

1. Consider we wish to compute change for 48 cents given coins of denomination

4 / 4 points

{ 2, 5, 10, 20} cents. We design two tables

Tbl[j] that records the best solution in terms of number of coins for j cents.

S[j] that records the "first" coin denomination that we need to use for obtaining the solution for Tbl[j]

Select all the correct facts from the list below.

☐ Tbl[j] = $-\infty$ for $j < 0$

☒ $Tbl[j] = \min(1 + Tbl[j - 2], 1 + Tbl[j - 5], 1 + Tbl[j - 10], 1 + Tbl[j - 20])$

✓ Correct
Correct

☒ $Tbl[3] = \infty$ denoting that we cannot make change for 3 cents using the given denominations.

✓ Correct

☒ Suppose we wish to recover the solution, let $S[48]$ have the value 20 after we finish implementing the memoization. The solution recovery will add a 20 cent coin to our solution list and look up $S[28]$

✓ Correct
Correct

☐ Following the previous option, suppose we look up $S[28]$ and encounter $S[28] = 2$, we will look up $S[20]$ next.

2. Consider the usual solution that people use to make change for target T .

- Take the largest denomination coin that is $\leq T$ let it be c_j .
- Give c_j and recursively make change for $T - c_j$.
- Stop when the remaining change is 0.

Consider the denominations $\{1, 2, 5, 10, 20, 25\}$ cents.

- ☒ Suppose we wish to make change for 50 cents, our approach will provide two 25 cent coins as change, which is optimal.

☒ **Correct**
Correct

- ☐ Suppose we wish to make change for 40 cents, our approach will use two 20 c coins, which is optimal.
- ☐ The algorithm presented above always produces the optimal solution for any coin denominations and target.
- ☒ The algorithm makes optimal decision for $T = 49$, using four coins: one 25 cent, one 20 cent and two 2 cent coins.

☒ **Correct**
Correct