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CSE 420-01

Homework 2

Homework 2 Report

Part 1: (success)

a) $(1, 1, 1), (1, 2, 1), (3, 0, 4)$

$$A = P_2 - P_1 = (1, 2, 1) - (1, 1, 1) = (0, 1, 0)$$

$$B = P_3 - P_1 = (3, 0, 4) - (1, 1, 1) = (2, -1, 3)$$

$$N = A \times B = (3 - 0)i + (0 - 0)j + (0 - 2)k = \underline{3i + 0j - 2k}$$

b) $(6, 3, -4), (0, 0, 0), (2, 1, -1)$

$$A = P_2 - P_1 = (0, 0, 0) - (6, 3, -4) = (-6, -3, 4)$$

$$B = P_3 - P_1 = (2, 1, -1) - (6, 3, -4) = (-4, -2, 3)$$

$$N = A \times B = (-9 + 8)i + (-16 + 18)j + (12 - 12)k = \underline{-1i + 2j + 0k}$$

$$\text{Plane} \rightarrow 5x - 3y + 6z = 7$$

$$\text{Unit normal} = N/|N| = (5, -3, 6) / \sqrt{5^2 - 3^2 + 6^2} = (5, -3, 6) / \sqrt{70}$$

$$= \underline{(5/\sqrt{70}, -3/\sqrt{70}, 6/\sqrt{70})}$$

$$F(P_1) = F(1, 5, 2) = 5(1) - 3(5) + 6(2) - 7 = -5 \rightarrow -5 < 0 \text{ so behind the plane}$$

$$F(P_2) = F(-3, -1, -2) = 5(-3) - 3(-1) + 6(-2) - 7 = -7 \rightarrow -7 < 0 \text{ so behind the plane}$$

Both points are behind the plane

Part 2: (success)

$$P = (1, 2, 3)$$

$$\text{a) Sphere: } x^2 + y^2 + z^2 = 14$$

$$N = (1, 2, 3) - (0, 0, 0) = (1, 2, 3)$$

$$\text{Unit normal} = (1, 2, 3) / \sqrt{1^2 + 2^2 + 3^2} = (1, 2, 3) / \sqrt{14}$$

$$= \underline{(1/\sqrt{14}, 2/\sqrt{14}, 3/\sqrt{14})}$$

$$\text{b) Plane: } 3x - 4y + 2z - 1 = 0$$

$$N = (3, -4, 2)$$

$$\text{Unit Normal} = (3, -4, 2) / \sqrt{3^2 - 4^2 + 2^2} = (3, -4, 2) / \sqrt{29}$$

$$= \underline{(3/\sqrt{29}, -4/\sqrt{29}, 2/\sqrt{29})}$$

Part 3: (success)

a) Q1 using Newell's method

$$N_x = (1 - 2)(1 + 1) + (2 - 0)(1 + 4) + (0 - 1)(4 + 1) = 3$$

$$N_y = (1 - 1)(1 + 1) + (1 - 4)(1 + 3) + (4 - 1)(3 + 1) = 0$$

$$N_z = (1 - 1)(1 + 2) + (1 - 3)(2 + 0) + (3 - 1)(0 + 1) = -2$$

Normal = (3, 0, -2), same answer

b) (1, 1, 2), (2, 0, 5), (5, 1, 4), (6, 0, 7)

$$N_x = (1 - 0)(2 + 5) + (0 - 1)(5 + 4) + (1 - 0)(4 + 7) + (0 - 1)(7 + 2) = 0$$

$$N_y = (2 - 5)(1 + 2) + (5 - 4)(2 + 5) + (4 - 7)(5 + 6) + (7 - 2)(6 + 1) = 0$$

$$N_z = (1 - 2)(1 + 0) + (2 - 5)(0 + 1) + (5 - 6)(1 + 0) + (6 - 1)(0 + 1) = 0$$

Normal = (0, 0, 0)

Part 4: (success)

$$A = (2, -1, 1)^T$$

$$B = (1, 1, -1)^T$$

$$a) \quad |A| |B| \cos(\theta) = A \cdot B$$

$$A \cdot B = (2)(1) + (-1)(1) + (1)(-1) = 2 - 1 - 1 = 0$$

$$|A| = \sqrt{2^2 - 1^2 + 1^2} = \sqrt{6}$$

$$|B| = \sqrt{1^2 + 1^2 - 1^2} = \sqrt{3}$$

$$\cos(\theta) = 0 / (\sqrt{6} * \sqrt{3}) = 0$$

$$\theta = \cos^{-1}(0) = \underline{90 \text{ degrees}}$$

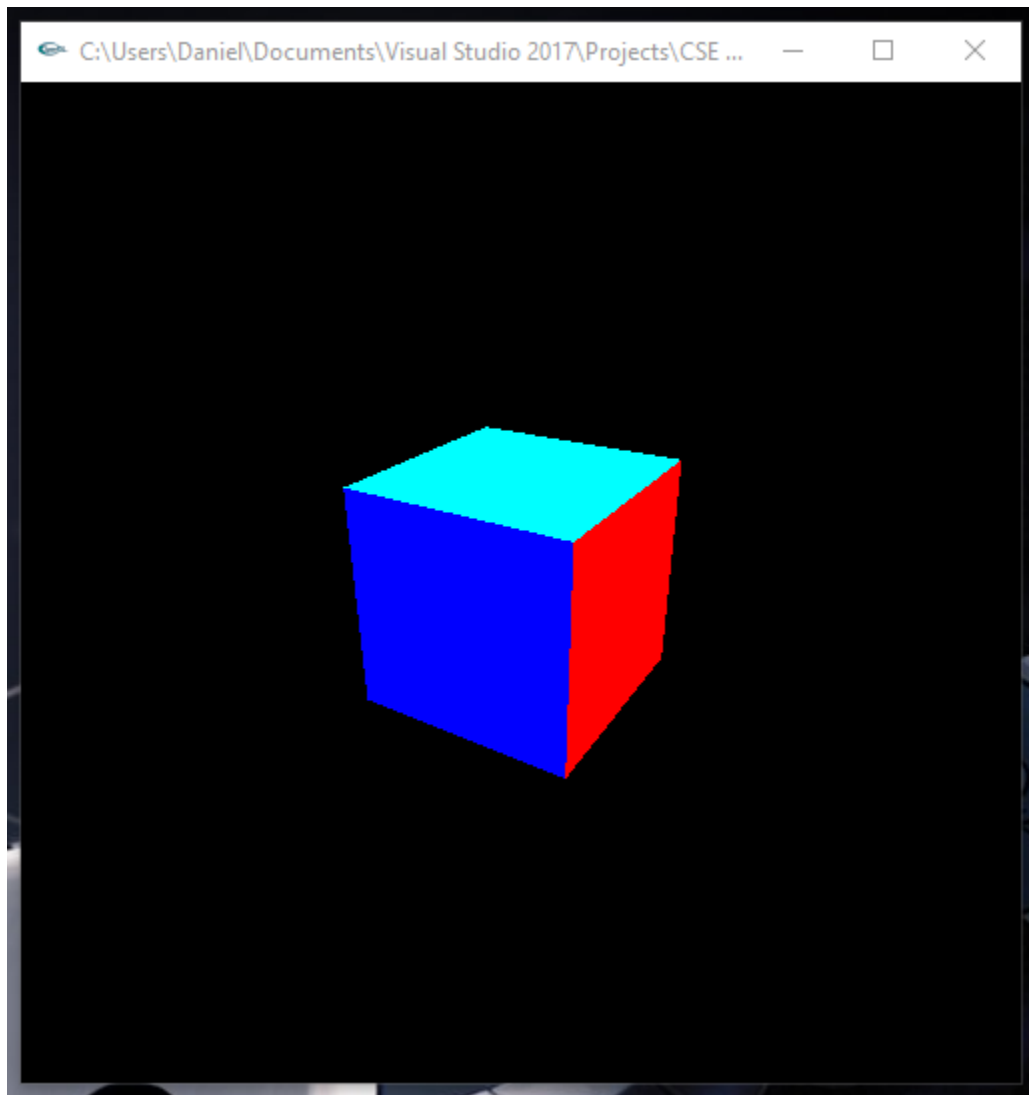
$$b) \quad \text{Unit normal} = N / |N| = A \times B / |A \times B|$$

$$A \times B = (1 - 1)i + (1 + 2)j + (2 + 1)k = 0i + 3j + 3k$$

$$\text{Unit normal} = (0, 3, 3) / \sqrt{0^2 + 3^2 + 3^2} = (0, 3, 3) / \sqrt{18}$$

$$= \underline{(0, 3/\sqrt{18}, 3/\sqrt{18})}$$

Part 5: (success)



```
void drawCube()
{
    glLoadIdentity();           /* clear the matrix */
    /* viewing transformation */
    gluLookAt(3.0, 3.0, 5.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0);

    static GLint vertices[] = { -1, -1, -1, //0
                                1, -1, -1,
                                1, 1, -1,
                                -1, 1, -1, //3
                                -1, -1, 1,
                                1, -1, 1,
                                1, 1, 1, //6
                                -1, 1, 1 }; //7
```

```

glVertexPointer(3, GL_INT, 0, vertices);

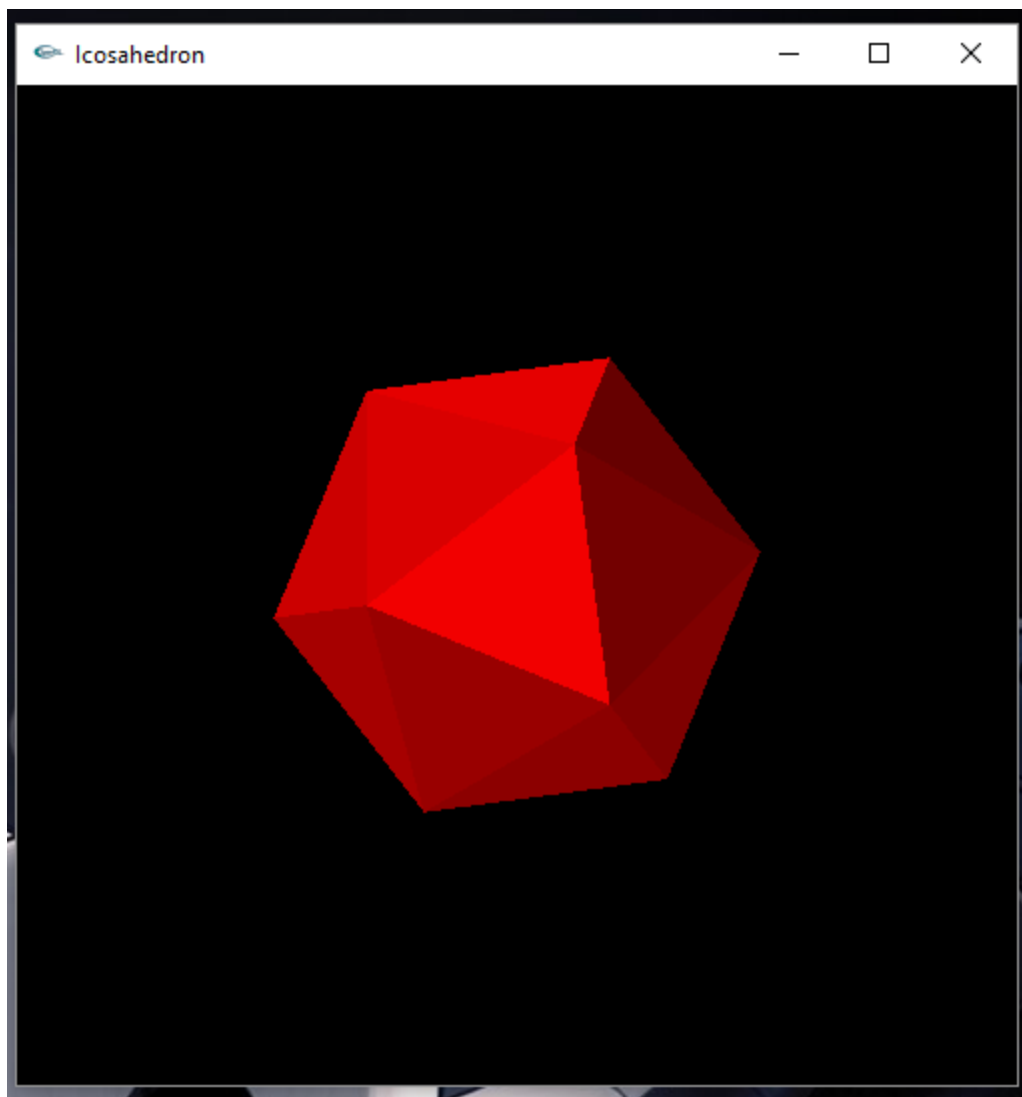
glEnable(GL_CULL_FACE);
glCullFace(GL_BACK);

static GLubyte frontIndices[] = { 4, 5, 6, 7 };
static GLubyte rightIndices[] = { 1, 2, 6, 5 };
static GLubyte bottomIndices[] = { 0, 1, 5, 4 };
static GLubyte backIndices[] = { 0, 3, 2, 1 };
static GLubyte leftIndices[] = { 0, 4, 7, 3 };
static GLubyte topIndices[] = { 2, 3, 7, 6 };

glColor3f(0.0, 0.0, 1.0);
glDrawElements(GL_QUADS, 4, GL_UNSIGNED_BYTE, frontIndices);
glColor3f(1.0, 0.0, 0.0);
glDrawElements(GL_QUADS, 4, GL_UNSIGNED_BYTE, rightIndices);
glColor3f(1.0, 1.0, 0.0);
glDrawElements(GL_QUADS, 4, GL_UNSIGNED_BYTE, bottomIndices);
glColor3f(1.0, 0.0, 1.0);
glDrawElements(GL_QUADS, 4, GL_UNSIGNED_BYTE, backIndices);
glColor3f(0.0, 1.0, 0.0);
glDrawElements(GL_QUADS, 4, GL_UNSIGNED_BYTE, leftIndices);
glColor3f(0.0, 1.0, 1.0);
glDrawElements(GL_QUADS, 4, GL_UNSIGNED_BYTE, topIndices);
}

```

Part 6: (success)



```
#define X .525731112119133606
#define Z .850650808352039932

static GLfloat vdata[12][3] = {
    {-X, 0.0, Z}, {X, 0.0, Z}, {-X, 0.0, -Z}, {X, 0.0, -Z},
    {0.0, Z, X}, {0.0, Z, -X}, {0.0, -Z, X}, {0.0, -Z, -X},
    {Z, X, 0.0}, {-Z, X, 0.0}, {Z, -X, 0.0}, {-Z, -X, 0.0}
};
static GLuint tindices[20][3] = {
    {0,4,1}, {0,9,4}, {9,5,4}, {4,5,8}, {4,8,1},
    {8,10,1}, {8,3,10}, {5,3,8}, {5,2,3}, {2,7,3},
    {7,10,3}, {7,6,10}, {7,11,6}, {11,0,6}, {0,1,6},
```

```
{6,1,10}, {9,0,11}, {9,11,2}, {9,2,5}, {7,2,11} };
```

```
void display(void)
{
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
    glMatrixMode(GL_MODELVIEW); // position and aim the camera
    glLoadIdentity();
    gluLookAt(8.0, 8.0, 8.0, 0.0, 0.0, 0.0, 1.0, 0.0);

    glEnable(GL_CULL_FACE);
    glCullFace(GL_BACK);

    glBegin(GL_TRIANGLES);
    for (int i = 0; i < 20; i++)
    {
        glColor3f(i / 20.0, 0.0, 0.0); //has no effect if Light
enabled
        glVertex3fv(&vdata[tindices[i][0]][0]);
        glVertex3fv(&vdata[tindices[i][1]][0]);
        glVertex3fv(&vdata[tindices[i][2]][0]);
    }
    glEnd();
    glFlush();
}
```

Summary:

This assignment focused on finding the dot product, cross product (normal), and unit normal of various vectors, a plane, and a sphere. I was able to calculate these as seen by the steps shown above and also used a new method provided called Newell's method to find the normal of two different sets of vectors. The next half of the assignment was to create a program that draws a cube with different colored faces of which I was able to create, compile, and run without errors. The next part of the programming section was to create either an icosahedron or a dodecahedron of which I made the former and was able to compile and run without errors. I believe I have earned the full 60 points for the assignment.