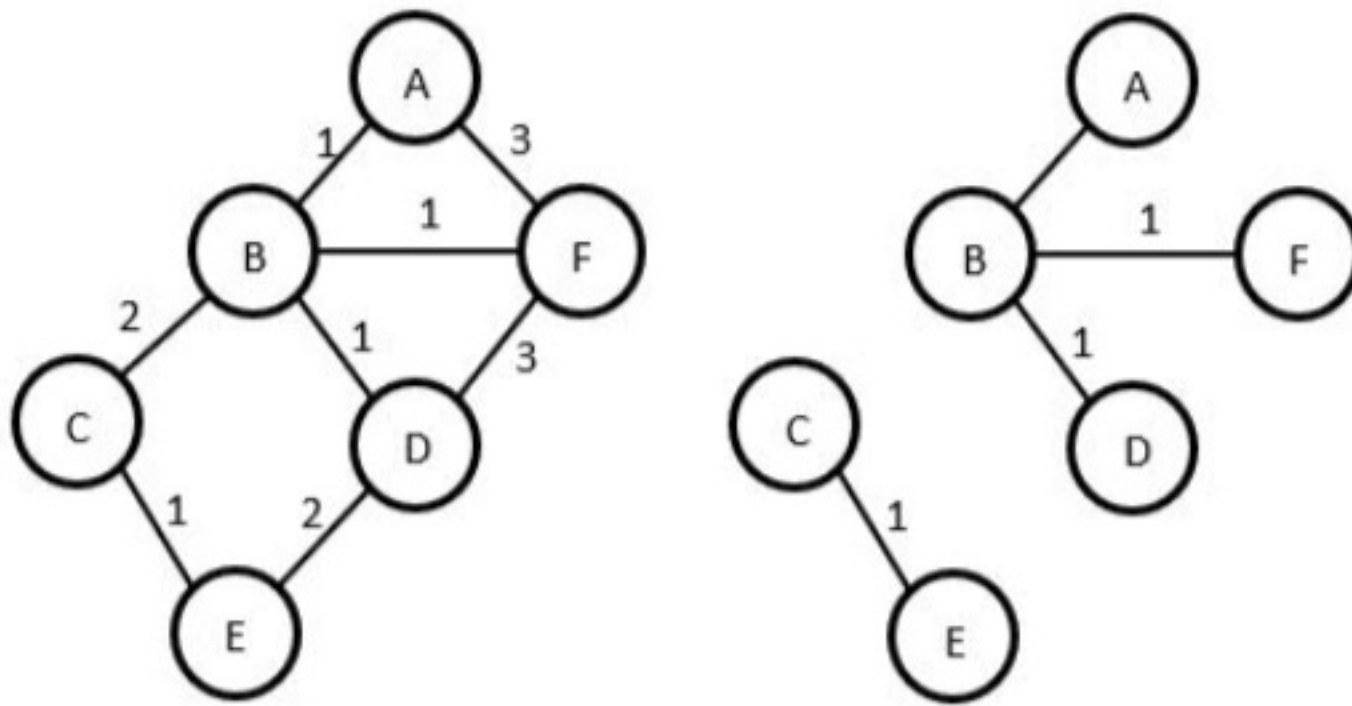


1. Consider the graph shown below and an intermediate stage of running Kruskal's algorithm on the graph.



The remaining edges to be processed in ascending order of weights are [C-B, E-D, A-F, D-F].

Select all correct answers from the list below.

☐ The edge C-B, when inserted, will connect two nodes that belong to the same tree in the forest.

☒ After the edge C-B is added, there is exactly one tree in the forest.

✓ **Correct**  
Correct.

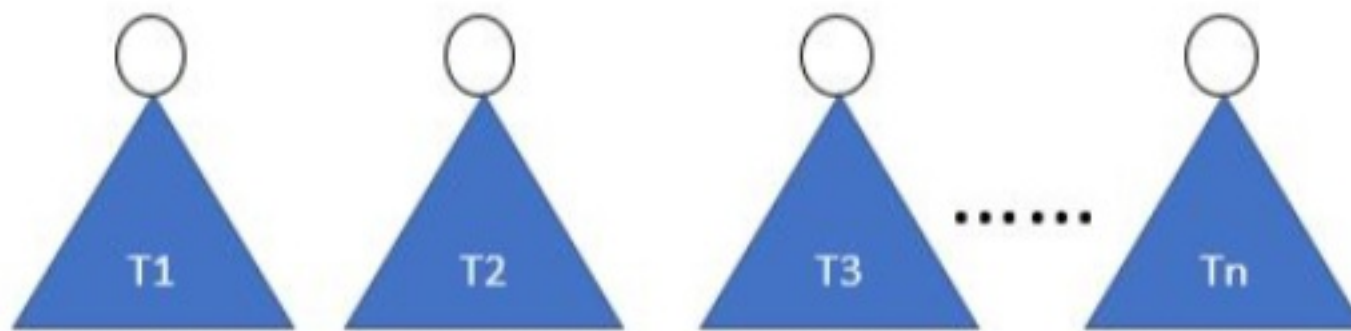
☒ The edges E-D, A-F and D-F are not added to the spanning tree because their two nodes are part of the same tree in the forest.

✓ **Correct**  
Correct. Because C-B is added first, there will only be one tree in the forest by the time E-D is considered.

☒ Given a forest of trees, finding if two nodes belong to the same tree can be achieved in time at most  $O(|V|)$ , where  $|V|$  is the total number of nodes.

✓ **Correct**  
Correct.

2. The schematic below represents a forest during an intermediate state of the Kruskal's algorithm. Each triangle is a tree.



Select all the correct facts about the operation of Kruskal's algorithm for minimum spanning tree referring to the figure above.

- ☒ Suppose we attempt to insert an edge  $(A, B)$  with weight  $W$ , wherein  $A$  and  $B$  belong to the same tree. Then every edge in the existing path from  $A$  to  $B$  must have weight less than or equal to  $W$ .
 

☒ **Correct**  
Correct. Otherwise, the edge A-B would have been added before the other path between A and B existed.
- ☒ Suppose we attempt to insert an edge  $(A, B)$  and  $A$  and  $B$  belong to two different trees in the forest. Then such an edge will be part of the final spanning tree output by Kruskal's algorithm.
 

☒ **Correct**  
Correct.
- ☒ If the edges are not inserted in ascending order of weights, the resulting spanning tree would not necessarily be minimal.
 

☒ **Correct**  
Correct.
- ☒ Kruskal's algorithm can be made faster if we have a way to rapidly check if two nodes in the forest are part of the same tree.
 

☒ **Correct**  
Correct.