a$

$C_b \rightarrow b$

$D_1 \rightarrow SA$

$G_2 = ( \{ S, A, B, C_a, C_b, D_1 \}, \{ a, b \}, P', S )$



Viva Questions

1. What is Chomsky Normal Form (CNF) in the context of context-free grammars, and what are its key characteristics?  
 Answer:

Any CFG without  $\epsilon$  is generated by a grammar in which all productions are of the form  $A \rightarrow BC$  or  $A \rightarrow a$ . Here  $A, B$  and  $C$  are variables and  $a$  is terminal.

$$V \rightarrow VV$$

$$V \rightarrow T$$

2. Why is it necessary to remove  $\epsilon$ -productions when converting to Chomsky Normal Form?  
 Answer:

Let  $G$  be any CFG with  $\epsilon$  is not in  $L(G)$  then there exist an equivalent grammar  $G'$  having no  $\epsilon$ -production.

(For Evaluator's use only)

Comment of the Evaluator (if Any)	Evaluator's Observation
	Marks Secured: <u>18</u> out of <u>50</u>
	Full Name of the Evaluator:
	Signature of the Evaluator Date of Evaluation: