



MRBTP: Efficient Multi-Robot Behavior Tree Planning and Collaboration

Session: Robotics (2/4)

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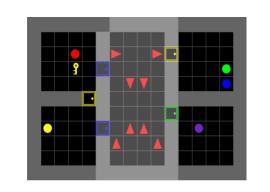
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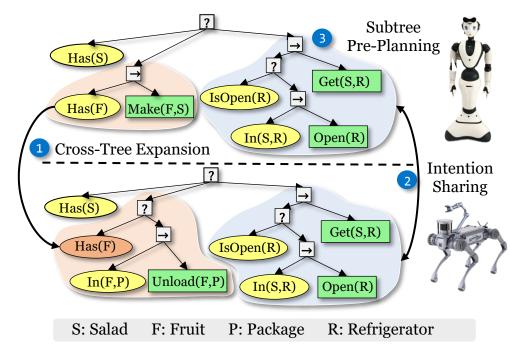
Introduction

- Multi-robot systems (MRS)
 - robots with diverse capabilities, improved performance and fault tolerance
 - requires an efficient and robust control architecture
- Behavior Trees (BTs)
 - a popular control architecture for robot behaviors
 - modularity, interpretability, reactivity, and robustness

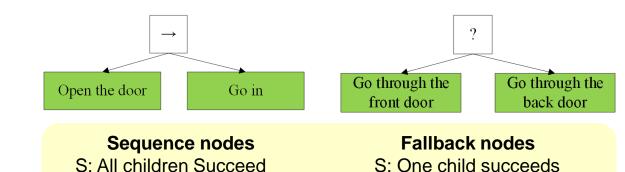
■ BT in MRS

- BT Planning for a Single Robot
 - > **Sound and Complete** (Proven by BT Expansion^[1])
- Our Contribution in BT Planning for Multi-Robots
 - > MRBTP: theoretical guarantees of both soundness and completeness
 - > Cross-Tree Expansion and Intention Sharing: Maintain robustness while enhancing execution performance
 - > Optional Plugin (LLM-based subtrees pre-planning): Improves planning and execution efficiency





- ☐ Classic Behavior Tree Representation
 - BT: a directed rooted tree
 - Root at the top (usually omitted in graphics)
 - Internal: control-flow nodes
 - Leaf: condition/action nodes
 - Returns to the parent: R={Success, Running, Failure}*
- Behavior Trees: a running example
 - Robot entering a room



Other control-flow nodes: Parallel nodes and decorator nodes.

Go in Break the door Open the door Door is open

The BT can react and adapt to different run-time situations:

Door is open

F: One child Fails

R: Others

Directly go in

Door not open

Open the door

Opening fails

Break the door

Someone helps open it → Skip breaking and go in

F: All children fail

R: Others

For more details, we refer the readers to the book Behavior Trees in Robotics and AI: An Introduction, Michele Colledanchise, Petter Ögren, CRC Press.

^{*}Condition nodes only return success or failure.

- BT Expansion^[1]: A sound and complete algorithm for single-robot BT planning
 - STRIPS-style planning states and actions
 - > An action a is a three tuple pre(a),add(a),del(a)>, consisting of the precondition, add effects and delete effects of the action.

$$add(a) \cap del(a) = \emptyset$$

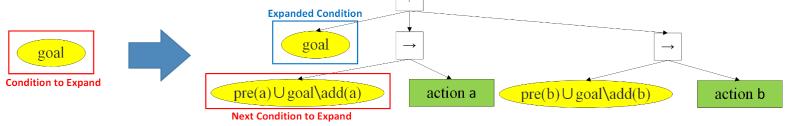
 $add(a) \cap pre(a) = \emptyset$

 $s_{t+k} = f_a(s_t) = s_t \cup add(a) \backslash del(a)$

Properties for well-defined actions*

State transition of a BT executing a*

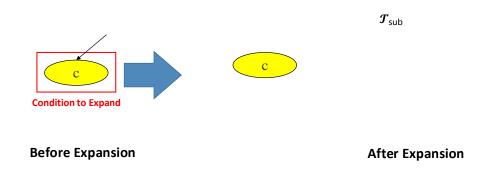
- Input & Output
 - ➤ **Input**: Goal, Initial State, the finite set of actions
 - > Output: Goal-Oriented BT
- The one-step expansion



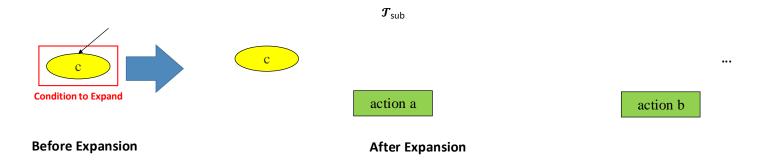
The Primary BT

BT Expanded after One Iteration

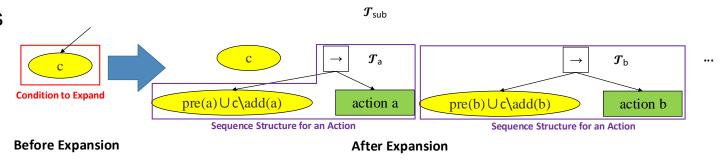
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 - ➤ Input: Goal, Initial State, the finite set of actions
 - ➤ Output: Goal-Oriented BT
 - The one-step expansion
 - 1. Preserve condition c



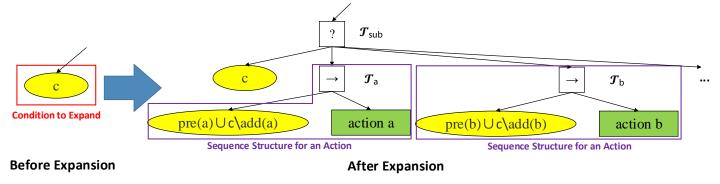
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 - The one-step expansion
 - 1. Preserve condition c
 - 2. Select actions



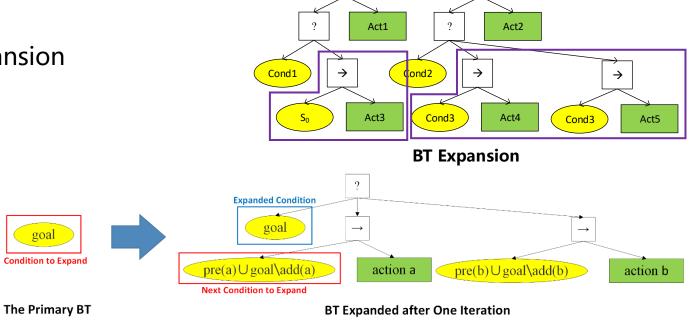
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 - The one-step expansion
 - 1. Preserve condition c
 - 2. Select actions
 - 3. Construct sequence structures



- BT Expansion^[1]: A sound and complete algorithm for single-robot BT planning
 - Input & Output
 - ➤ Input: Goal, Initial State, the finite set of actions
 - ➤ Output: Goal-Oriented BT
 - The one-step expansion
 - Preserve condition c
 - 2. Select actions
 - Construct sequence structures
 - 4. Link to the top fallback node



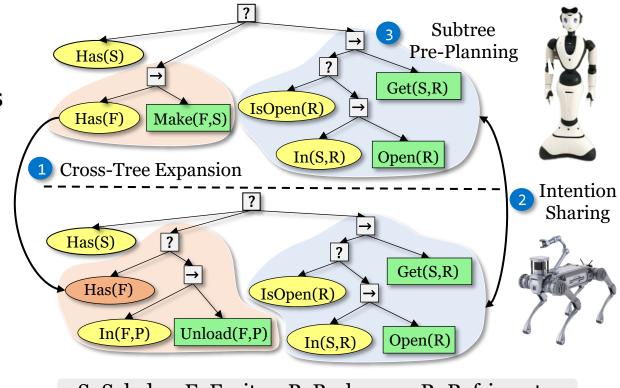
- BT Expansion^[1]: A sound and complete algorithm for single-robot BT planning
 - Input & Output
 - ➤ Input: Goal, Initial State, the finite set of actions
 - ➤ Output: Goal-Oriented BT
 - The one-step expansion -> BT Expansion
 - Preserve condition c
 - 2. Select actions
 - 3. Construct sequence structures
 - 4. Link to the top fallback node
 - 5. Repeat 2-4 until the BT can run in *Initial State*, or all conditions expanded.



 \rightarrow

Goal

- BT Planning for Multi-Robots
 - Input & Output
 - > Input: Team Goal, Initial State, Finite Action Set for each Robot
 - > Output: Goal-Oriented BT for each Robot
- □ Challenges
 - How to coordinating **heterogeneous actions** across multiple BTs to achieve team goals?
 - How to enhancing fault tolerance for **homogeneous actions** without redundant execution?

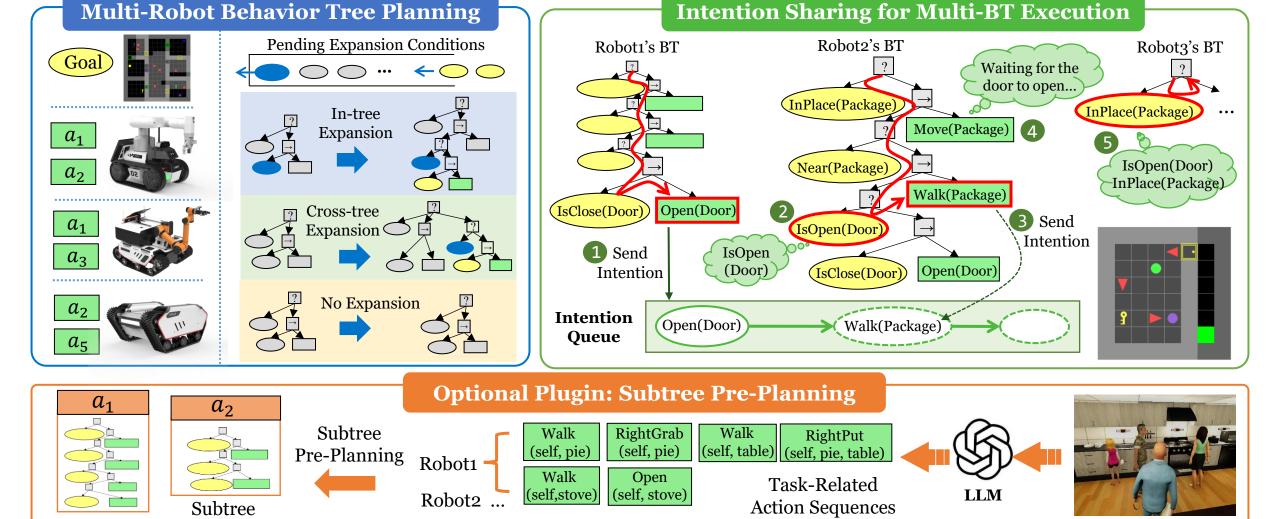


S: Salad

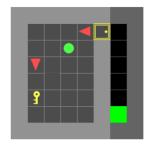
F: Fruit

P: Package

R: Refrigerator







① Multi-Robot Behavior Tree Planning

Preserve condition g

```
Move(P)

Open(Door)
```

```
Algorithm 2: MABTP
```

```
Input: problem \langle \mathcal{S}, \mathcal{L}, \{\mathcal{A}_i\}_{i=1}^n, \mathcal{M}, s_0, c \rangle
Output: solution \Phi = \{\mathcal{T}_i\}_{i=1}^n
```

```
1: C_U \leftarrow \{g\} \triangleright conditions to be explored

2: C_E \leftarrow \emptyset \triangleright expanded conditions

3: for i = 1 to n do

4: T_i \leftarrow Fallback(g) \triangleright init the BTs

5: while C_U \neq \emptyset do
```

```
5: while C_U \neq \emptyset do
          c \leftarrow \text{Pop}\left(\mathcal{C}_{U}\right)
                                                                                \triangleright explore c
          if HasSubSet (c, C_E) then continue
                                                                                    ▷ prune
          for i = 1 to n do
             \mathcal{T}_i, \mathcal{C}_{new} \leftarrow \texttt{ExpandOneRobot}(\mathcal{T}_i, \mathcal{A}_i, c)
              if HasSubSet (s_0, \mathcal{C}_{new}) then
10:
                  return \Phi = \{\mathcal{T}_i\}_{i=1}^n
                                                                   > return a solution
11:
              \mathcal{C}_E \leftarrow \mathcal{C}_E \cup \mathcal{C}_{new}
12:

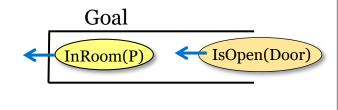
    b add new conditions

13:
              \mathcal{C}_U \leftarrow \mathcal{C}_U \cup \mathcal{C}_{new}
14: return Unsolvable
```

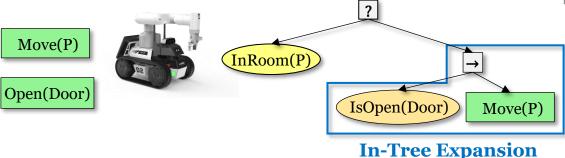


① Multi-Robot Behavior Tree Planning

- 1. Preserve condition g
- 2. One-step expansion of each robot's BT







Algorithm 2: MABTP

Input: problem $\langle S, \mathcal{L}, \{\overline{\mathcal{A}_i}\}_{i=1}^n, \overline{\mathcal{M}}, s_0, c \rangle$ **Output**: solution $\Phi = \{\mathcal{T}_i\}_{i=1}^n$

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```

```
5: while C_U \neq \emptyset do
6: c \leftarrow \text{Pop}(C_U)
```

6: $c \leftarrow \text{Pop}(\mathcal{C}_U)$ \triangleright explore c7: **if** HasSubSet (c, \mathcal{C}_E) **then continue** \triangleright prune

```
8: for i=1 to n do
9: \mathcal{T}_i, \mathcal{C}_{new} \leftarrow \texttt{ExpandOneRobot}(\mathcal{T}_i, \mathcal{A}_i, c)
```

```
10: if HasSubSet (s_0, \mathcal{C}_{new}) then
11: return \Phi = \{\mathcal{T}_i\}_{i=1}^n  \triangleright return a solution
```

12: $C_E \leftarrow C_E \cup C_{new}$

13: $C_U \leftarrow C_U \cup C_{new}$ \triangleright add new conditions

14: return Unsolvable



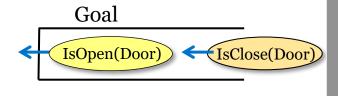
① Multi-Robot Behavior Tree Planning

- 1. Preserve condition g
- 2. One-step expansion of each robot's BT
 - In-Tree Expansion
 - Cross-Tree Expansion

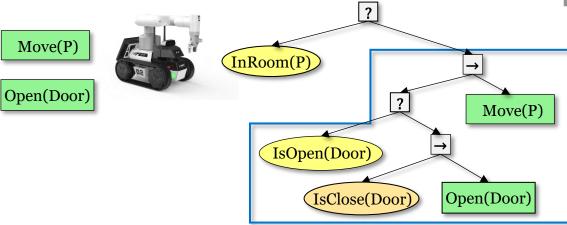
Algorithm 1: One-step cross-tree expansion

- 1: **function** ExpandOneRobot ($\mathcal{T}, \mathcal{A}, c$)
- 2: $\mathcal{T}_{new} \leftarrow c$ \triangleright newly expanded subtree
- 3: $C_{new} \leftarrow \emptyset$ pewly expanded conditions
- 4: **for each** action $a \in A$ **do**
- 5: **if** $c \cap (pre(a) \cup add(a) \setminus del(a)) \neq \emptyset$ and $c \setminus del(a) = c$ **then**
- 6: $c_a \leftarrow pre(a) \cup c \setminus add(a)$
- 7: $\mathcal{T}_a \leftarrow Sequence(c_a, a)$
- 8: $\mathcal{T}_{new} \leftarrow Fallback(\mathcal{T}_{new}, \mathcal{T}_a)$
- 9: $C_{new} \leftarrow C_{new} \cup \{c_a\}$
- 10: **if** $C_{new} \neq \emptyset$ **then**
- 11: **if** ConditionInTree(c, \mathcal{T}) **then**
- 12: Replace c with \mathcal{T}_{new} in \mathcal{T} \triangleright in-tree expand
- 13: else if $\mathcal{T}_{new} \neq c$ then
- 14: $\mathcal{T} \leftarrow Fallback(\mathcal{T}, \mathcal{T}_{new}) \triangleright cross-tree expand$

15: **return** $\mathcal{T}, \mathcal{C}_{new}$







In-Tree Expansion



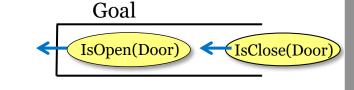
① Multi-Robot Behavior Tree Planning

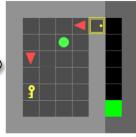
- Preserve condition g
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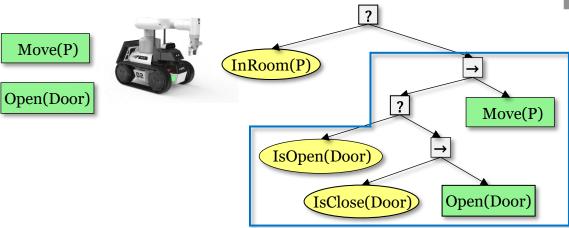
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- 13: else if $\mathcal{T}_{new} \neq c$ then
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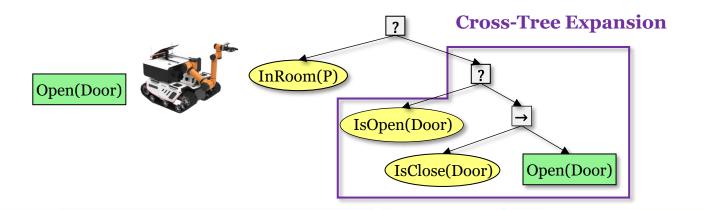
15: **return** $\mathcal{T}, \mathcal{C}_{new}$







In-Tree Expansion



1 Multi-Robot Behavior Tree Planning

- Preserve condition g
- 2. One-step expansion of each robot's BT
 - In-Tree Expansion
 - Cross-Tree Expansion

☐ Proof of Soundness and Completeness

Definition 1 (Multi-BT System). A n-robot BT system is a four-tuple $\langle \Phi, f_{\Phi}, r_{\Phi}, \Delta t_{\Phi} \rangle$, where $\Phi = \{\mathcal{T}_i\}_{i=1}^n$ is the set of BTs, $f_{\Phi} : \mathcal{S} \mapsto \mathcal{S}$ is the team state transition function, Δt_{Φ} is the team time step, $r_{\Phi} : \mathcal{S} \mapsto \{S, R, F\}$ is the team region partition.

Definition 2 (Finite Time Successful). Φ is finite time successful (FTS) from region of attraction (ROA) R to condition c, if $\forall s_0 \in R$ there is a finite time τ such that for any $t < \tau$, $r_{\Phi}(s_t) = R$, and for any $t \geq \tau$, $r_{\Phi}(s_t) = S$, $c \in s_t$.

```
Algorithm 2: MABTP
Input: problem \langle \mathcal{S}, \mathcal{L}, \{\mathcal{A}_i\}_{i=1}^n \overline{\mathcal{M}, s_0, c} \rangle
Output: solution \Phi = \{\mathcal{T}_i\}_{i=1}^n
  1: \mathcal{C}_U \leftarrow \{g\}
                                                  ⊳ conditions to be explored
  2: C_E \leftarrow \emptyset
                                                          3: for i = 1 to n do
  4: \mathcal{T}_i \leftarrow Fallback(q)
                                                                        ⊳ init the BTs
  5: while C_{IJ} \neq \emptyset do
          c \leftarrow \text{Pop}\left(\mathcal{C}_{U}\right)
                                                                            \triangleright explore c
          if HasSubSet (c, \mathcal{C}_E) then continue
          for i = 1 to n do
              \mathcal{T}_i, \mathcal{C}_{new} \leftarrow \text{ExpandOneRobot}(\mathcal{T}_i, \mathcal{A}_i, c)
              if HasSubSet (s_0, \mathcal{C}_{new}) then
                 return \Phi = \{\mathcal{T}_i\}_{i=1}^n
11:
                                                                ⊳ return a solution
              C_E \leftarrow C_E \cup C_{new}

    b add new conditions

              \mathcal{C}_U \leftarrow \mathcal{C}_U \cup \mathcal{C}_{new}
 14: return Unsolvable
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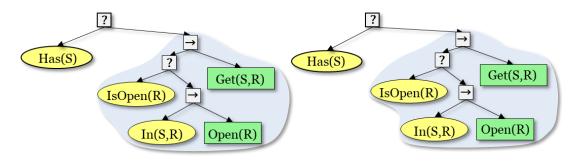
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Algorithm 1: One-step cross-tree expansion
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                                                  \mathcal{T}_{new} \leftarrow c
                                             > newly expanded conditions
         \mathcal{C}_{new} \leftarrow \emptyset
          for each action a \in \mathcal{A} do
             if c \cap (pre(a) \cup add(a) \setminus del(a)) \neq \emptyset and c \setminus
              del(a) = c then
                  c_a \leftarrow pre(a) \cup c \setminus add(a)
                  \mathcal{T}_a \leftarrow Sequence(c_a, a)
                  \mathcal{T}_{new} \leftarrow Fallback(\mathcal{T}_{new}, \mathcal{T}_a)
                  C_{new} \leftarrow C_{new} \cup \{c_a\}
         if C_{new} \neq \emptyset then
             if ConditionInTree(c, \mathcal{T}) then
                  Replace c with \mathcal{T}_{new} in \mathcal{T} \triangleright in-tree expand
              else if \mathcal{T}_{new} \neq c then
                  \mathcal{T} \leftarrow Fallback(\mathcal{T}, \mathcal{T}_{new}) \quad \triangleright \text{ cross-tree expand}
15: return \mathcal{T}, \mathcal{C}_{new}
```

Proposition 1. Given \mathcal{T} is FTS from R to g, if \mathcal{T} is expanded by Algorithm 1 to \mathcal{T}' given c, c is in \mathcal{T} and $C_{new} \neq \emptyset$, then \mathcal{T}' is FTS from $R' = R \cup \{s \in \mathcal{S} | c_a \subseteq s, c_a \in \mathcal{C}_{new}\}$ to g.

Proposition 2. If \mathcal{T} is expanded by Algorithm 1 to \mathcal{T}' given c, c is not in \mathcal{T} and $\mathcal{C}_{new} \neq \emptyset$, then \mathcal{T}' is FTS from $\mathcal{S}_{new} = \{s \in \mathcal{S} | c_a \subseteq s, c_a \in \mathcal{C}_{new}\}$ to c.

Proposition 4. Algorithm 2 is sound, i.e. if it returns a result Φ rather than Unsolvable, then Φ is a solution of Problem 1.

Proposition 5. Algorithm 2 is complete, i.e., if Problem 1 is solvable, the algorithm returns a Φ which is a solution.



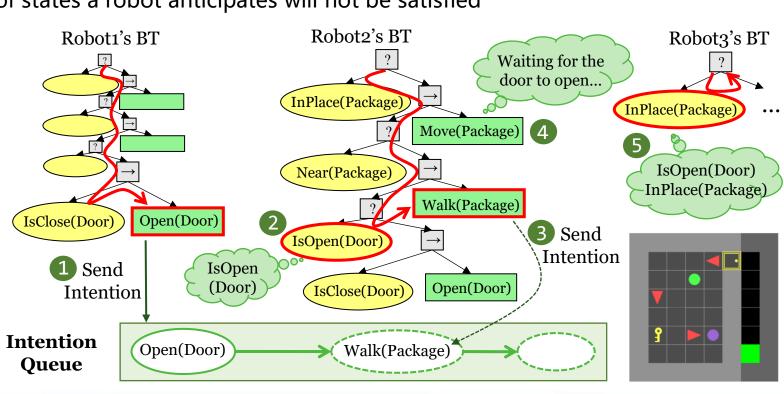
② Intention Sharing for Multi-BT Execution

- Enhancing fault tolerance for homogeneous actions without redundant execution
- Intention Queue
 - > Belief Success Space: The set of states a robot anticipates will be satisfied
 - > Belief Failure Space: The set of states a robot anticipates will not be satisfied
- Parallelism and Blocking

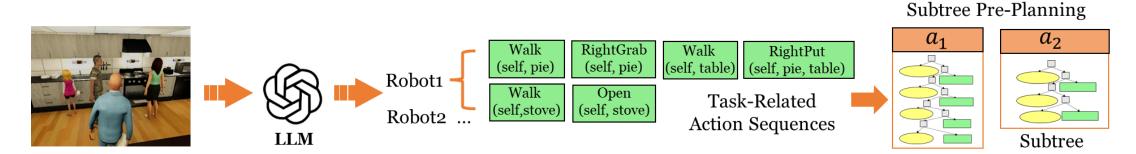
$$\mathcal{B}_i^S = \bigcup_{k=1}^{j-1} \left(add(a_k) \setminus del(a_k) \right)$$

$$\mathcal{B}_i^F = \bigcup_{k=1}^{j-1} \left(del(a_k) \setminus add(a_k) \right)$$

Robot i's Belief Space (j: Index in the Queue)



- **3 Optional Plugin: Subtree Pre-Planning**
 - During planning: Repeated tree generation due to overlapping action spaces
 - During execution: High communication overhead from short-horizon atomic actions

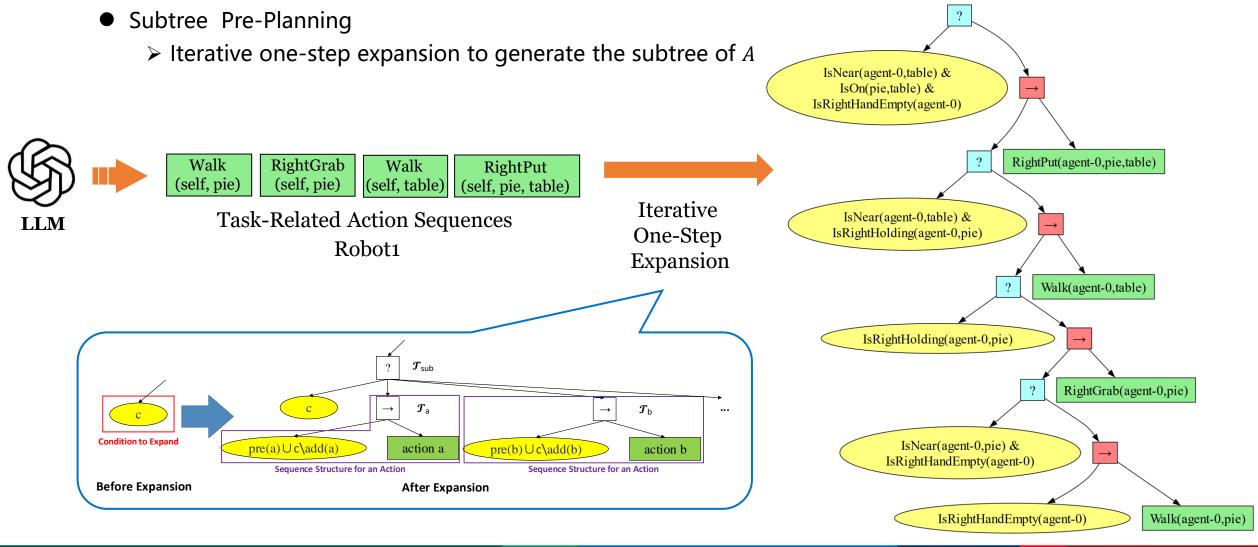


- Acquiring task-related action sequences via LLM
 - \triangleright Preconditions, Add Effects, and Delete Effects of the Action Sequence $A=(a_1,a_1,...,a_1)$

$$pre(A) = \bigcup_{j=1}^{m} \left(pre(a_j) \setminus \bigcup_{k=1}^{j} add(a_j) \right) \qquad add(A) = \bigcup_{j=1}^{m} \left(add(a_j) \setminus del(a_j) \right) - pre(A) \qquad del(A) = \bigcup_{j=1}^{m} \left(del(a_j) \setminus add(a_j) \right)$$

- Subtree Pre-Planning
 - ➤ Iterative one-step expansion to generate the subtree of A

3 Optional Plugin: Subtree Pre-Planning



- Scenarios
 - Warehouse Management
 - ➤ Minigrid^[1], 4-8 robots in 4 rooms with random packages
 - **■** Home Service
 - ➤ VirtualHome^[2], 2-4 robots handle 10+ objects and 100+ actions
- Settings
 - \blacksquare Homogeneity α
 - > The proportion of redundant actions assigned to robots
 - $> \alpha = 1$: complete homogeneity
 - $> \alpha = 0$: complete heterogeneity
 - Intention Sharing
 - ➤ Atomic IS: intention sharing among atomic action
 - > Subtree IS: intention sharing among subtree

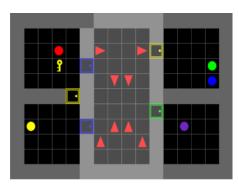




Table 1: Action predicates for different scenarios

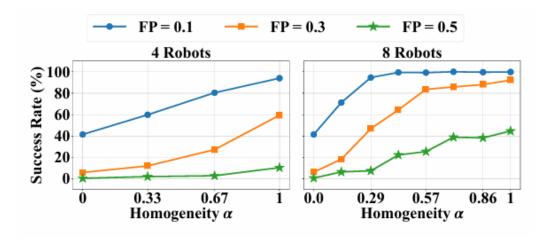
	-							
Scenarios	Included Action Predicates							
Warehouse Mangement	GoToInRoom, GoBtwRoom, PickUp, PutInRoom, PutNearInRoom, Toggle							
Home Service	Walk, LeftPut, LeftPutIn, LeftGrab, RightGrab, Open, Close RightPut, RightPutIn, SwitchOn,SwitchOff							

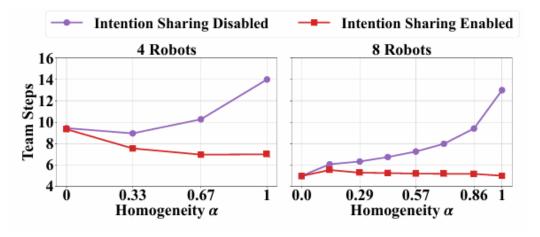
- **□** Evaluation Metrics
 - Success Rate (SR): Task success rate across trials
 - Team Steps (TS): Total steps for all robots to complete tasks in parallel
 - Total Robot Steps (RS): Sum of steps taken by each robot independently
- Performance Comparison
 - MRBTP achieves a 100% success rate across all settings due to its cross-tree expansion
 - MRBTP outperforms BT-Expansion in execution efficiency due to intention sharing

Table 1: Performance comparison with baseline in warehouse management (4 robots, averaged over 500 trials).

Method	α	= 1		lphapprox0.5	$\alpha = 0$			
Withou	SR(%)	TS	RS	SR(%)	SR(%)			
BT-Expansion	100		33.8	12.4	4.6			
MRBTP	100	5.8	15.3	100	100			

- Robustness
 - Action Failure Probability (FP): The probability that a robot fails to execute an action
 - Robustness improves with higher homogeneity and more robots
- ☐ Impact of Intention Sharing on Execution Efficiency
 - Intention sharing **reduces team steps** and maintains superior execution efficiency
 - In fully heterogeneous scenarios, intention sharing achieves the greatest efficiency gains





(a) The impact of homogeneity on robustness

(b) The impact of intention sharing on execution efficiency

■ Impact of Task-Specific Subtree Pre-Planning

- Subtree pre-planning and reuse significantly reduces BTs planning time
- Intention sharing within subtrees improves execution efficiency while minimizing communication overhead

□ LLMs and Feedback

- Feedback (F) and No Feedback (NF)
- Feedback: grammar errors, Insufficient/incoherent action sequences,
- Feedback effectively enhances both planning and execution efficiency
- It becomes more effective as the reasoning ability of LLMs improves

Table 4: Execution efficiency across different LLMs under $\alpha = 1$ with subtree and subtree intention sharing.

Models	N	o Feed	back	Feedback					
Wiodels	TS	RS	Comm.	TS	RS	Comm.			
GPT-3.5-turbo	81.6	223.6	5.1	80.0	219.0	5.1			
GPT-40-mini	78.9	217.4	6.7	77.1	205.2	6.6			
GPT-4o	77.4	200.9	6.3	74.9	190.7	6.3			

Table 3: Planning efficiency with pre-planned subtrees. The average response time per LLM invocation is 4.2 seconds.

Homogeneity	Subtree	Feedback	EC	PT (s)
	-	-	8033.3	Timeout
$\alpha = 1$	✓	-	998.1	12.4
	✓	✓	384.3	3.7
lphapprox 0.5	-	-	7882.5	Timeout
	✓	-	623.8	7.2
	✓	✓	267.9	2.6
lpha=0	-	-	2695.5	20.2
	✓	-	576.6	5.6
	✓	✓	146.8	1.4

Table 2: Execution efficiency with subtree pre-planning and intention sharing.

Homogo	eneity	,		α =	= 1		lphapprox 0.5 $lpha=0$												
Subtre Subtre Atomi	ee IS	- - -	- - ⁄	√ - -	✓ - ✓	✓ ✓ -	√ √ √	- - -	- - -	✓ - -	✓ - ✓	✓ ✓ -	√ √	- - -	- - ⁄	✓ - -	✓ - ✓	✓ ✓ -	1 1 1
TS	NF F	161	159.4 -		109.6 114.2				137.5		119.6 126.0			73.7	68.5	96.1 107.1	94.8 106.4	75.6 70.4	78.0 76.8
RS	NF F	570.8	557.3	374 377	359.4 370.9			385.2	380.1		326.6 348.2			128.6	128.6		128.6 128.6		128.6 128.6
Comm.	NF F	0.0	63.8	0.0	7.1 4.8	6.7 6.6	14.1 12.2	0.0	43.5	0.0	8.0 4.4	7.1 6.4	20.9 13.2	0.0	15.2	0.0	2.8 0.7	6.5 5.2	9.3 6.0

Summary

□ Conclusion

- > MRBTP, the first **sound and complete** algorithm for solving the multi-robot BT planning problem
- > MRBTP uses **cross-tree expansion** to coordinate heterogeneous actions and enhances robustness and execution efficiency with backup structures and **intention sharing**
- > Optional LLMs plugin speeds up planning and improves collaboration with pre-planned long-horizon subtrees

☐ Future Work

- > Real-time deadlock detection and resolution in BT execution
- > Efficient large-scale BT communication, coordination, and emergent intelligence
- > Planning under uncertainty and periodic tasks





MRBTP: Efficient Multi-Robot Behavior Tree Planning and Collaboration

Thank you!

Q & A

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Code: https://github.com/DIDS-EI/MRBTP