- 1. Consider a particle-in-a-box with length 5 units and the mass of the particle be 1 unit. Write a Fortran code to construct the hamiltonian matrix and diagonalize it to find out the eigenvalues and eigenvectors. Compare the numerical eigenvalues to exact eigenvalues by making a plot of the eigenvalues versus the number of points. Take the number of points to be 100. Remember that using finite differences, we derived the following: $\hat{H}_{ij} = (V_i + 2t)\delta_{i,j} t\delta_{i,j-1} t\delta_{i,j+1}$, where $\delta_{i,j}$ is the Kronecker delta. $t = \hbar^2/2mdx^2$.
- 2. Write a program for bisection method to solve the equation $x^2 + x 2 = 0$ using two sets of data points, (0.0,2.0) and (0.5,2.0). The code will print the final root, the functional value at the final root and the number of iterations.
- 3. Find the root using the false position method with two sets of starting points, (1.5,2.0) and (-3.0,0.0) The code will print the final root, the functional value at the final root and the number of iterations.