

Lab 2

Exercise 1 - Degrees of Flexibility... Regression vs Smooth Splines

- a) Fit a Regression model that predicts miles per gallon based on weight and then plot the regression line in red color with thickness=3.
- b) Fit a spline with 2 degrees of freedom to our data and then plot it. What do you observe?
- c) Increase the flexibility of our model by adding more d.f. (try 3, 20, 100 d.f.)
- d) Is the last spline produced above flexible? Does it match the data well? Would this model be powerful for prediction?

Exercise 2 - How to choose the optimal method? Cross-validation technique

- a) Divide the data equally into two groups (training and testing).
- b) Fit a spline with 5 degrees of freedom and then compute the prediction mean squared error on the testing data.
- c) Try many different splines and choose the one with the smallest prediction error (Hint: make a loop).
- d) Make a plot, where the x-axis will represent the degrees of freedom and y-axis will represent the cross validation error (or prediction mean squared error).