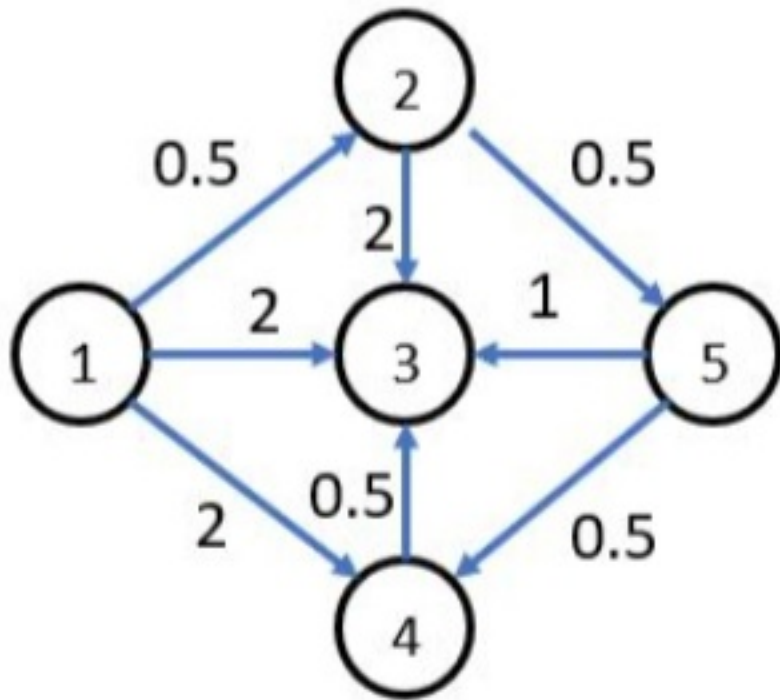


1. We will apply Dijkstra's algorithm for the following graph with the source vertex 1.



Here is the table of nodes with distances and parent values. Nodes 1 and 2 have already been visited or processed.

| Node | Distance | Parent |
|------|----------|--------|
| 1 | 0 | NIL |
| 2 | 0.5 | 1 |
| 3 | 2 | 1 |
| 4 | 2 | 1 |
| 5 | 1 | 2 |

Select all the correct facts about the subsequent working of the algorithm.

- ☐ The next node to be visited will be node 3.
- ☒ Dijkstra's algorithm will relax each edge exactly once during its entire execution.

✔ **Correct**

Correct. Specifically, an edge (u,v) is relaxed when its source node u is popped off the priority queue.

- ☐ The lowest priority node is node 1 and will be visited next.
- ☒ The priority queue (heap) has nodes 3, 4 and 5 with priorities 2, 2 and 1 respectively.

✔ **Correct**

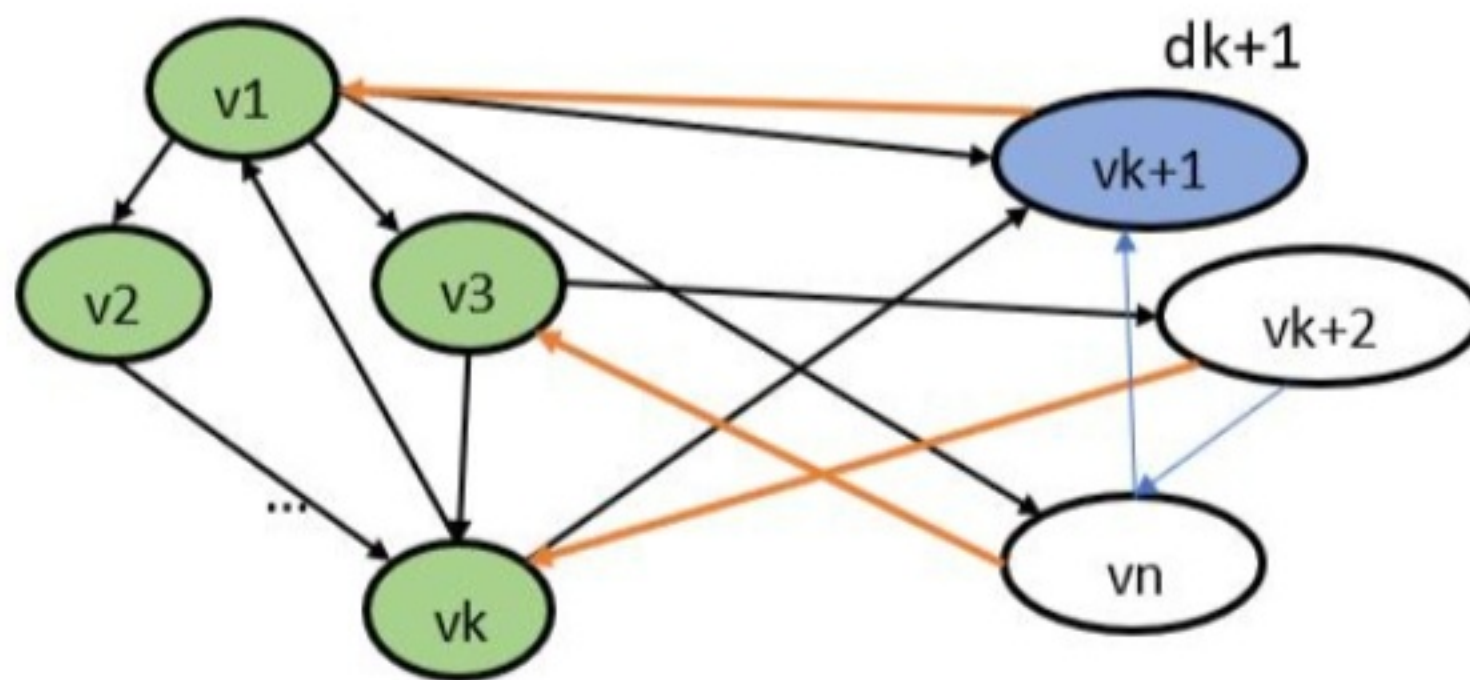
That is correct. Unvisited/unprocessed nodes will be in the priority queue with the distance estimates as the priority.

- ☒ The next node to be visited will be 5 and will cause edges $(5,4)$ and $(5,3)$ to be relaxed.

✔ **Correct**

Correct.

2. In this question, we will examine some of the properties that are true of Dijkstra's algorithm in general. Here is a schematic of a graph representing an intermediate stage of running the algorithm.



The green nodes v_1, \dots, v_k represent nodes already visited or processed. The other nodes v_{k+1}, \dots, v_n represent the as yet unprocessed nodes with v_{k+1} representing the node with lowest priority given by d_{k+1} (assume all other unvisited nodes have strictly larger priority). Select all the true facts about properties of Dijkstra's algorithm from the list below.

☐ A previously visited node can be added back to the priority queue as the algorithm runs.

☒ The shortest path to node v_{k+1} must have shortest path distance d_{k+1} .

✔ **Correct**

Correct, as we argued in the lecture.

☐ It is possible that when an outgoing edge from v_{k+1} is relaxed in the subsequent step, the distance estimate to some green previously visited node decreases.

☒ The next node that will be visited by Dijkstra's algorithm is v_{k+1} .

✔ **Correct**

Correct.

☒ For all visited nodes (green nodes in graph), the distance estimate is less than or equal to d_{k+1} .

✔ **Correct**

Correct. This is because all edge weights are non-negative.