

CS & IT ENGINEERING



Data Structures

Stacks and Queues

DPP


Discussion Notes



By- Pankaj Sharma sir



TOPICS TO BE COVERED



01 Question

02 Discussion

Q.1



Consider the following sequence of operations on an empty stack:

push (5); push (2); pop(); push(4); push(6); p=pop(); q=pop();
r=pop();

The value of $p+q-r$ is- 5.

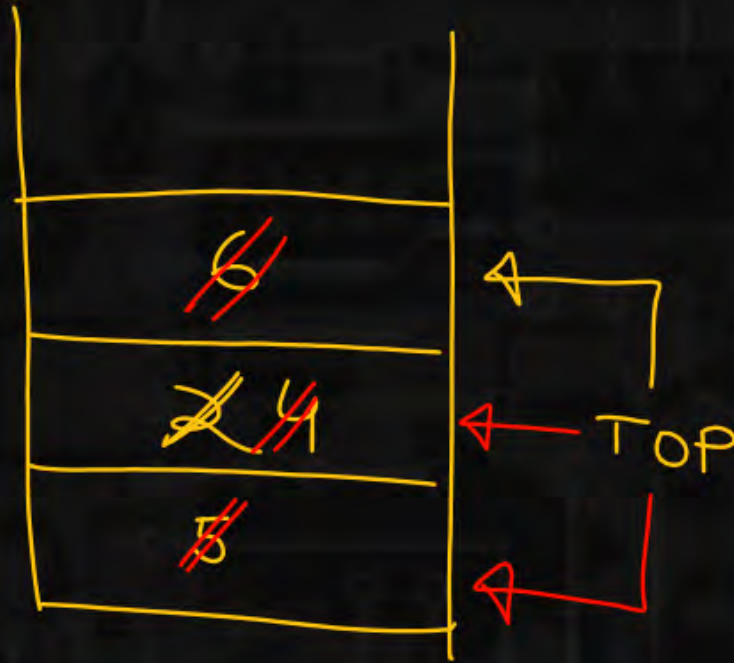
$$6 + 4 - 5 = 5$$

[NAT]

$$p = 6$$

$$q = 4$$

$$r = 5$$



Q.2

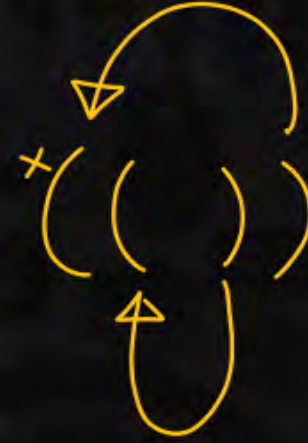
Which of the following includes the applications of stack?



[MCQ]

- ☒ A Recursive function calls
- ☒ B HTML and XML Tag matching
- ☒ C Checking if an expression contains balanced parantheses.
- ☐ D Finding the maximum element in a given sequence.

A, B, C



Q.3

A stack is implemented using array. S represents the pointer to the top element in the stack. Initially the stack contains the elements: $a(\text{top})$, b . Assume $\text{Push}(S, i)$ push an element i into the stack at index S . Whenever a Push operation will be performed, it will returns $S++$ after the push operation. $\text{Pop}()$ pops the topmost element and returns the next top index. $\text{Top}()$ is a function that returns the topmost element of the stack. Consider the following statements:

P: $\text{Top}(\text{Pop}(\text{Pop}(\text{Pop}(\text{Push}(\text{Push}(S, c), d)))) = a$

Q: $\text{Pop}(\text{Pop}(\text{Pop}(\text{Pop}(\text{Push}(\text{Pop}(\text{Push}(S, c)), d)))) = a$

Which of the following statements is/are INVALID?

[MCQ]

☐ B P only

☐ A Q only

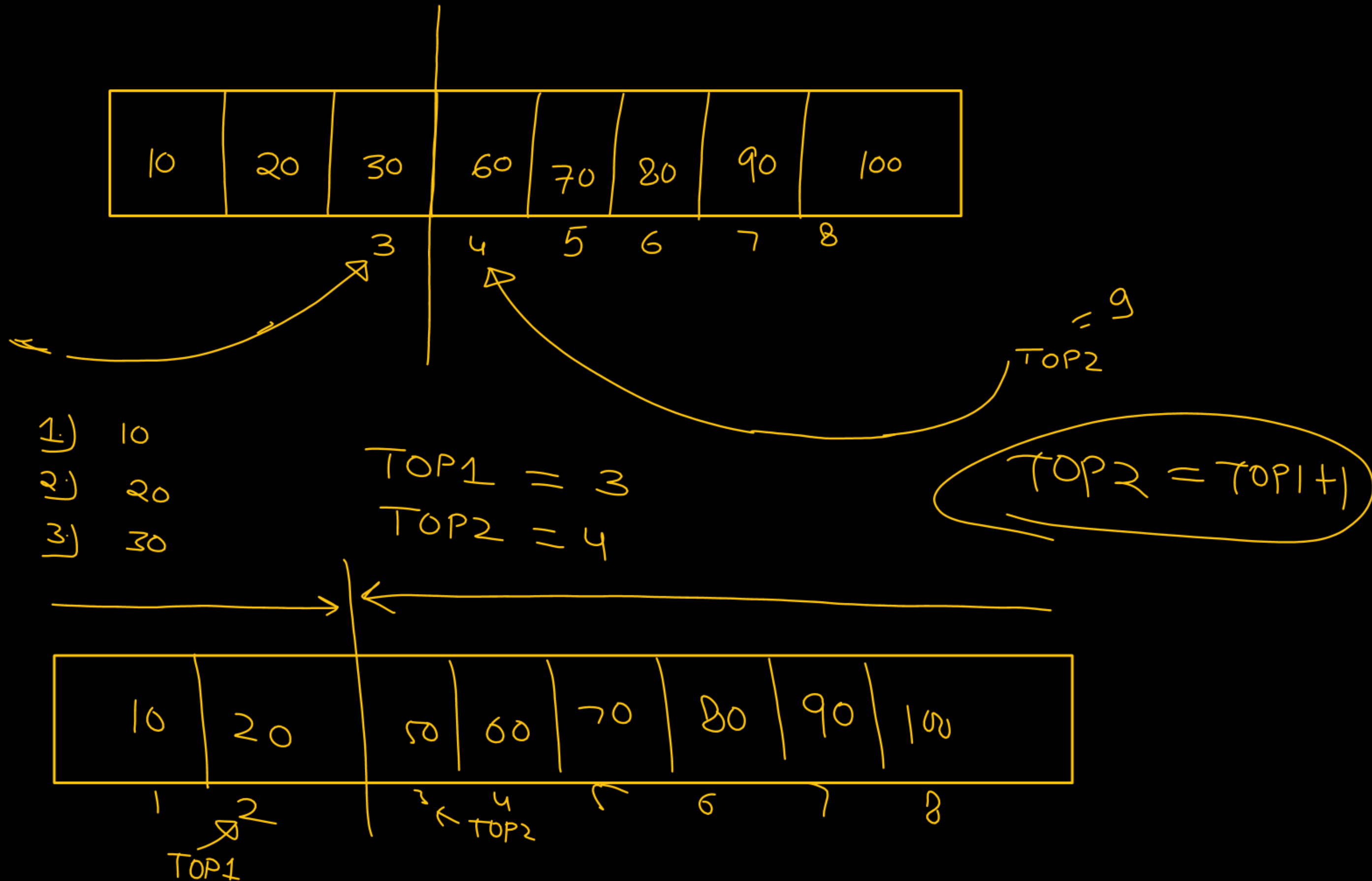
☒ C Both P and Q

☐ D Neither P nor Q

Q.4

A single array $A[1 \dots \text{MAXSIZE}]$ is used to implement two stacks. The two stacks grow from opposite ends of the array. Variables top1 and top2 ($\text{top1} < \text{top2}$) point to the location of the topmost element in each of the stacks. If the space is to be used efficiently, the condition for "stack full" is- [MCQ]

- A $(\text{top1} = \text{MAXSIZE}/2)$ and $(\text{top2} = \text{MAXSIZE}/2 + 1)$
- B $(\text{top1} = \text{MAXSIZE}/2)$ or $(\text{top2} = \text{MAXSIZE}/2 + 1)$
- C $\text{top1} + \text{top2} = \text{MAXSIZE}$
- ☒ D $\text{top1} = \text{top2} - 1$



Q.5



[MCQ]

A stack is implemented using a singly linked list that uses node structure-

```
struct node{  
    int data;  
    struct node *next;  
}node;
```

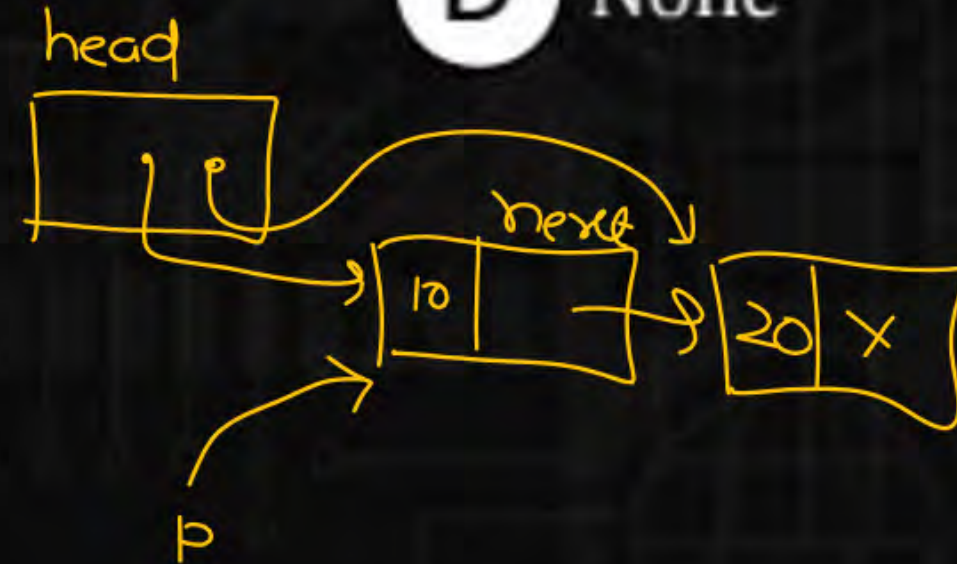
Let head denote the address of the start node respectively. Assume, the stack is not empty.

Consider the following function that intends to delete the topmost element of the stack:

```
node * f(node *head){  
    node *p=head; _____;  
    free(p);  
    p=NULL;  
}
```

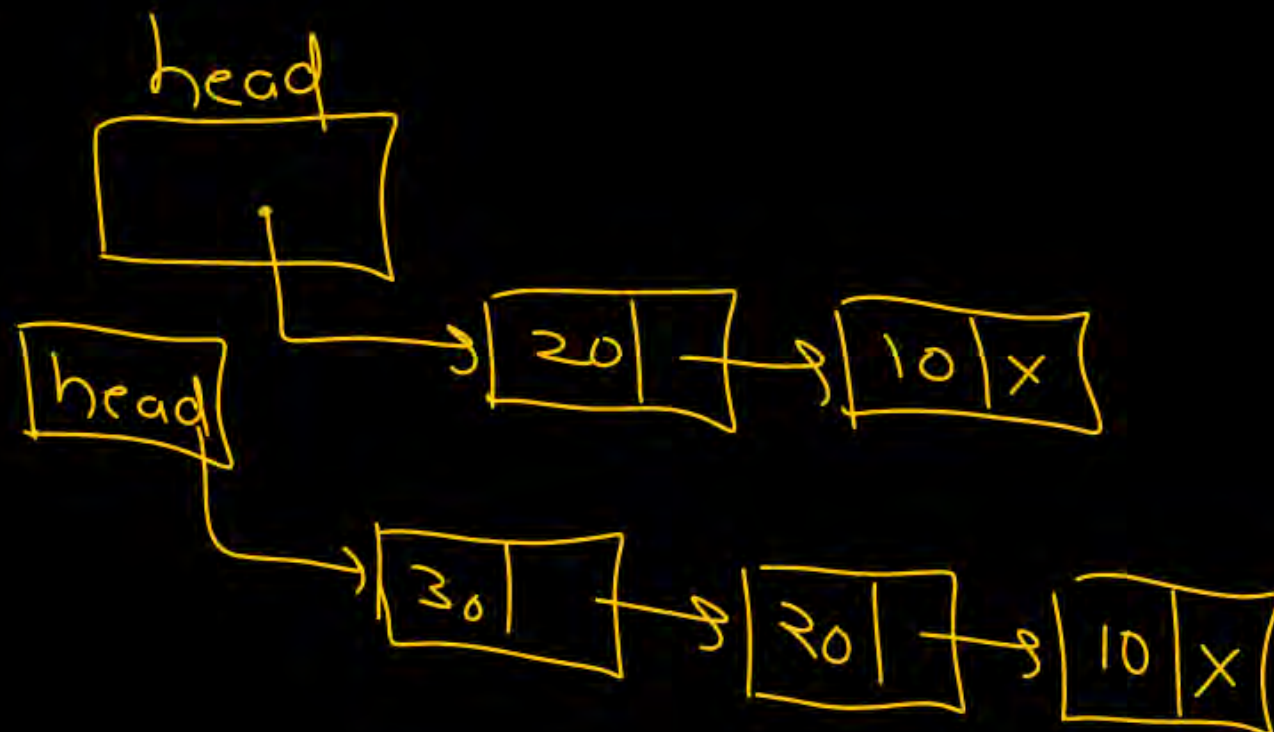
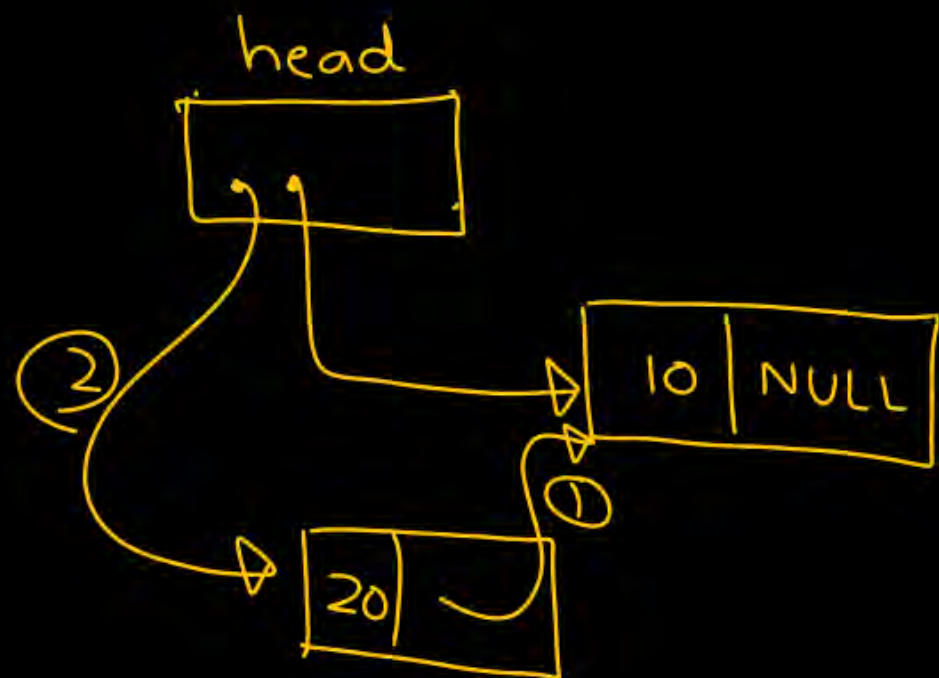
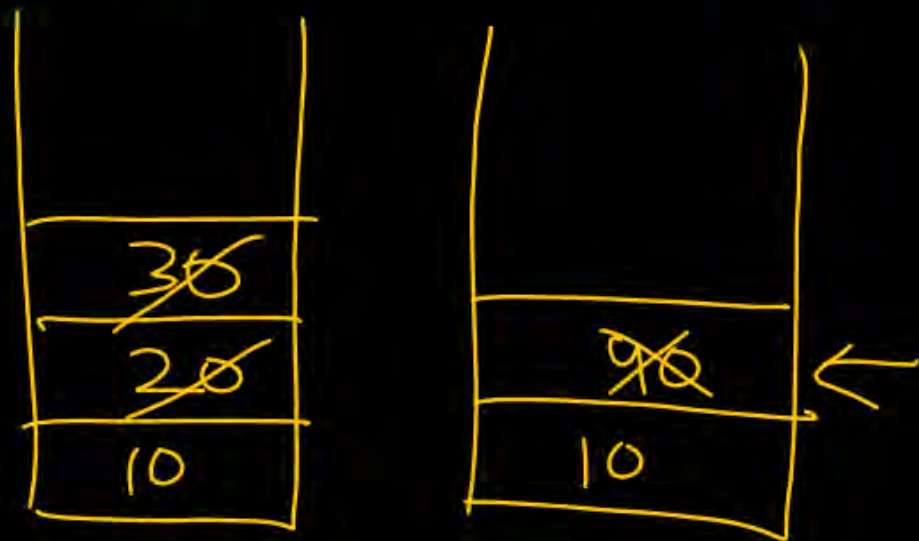
The missing blank is-

- ☒ A while(p → next!=NULL)
p=p→next;
- ☐ B p=p → next;
- ☒ C head=head → next;
- ☐ D None



Push

~~10~~, ~~20~~, 30, Pop, pop, push(40), pop



Q.6



Which one of the following permutations cannot be obtained in the output string using a stack and assuming that the input sequence is a, b, ^xc, d, e in the same order?

$\xrightarrow{\quad}$ $\xrightarrow{\quad}$ A, B

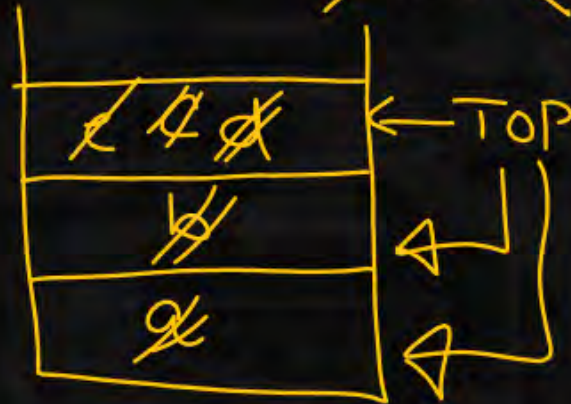
~~A~~ c d e a b

~~B~~ a e b c d

~~C~~ c d e b a

~~D~~ e d c b a

Pop()
Push(a)
Pop()
Push(e)
Pop()
Pop()

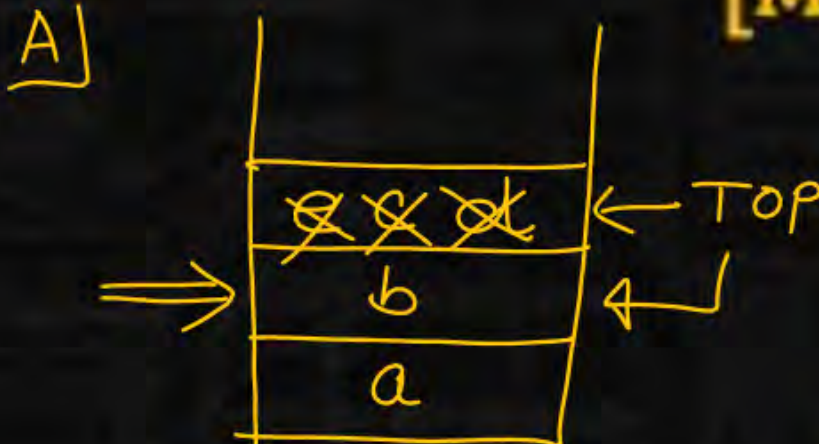


Push(a)
Pop()
Pop()
Push a, b, c, d, e



Pop()
Push(a)
Pop()
Push(e)
Pop()

c d e
[MSQ]



Q.7



A stack is implemented using array of size 4. S represents the pointer to the top element in the stack. Initially the stack contains the elements- $a(\text{top})$, b . Assume $\text{Push}(S, i)$ push an element i into the stack at index S . Whenever a Push operation will be performed, it will returns $S++$ after the push operation. $\text{Pop}()$ pops the topmost element and returns the next top index. $\text{isEmpty}()$ returns TRUE if the stack is empty. $\text{isFull}()$ returns TRUE if the stack is full. Consider the following statements:

Valid

P: $\text{isFull}(\text{Push}(\text{Pop}(\text{Push}(\text{Push}(S, c), d))), e)) = \text{TRUE}$

Valid

Q: $\text{isEmpty}(\text{Push}(\text{Pop}(\text{Pop}(\text{Push}(\text{Pop}(\text{Push}(S, c), d)))))$, $e) = \text{FALSE}$

(C)

Which of the following statements is/are VALID?

[MCQ]

A

P only

B

Q only

C

Both P and Q

D

Neither P nor Q

b	e	x	
---	--------------	--------------	--

0

↑
S

↑
S

↑
S

b	a	c	e
---	---	---	---

0

1

2

3

4

↑
S

↑
S

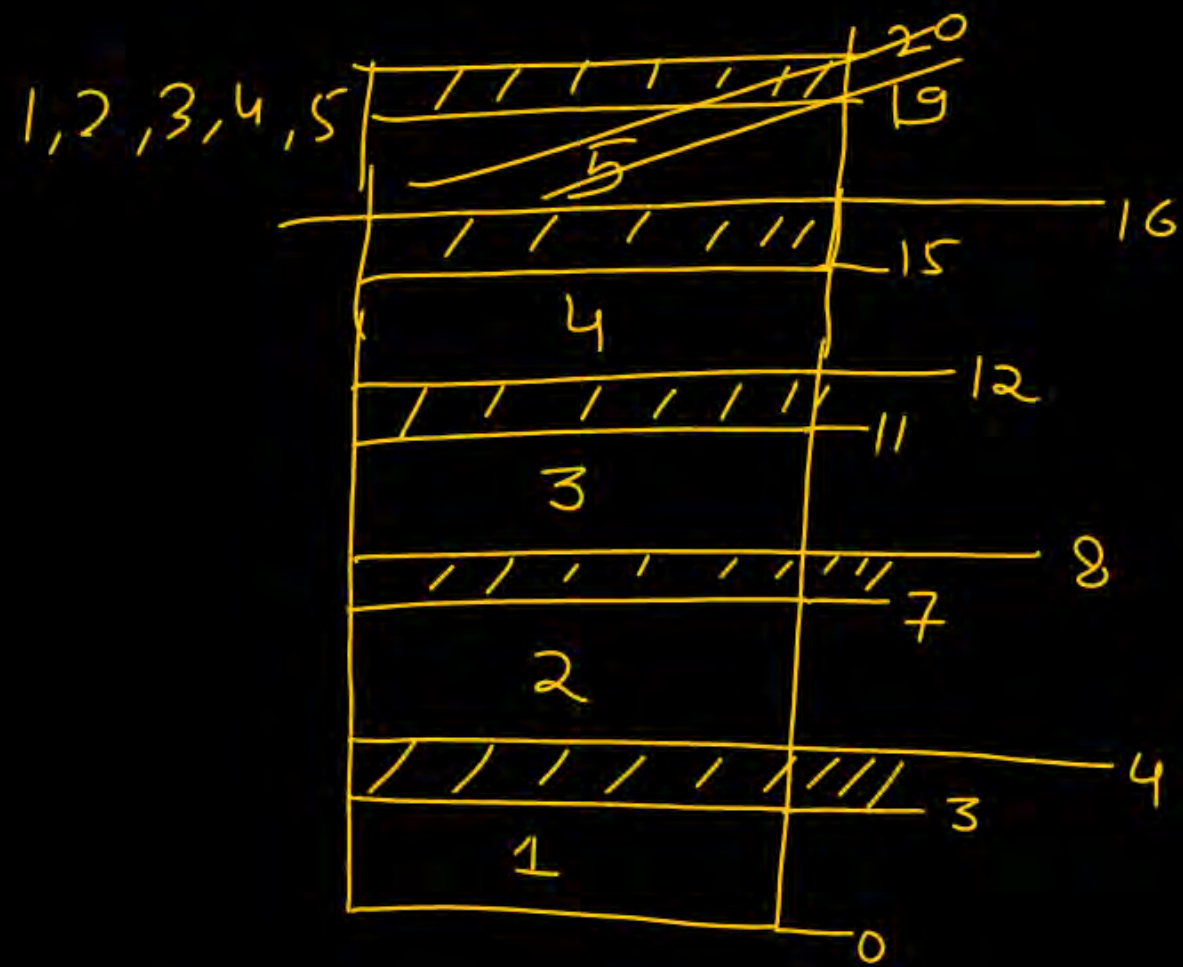
Q.8

Let S be a stack of size $n \geq 1$. Starting with the empty stack, suppose we push the first 5 natural numbers in sequence, and then perform 5 pop operations. Assume that Push and Pop operations take 3 seconds each, and 1 seconds elapse between the end of one such stack operation and the start of the next operation. The average stack-life of an element of this stack is

17.

[NAT]





1] Push(1)

2] Push(2)

3] Push(3)

4] Push(4)

5] Push(5)

	Push ends	Pop start	Pop end
1	3	36	39
2	7	32	35
3	11	28	31
4	15	24	27
5	19	20	23

$$\text{Avg life} \Rightarrow \left((20-19) + (24-15) + (28-11) + (32-7) + (36-3) \right) / 5$$

$$= (1+9+17+25+33) / 5$$

$$= \boxed{17}$$

Q.1

Consider the following infix expression:

$$P-Q/(R*S)+T*U$$

The prefix notation of the given expression is-

☐ A $-+P/Q*RS*TU$

☒ B $+ -P/Q*RS*TU$

☐ C $+ -/PQ*RS*TU$

☐ D None of the above.

(B)

$$+ -P/Q*RS*TU$$

$$P-Q/(R \times S)+T \times U$$

[MCQ]

$$P-Q/[\times RS]+T \times U$$

$$P-[/Q \times RS]+T \times U$$

$$P-[/Q \times RS]+[\times TU]$$

$$[-P/Q \times RS]+[\times TU]$$



Q.2

Consider the following expression:

$$P + Q/R - S * T^U / V - W$$

$$PQR/+STU^*V/-W-$$

The post fix notation of the given expression is-

[MCQ]

☒ A $PQR/+STU^*V/-W-$

☐ B $PQ+RS-TU^*V/-W-$

☐ C $PQR/-STU^*V/W+-$

☐ D None of the above

$$\begin{aligned} &P + Q/R - S * T^U / V - W \\ &\quad \quad \quad \Downarrow \\ &P + Q/R - S * [T^U] / V - W \\ &\quad \quad \quad \Downarrow \\ &P + [Q/R] - S * [T^U] / V - W \end{aligned}$$

$$\begin{aligned} &P + [Q/R] - [STU^*] / V - W \\ &\quad \quad \quad \Downarrow \\ &P + [Q/R] - [STU^*V/] - W \\ &\quad \quad \quad \Downarrow \\ &[PQR/+] - [STU^*V/] - W \\ &\quad \quad \quad \Downarrow \\ &[PQR/+STU^*V/-] - W \end{aligned}$$

Q.3

Consider the following prefix notation:
 $/^{\wedge} * + abc / de^{\wedge} gh$

$$((a+b)*c)^{\wedge}(d/e) / (g^{\wedge}h)$$



The postfix notation of the given expression is-

[MCQ]

B $ab+c*de/^{\wedge}gh^{\wedge}/$

A $abc+*de/^{\wedge}gh^{\wedge}/$

C $abc+de/*^{\wedge}gh^{\wedge}/$

D None of the above

Handwritten conversion steps for the prefix expression $/^{\wedge} * + abc / de^{\wedge} gh$:

$$\begin{aligned} & /^{\wedge} * + abc / de^{\wedge} gh \\ & /^{\wedge} * + abc (de)^{\wedge} gh \\ & /^{\wedge} * (+ab)c (d/e), (g^{\wedge}h) \end{aligned}$$

Handwritten conversion steps for the prefix expression $((a+b)*c)^{\wedge}(d/e) / (g^{\wedge}h)$:

$$\begin{aligned} & /^{\wedge} * (a+b), c, d/e, g^{\wedge}h \\ & /, ^{\wedge}, (a+b)*c, d/e, g^{\wedge}h \\ & /, [(a+b)*c]^{\wedge}(d/e), g^{\wedge}h \end{aligned}$$

Q.3

Consider the following prefix notation:
 $/^*+abc/de^gh$

The postfix notation of the given expression is-

$$\frac{((a+b)*c)^{(d/e)}}{(g^h)}$$

$[ab+]*c$

$$\frac{([ab+cx]^{[de/]})}{(g^h)} \quad \text{[MCQ]}$$

☒ B $ab+c*de/^gh^/$

☐ A $abc+*de/^gh^/$

☐ C $abc+de/*^gh^/$

☐ D None of the above

$$\frac{[ab+cxde/^]}{(g^h)}$$
$$[ab+cxde/^]/[g^h]$$

Q.4

Consider the following infix expression:

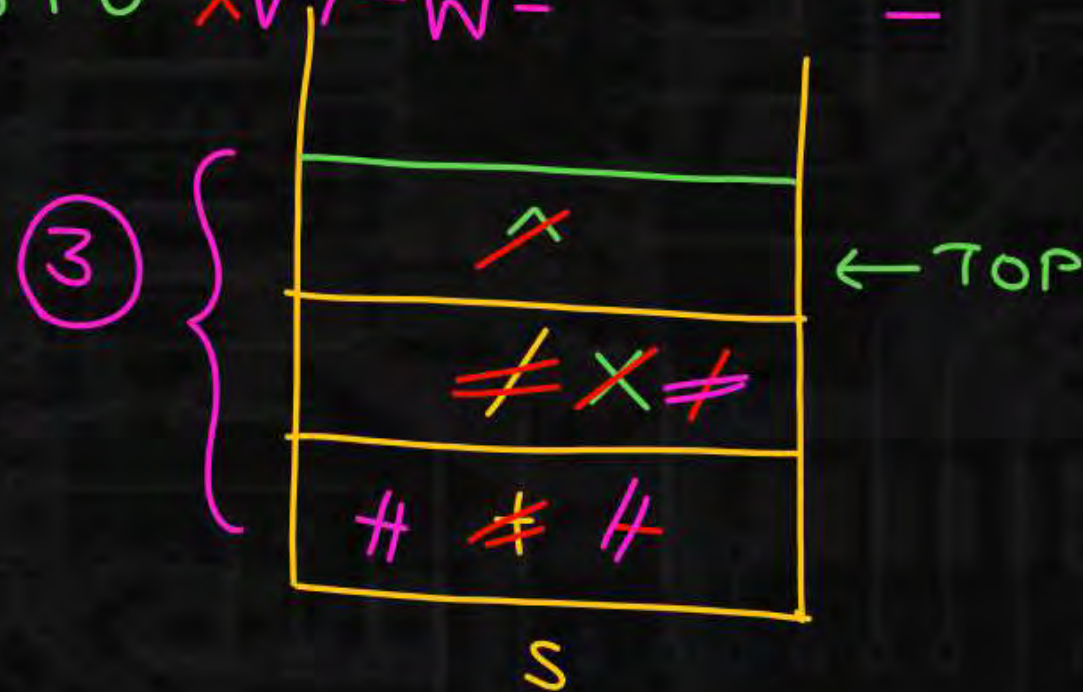
$$P+Q/R-S*T^U/V-W$$

The maximum size of the operator stack required to convert the given infix to postfix notation is 3.

[NAT]

infix: $P+Q/R-S \times T^U/V-W$ End

o/p: $PQR/+STU^XV/-W-$



Q.5

Consider the following infix expression:

$P*Q/R-S*T+U/V*W$

On reaching the symbol V, the top two contents of the operator stack are:

A $/, *$

B $/, -$

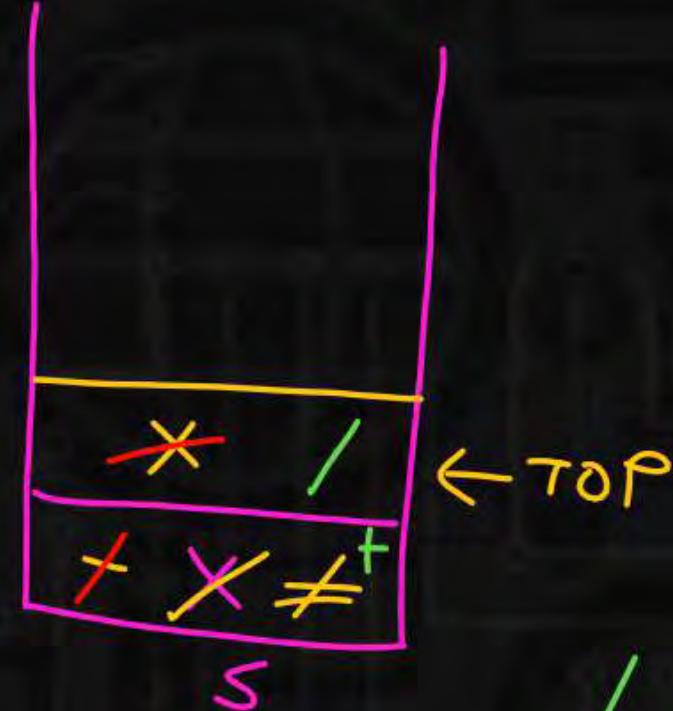
C $*, +$

☒ D $/, +$

[MCQ]

i/p: $P \times Q / R - S \times T + U / V \times W$

o/p: $PQ \times R / ST \times - UV$



$/, +$

Q.6

Consider the following postfix expression:

$8\ 2\ 3\ /\ 5\ 3\ \times + 2\ 1\ /\ -$

The result of evaluating the above postfix expression is 14.

[NAT]

$8\ 2\ 3\ /\ 5\ 3\ \times + 2\ 1\ /\ -$

$(8\ 2\ /)\ 5\ 3\ \times + 2\ 1\ /\ -$

$1\ (5\ 3\ \times) + 2\ 1\ /\ -$

$1\ 15\ +\ 2\ 1\ /\ -$

$16\ (2\ 1\ /\ -)$
 $16\ 2\ -$

(14)

Q.7



Let X be the result when the below postfix expression is evaluated:

$$X = 8 \ 3 \ 1 + - \ 2 \wedge 7 \ 1 \ 2 - * +$$

And Y be the result of the following postfix expression:

$$Y = X \ 3 / 4 +$$

The value of $(X+Y)0.5$ is 4

$$Y = (9 \ 3 /) 4 +$$

[NAT]

$$8 \ (3 \ 1 +) - 2 \wedge 7 \ 1 \ 2 - * +$$

$$(8 \ 4 -) 2 \wedge 7 \ 1 \ 2 - * +$$

$$(4 \ 2 \wedge) 7 \ 1 \ 2 - * +$$

$$16 \ 7 \ (1 \ 2 -) * +$$

$$16 \ 7 \ (-1) * +$$

$$16 - 7 +$$

9

$$Y = 7$$

$$X = 9$$

$$3 \ 4 +$$

$$16^{1/2}$$

$$= 4$$

Q.8



Let X be the result when the below postfix expression is evaluated:

$X = 4\ 5\ 1\ +\ * \ 2\ /\ 3\ 1\ 2\ +\ *\ +$ End

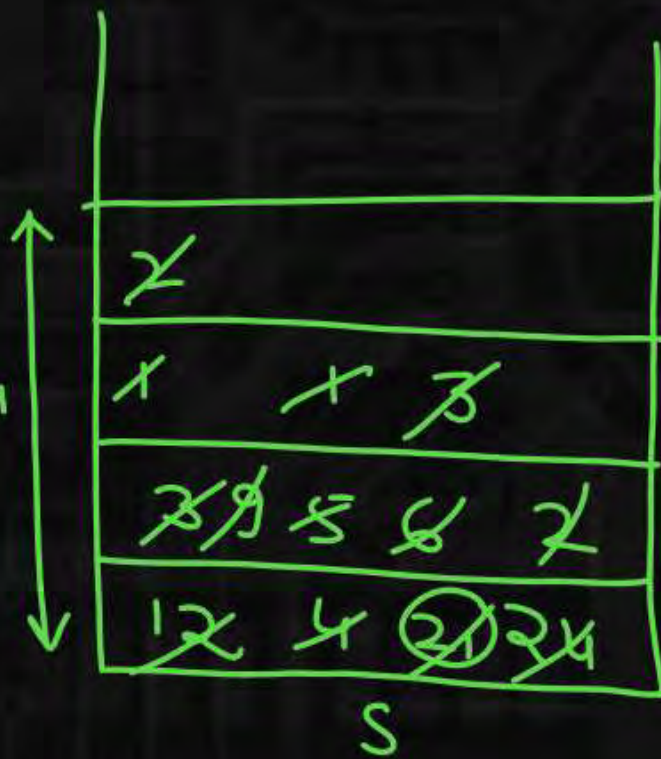
Let Y be the maximum size of the operand stack, the value of X-Y is _____

[NAT]

$X = 21$
 $Y = 4$
 $21 - 4 = 17$

1, 5
↓
5 + 1 = 6
9, 12
↓

*
6, 4, 4
↓
4 * 6 = 24



2, 24
↓
24 / 2 = 12

