Partial Persistent Data-structure

Pointer Machine Model

Ephemeral Linked List

Operations:

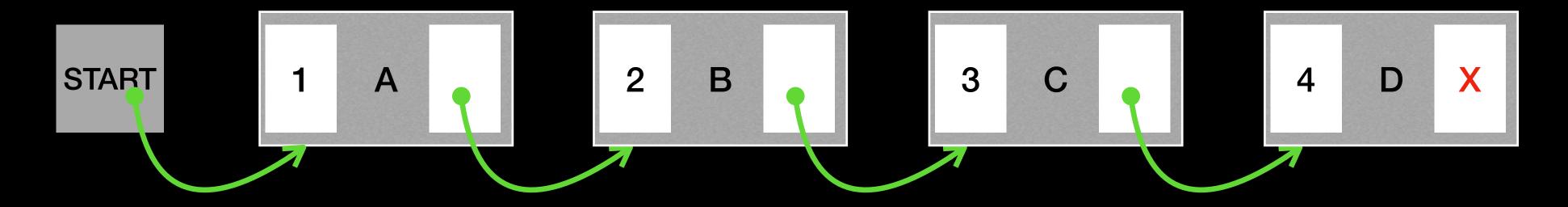
- start = init(): To initiate linked list and "start" pointer holds the starting position
- add(x, y) : Add new node x after y
- remove(x): Remove node x
- iterate_over_LL(): Iterate over the whole linked list
- update(f_i,x,val): Update the i-th field in node x to new value 'val'

Ephemeral Linkedlist

Node structure

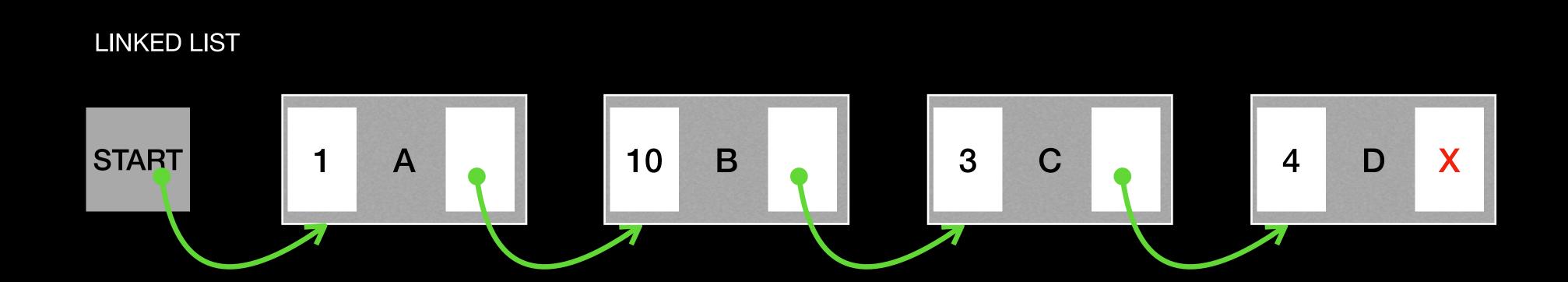


LINKED LIST

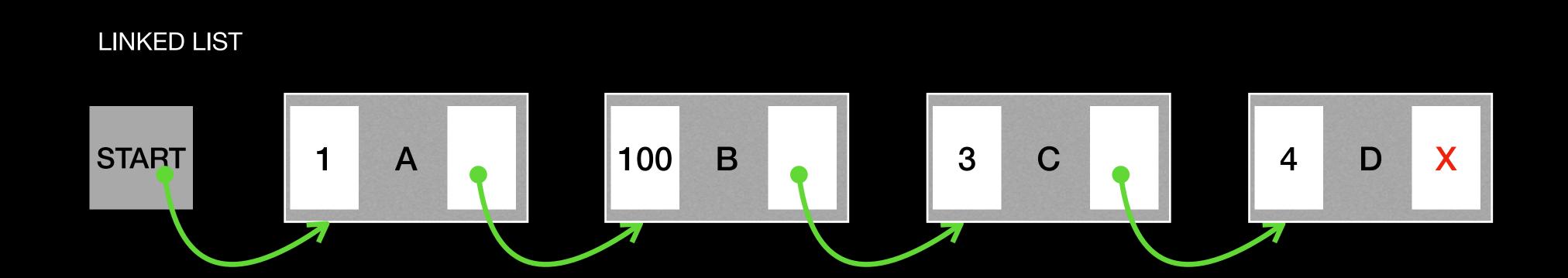


HERE IN-DEGREE OF A NODE IS <= 1 AND OUT-DEGREE OF A NODE IS <=1

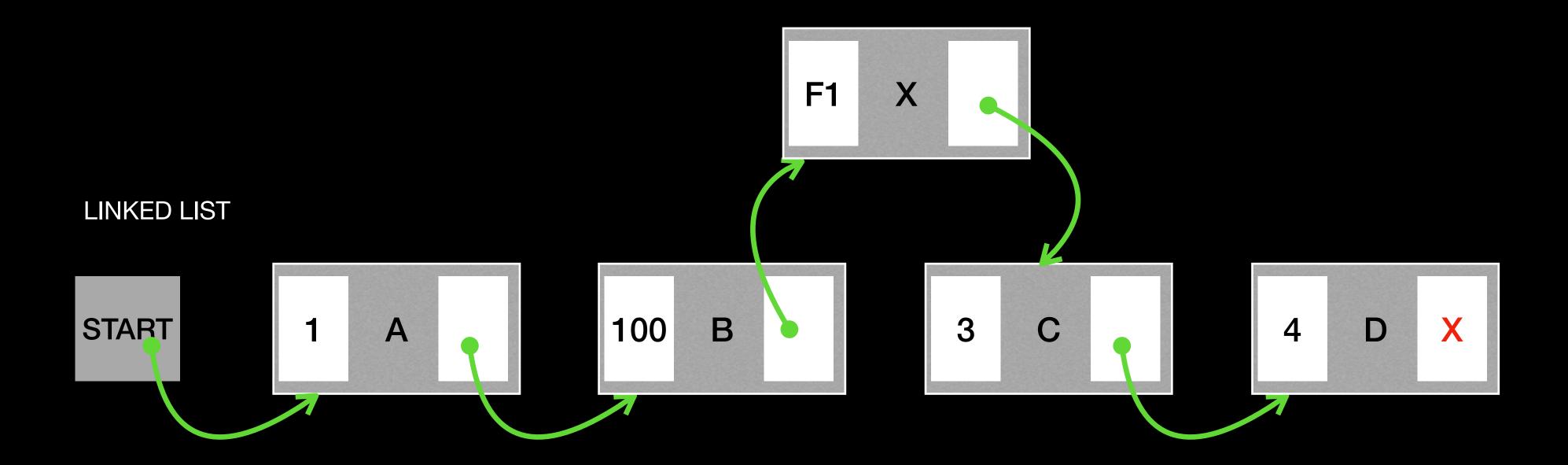
update(f1,B,10)



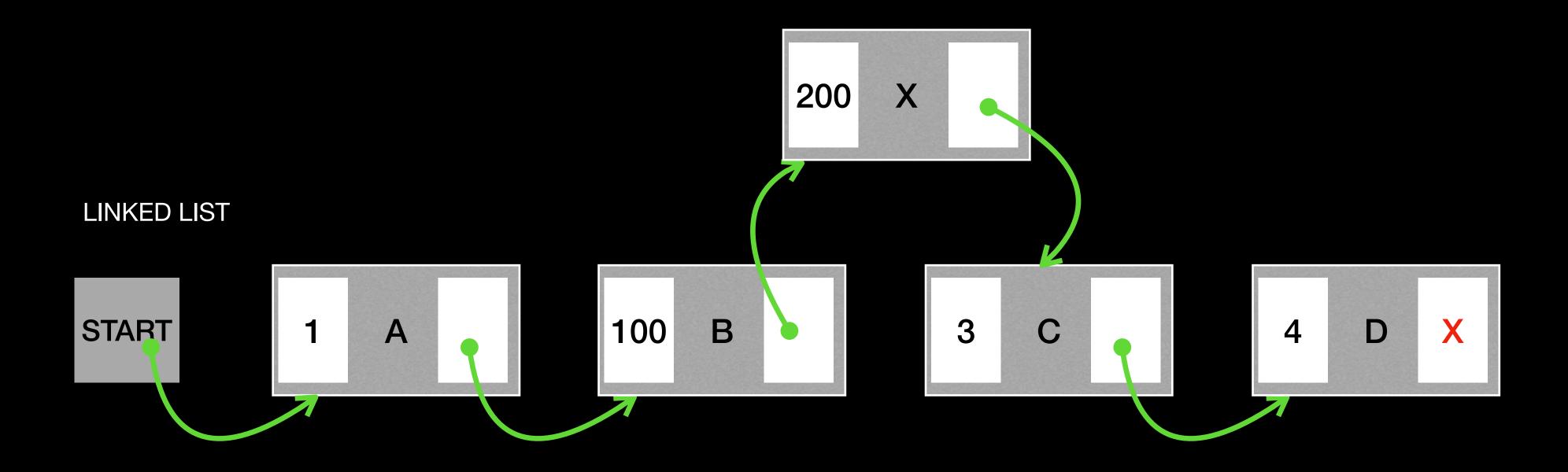
update(f1,B,100)



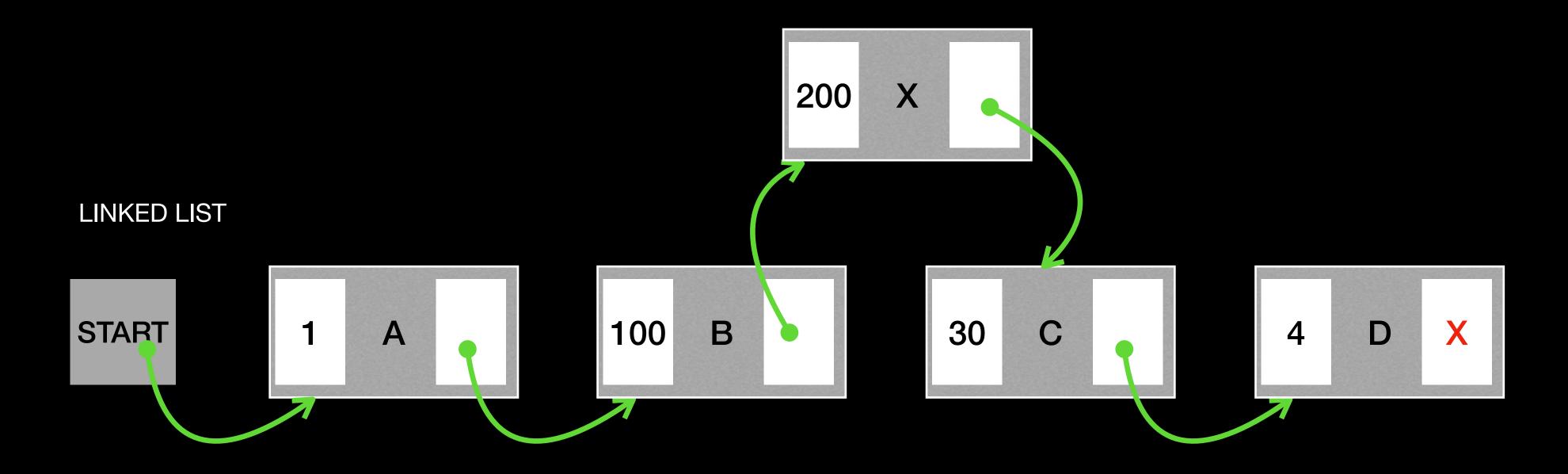
SOME OPERATIONS add(X,B)



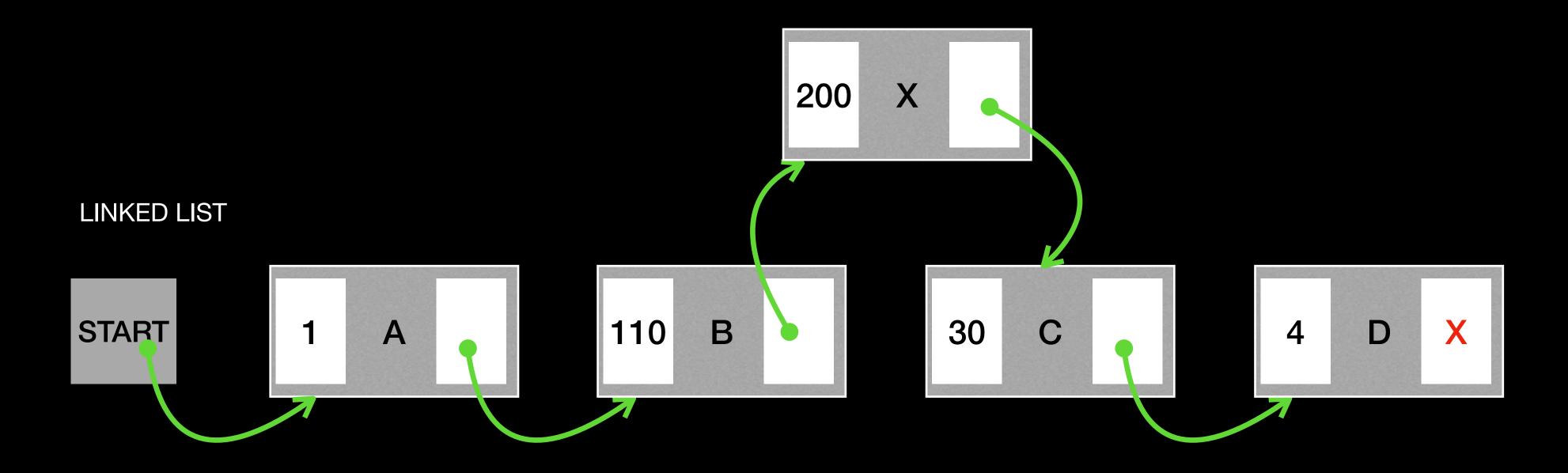
update(f1,X,200)



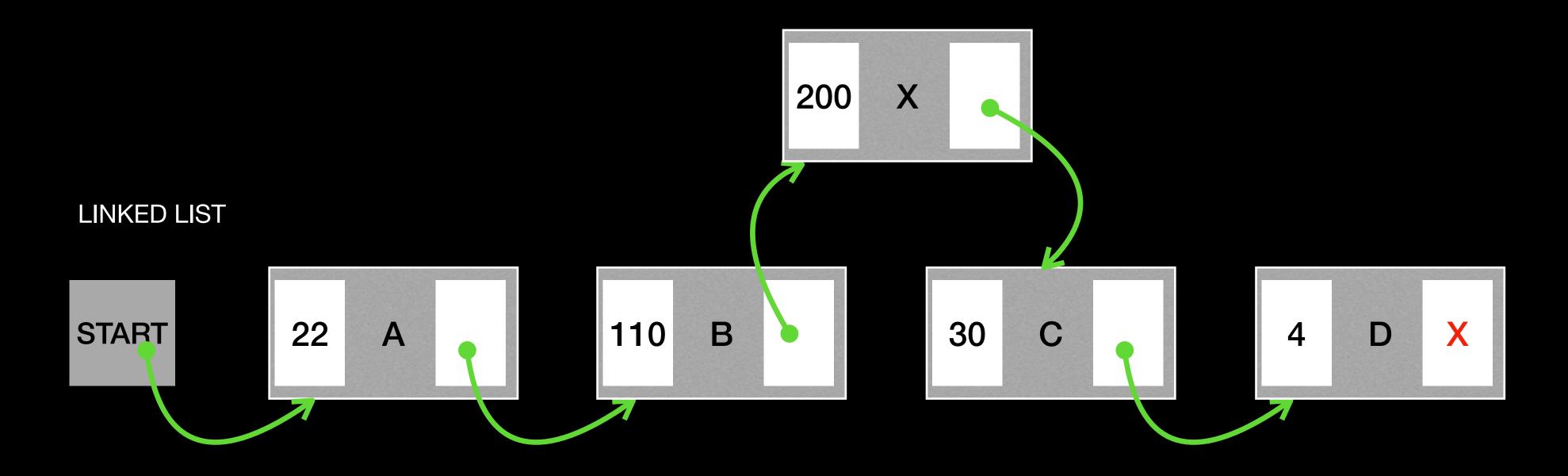
update(f1,C,30)



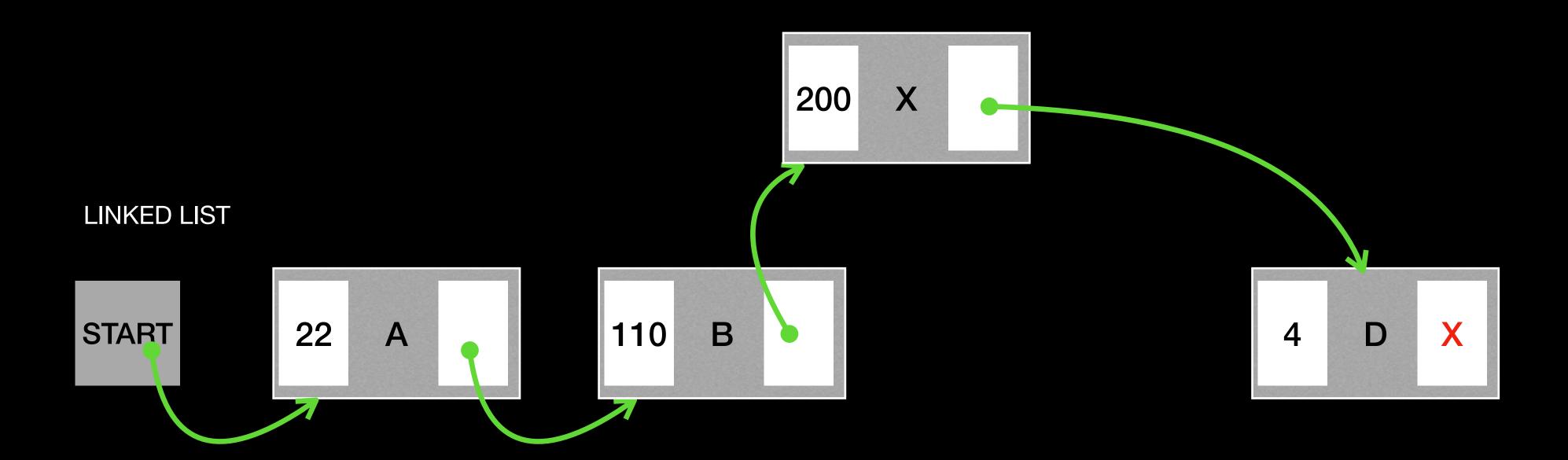
update(f1,B,110)



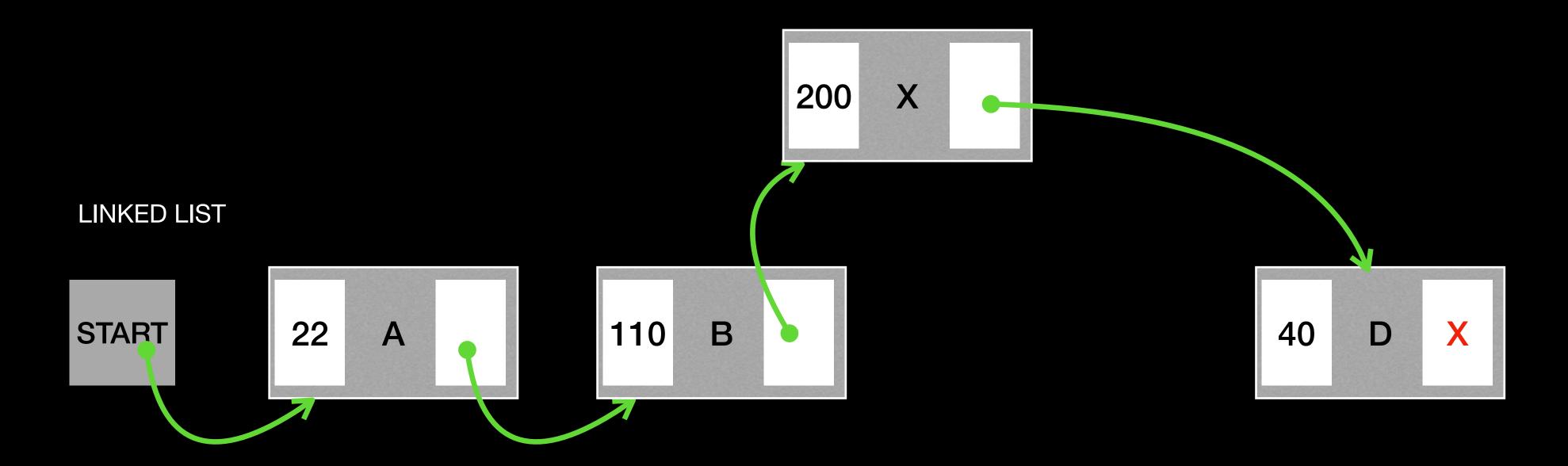
update(f1,A,22)



SOME OPERATIONS remove(C)



update(f1,D,40)



Partial Persistent Linked List Operations:

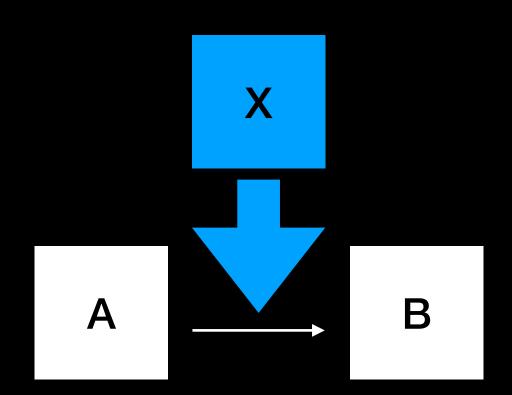
- start = init(): To initiate linked list and "start" pointer holds the starting position in v0
- create_node(x, a): Allocate a new node x with f1 = a and f2 = NULL, and set its
 default version to current version
- add(x, y, a) : Add new node x with value = a after y and update the version
- remove(x): Remove node x and update the version
- iterate_over_LL(v): Iterate over the whole linked list in version v
- update(f_i,x,val): Update the i-th field in node x to new value 'val' and update the version

Interesting thing!

add(x,y) and remove(x) are not Elementary operations

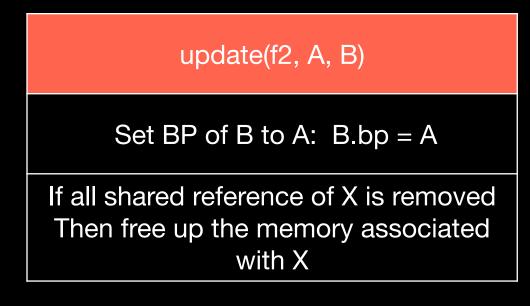
add(X,C,123) consists of

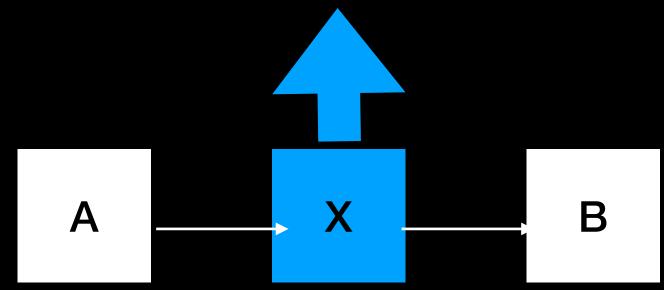
Create node X with value 123				
Modify f2 of A to X: update(f2, A, X)				
Modify f2 of X to C: update(f2, X, C)				
Set BP of X to A: X.bp = A				
Set BP of B to X: B.bp = X				
Set f1 of X(optional)				



remove(x) consists of

Modify F2 of Parent C (i.e., X) -> F2 of C (successor of C)





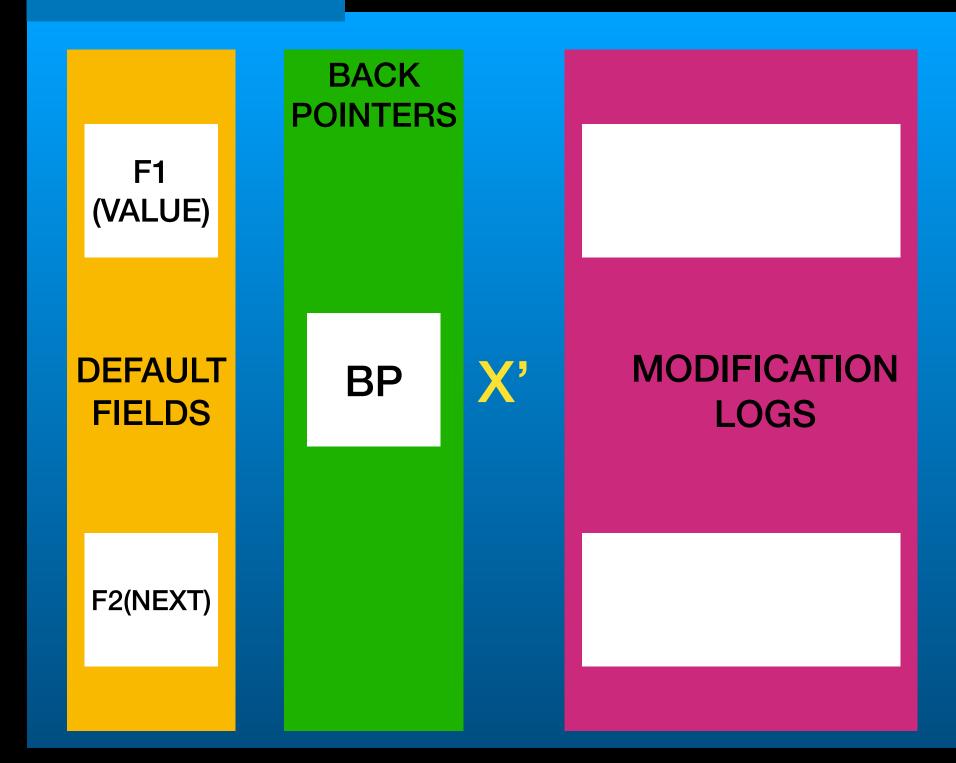
Elementary Operations:

```
start = init()
create_node(x, a)
iterate_over_LL(v)
update(f_i,x,val)
```

Persistent Linked List Node

VERSION REDIRECTOR MODULE DEFAULT VERSION BACK POINTERS F1 (VALUE) **MODIFICATION** DEFAULT X BP LOGS **FIELDS** F2(NEXT)

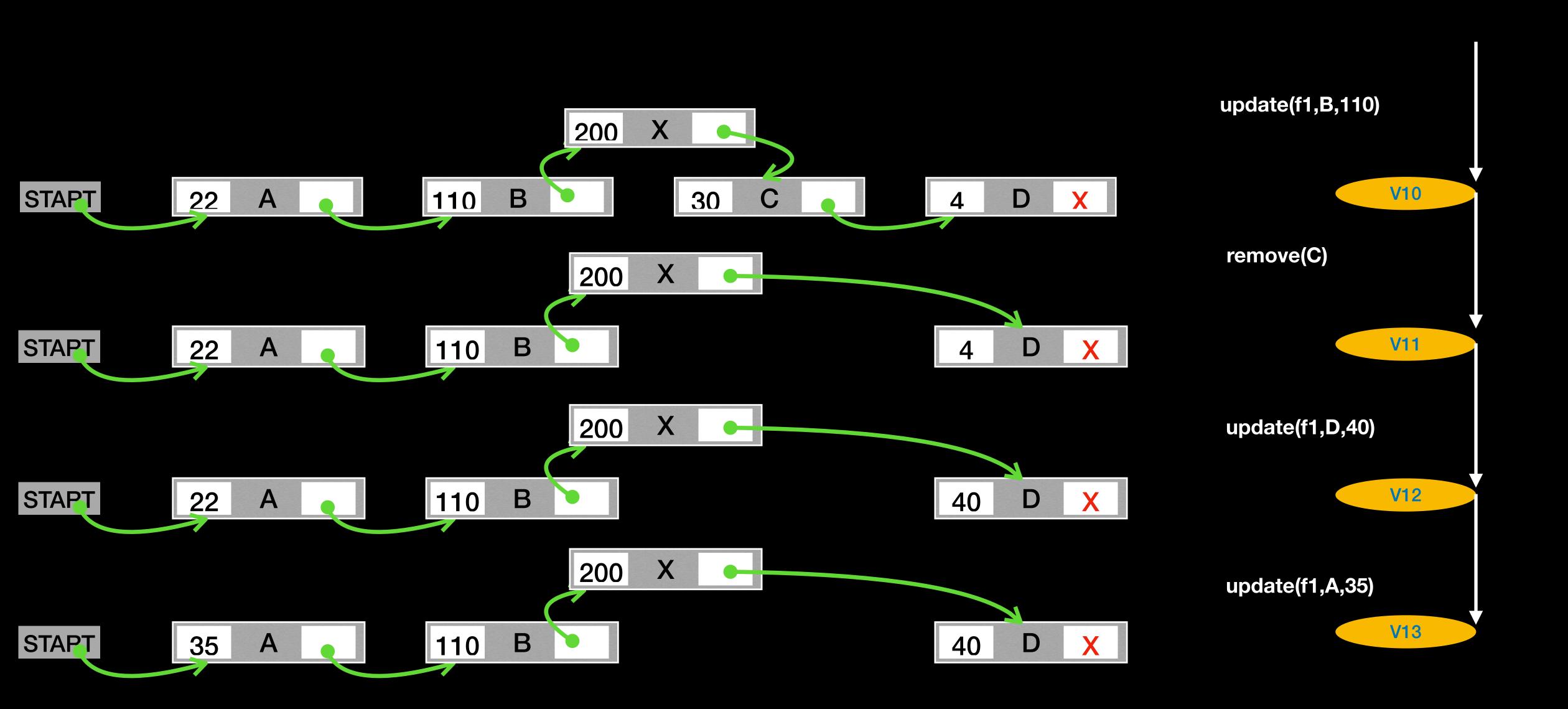
DEFAULT VERSION



Ephemeral List and Corresponding Versions



Ephemeral List and Corresponding Versions (contd.)



IMPLEMENTATION IN PERSISTENT POINTER MACHINE MODEL



BACK POINTER

х А

MODIFICATION LOGS

V1

DEFAULT FIELDS START MODULE

add(A,START,1)

Ver	block
1	А

START MODULE

add(B,A,2)



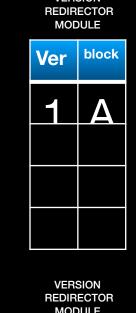
Ver	block
1	А

Ver	block			
2	В			

	V1				
		BA ⁽ POIN			
	1	POIN			
	FAULT ELDS	×	(Α	MODIFICATION LOGS
	В				
L	В				
	1/2			1	
	V2	BA	CK		
Г	2	POIN	TE/k		
	FAULT			В	MODIFICATION
FI	ELDS				LOGS
	X				

START MODULE

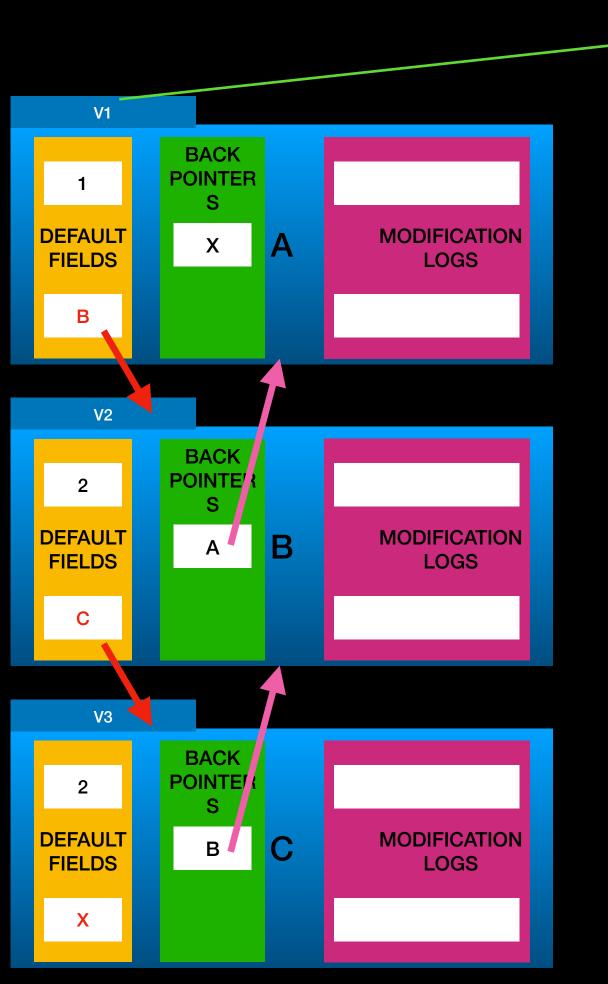
add(C,B,3)

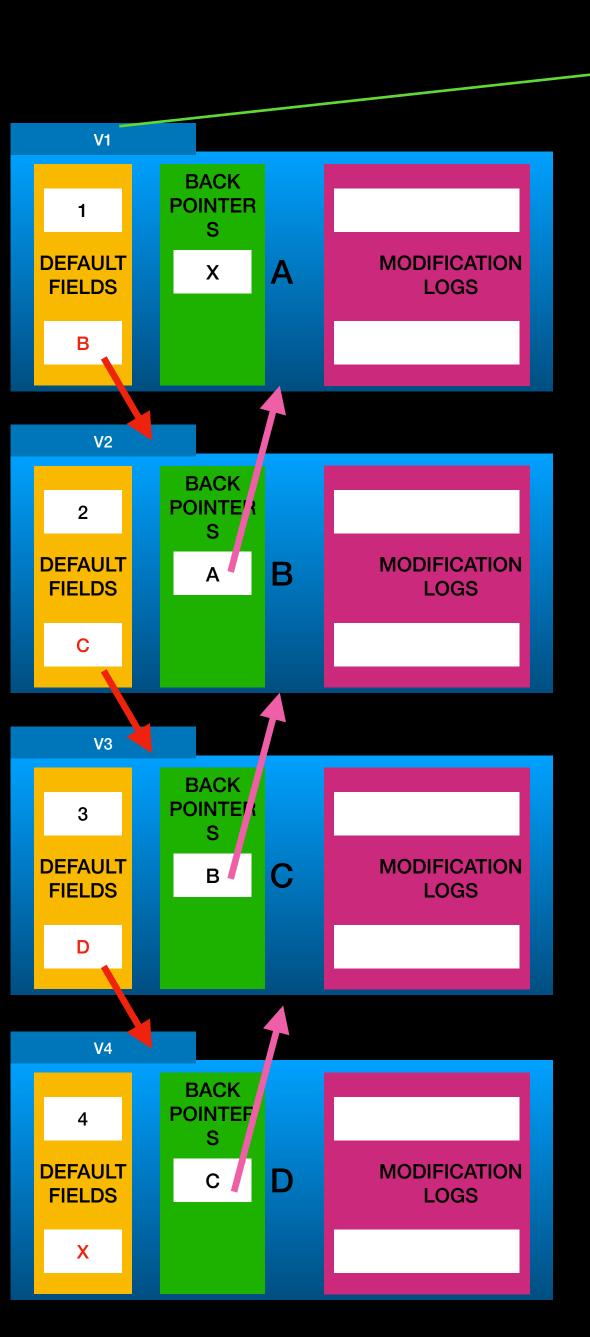




VERSION	
REDIRECTOR	
MODULE	

Ver	block
3	C





redirector Module

Ver block

1 A

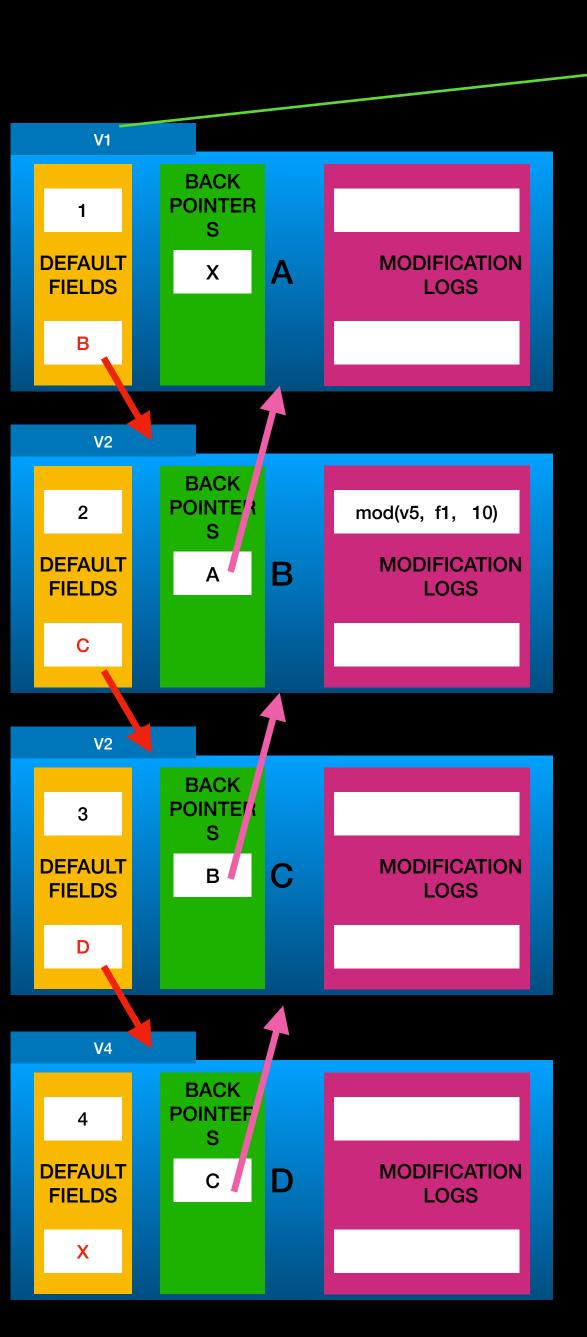
VERSION REDIRECTOR MODULE

MODULE				
Ver	block			
2	R			

VERSION REDIRECTOR MODULE

Ver	block
3	C

Ver	block



REDIRECTOR MODULE		
Ver	block	
	Α	

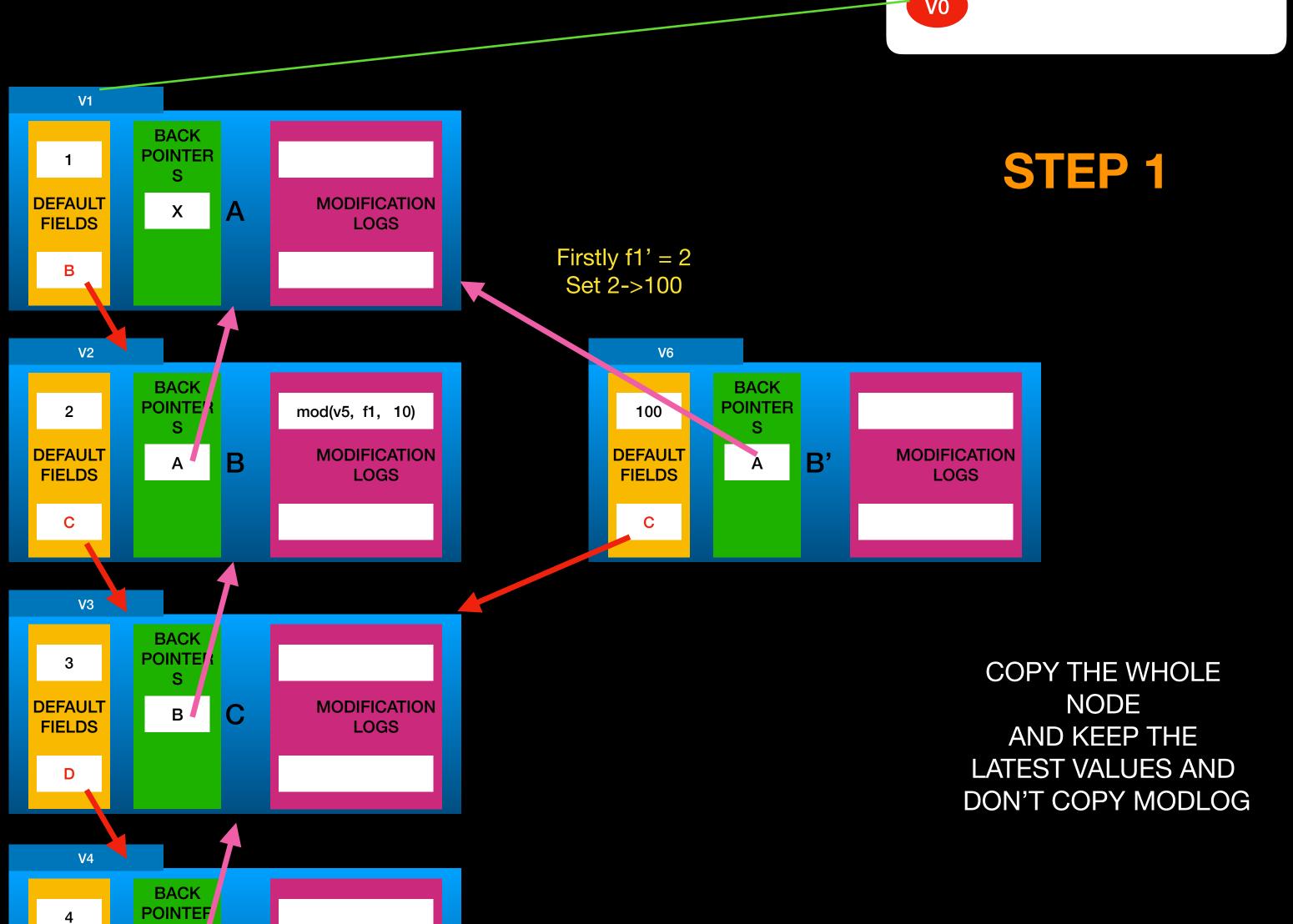
VERSION REDIRECTOR MODULE

Ver	block
2	R



Ver	block
3	C

Ver	block
4	D



DEFAULT

FIELDS

c D

MODIFICATION

LOGS

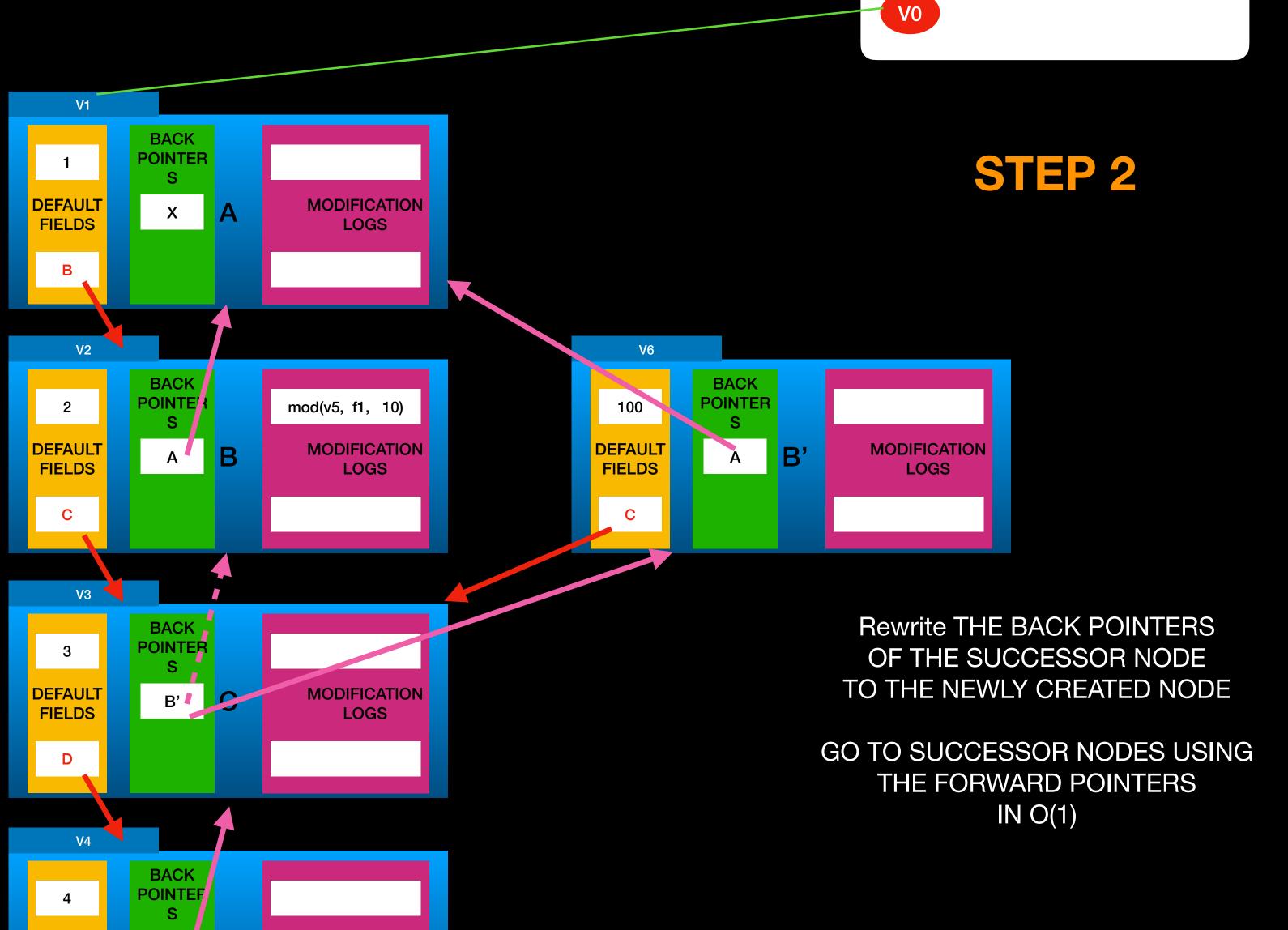
MODULE	
Ver	block
1	А

Ver	block
2	В
6	B'

Ver	block
3	С

Ver	block
4	D

MODULE	
er	block
4	D



DEFAULT

FIELDS

c D

MODIFICATION

LOGS

REDIRECTOR MODULE

Ver	block
1	А

VERSION REDIRECTOR MODULE

2 6	B B'

VERSION REDIRECTOR MODULE

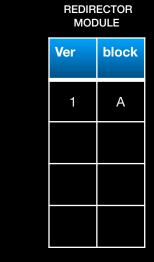
Ver	block
3	С

Ver	block
4	D

GO TO ANCESTOR NODES RECURSIVELY

AND DO

update(f2,cur_node,NEW_NODE)



VERSION REDIRECTOR MODULE

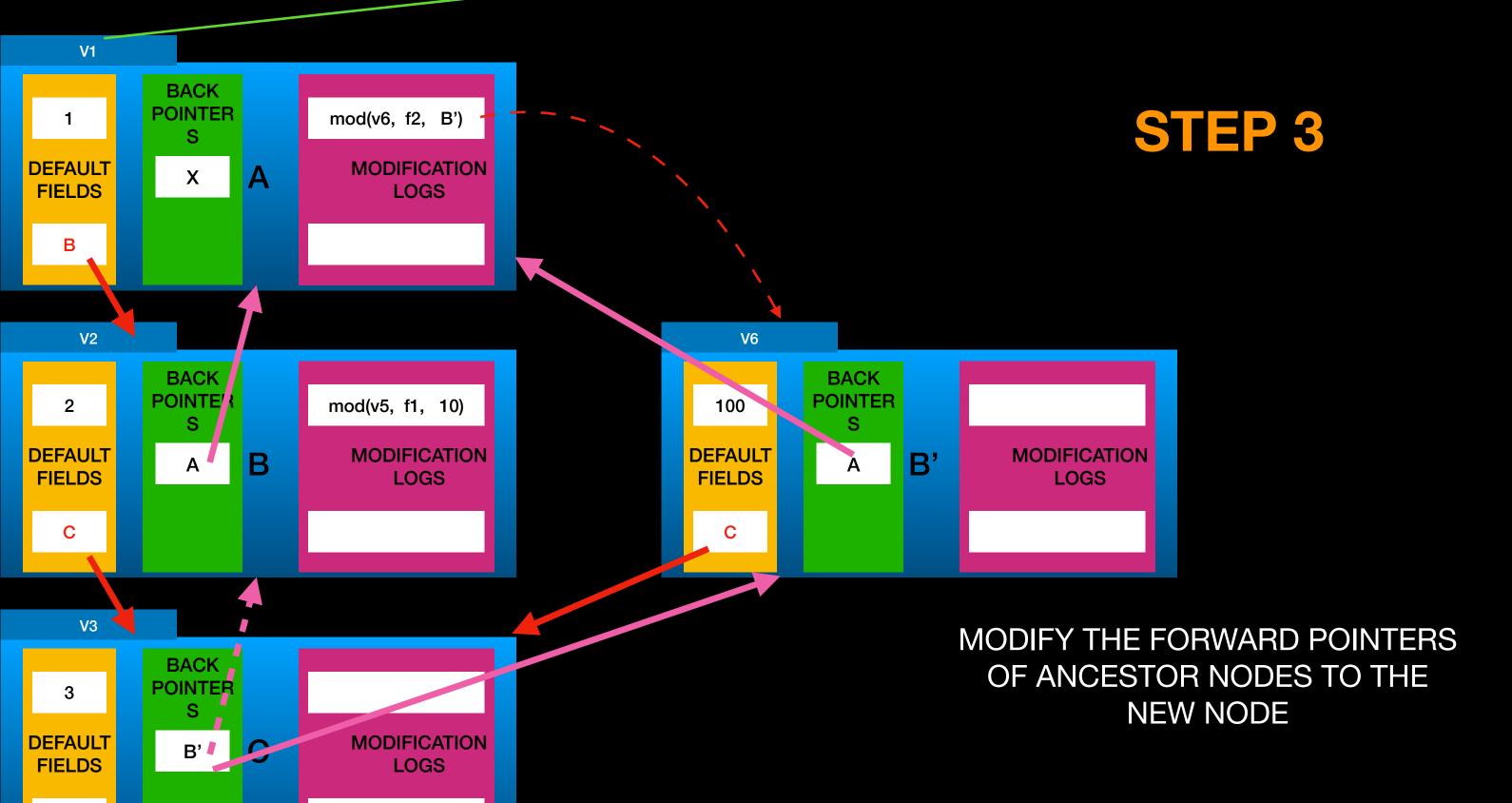
Ver	block
2	В
6	B'

VERSION REDIRECTOR MODULE

Ver	block	
3	С	

VERSION REDIRECTOR MODULE

4	D



POINTER

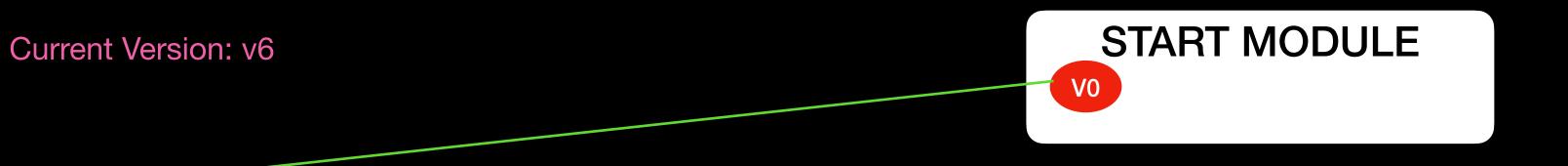
c D

MODIFICATION

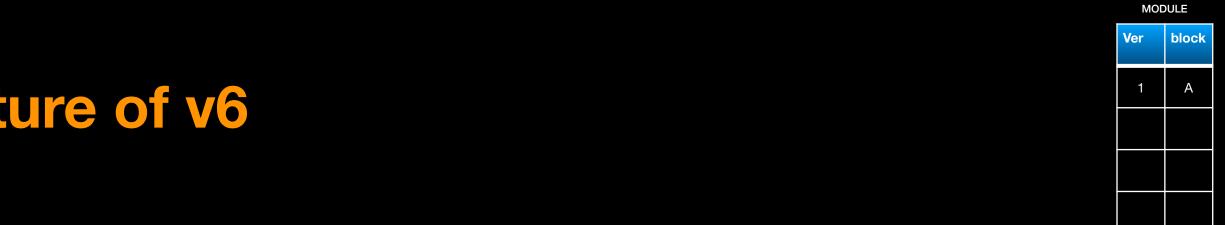
LOGS

DEFAULT

FIELDS



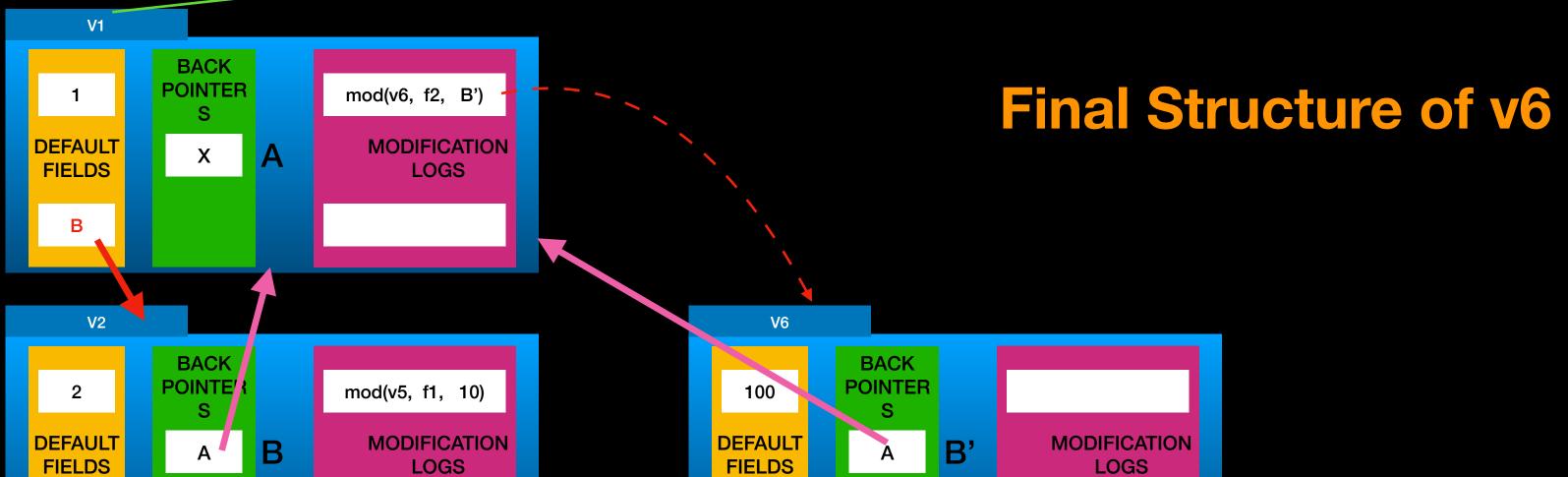
LOGS



Ver	block
2	В
6	B'

Ver	block
3	С

Ver	block	
4	D	



LOGS

MODIFICATION

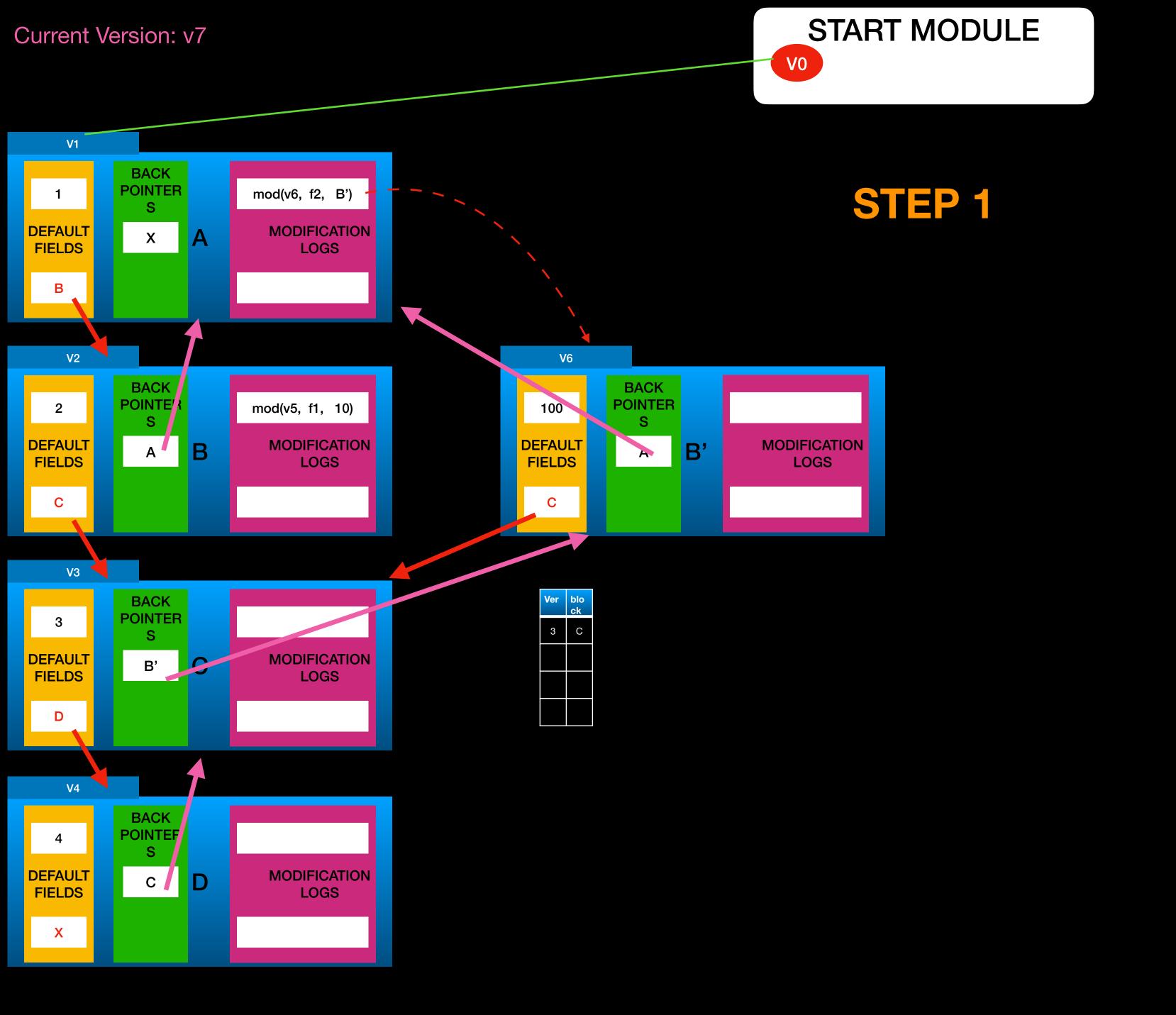
LOGS

					4	
	V 4					
				ACK		
	4		PO	INTER S		
	DEFAULT FIELDS			С	D	MODIFICATION LOGS
	Х					

BACK POINTER

DEFAULT

FIELDS



 $add(X,B,\underline{\hspace{0.1cm}})$

add(X,B,_) consists of

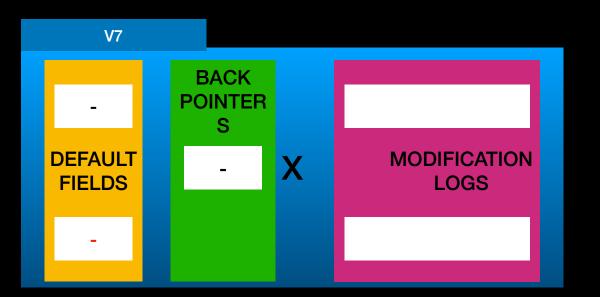
Create node X		
Modify f2 of B' to X		
Modify f2 of X to C + Set BP of X to B'		
Update BP of C to X		
Set f1 of X		

VERSION REDIRECTOR MODULE

Ver	block
1	А

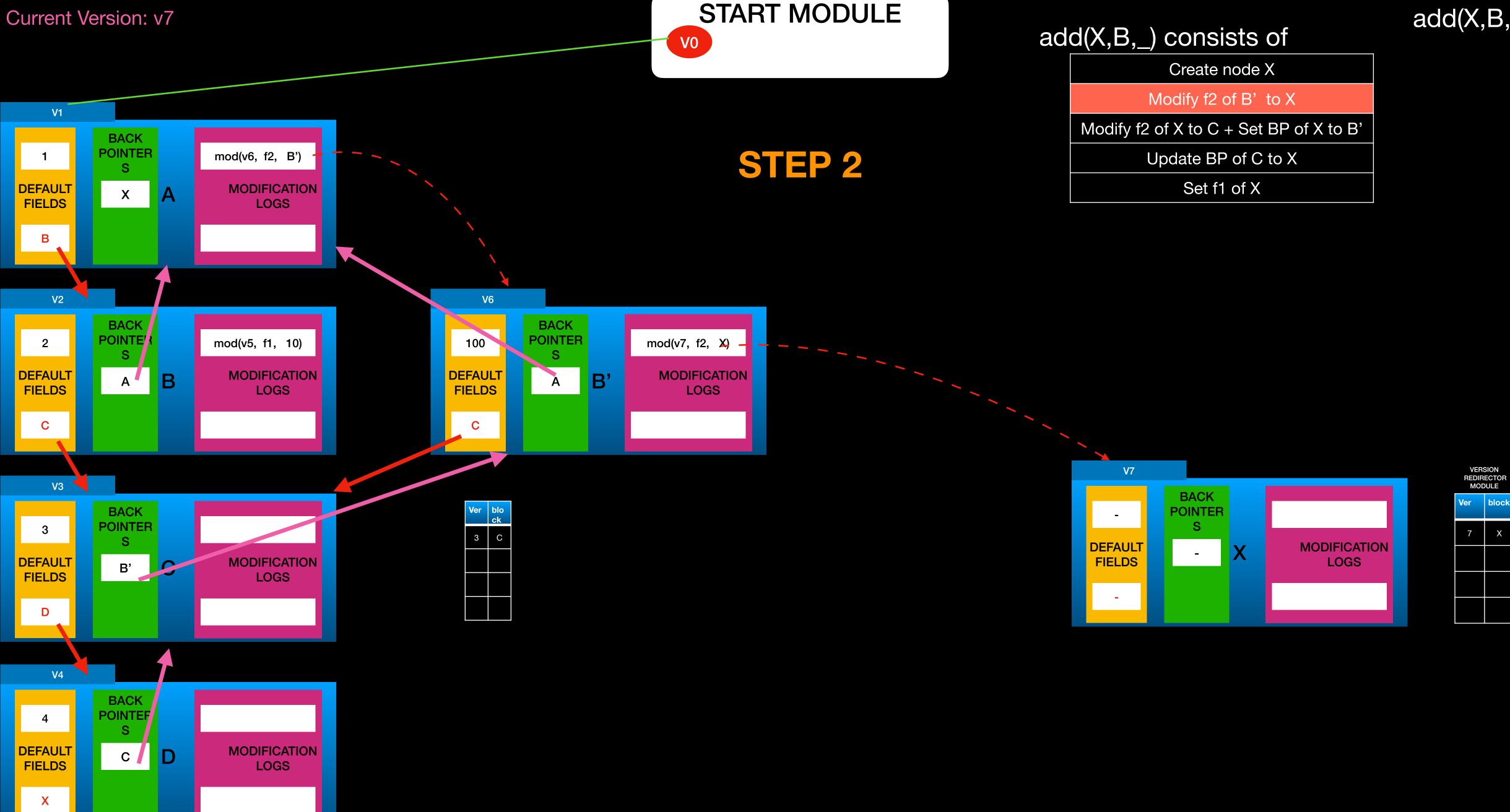
VERSION REDIRECTOR MODULE

Ver	block
2	В
6	B'



REDIRECTOR MODULE		
Ver	block	
7	Х	

Ver	block
4	D



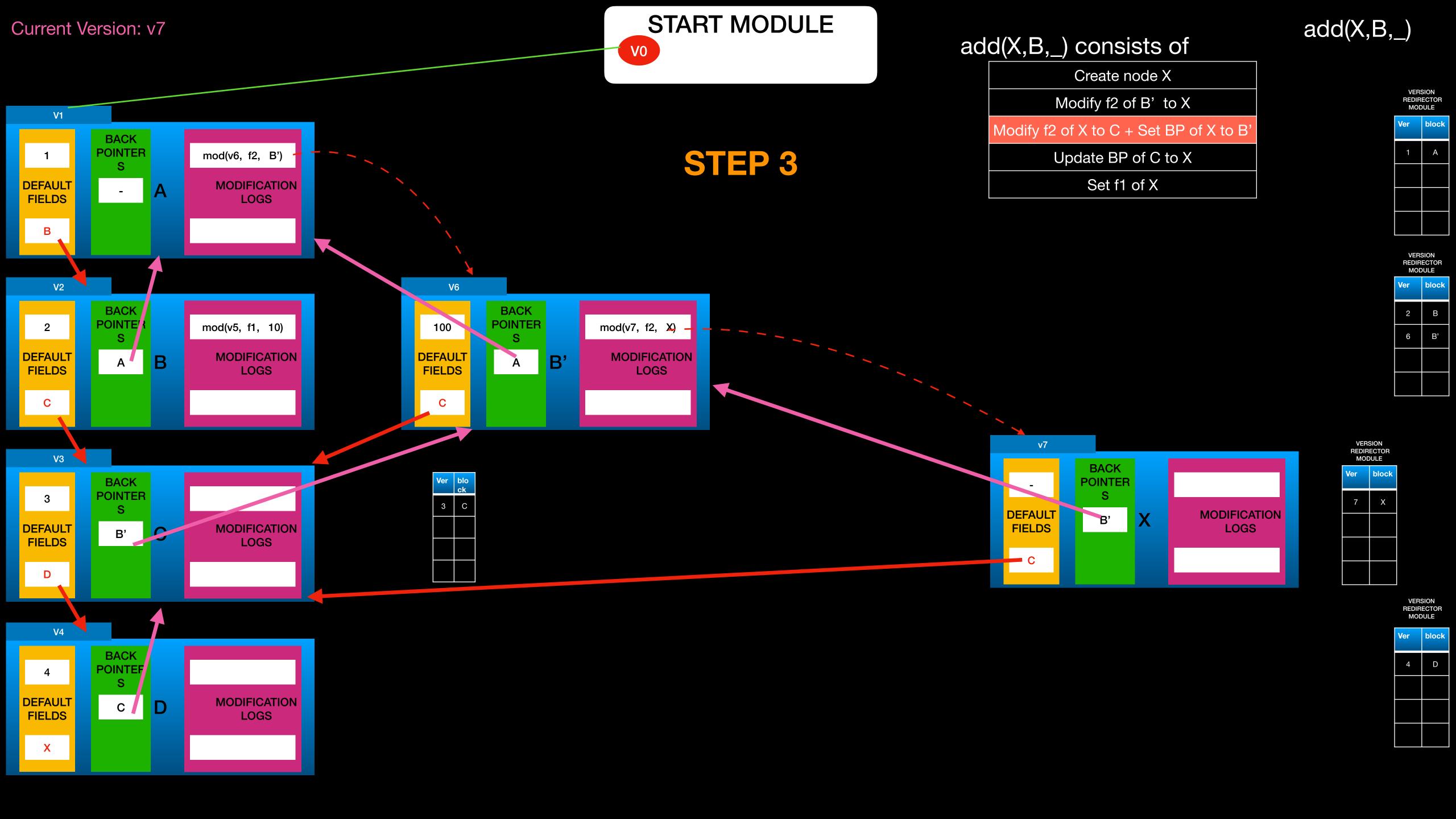
add(X,B,_)

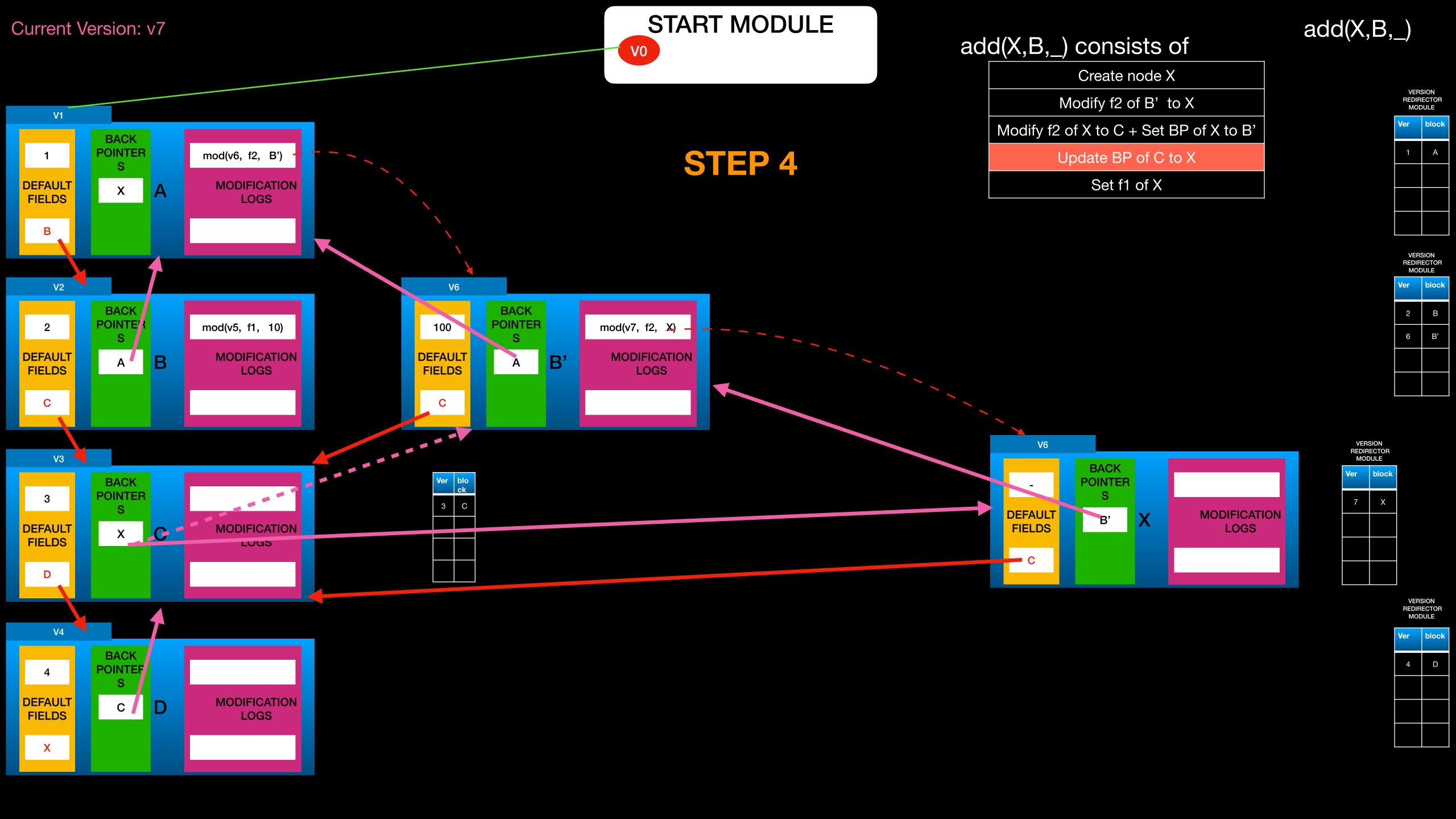
Ver	block
1	Α

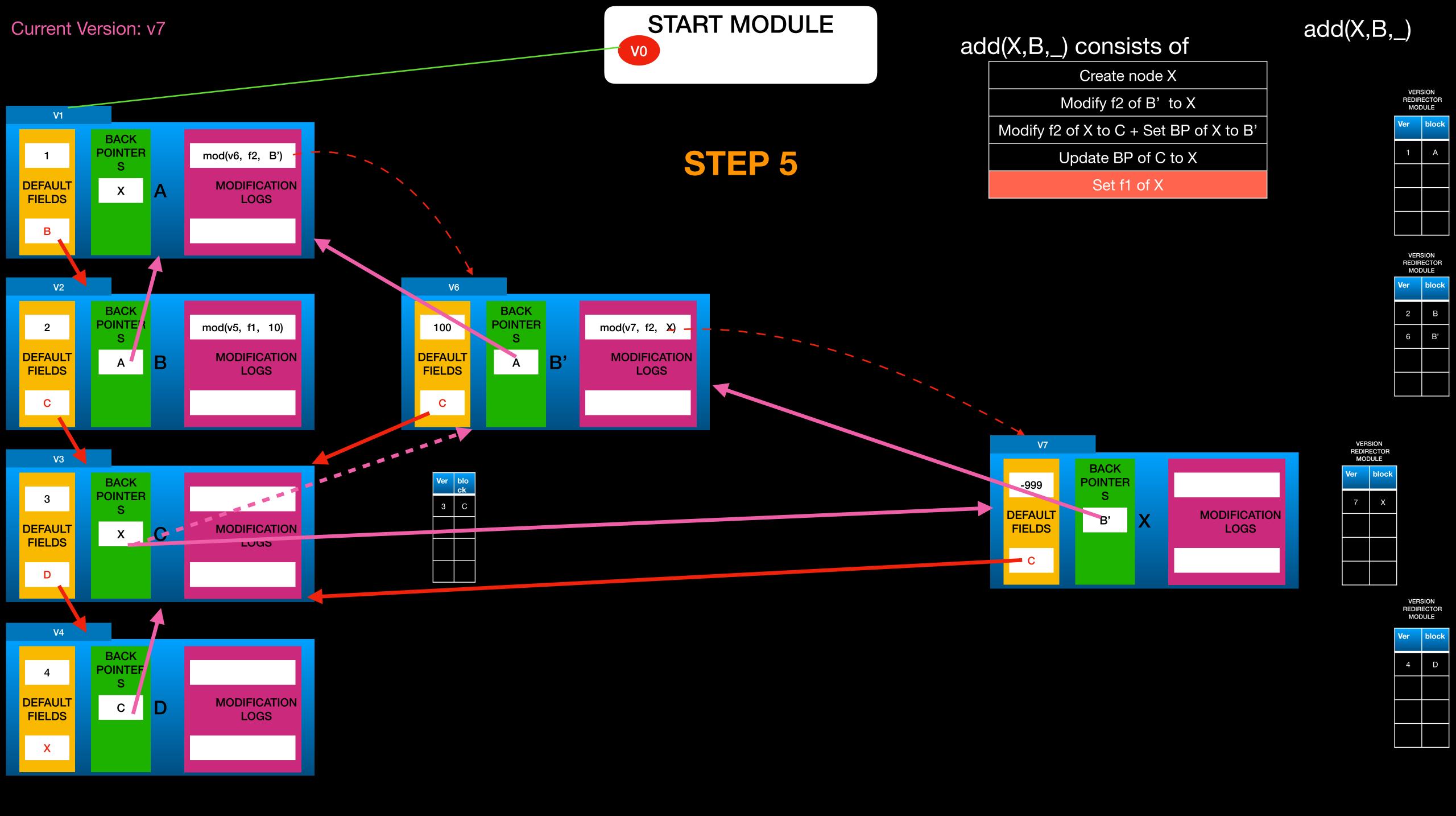
Ver	block	
2	В	
6	B'	

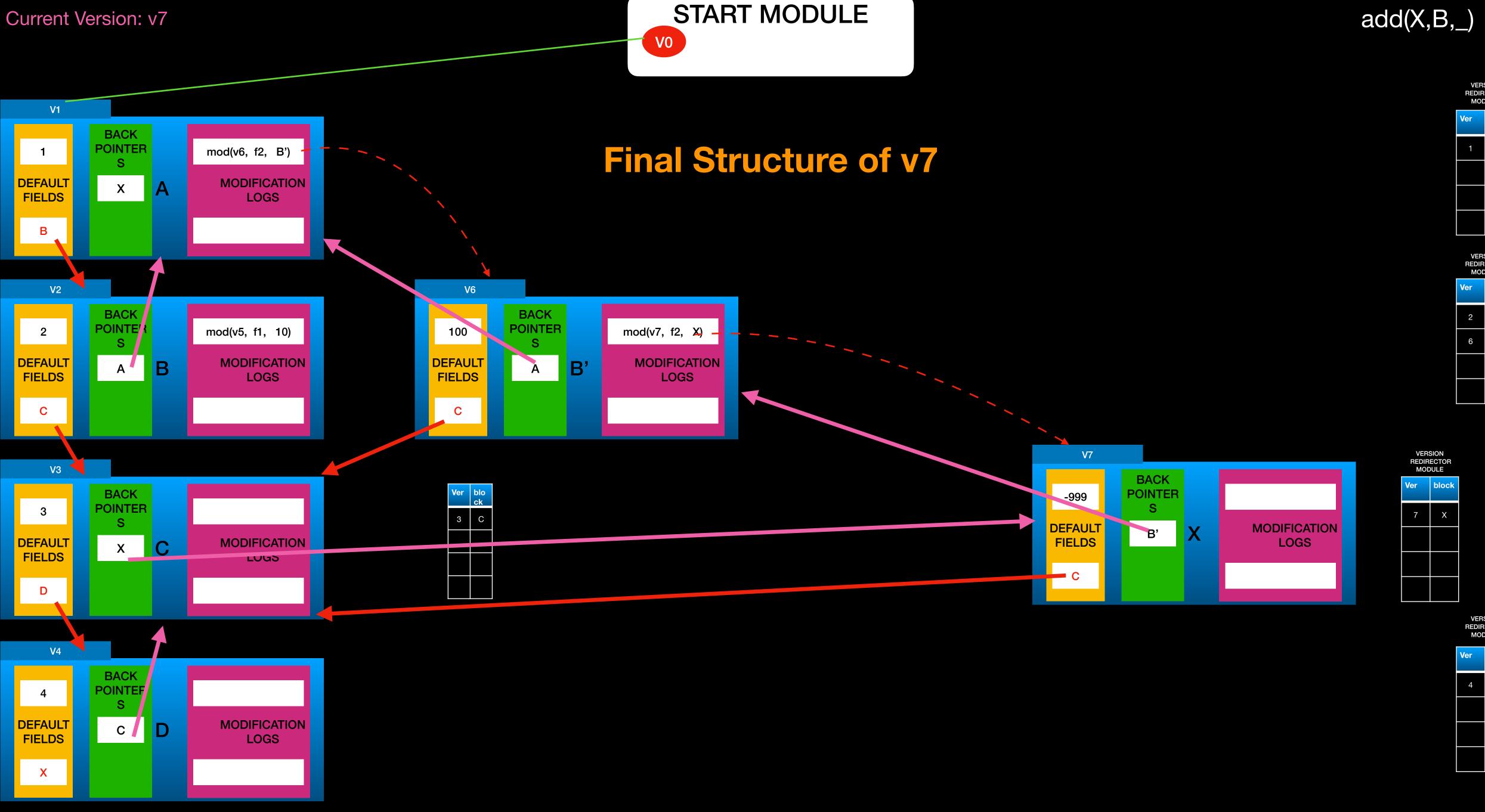
7	X

Ver	block
4	D





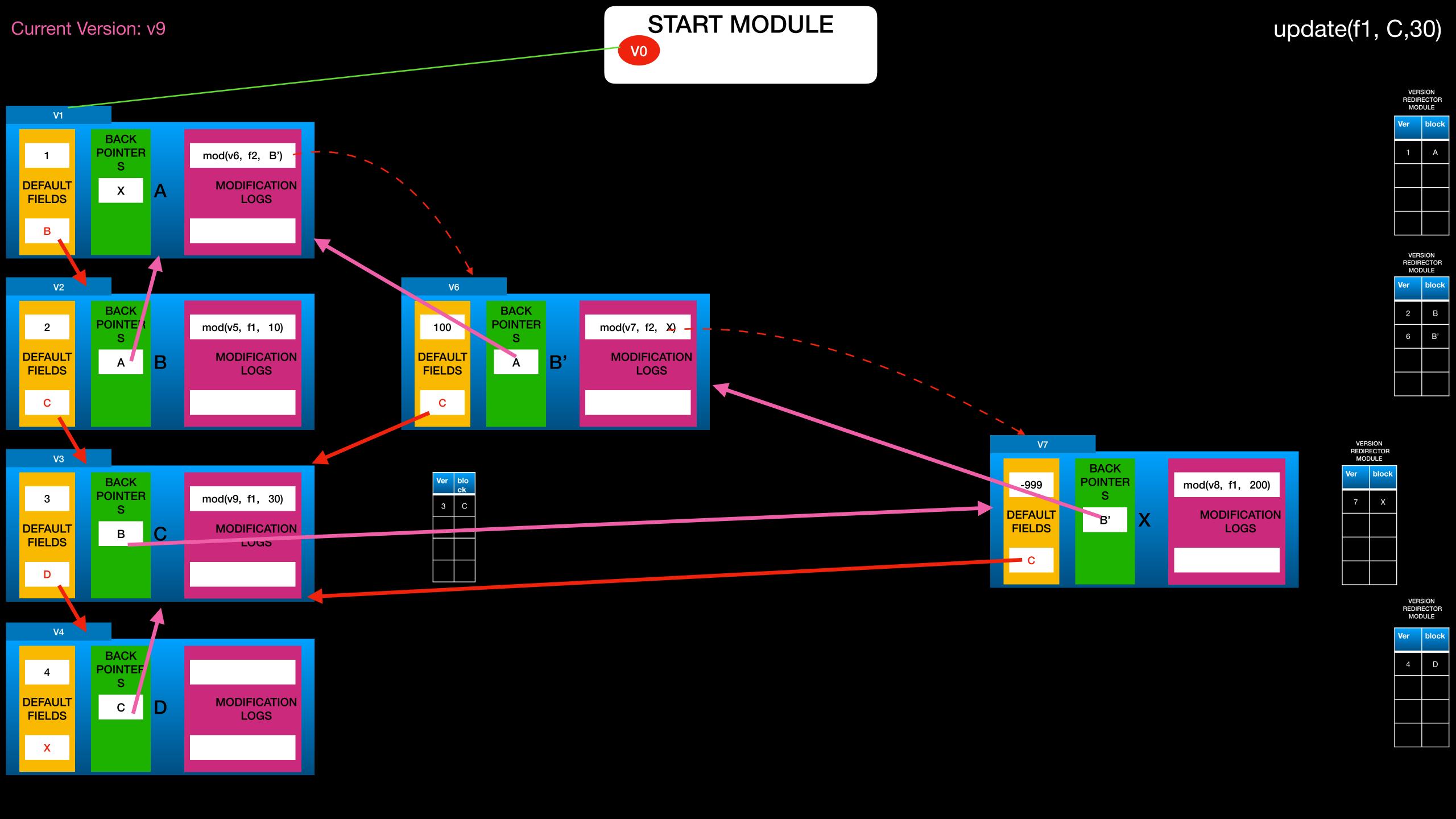




Ver	block
1	Α

Ver	block
2	В
6	B'

Ver	block
4	D



Ver	block
1	А

VERSION REDIRECTOR MODULE

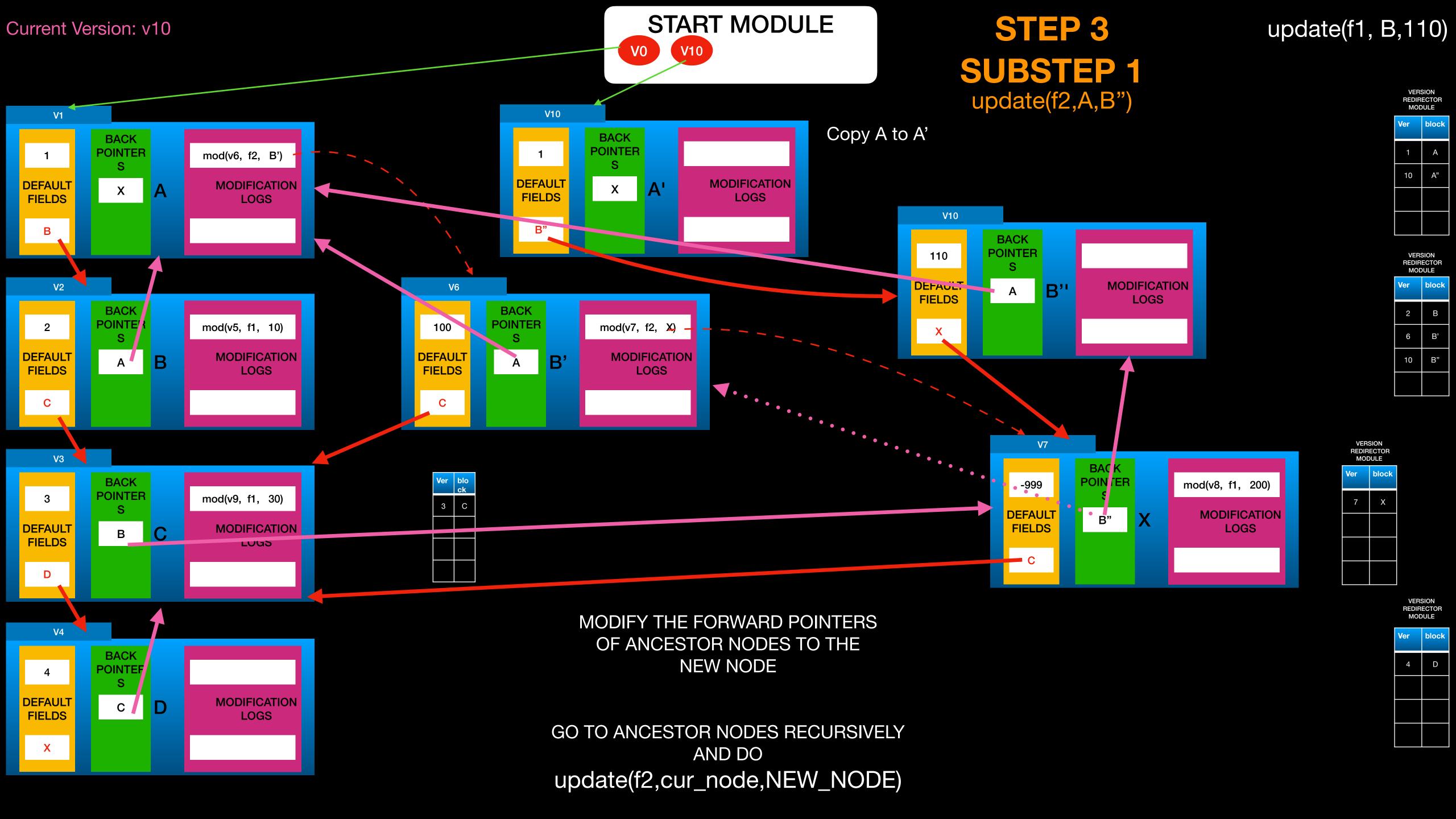
Ver	block
2	В
6	B'
10	В"

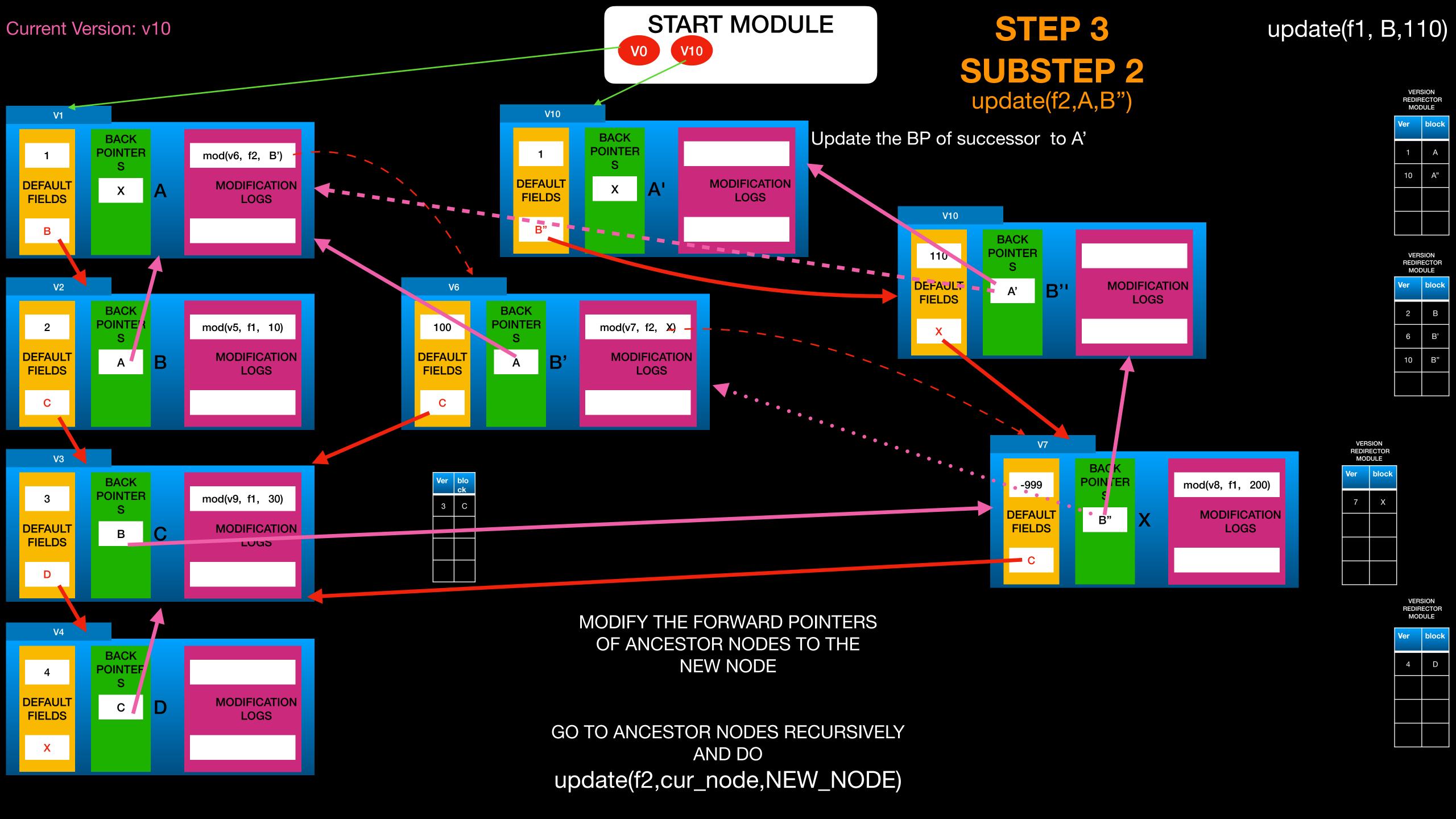
VERSION REDIRECTOR

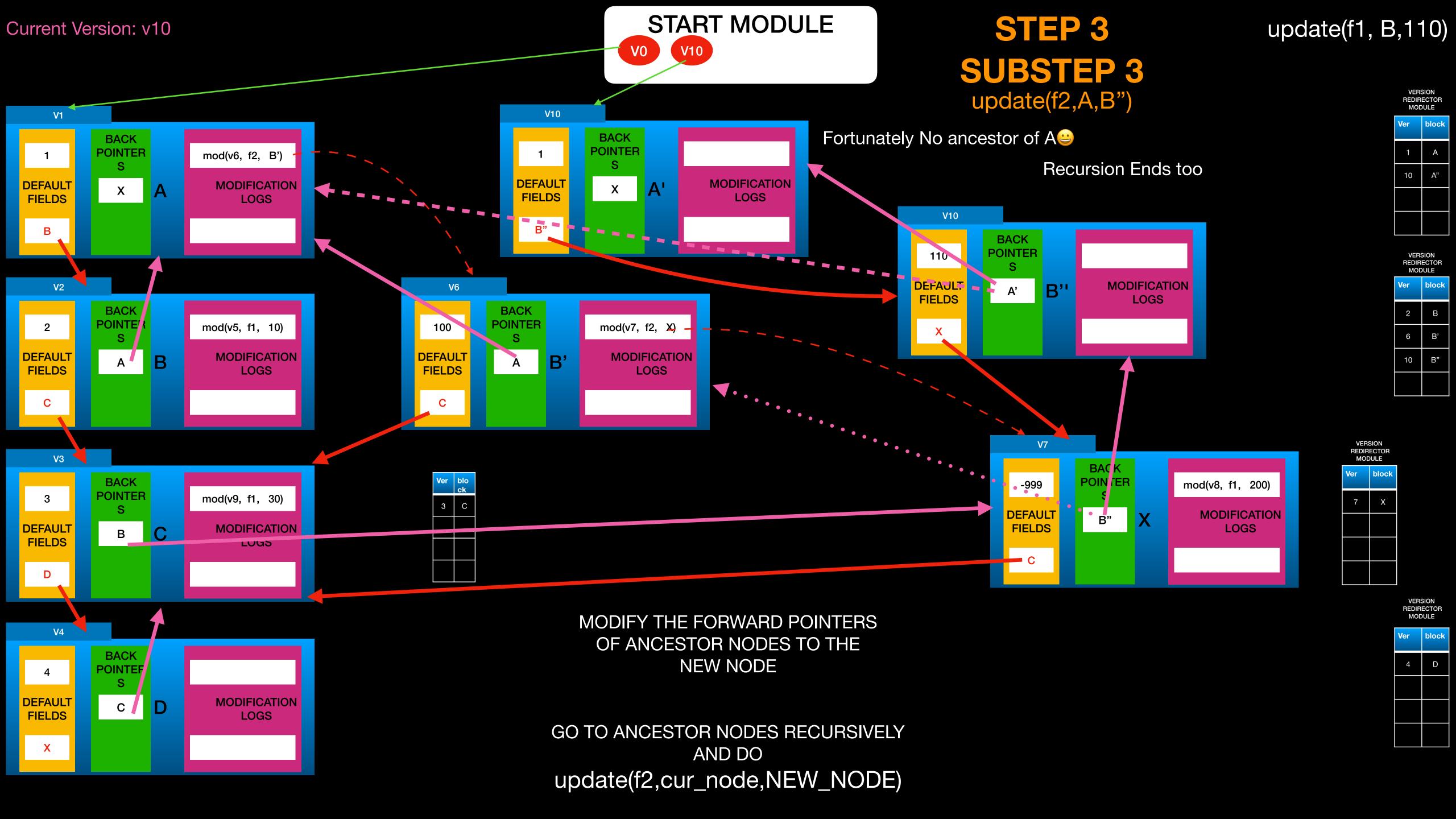
Ver	block	
4	D	

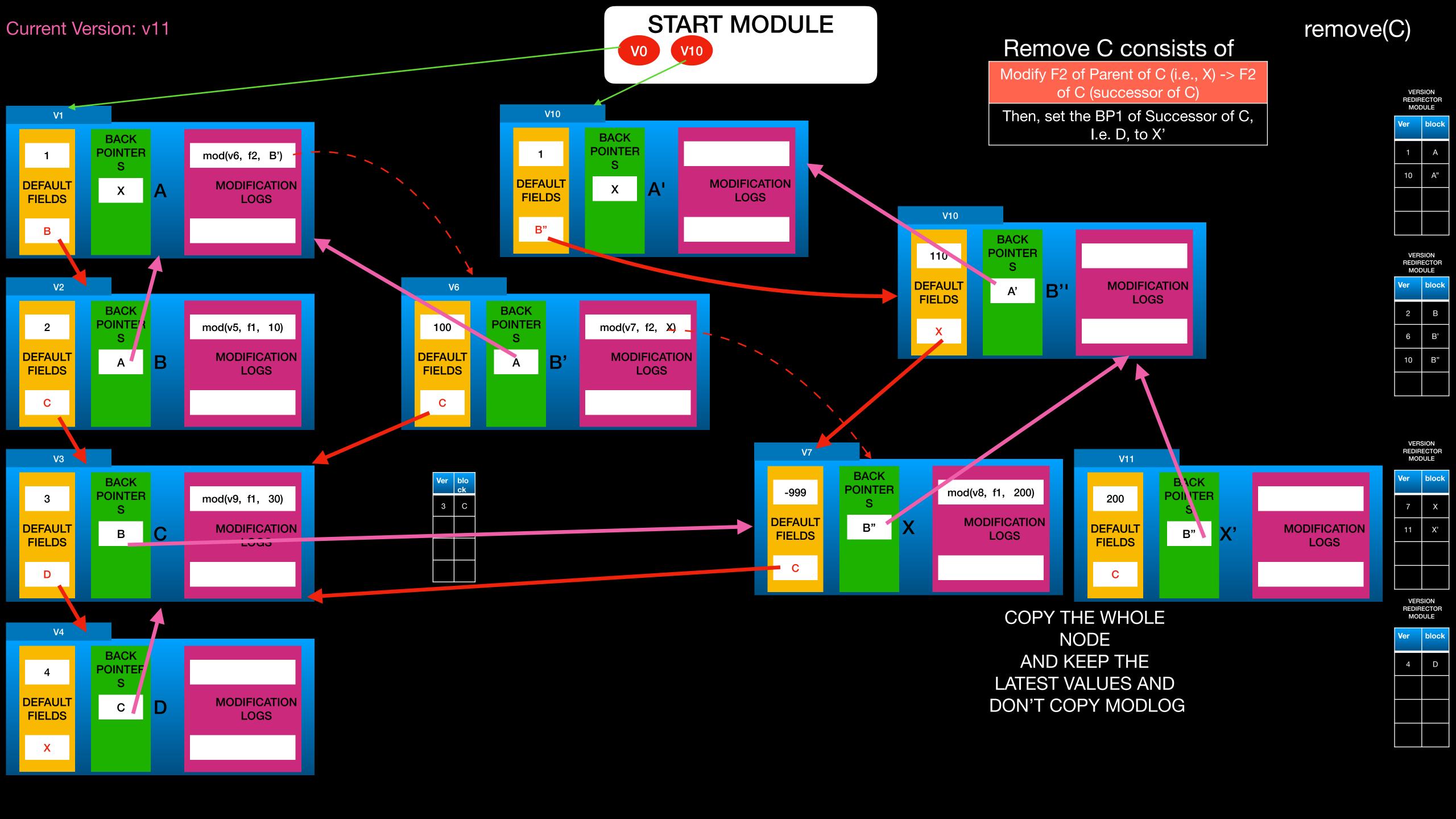
В

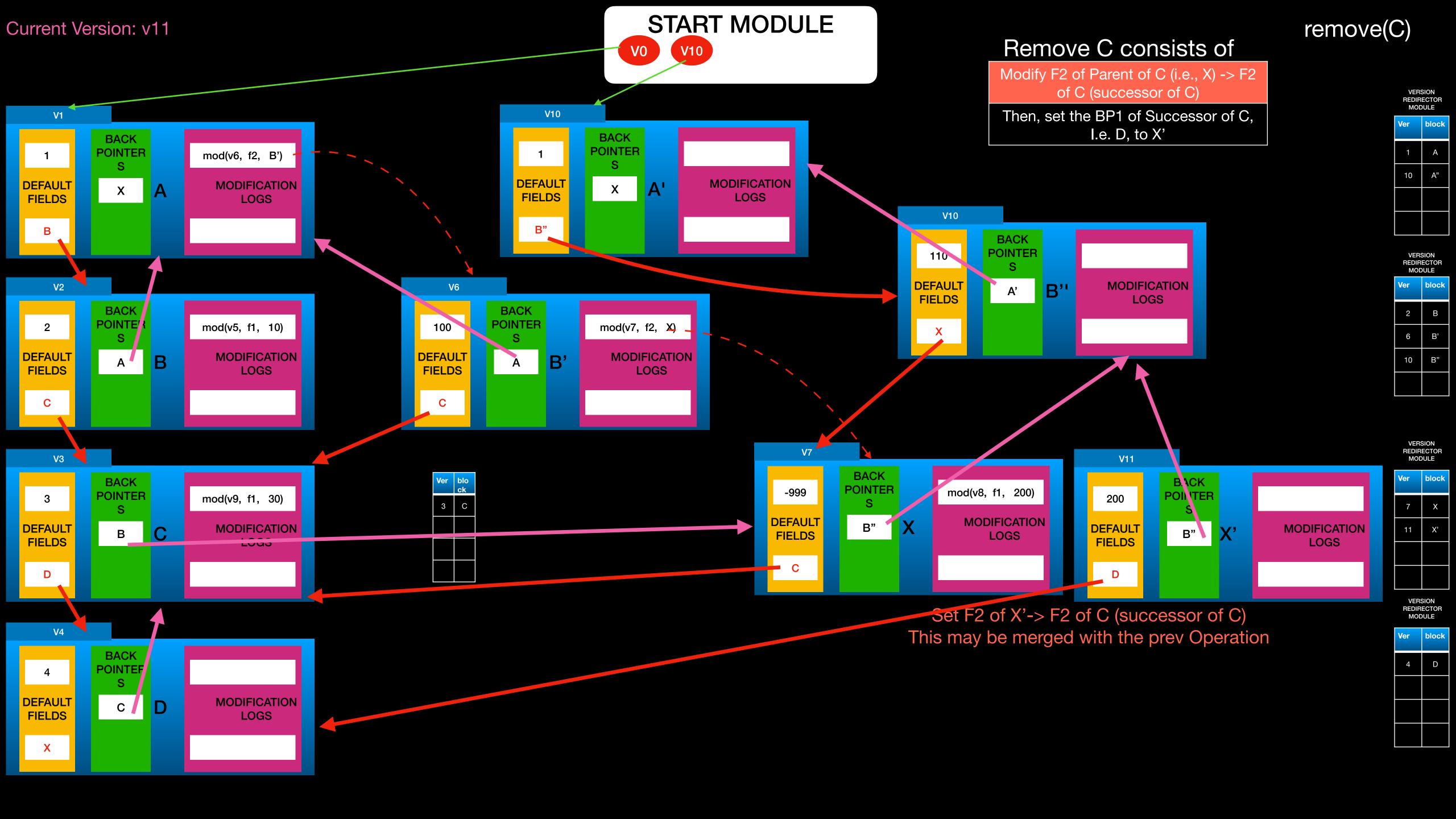
B'

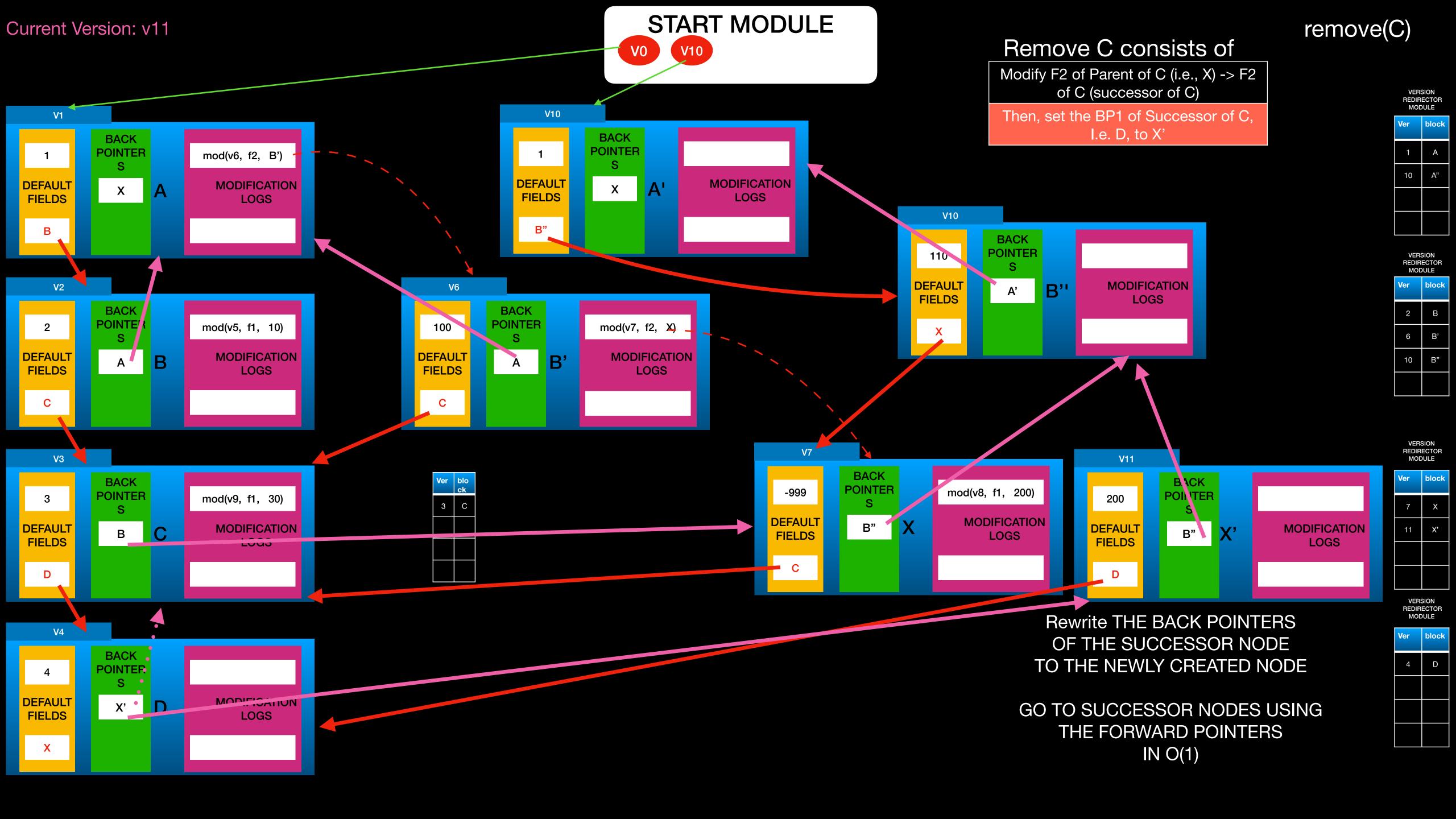


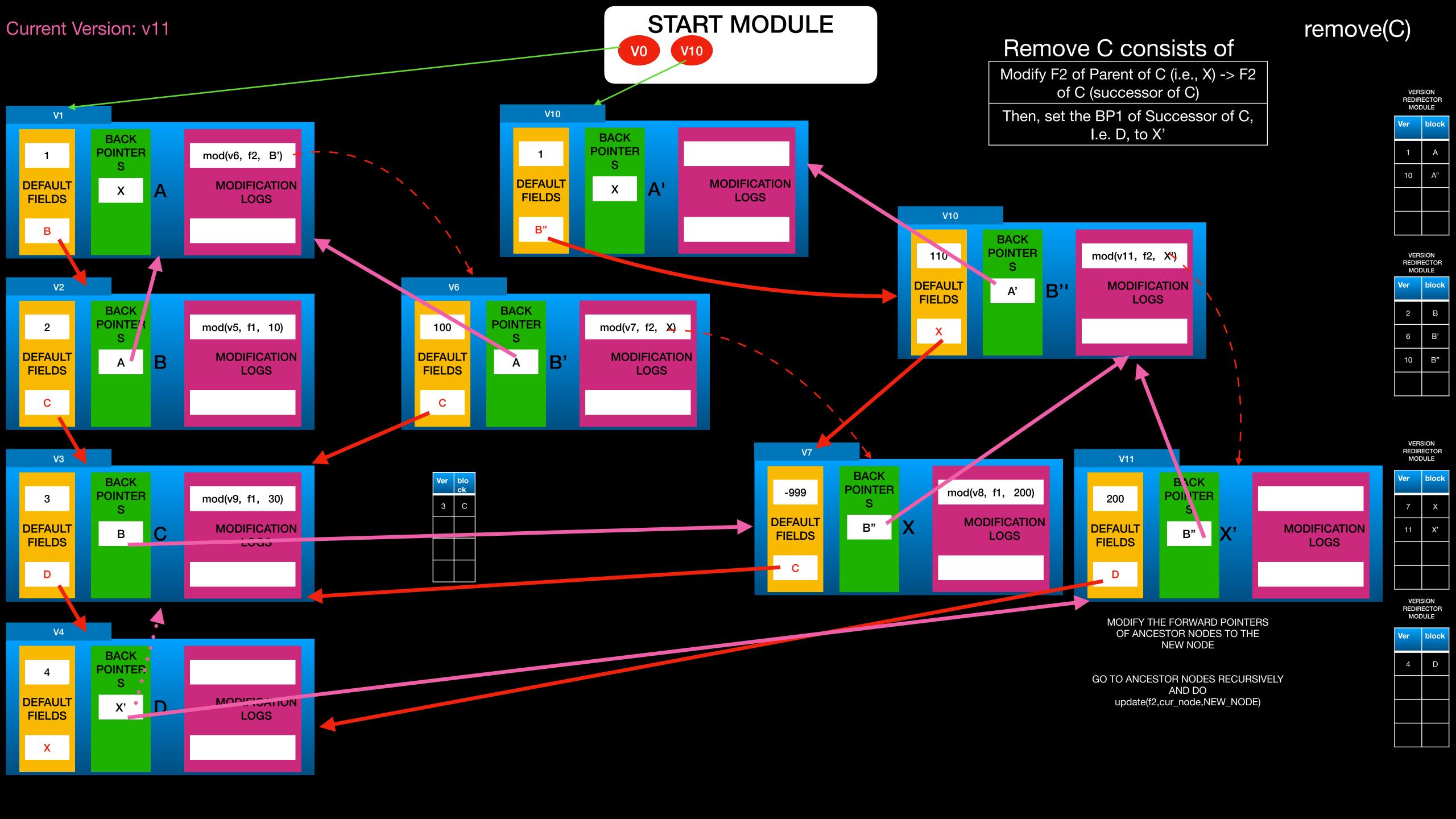


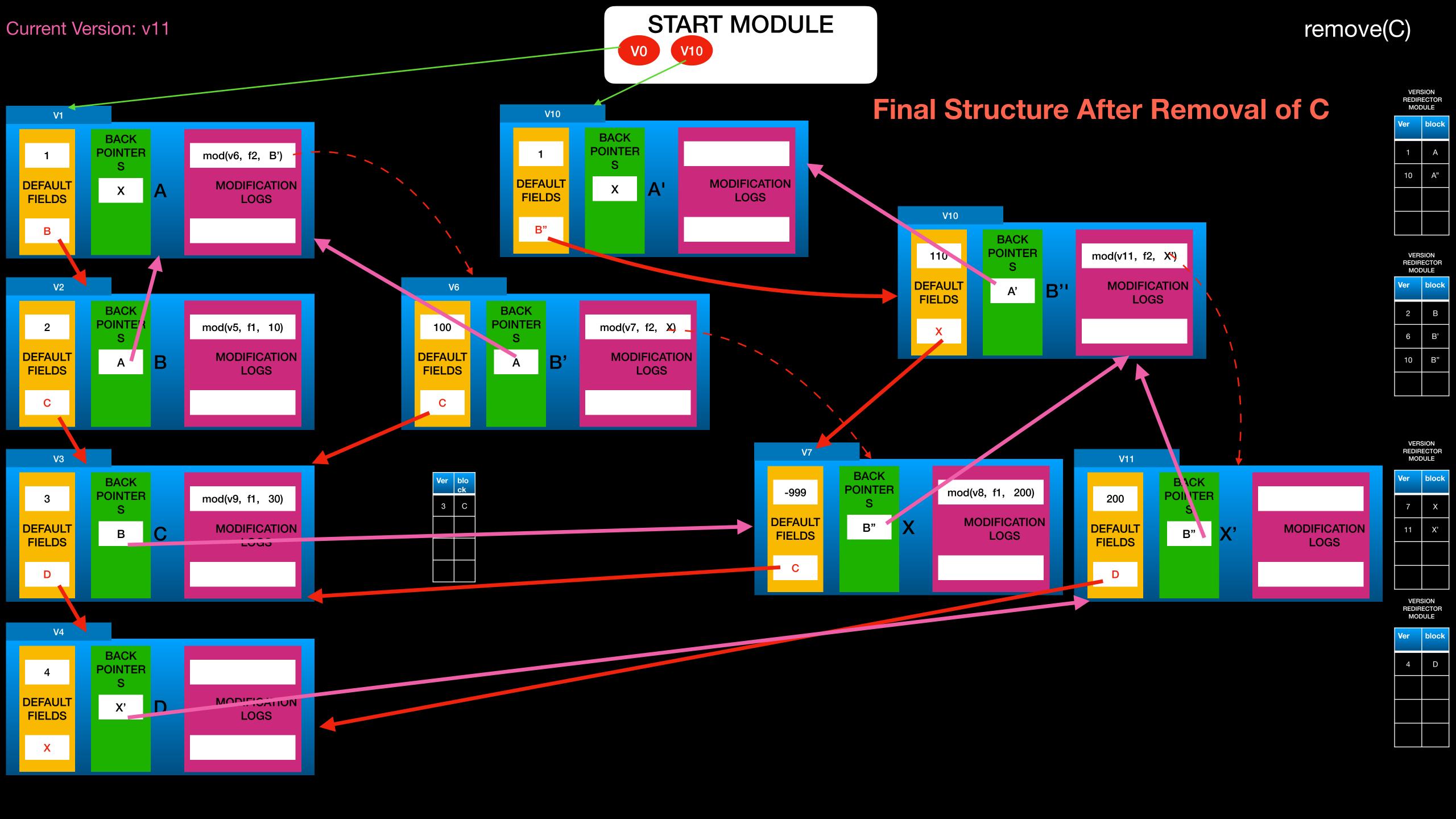


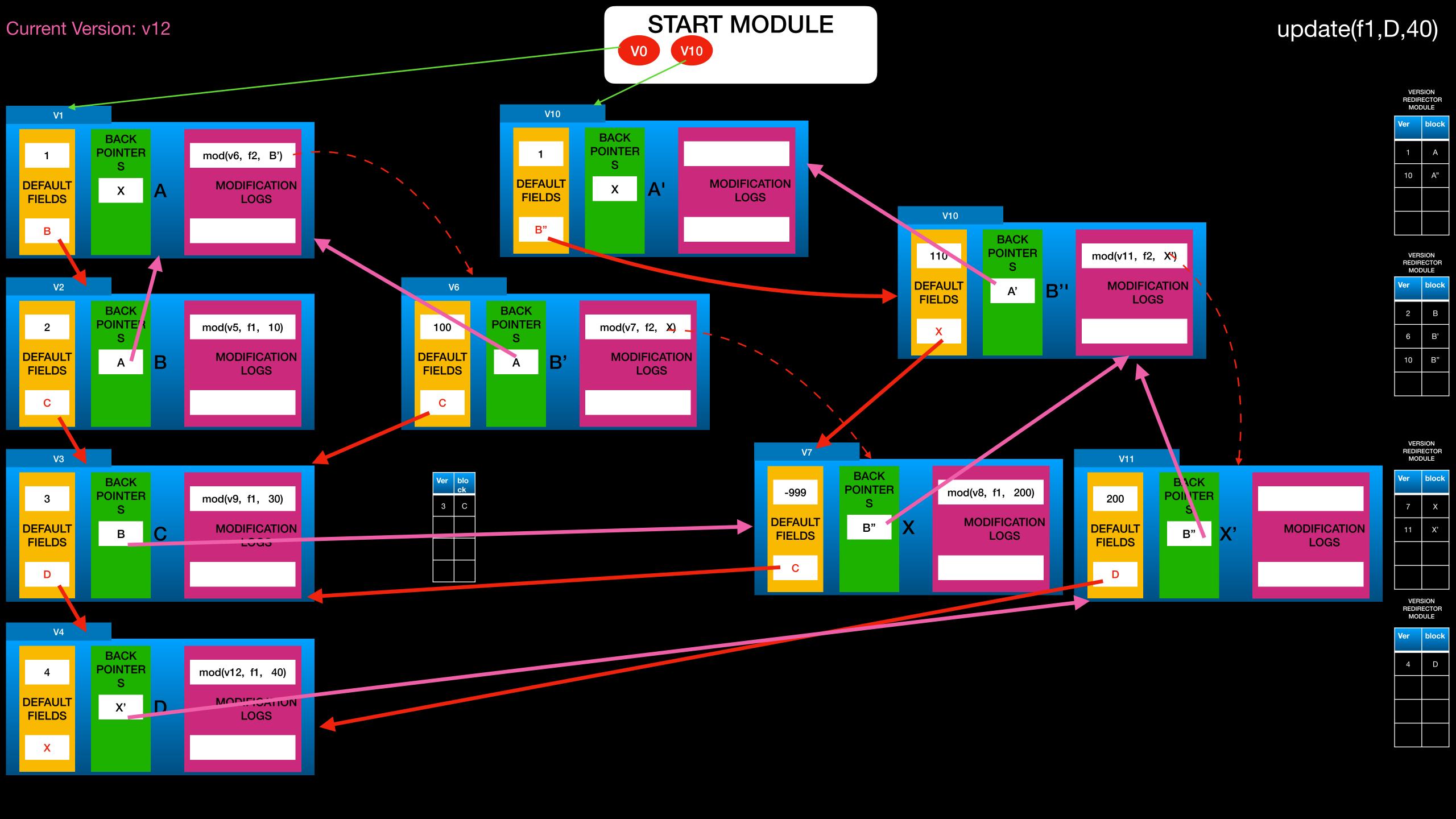


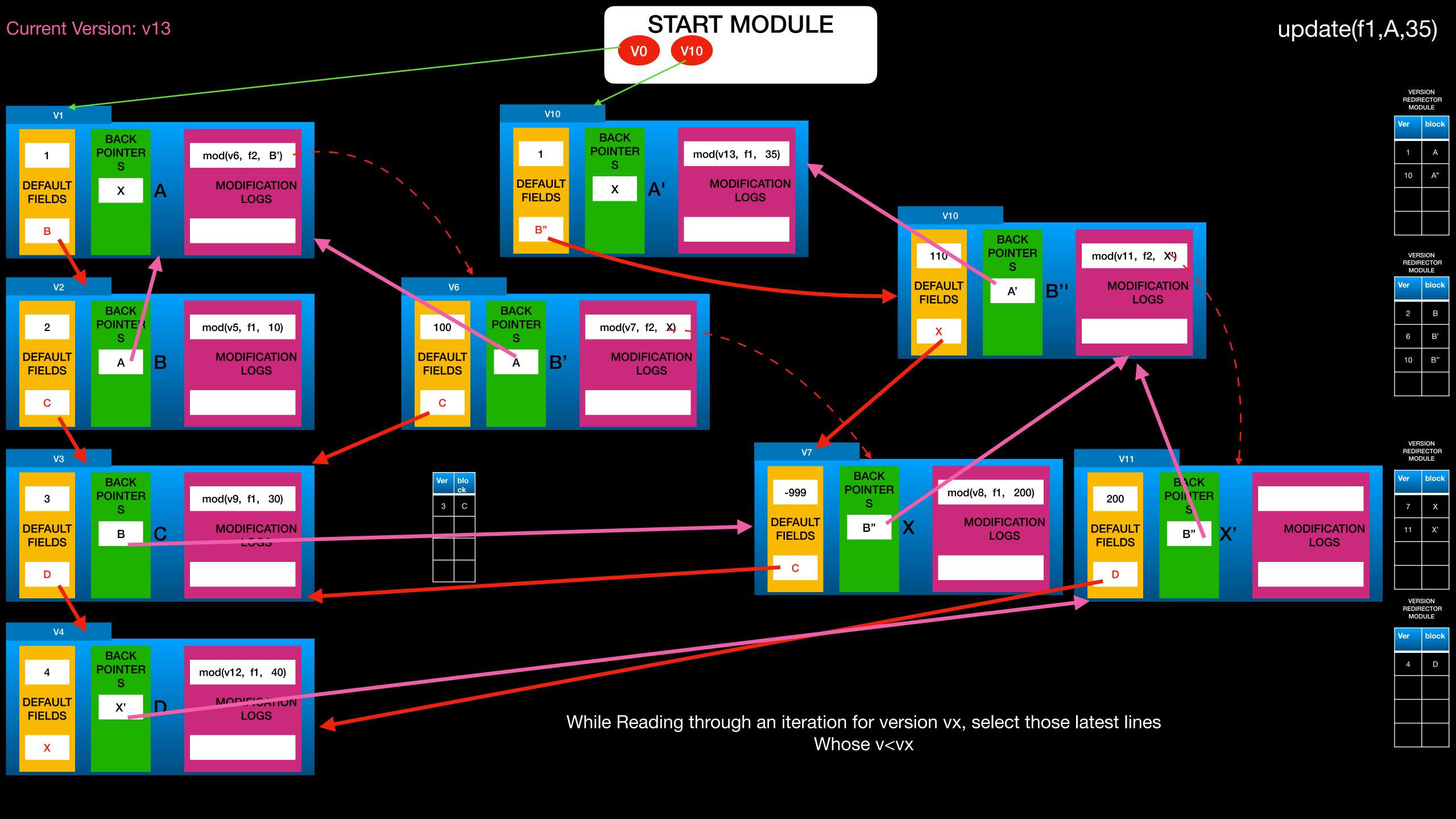








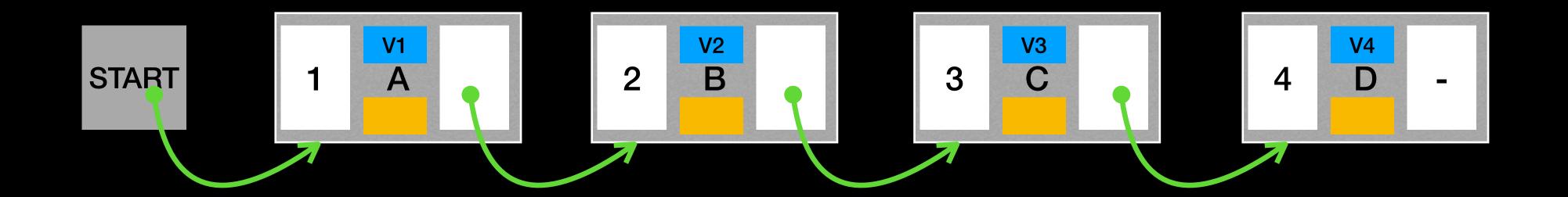


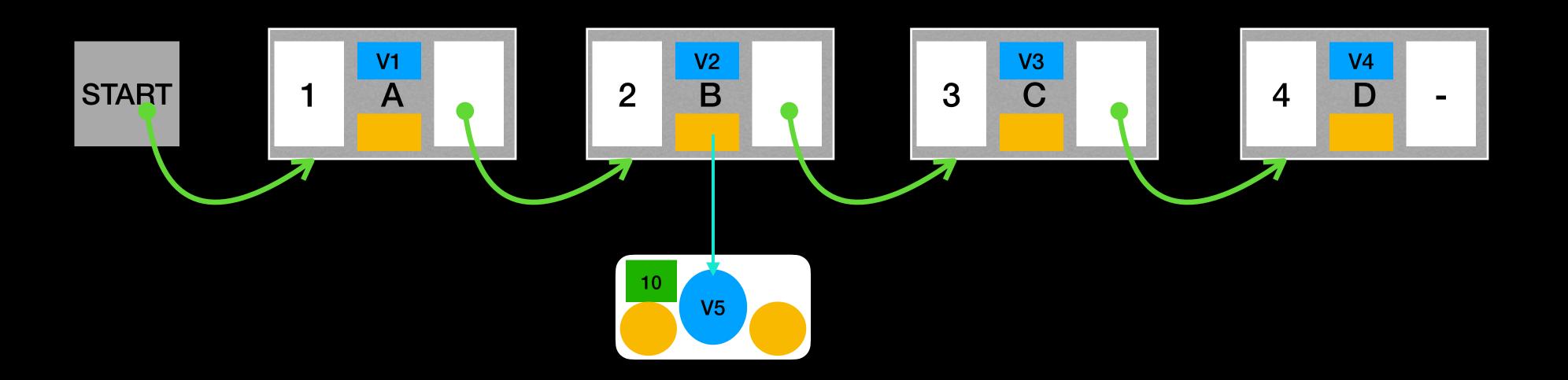


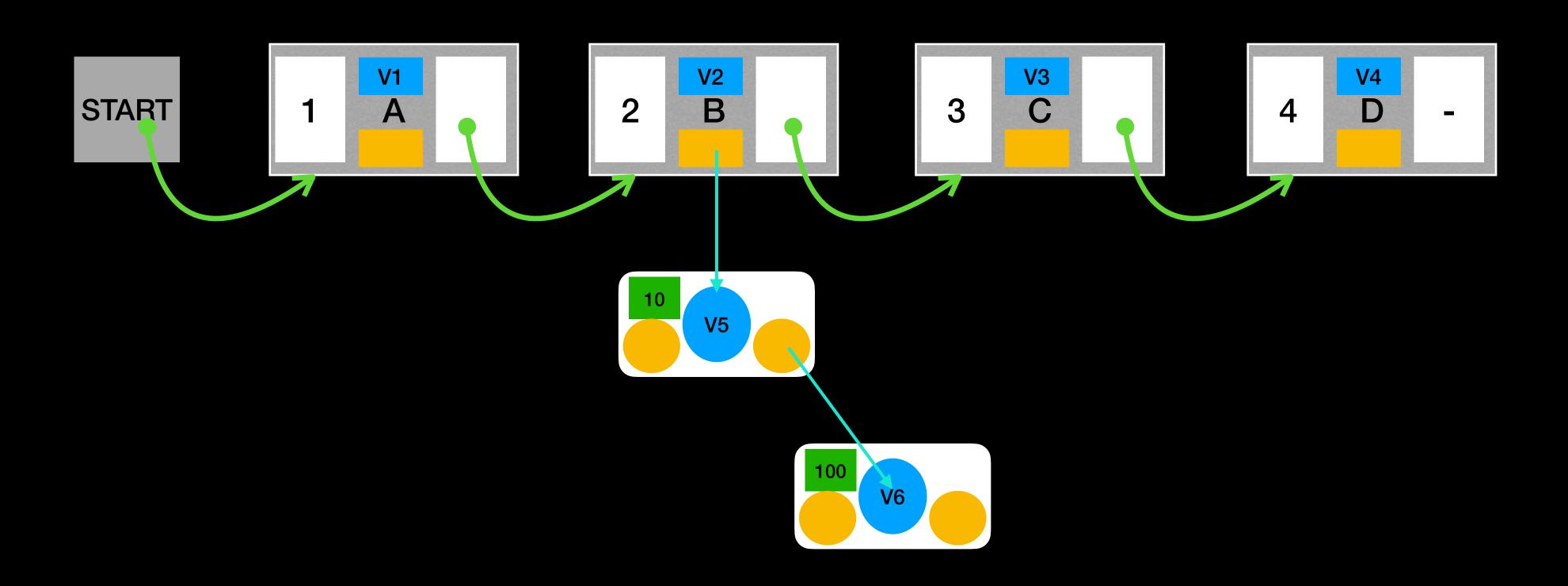
iterate LL_at_v(vx) To print the list at v_x

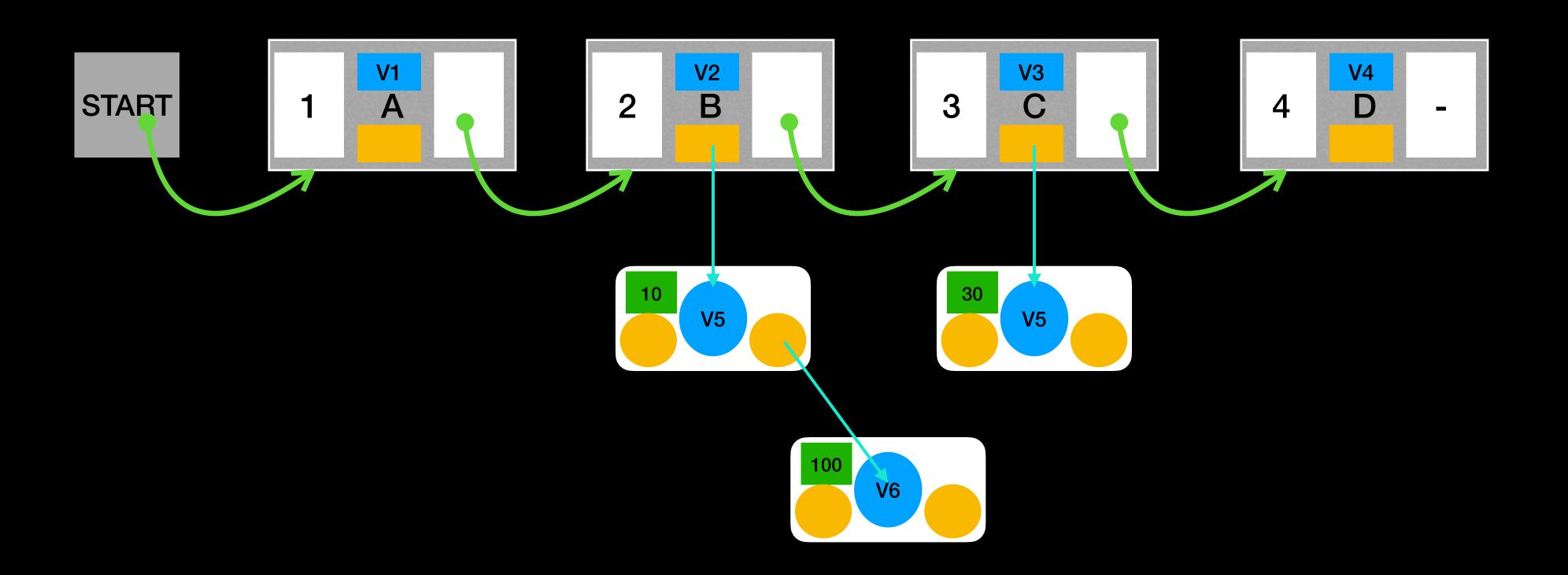
- Start from start module
- Choose those lines whose version IS JUST LESS THAN OR EQUAL TO v_x
 (as, suppose if we are traversing for v5, either v0,v1,v2,v3, v4 or v5 can be on
 that path, lines>v5 can't be on that).
- The word "JUST LESS" is written because if a NODE has two version lines in that, e.g. v2 and v4 and we are searching for v5, then we should prefer v4 line over v2.

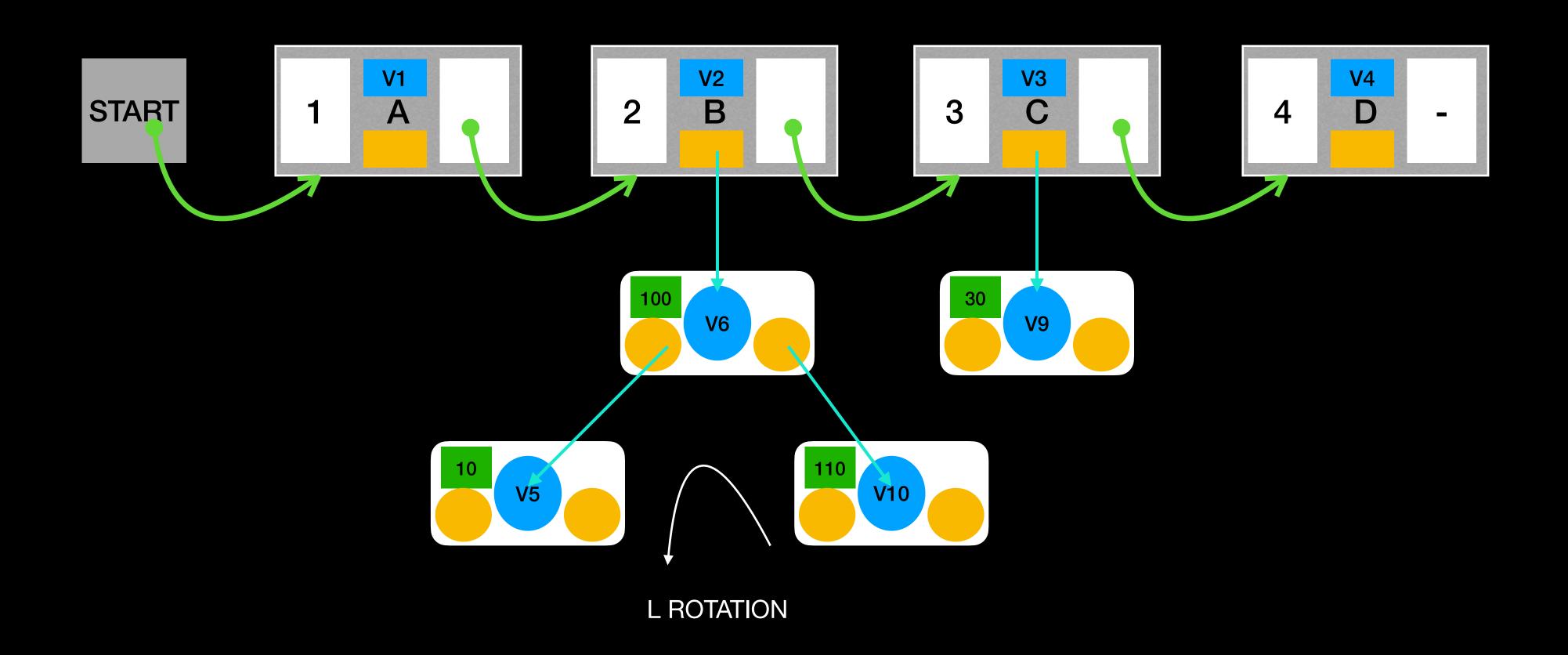
Normal Implementation (using balanced BST [may use just LL])





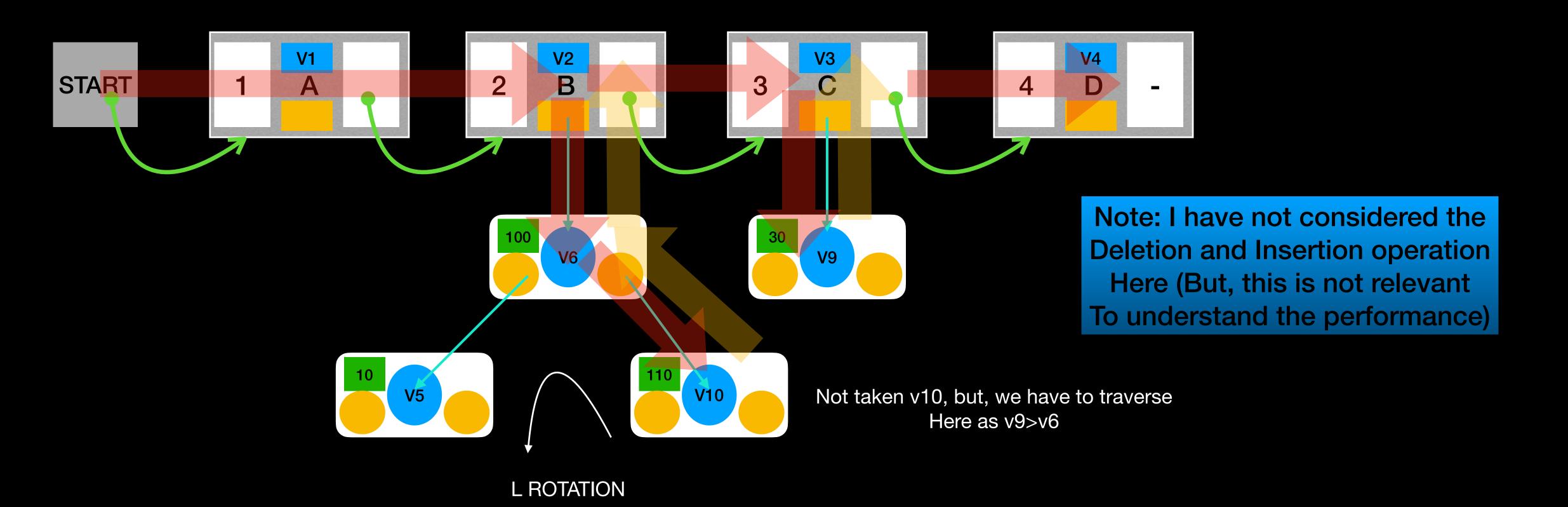






Normal Implementation (using balanced BST) (Reading v9)

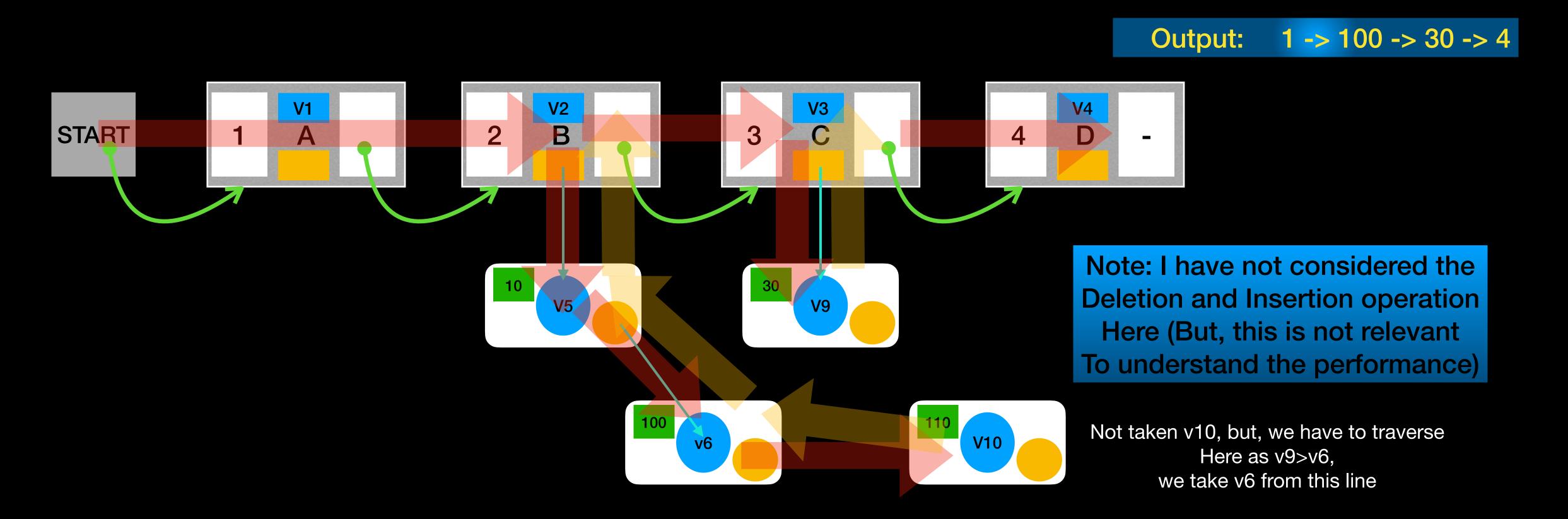
Output: 1 -> 100 -> 30 -> 4



So, the time complexity of reading list v9 ... n * O(log m) n is length of LL and m is is #mods per node

Also the creation of the AVL of version to node Takes O(log m) each time

Normal Implementation (Using List) (Reading v9)



So, the time complexity of reading list v9 ... n * O(m) n is length of LL and m is is #mods per node

The creation of the List of version to node Takes O(1) each time

Pointer Machine (Reading v9)

We are taking O(2k.n)->O(n) time for iterating over the Linked List Here k is the in-degree (Here 1) of the DS

We are taking O(2) <u>amortised time</u> for modifying/adding each node to the Linked List Here k is the in-degree (Here 1) of the DS

