

D-M LQ MAT121

NOTE: Students are expected to go through the ~~above~~ ^{below} questions and try to attempt them. [30 questions from the L and F and differentiation respectively].

Limits and functions

1) The limit of the function $f(x) + g(x)$ as x approaches a can be written as _____

Ans $\lim_{x \rightarrow a} f(x) + \lim_{x \rightarrow a} g(x)$

[Hint; Since we're dealing with two functions $f(x)$ and $g(x)$ just take their limit at a specific approaching]

2) $\lim_{x \rightarrow 0} \frac{2x^3 + 3x - 2}{x^2 + 4x - 8}$

[Hint; Direct substitution and you will have a true answer]

Ans $\frac{1}{4}$

3) $\lim_{x \rightarrow -2} \sqrt{x^4 + 3x + 6}$

Ans 4

[Hint; Direct substitution and you will have a true answer.
Note; If your answer is false you will have to either differentiate or factorize]

4) $\lim_{x \rightarrow 0} \frac{x^3 + 2x^2 + x}{x^2 + 3x}$

[Hint; A false function, therefore apply L'Hopital principle (i.e. differentiate)]

Ans $\frac{1}{3}$

5) $\lim_{a \rightarrow \frac{2}{3}} \frac{a^2 - 7a + 17}{a - \frac{2}{3}}$

[Hint; A false function, then differentiate.
Note; A false function can either be $\frac{0}{0}$ (undefined) or $\frac{a}{0}$ where $a = 0, 1, \dots, n$]

6) $\lim_{y \rightarrow 0} \frac{e^{9y} - e^{-9y}}{y}$

[A false function, then differentiate
Mind you anything raise to power of zero = 1 except $0^0 = 0$]

Ans 18

7) $\lim_{n \rightarrow 1} \frac{\ln n}{n^2 - 1}$

[mind you $\ln(1)$ is zero so it is a false function, therefore we'll differentiate]

Ans $\frac{1}{2}$

NOTE: We can apply 3 methods in limit and function

- 1) Substitution method
- 2) factorization method
- 3) L'Hopital principle

There are some functions that we can substitute direct at a required approaching value of a variable and it will give us a ~~false~~ ^{True} answer (all except an undefined functions). If you come across this, just check the options and you will surely see your answer (No need to differentiate).

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for factorization; we have some false functions that require factorization. If you come across such then use your (No 32)

L'Hopital principle: This is the easiest way to tackle a false function. As it is also applicable in factorization. It is advisable to use or apply L'Hopital principle for a false function to avoid wracking of brain.

$$8) \lim_{n \rightarrow 2} \frac{(n-2)(n^2+3n-2)}{n^2-4}$$

Ans 2

[Hint; A false function. As we have a common factor, we can go for factorization. Remember $(n^2-4) = (n-2)(n+2)$]

$$9) \lim_{n \rightarrow 0} \frac{\sin n - n}{n^3}$$

Ans $-\frac{1}{6}$

[Hint; A false function because $\sin(0)=0$ & (undefined). Using L'Hopital principle differentiate the function till you have a false answer]

$$10) \lim_{n \rightarrow 2} \frac{n^2-n-2}{n-2}$$

Ans 3

[Hint; A false function, then apply either factorization or L'Hopital principle]

$$11) \lim_{n \rightarrow 3} \frac{5n-3}{n^2-9}$$

Ans $\frac{1}{1253}$

[Hint; To avoid rationalization, you can differentiate directly]

$$12) \lim_{h \rightarrow 0} \frac{(x+h)^4 - x^4}{h}$$

Ans $4x^3$

[Hint; A false function, then going by d shortcut, I will differentiate the standing variable and ignore the sign we get]

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$$13) \lim_{y \rightarrow -1} \frac{y^2 - 3y - 4}{y + 1}$$

Ans -5

[Hint] A false function, then apply L'Hopital rule

$$14) \lim_{p \rightarrow 3} \frac{p^2 - 9}{p - 3}$$

[Hint] A false function, then we can apply factorization.

[Note] $p^2 - 9 = (p - 3)(p + 3)$

$$15) \lim_{t \rightarrow 0} \left[\frac{1}{t} - \frac{1}{t^2 + t} \right]$$

ans 1

[Hint] A false function, then we can either simplify or differentiate. Simplify (i.e. by taking the L.C.M)

$$16) \lim_{h \rightarrow 0} \frac{(3+h)^2 - 9}{h}$$

Ans 6

[mind you the question's form is different from $(x+h)$, you can see now dat a number is now connecting with a variable. :- Differentiate $\frac{d}{dx}$ function (chain rule).

$$17) \lim_{y \rightarrow 0} \frac{y^3}{y - \sin y}$$

Ans 6

[false function; then differentiate all you have a true answer. - Yes! it is necessary your first derivative to still be undefined ($\frac{0}{0}$, $\frac{a}{0}$ as $a \neq 0$). - you will just continue with your differentiation until you have a true answer ✓

$$18) \lim_{m \rightarrow -3} \frac{m^2 - 9}{2m^2 + 7m + 3}$$

Ans $\frac{6}{5}$

[A false function, then apply L'Hopital principle. - make sure you always differentiate with your parameter ✓

Don't forget these are likely questions and you are expected to attempt them. No need to

$$19) \lim_{y \rightarrow -4} \frac{\frac{1}{4} + \frac{1}{y}}{4+y}$$

Ans $-\frac{1}{16}$

$$20) \lim_{n \rightarrow \infty} \frac{1}{n}$$

Ans 0

$$21) \lim_{n \rightarrow \infty} \frac{3n^3 + 2n^2 + 8}{2n^3 + n^2 - 4}$$

Ans $\frac{3}{2}$

$$22) \lim_{n \rightarrow 0} \frac{\tan n - n}{\sin n - n}$$

$$23) \lim_{n \rightarrow \infty} \frac{n^2 - 3n + 5}{2n^2 + 8n - 2}$$

Ans $\frac{1}{2}$

$$24) \lim_{m \rightarrow -4} \frac{m^2 + 5m + 4}{m^2 + 3m - 4}$$

Ans $\frac{3}{5}$

[Hint] A false function, then apply l'hopital principle i.e differentiate the function.

Have it in your mind that anything $+$, \times and $-$ by infinity is equals to ∞
 i.e $5 - \infty = \infty$
 $4 + \infty = \infty$
 $2 \times \infty = \infty$
 Also anything divided by ∞ infinity will be zero
 i.e $\frac{1}{\infty} = 0 \Rightarrow \frac{n}{\infty} = 0$ (where $n = 1, 2, 3, \dots$)

[Hint; going by Δ Shortcut: Check the highest power of Δ variable present in Δ function (and which n^3) then compare the coefficient of it (i.e both Δ numerator and denominator

[Hint; A false function; Then apply l'hopital rule (i.e differentiate) mind you; it is not compulsory your first derivate to give a true function If happens, then continue differentiating

[Hint; going by Δ Shortcut compare Δ coefficient of highest power of Δ present variable (i.e n^2)

[Hint; A false function. Then you can either apply l'hopital rule (differentiate) or cancel out the common terms from the question i.e m^2 cancel m^2 and 4 cancel 4 but because of the negative sign you aren't expected to go with det :- differentiate Δ function

$$25) \lim_{n \rightarrow 2} \frac{n^2 + n - 6}{n - 2}$$

Ans 5

[Hint; A false function. So it's either you differentiate this or factorize this because there is a common factor which is $(n-2)$. But for those that can't recall their quadratic equation you are expected to differentiate]

$$26) \lim_{n \rightarrow -2} \frac{n^3 + 8}{n + 2}$$

[Hint; A false function, then apply L'Hopital rule (i.e. differentiate d function),

$$27) \lim_{n \rightarrow 0} \frac{n^{500}}{n^2 + 3n + 5}$$

Ans 0

[Hint; A True function then substitute directly.
Mind you $0^{500} = 0$

$$28) \lim_{n \rightarrow 1} \frac{\ln n}{n^2 + n - 2}$$

Ans $\frac{1}{3}$

[Hint; A false function, then differentiate.
mind you $\ln 1 = 0$

$$29) \lim_{y \rightarrow 0} \frac{\sin 2y + \sin y}{y}$$

[Hint; A false function, then apply L'Hopital principle.
Recall; our first derivative too may be undefined. Therefore, you are expected to continue with d differentiation if you come across such.

$$30) \lim_{m \rightarrow \infty} \frac{4m^4 + 3m^3 + 2m + 1}{8m^4 + 2m^3 + 3m - 3}$$

[Hint; A false function. Going by d shortcut. take d highest power of d variable (m) i.e. m^4 and compare their coefficient
Mind you this is only applicable if and if a variable tends to ∞ i.e. $m \rightarrow \infty$

PART B

DIFFERENTIATION

NOTE: Differentiation is linear stuff (100%) but you have to be very careful when differentiating because it's well with whatever way you decide to take (i.e. if you differentiate rubbish you will still see your rubbish answer.
Again! be careful when differentiating.

① find $\frac{d}{dx}$ of $5e^{\sin x}$

Ans $5\cos x e^{\sin x}$

[Hint; (function of a function) then by going with a shortcut, differentiate the first function as if a other one doesn't exist (i.e. keep it) then go to a second function and differentiate then take their product (i.e. $\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$)

② what is second derivative (y'') of $y = px^q$

Ans $pq(q-1)x^{(q-1)(q-2)}$

[Hint; Apply the general monomial formula [i.e. nqn^{n-1}]

③ $y = 3x^3 + 9x^2 + 8x - 4$
find $\frac{d^3y}{dx^3}$

Ans 18

[Hint; Differentiate a function 3 times

4) find $\frac{dy}{dx}$ if $y = \frac{4}{3\sqrt{x^5}}$
Ans $-\frac{8}{3\sqrt{x^5}}$

[Hint; change the question form to a differentiable one then differentiate and change your answer back to a initial form

5) find a differential coefficient of $y = 4x^2 \tan x$

Ans $4x(x \sec^2 x + 2 \tan x)$

[Hint; mind you differential coefficient also means derivative And this function is an UV function (product Rule). Then - going by a shortcut, leave a 1st function and differentiate a second one + leave a second one and differentiate a 1st one i.e.
 $\frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$

⑥ If $y = p(x)q(x)$ find y'

[Hint; product Rule]

Ans $p(x) \frac{dq(x)}{dx} + q(x) \frac{dp(x)}{dx}$

⑦ Find the derivative of $\cos(\sin x)$

[Hint; mind you we're applying chain rule here because it's just a single variable]

Ans $-\sin^2 x \cos x$

8) Find y' if $y = 4 \cos(7x+2)$

Ans $-28 \sin(7x+2)$

[Hint; A Chain Rule function]
Apply your shortcut

⑨ If $y = \frac{1+x}{1-x}$ find $\frac{dy}{dx}$

Ans $\frac{2}{(1-x)^2}$

[Hint; A quotient function, then apply your shortcut i.e. leave the denominator, differentiate the numerator — (minus) leave the numerator, differentiate the denominator. Everything divided by the denominator squared (i.e. $\frac{\frac{dy}{dx} - u \frac{dy}{dx}}{v^2}$)

10) Find $\frac{dy}{dx}$ if $y = (mx+b)^n$

Ans $nm(mx+b)^{n-1}$

[Hint; A Chain Rule function]
then apply your shortcut

11) Find the differential coefficient of $x^3 \sin x$

Ans $x^2(x \cos x + 3 \sin x)$

[Hint; A product function]
then apply your shortcut

NOTE;

Recall that students are expected to solve these for building his/her confidence and for improvement.

I'm very sure you are getting this, if not then

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12) find y' if $y = \ln(3 - 4\cos x)$

Ans $\frac{4 \sin x}{3 - 4\cos x}$

{Hint; A Chain Rule function}
then apply your shortcut}

13) find m' if $m = \frac{\sin x}{x^2}$

Ans $\frac{x(\cos x - 2\sin x)}{x^4}$

{Hint; A quotient function then
apply your shortcut}

14) find $\frac{dy}{dx}$ if $y = x^3 e^{2x}$

Ans $x^2 e^{2x} (2x + 3)$

{Hint; A product function (product Rule) den apply your shortcut}

15) find $\frac{dy}{dx}$ of $x^2 + 2xy + 3y^2 = 4$

Ans $-\frac{(x+y)}{x+3y}$

{Hint; Implicit function
Don't forget dat when differentiating y it will follow by $\frac{dy}{dx}$
then collect d like term and get your $\frac{dy}{dx}$. (Simple ✓)}

16) if $y = \frac{p(x)}{q(x)}$ find y'

Ans $\frac{q \frac{dp}{dx} - p \frac{dq}{dx}}{q^2}$

{Hint; A quotient function
den compare it with $\frac{u}{v}$ and differentiate}

17) find d slope of d Curve $x^2 - xy + y^2 = 7$
at $x = 3, y = 2$

Ans -4

{Hint; firstly apply implicit rule then substitute d value of x and y after differentiating}

NOTE;

Also Students are not allow 3 memorize these answers
Study them well and make use of them incase you are
dealing with the same set of questions but of different variable

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18) $y = \frac{\sin 2x}{2x+5}$ find y'

Ans $\frac{2(2x+5)\cos 2x - 2\sin 2x}{(2x+5)^2}$

{Hint; A quotient function}
Apply your shortcut

19) find $\frac{d}{dx}$ derivative of $(4x-3)^5$

Ans $20(4x-3)^4$

{Hint; A Chain function}
Apply your shortcut

20) If $y = \sin^2(2x^2+4)$ find y'

Ans $32x \sin(2x^2+4)^4 \cos(2x^2+4)^4 (2x^2+4)^3$

{Hint; A Chain function}
Apply your shortcut
It's simple now lol

21) If $y = \sin^{-1} x$ find y'

Ans $\frac{1}{\sqrt{1-x^2}}$

{Hint; derivative of inverse trigonometric function. Then by shortcut} ←

NOTE;

$\sin^{-1} x = \frac{1}{\sqrt{1-x^2}}$

$\cos^{-1} x = \frac{-1}{\sqrt{1-x^2}}$

$\tan^{-1} x = \frac{1}{1+x^2}$

A hyperbolic function

$\sinh^{-1} x = \frac{1}{\sqrt{1+x^2}}$

$\cosh^{-1} x = \frac{1}{\sqrt{x^2-1}}$

$\tanh^{-1} x = \frac{1}{\sqrt{1-x^2}}$

22) If $y = \cosh^{-1} 3-2x$ find y'

Ans $\frac{-2}{\sqrt{(3-2x)^2-1}}$

{Hint; derivative of inverse hyperbolic function. Then by shortcut $\cosh^{-1} u = \frac{1}{\sqrt{u^2-1}}$ then apply Chain Rule.
As simple as that (100%) ✓

23) If $x^2 + y^2 = 5$ find $\frac{dy}{dx}$

Ans $-\frac{x}{y}$

{Hint; An implicit function. Don't forget add $\frac{dy}{dx}$ when differentiating y , try to collect the like terms then find or make $\frac{dy}{dx}$ the subject of $\frac{d}{dx}$ formula

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24) The equivalent 2 d form derivation of $y = \sin x$
Ans y

{ mind you if you differentiate $\sin x$ four times, you will still get $\sin x$ and which is $= y$
 my bro and sis 2
 No time 0!!! }

25) If $y = 3u^4 + 2u^3 + 8u + 8$
 find $\frac{d^3y}{du^3}$

Ans $72u$

{ Hint; Differentiate 3 times.
 Note; $\frac{d^3y}{du^3} = y'''$ }

26) If $y = 3 \tan^2 2x$ find y'

Ans $12 \tan 2x \sec^2 2x$

{ Hint; Chain Function
 Apply d shortcut and get your answer }

27) If $y = \sin^{-1} x^2$ find y'

Ans $\frac{2x}{\sqrt{1-x^2}}$

{ Hint; Inverse trig function
 Apply d shortcut }

28) find d/derivative of $xy = 1$

Ans $-\frac{y}{x}$

{ Hint; Implicit function
 Apply d normal process and get your $\frac{dy}{dx}$ }

29) If $y = \ln x^2$ find y'

Ans $\frac{2}{x}$

{ Hint; Chain function
 Apply d shortcut }

30) If $y = x^5 e^x$ find y'

Ans $x^4 e^x (x+5)$

{ Hint; A product function
 Apply d shortcut }

Please make sure you attempt them and compare your answers with mine. In case any of it is not correct, fine - put the correct one (Nobody is above mistake)
 WISHING YOU GUYS ALL THE VERY BEST!!!

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