

|            |                           |              |            |
|------------|---------------------------|--------------|------------|
| Tutorial # | 2                         | Student ID   | 2300032601 |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | M. KOUJHIK |

**Pre-Tutorial (To be completed by student before coming to tutorial class)**

1. Draw a NFA that accepts the language  $\emptyset^*$ . Explain your answer.

**Solution:**

The language  $\emptyset^*$  represent the set all string over the alphabet  $\Sigma$  that are in the Kleene star of the empty set  $\emptyset$

$$\rightarrow \textcircled{q_0} \quad S = \{ q_0 \}$$

$$A = \Sigma$$

$$IS = q_0$$

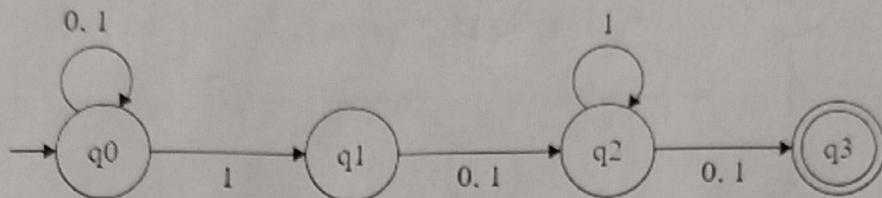
$$FS = q_1$$

No Transition

|                |                       |                        |
|----------------|-----------------------|------------------------|
| Course Title   | THEORY OF COMPUTATION | ACADEMIC YEAR: 2024-25 |
| Course Code(s) | 23MT2014              | Page 18 of 261         |

|            |                           |              |                           |
|------------|---------------------------|--------------|---------------------------|
| Tutorial # | <TO BE FILLED BY STUDENT> | Student ID   | <TO BE FILLED BY STUDENT> |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | <TO BE FILLED BY STUDENT> |

2. Consider the finite automaton in the following figure.



What is the set of reachable states for the input string 0011? What is the language accepted by the above automaton.

Solution:

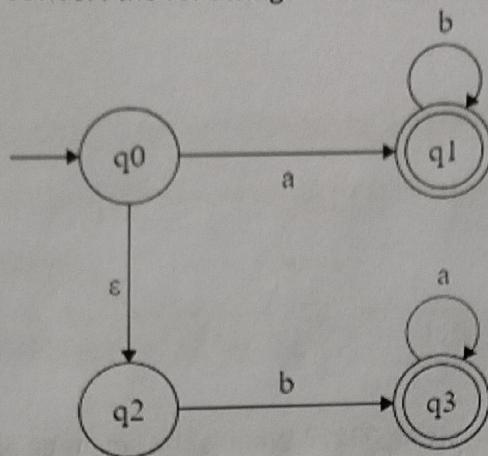
$$L = \{ (0+1)^* 1 (0+1)^* (0+1)^* \}$$

$L = \{ \omega \in \{0, 1\}^* \text{ condition on odd number of } 1's \}$

|       | 0           |             |
|-------|-------------|-------------|
| $q_0$ | $q_{f0}$    | $q_1, q_m$  |
| $q_1$ | $q_2$       | $q_2$       |
| $q_2$ | $q_3$       | $q_1, q_3$  |
| $q_3$ | $\emptyset$ | $\emptyset$ |

|            |                           |              |                           |
|------------|---------------------------|--------------|---------------------------|
| Tutorial # | <TO BE FILLED BY STUDENT> | Student ID   | <TO BE FILLED BY STUDENT> |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | <TO BE FILLED BY STUDENT> |

3. Convert the following  $\epsilon$ -NFA to NFA without  $\epsilon$ -transition.

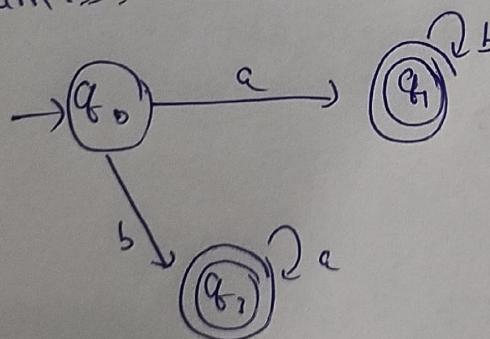


**Solution:**

E-NFA to NFA

| NFA $\rightarrow$ | a           | b           |
|-------------------|-------------|-------------|
| $q_0$             | $q_1$       | $q_3$       |
| $q_1^*$           | $\emptyset$ | $q_1$       |
| $q_2^*$           | $q_3$       | $\emptyset$ |

$\Rightarrow$  Diagram ...



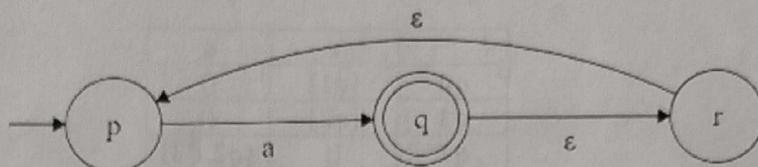
$\rightarrow$  If we can reach to final state from that node by using ' $\epsilon$ ' then it will be a final state

|                |                       |                        |
|----------------|-----------------------|------------------------|
| Course Title   | THEORY OF COMPUTATION | ACADEMIC YEAR: 2024-25 |
| Course Code(s) | 23MT2014              | Page 20 of 261         |

|            |                           |              |                           |
|------------|---------------------------|--------------|---------------------------|
| Tutorial # | <TO BE FILLED BY STUDENT> | Student ID   | <TO BE FILLED BY STUDENT> |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | <TO BE FILLED BY STUDENT> |

### IN-TUTORIAL (To be carried out in presence of faculty in classroom)

1. What is the complement of the language accepted by the NFA shown below? Draw the NFA for the language found out. Assume  $\Sigma = \{a\}$  and  $\epsilon$  is the empty string.



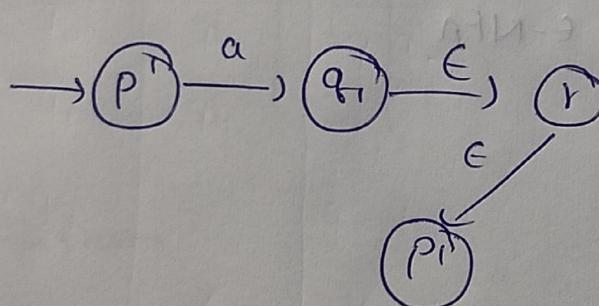
Solution:

$$\text{state} = \{p, q, r\}$$

$$\epsilon\text{-closure}(p) = \{p, q, r\}$$

$$\epsilon\text{-closure}(q) = \{q, r\}$$

$$\epsilon\text{-closure}(r) = \{p, r\}$$



|            |                           |              |                           |
|------------|---------------------------|--------------|---------------------------|
| Tutorial # | <TO BE FILLED BY STUDENT> | Student ID   | <TO BE FILLED BY STUDENT> |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | <TO BE FILLED BY STUDENT> |

2. Consider the following  $\epsilon$ -NFA,  $M = (\{q_0, q_1, q_2, q_3\}, \{a\}, \delta, q_0, \{q_3\})$  where  $\delta$  is given in the transition table below. What is the minimum length of string to reach to the final state.

|       | $\epsilon$ | a              |
|-------|------------|----------------|
| $q_0$ | $\{q_1\}$  | $\{\}$         |
| $q_1$ | $\{q_2\}$  | $\{\}$         |
| $q_2$ | $\{\}$     | $\{q_2, q_3\}$ |
| $q_3$ | $\{\}$     | $\{\}$         |

Solution:

$$M = (Q, \Sigma, \delta, q_0, q_3)$$

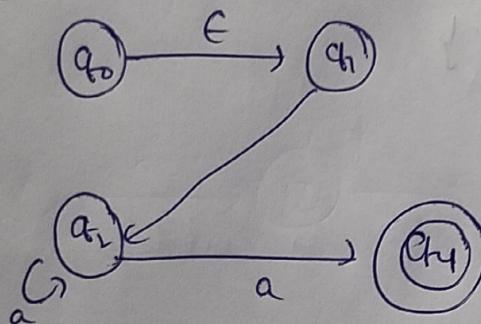
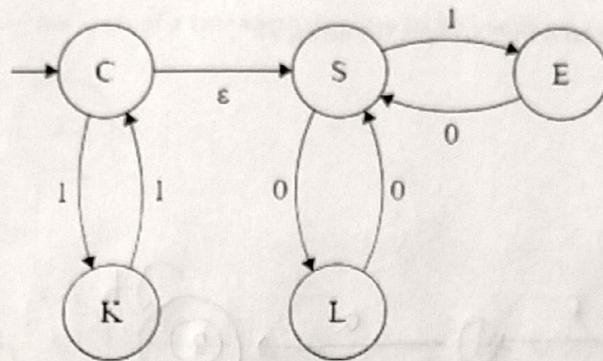


Diagram of  $\epsilon$ -NFA

|                |                       |                        |
|----------------|-----------------------|------------------------|
| Course Title   | THEORY OF COMPUTATION | ACADEMIC YEAR: 2024-25 |
| Course Code(s) | 23MT2014              | Page 22 of 261         |

|            |                           |              |                           |
|------------|---------------------------|--------------|---------------------------|
| Tutorial # | <TO BE FILLED BY STUDENT> | Student ID   | <TO BE FILLED BY STUDENT> |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | <TO BE FILLED BY STUDENT> |

3. Convert the following  $\epsilon$ -NFA to NFA without  $\epsilon$ -transitions.

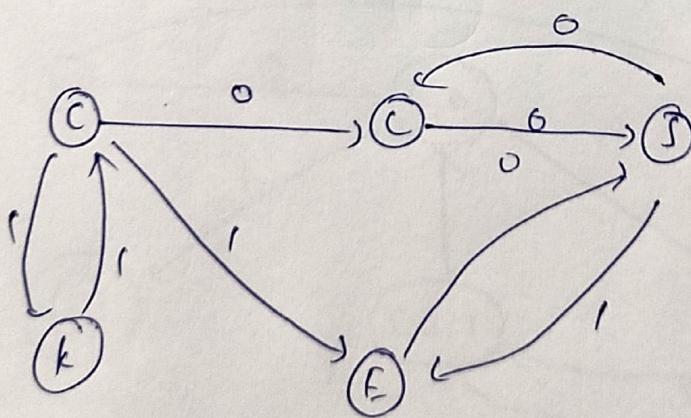


Solution:

Table of NFA

|   | 0 | 1    |
|---|---|------|
| C | L | K, E |
| L | S | ∅    |
| K | ∅ | C    |
| E | S | -    |
| S | C | E    |

Diagram



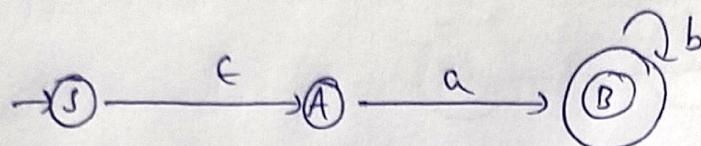
|            |                           |              |                           |
|------------|---------------------------|--------------|---------------------------|
| Tutorial # | <TO BE FILLED BY STUDENT> | Student ID   | <TO BE FILLED BY STUDENT> |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | <TO BE FILLED BY STUDENT> |

**Post-Tutorial (To be carried out by student after Tutorial session is over)**

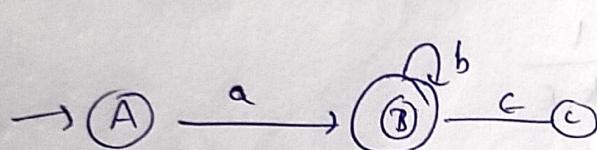
1. Construct an  $\epsilon$ -NFA that accepts the string  $ab^*$ .

**Solution:**

$\Rightarrow ab^*$



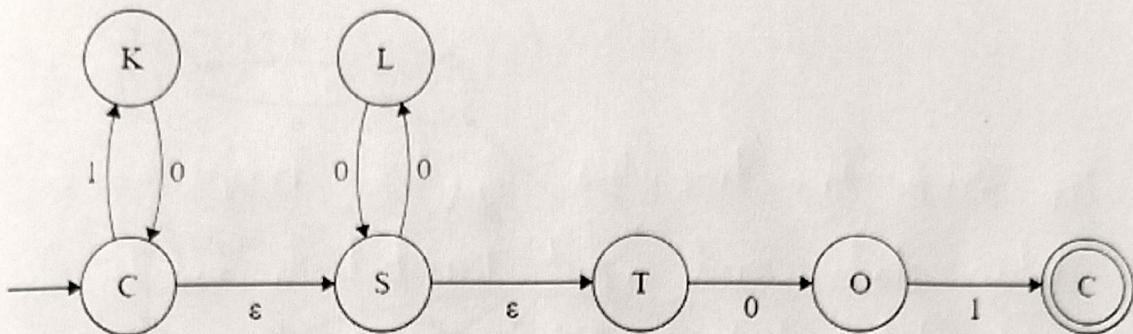
(Ans)



|                |                       |                        |
|----------------|-----------------------|------------------------|
| Course Title   | THEORY OF COMPUTATION | ACADEMIC YEAR: 2024-25 |
| Course Code(s) | 23MT2014              | Page 24 of 261         |

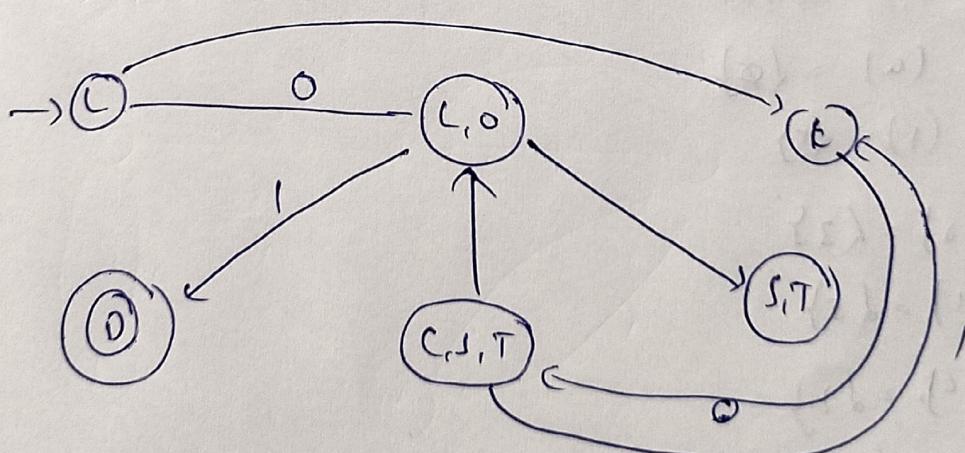
|            |                           |              |                           |
|------------|---------------------------|--------------|---------------------------|
| Tutorial # | <TO BE FILLED BY STUDENT> | Student ID   | <TO BE FILLED BY STUDENT> |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | <TO BE FILLED BY STUDENT> |

2. Convert the  $\epsilon$ -NFA given in the form of a transition diagram to NFA without  $\epsilon$ -transition.

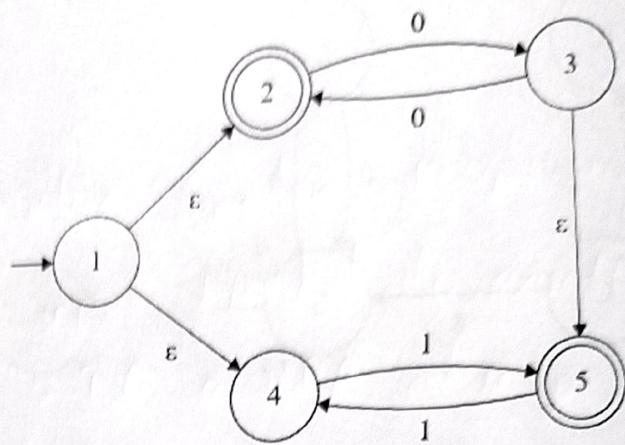


Solution:

|         | 0            | 1            |
|---------|--------------|--------------|
| C       | C, O         | K            |
| L, O    | S, T         | D            |
| K       | C, S, T      | <del>D</del> |
| D       | <del>∅</del> | <del>∅</del> |
| C, S, T | C, O         | K            |



3. Transform the following  $\epsilon$ -NFA to NFA.



**Solution:**

$$Q = \{1, 2, 3, 4, 5\}$$

$$\Sigma = \{0, 1\}$$

$$\epsilon \text{ close } (1) = \{1, 2, 4\}$$

$$\epsilon \text{ close } (2) = \{\emptyset\}$$

$$\epsilon \text{ close } (3) = \{3, 5\}$$

$$\epsilon \text{ close } (4) = \{\emptyset\}$$

$$\epsilon \text{ close } (5) = \{5\}$$

$$\delta' (1, 0) = \{3\}$$

$$\delta' (1, 1) = \{5\}$$

$$\delta' (3, 0) = \{2\}$$

$$\delta' (3, 1) = \{\emptyset\}$$

$$\delta' (5, 0) = \{\emptyset\} \quad \delta' (5, 1) = \{4\}$$

Course Title

Course Code(s)

THEORY OF COMPUTATION

23MT2014

ACADEMIC YEAR: 2024-25

Page 26 of 261

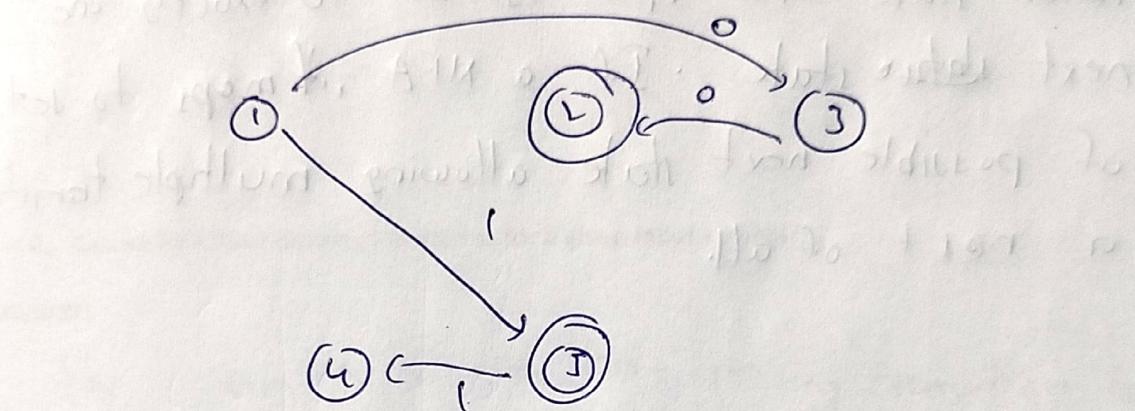
26

|            |                           |              |                           |
|------------|---------------------------|--------------|---------------------------|
| Tutorial # | <TO BE FILLED BY STUDENT> | Student ID   | <TO BE FILLED BY STUDENT> |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | <TO BE FILLED BY STUDENT> |

$$f'(1,0) = \text{closure}(1) = \{2\}$$

$$f'(1,1) = \text{closure}(1) = \{5\}$$

Diagram of NFA



|                |                       |                        |
|----------------|-----------------------|------------------------|
| Course Title   | THEORY OF COMPUTATION | ACADEMIC YEAR: 2024-25 |
| Course Code(s) | 23MT2014              | Page 27 of 261         |

|            |                           |              |                           |
|------------|---------------------------|--------------|---------------------------|
| Tutorial # | <TO BE FILLED BY STUDENT> | Student ID   | <TO BE FILLED BY STUDENT> |
| Date       | <TO BE FILLED BY STUDENT> | Student Name | <TO BE FILLED BY STUDENT> |

### Viva Questions

1. How does an NFA differ from a DFA in terms of the transition function?

Answer:

In DFA the transition function maps each state to exactly one next state. If a NFA maps to set of possible next state allowing multiple transitions or none at all.

2. What is the purpose of  $\epsilon$ -transitions in an NFA?

Answer:

They allow the NFA to move b/w states without consuming any input symbolic provides more flexibility.

|                |                       |                        |
|----------------|-----------------------|------------------------|
| Course Title   | THEORY OF COMPUTATION | ACADEMIC YEAR: 2024-25 |
| Course Code(s) | 23MT2014              | Page 28 of 261         |

|            |                         |              |                         |
|------------|-------------------------|--------------|-------------------------|
| Tutorial # | TO BE FILLED BY STUDENT | Student ID   | TO BE FILLED BY STUDENT |
| Date       | TO BE FILLED BY STUDENT | Student Name | TO BE FILLED BY STUDENT |

3. How does an NFA determine whether an input string is accepted?

Answer:

An NFA accepts an input if there exists at least one path through the states that leads to an accepting state.

4. Can an NFA have missing transitions for a given input symbol?

Answer:

Yes, an NFA can have missing transition for some input symbols. It can still accept the string if there are valid paths to an accepting state.

|                                      |  |
|--------------------------------------|--|
| Comment of the Evaluator<br>(if Any) | <p><b>Evaluator's Observation</b></p> <p>Marks Secured: _____ out of <u>50</u></p> <p>Full Name of the Evaluator:</p> <p>Signature of the Evaluator</p> <p>Date of Evaluation:</p> |
|--------------------------------------|--|