

给出循环队列实现，入队，出队

```
public void enqueue(Object x) throws Overflow{ /*入队*/
    if(isFull()){
        throws new Overflow();
    }
    else{
        length++;
        rear = (rear+1)%m;
        Q[rear] = x;
    }
}

public Object dequeue() throws Underflow{ /*出队*/
    if(isEmpty()){
        throws new Underflow();
    }
    else{
        length--;
        return Q[(rear-length+m)%m];
    }
}
```

二叉树的机内存储（表示）：广义表表示，双亲表示法，左子女—右兄弟表示法

森林的后根遍历与对应的二叉树中序遍历一致

非递归中序遍历

Inorder non-recursive algorithm

```
void Inorder(BinaryNode <T> * t)
{ Stack<BinaryNode<T>*> s(10);
  BinaryNode<T> * p = t;
  for ( ; ; )
  { 1) while(p!=NULL)
      { s.push(p); p = p->Left; }
    2) if (!s.IsEmpty( ))
      { p = s.pop( );
        cout << p->element;
        p = p->Right;
      }
    else return;
  }
}
```

排序算法的稳定性:

如果待排序的对象序列中, 含有多个关键码值相等的对象, 用某种方法排序后, 这些对象的相对次序不变的, 则是稳定的, 否则为不稳定的。

复习例题---在 $O(n)$ 时间内实现将负数排在所有非负数之前。

```
void sort ( float [ ] a, int n )
{ int i = 0 , j = n-1 ;
  while ( i != j )
  { while ( a[j] >= 0.0 && i < j ) j-- ;
    while ( a[i] < 0 && i < j ) i++ ;
    float temp = a[i] ; a[i] = a[j]; a[j] = temp;
    j-- ; i++ ;
  }
}
```

信号量解决读者写者问题：写者优先

```
semaphore rmutex, wmutex, S;
  rmutex=1; wmutex=1; S=1; //增加互斥信号量S
int readcount=0; //读进程计数
```

```
process reader_i( ) {
  while (true) {
    P(S);
    P(rmutex);
    if (readcount==0) P(wmutex);
    readcount++;
    V(rmutex);
    V(S);
    读文件;
    P(rmutex);
    readcount--;
    if(readcount==0) V(wmutex);
    V(rmutex);
  }
}
```

```
process writer_i( ) {
  while(true) {
    P(S);
    P(wmutex);
    写文件;
    V(wmutex);
    V(S);
  }
}
```

读者/写者问题(写者优先)

```
int readcount = 0, writecount = 0;
semaphore x=1, y=1, z=1; // readcount,writecount互斥
semaphore rmutex=1,wmutex=1; // 读锁, 写锁
```

process reader

```
{
  P(z);
  P(rmutex);
  P(x);
  readcount++;
  if (readcount==1) P(wmutex);
  V(x);
  V(rmutex);
  V(z);
  read;
  P(x);
  readcount--;
  if (readcount==0) V(wmutex);
  V(x);
};
```

process writer

```
{
  P(y);
  writecount++;
  if (writecount==1) P(rmutex);
  V(y);
  P(wmutex);
  write;
  V(wmutex);
  P(y);
  writecount--;
  if (writecount==0) V(rmutex);
  V(y);
};
```

所有边权均不相同的无向图最小生成树是唯一的

a) 检测回文单词

- ◆ 比较头尾两个字符，相同则向中间靠拢比较，不相同则返回false。
 - ◆ 边界条件和递归返回段：
 - ◆ 要比较的子字符串为空，返回true
 - ◆ 递归前进段：截取当前字符串从位置1到位置length-1的子字符串，返回其回文性。

```
public static boolean palindrome0(String word, int low, int high) {  
    if (low > high)  
        return true;  
    if (word.charAt(low) == word.charAt(high)  
        || Math.abs(word.charAt(low) - word.charAt(high)) == 32)  
        return palindrome(word, low+1, high-1);  
    else  
        return false;  
}
```

b) 检测回文句子

- ◆ 在递归过程中去除不符合要求的字符

```
public static boolean palindrome(String word, int low, int high) {  
    if (low > high)  
        return true;  
    while (!Character.isLetter(word.charAt(low)))  
        low++;  
    while (!Character.isLetter(word.charAt(high)))  
        high--;  
    if (word.charAt(low) == word.charAt(high)  
        || Math.abs(word.charAt(low) - word.charAt(high)) == 32)  
        return palindrome(word, low+1, high-1);  
    else  
        return false;  
}
```

编写一个非递归方法以 $O(n)$ 的时间复杂度反转单链表

代码

```
public void reverse() {
    ListNode p1 = header.next;
    if (p1 == null)    return;
    ListNode p2 = p1.next;
    if (p2 == null)    return;
    ListNode p3 = p2.next;
    p1.next = null; // 将firstNode.next设为null

    // node.next设为前一个node,然后指针前移一个位置
    while (p3 != null) {
        p2.next = p1;
        p1 = p2;
        p2 = p3;
        p3 = p3.next;
    }
    p2.next = p1; // 最后一个元素指向倒数第二个元素
    header.next = p2; // 将头指针指向最后一个元素
}
```

循环左移算法

```
◆ void Converse(int R[],int n,int p){
    ◆ Reverse(R,0,p-1);
    ◆ Reverse(R,p,n-1);
    ◆ Reverse(R,0,n-1);
    ◆ }

◆ void Reverse(int R[],int from,int to) {
    ◆ int i,temp;
    ◆ for(i = 0; i < (to-from+1)/2; i++)
    ◆ {
        ◆ temp = R[from+i]; R[from+i] = R[to-i]; R[to-i] = temp; }
    ◆ }
    }
```

◆ 1) 统计二叉树中叶结点的个数。

```
public static int leafNum(BinaryNode root) {  
    if (root == null)  
        return 0;  
    if (root.left == null && root.right == null)  
        return 1;  
    return leafNum(root.left) + leafNum(root.right);  
}
```

◆ 2) 以二叉树为参数，交换每个结点的左子女和右子女

```
public static void switchLR(BinaryNode root) {  
    if (root == null)  
        return;  
    BinaryNode tmp = root.left;  
    root.left = root.right;  
    root.right = tmp;  
    switchLR(root.left);  
    switchLR(root.right);  
}
```

写一递归函数实现在带索引的二叉搜索树(IndexBST)中查找第 k 个小的元素

```
Public BinaryNode findkth(BinaryNode t, int k)
{
    if(k<=0 || t==null)
        return null;
    if(k<t.leftsize)
        return findkth(t.left ,k);
    else if(k>t.leftsize)
        return findkth(t.right ,k-
            t.leftsize);
    else
        return t;
}
```

对于一个有N 个结点的AVL 树，其最大高度是多少？ 最小高度是多少？

∴费波那契数树是具有相同高度的所有平衡二叉树中结点个数最少的，

$$n+1 \geq N_h+1 = \frac{1}{\sqrt{5}} \left(\frac{1+\sqrt{5}}{2} \right)^{h+3} + O(1)$$
$$\therefore h \leq \frac{1}{\log_2 \frac{1+\sqrt{5}}{2}} \log_2 (n+1) + O(1) \approx \frac{3}{2} \log_2 (n+1)$$

这就是h的最大值；

至于h的最小值，是一颗完全二叉树的时候，高度最小，有

$$2^{h+1}-1=n, \text{ 所以 } h=\log_2(n+1)-1.$$

如果 str 是“abc”，那么输出的串则是 abc, acb, bac, bca, cab, 和 cba。

代码

```
void permute(char [] str, int low, int high){  
    //low=0,high=str.length-1  
    if(low==high) {  
        System.out.println(str);  
    } else {  
        for(int i=low; i<=high; i++){  
            char temp;  
            temp = str[i]; str[i] = str[low]; str[low] = temp;  
            permute(str, low+1, high);  
            temp = str[i]; str[i] = str[low]; str[low] = temp;  
        } //end of for  
    }  
}
```

递归求解链表长度

代码

```
public class Length{  
    public static int length = 0;  
    public static int GetLength(Iterator it){  
        if(!it.hasNext())  
            return 0;  
        else{  
            it.next();//遍历  
            return 1+GetLength(it);  
        }  
    }  
}
```


设n为正整数，分析下列各程序段中加下划线的语句的执行次数。

2)

x = 0; y = 0;

for (int i = 1; i <= n; i++)

for (int j = 1; j <= i; j++)

for (int k = 1; k <= j; k++)

x = x+y;

$$f(n) = \sum_{i=1}^n \sum_{j=1}^i \sum_{k=1}^j 1 = \frac{1}{6} n(n+1)(n+2)$$

```
public static int findMax(int[] a, int n){
//n表示第n个元素，它在数组中位于a [n-1]处
    if(n==1){
        return a [0];
    }
    else{
        int temp=findMax(a,n-1);
        return temp>a [n-1]?temp:a [n-1];
    }
}
```

Special Matrix

3) Tridiagonal

$$\begin{pmatrix} a_{11} & a_{12} & & & \\ & a_{21} & a_{22} & a_{23} & \\ & & a_{32} & a_{33} & a_{34} \\ & & & \dots & \\ & & & & a_{n,n-1} & a_{n,n} \end{pmatrix}$$

Location mapping in row-major order:

$$\text{Loc}(a(i,j)) = \text{Loc}(a(1,1)) + [(i-1)*3-1 + (j-i+1)]*l$$

6.3 Heaps

```
private void percolateDown( int hole )
{
    int child;
    Comparable tmp = array[ hole ];
    for( ; hole * 2 <= currentSize; hole = child )
    {
        child = hole * 2;
        if ( child != currentSize && array[ child + 1 ].compareTo( array[ child ] ) < 0 )
            child++;
        if ( array[ child ].compareTo( tmp ) < 0 )
            array[ hole ] = array[ child ];
        else
            break;
    }
    array[ hole ] = tmp;
}
```

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最小根 percUp

```
private static void percUp( Comparable [ ] a, int start )  
{  
    int j = start, i = j / 2;  
    Comparable temp = a [j];  
    while (j > 1)  
    {  
        if ( a[i] <= temp) break;  
        else { a[j] = a[i]; j = i; i = i / 2; }  
    }  
    a[j] = temp;  
}
```

非递归先序访问

借助一个栈，因为每次都是栈顶出栈，即栈顶都是先访问的节点，先序遍历的思想是先根，再左孩子，再右孩子。

故访问完当前节点后，应该先将右孩子入栈，再左孩子入栈即可。

```
void PreOrder1(BTNode *b)  
{  
    BTNode *St[MaxSize], *p;  
    int top = -1;
```

```
    if (b!=NULL)  
    {  
        top++;  
        St[top] = b;  
        while(top > -1)    //the stack is not empty then loop  
        {  
            p = St[top];  
            top--;  
            printf("%c", p->data);  
            if(p->rchild) St[top++] = p->rchild;  
            if(p->lchild) St[top++] = p->lchild;  
        }  
    }  
    printf("\n");  
}
```

层次遍历

```
void TrayLevel(BTNode* b)
{
    BTNode *Qu[MaxSize];
    int front, rear;
    front = rear = 0;
    if( b!= NULL)
        printf("%c", b->data);
    rear++;
    Q[rear]= b;
    while(rear != front)
    {
        front= (front+ 1)%MaxSize;    //front head come out;
        b = Qu[front];
        if(b->lchild != NULL)           //print left child, and
enter stack
        {
            printf("%c", b->lchild->data);
            rear = (rear+1)%MaxSize;
            Qu[rear] = b->lchild;
        }
        if(b->rchild != NULL)           //print right child, and
enter stack
```

```
        {
            printf("%c", b->rchild->data);
            rear = (rear+1)%MaxSize;
            Qu[rear]=b->rchild;
        }
    }
    printf("\n");
}
```