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Implementation - 1 :

if  $n \leq 0$  :  $\longrightarrow O(1)$

Print ("Invalid Input")

elif  $n \leq 2$  :  $\longrightarrow O(1)$

~~Print~~

return  $n-1$

else :

return fibonacci( $n-1$ ) + fibonacci( $n-2$ )

$$\therefore T(n) = T(n-1) + T(n-2) + 1$$

$$\text{Let, } T(n-2) \approx T(n-1)$$

$$\therefore T(n) = 2T(n-1) + c \quad [c = \text{constant}]$$

$$T(n-1) = 2T(n-2) + 2c = 2^2T(n-2) + (2^{2-1})c$$

$$\therefore T(n) = 2^k T(n-k) + (2^k - 1)c$$

$$= 2^n T(0) + (2^n - 1)c$$

$$= 2^n + (2^n - 1)c$$

$$= 2^n$$

$$\therefore \text{Time complexity} = O(2^n)$$

Implementation-2:

fibonacci\_array = [0, 1]  $\rightarrow O(1)$

if  $n < 0$ :  $\rightarrow O(1)$

Print("Invalid Input")

elif  $n \leq 2$ :  $\rightarrow O(1)$

return fibonacci\_array[n-1]

else:

for  $i$  in range(2, n):  $\rightarrow O(n)$

# atomics

$$\therefore \text{Time complexity} = O(1) + O(1) + O(1) + O(n) \\ = O(n)$$

For ① we got  $O(2^n)$  and for ② we  
got  $O(n)$  time complexity.

So, ② is more efficient as  $O(n) < O(2^n)$

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Given,

for  $i=0$  to  $n-1 \rightarrow O(n)$

for  $j=0$  to  $n-1 \rightarrow O(n)$

for  $k=0$  to  $n-1 \rightarrow O(n)$

$\therefore$  The time complexity =  $O(n^3)$

As there are 3 loops running

for  $n$ -amount of time, the

time complexity can be considered

$$as = O(n) \times O(n) \times O(n) = O(n^3)$$