2. Granger wants to create a magic potion. In order to make the magic potion, she needs to mix powder A and powder B in the ratio of  $M_a: M_b$ . The pharmacy sells n bottles, where bottle i costs  $c_i$ , contains  $a_i$  grams of powder A, and  $b_i$  grams of powder B. Provided that Granger has to use all the powder she bought, design a dynamic programming algorithm to determine the minimum budget needed to construct the potion, or assert that no such formulation is possible, and analyze the runtime. You may assume that  $M_a$ ,  $M_b$ ,  $a_i$  and  $b_i$  are all integers.