AIM-CU

Release 1.0.0

Smriti Prathapan, Berkman Sahiner, Dhaval Kadia, Ravi K. Samala

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A CUSUM-based tool for AI Monitoring

AIM-CU is a statistical tool for AI monitoring using cumulative sum (AIM-CU). AIM-CU computes:

- The parameter choices for change-point detection based on an acceptable false alarm rate
- Detection delay estimates for a given displacement of the performance metric from the target for those parameter choices.

CHAPTER

ONE

SYSTEM SETUP

Make sure R is installed in the system. Instructions for linux:

```
RUN wget -qO- https://cloud.r-project.org/bin/linux/ubuntu/marutter_pubkey.asc |  tee -a␣
↪/etc/apt/trusted.gpg.d/cran_ubuntu_key.asc
RUN add-apt-repository "deb https://cloud.r-project.org/bin/linux/ubuntu $(lsb_release -
↪cs)-cran40/"
RUN apt-get install -y --no-install-recommends r-base r-base-dev

# setup R configs
RUN echo "r <- getOption('repos'); r['CRAN'] <- 'http://cran.us.r-project.org';␣
↪options(repos = r);" > ~/.Rprofile
RUN Rscript -e "install.packages('ggplot2')"
RUN Rscript -e "install.packages('hexbin')"
RUN Rscript -e "install.packages('lazyeval')"
RUN Rscript -e "install.packages('cusumcharter')"
RUN Rscript -e "install.packages('RcppCNPy')"
RUN Rscript -e "install.packages('spc')"
```

CHAPTER

TWO

CODE EXECUTION

Clone AIM-CU repository.

```
git clone https://github.com/DIDSR/AIM-CU.git
```

Run the following commands to install required dependencies (Python = 3.10 is used).

```
apt-get -y install python3
apt-get -y install pip
cd AIM-CU
pip install -r requirements.txt
```

Run AIM-CU.

```
python3 app.py
```

Open the URL http://0.0.0.0:7860 that is running the AIM-CU locally.

CHAPTER

THREE

DEMO

AIM-CU can also be run through the demo available at https://huggingface.co/spaces/didsr/AIM-CU. If Space is paused, click on Restart button.

3.1 Methods

3.1.1 CUSUM parameters

Table 1: CUSUM parameters

Parameter	Description
μ_in	The mean of the performance metric when the process is in-control, i.e., when there is no performance drift
ARL_0	Number of observations before the control chart signals a false detection
σ_in	The in-control standard deviation of the metric
ARL_1	Number of observations before the control chart signals a true detection
k	The normalized reference value, which is related to the magnitude of change that one is interested in detecting. k = 0.5 is the default choice for detecting a unit standard deviation change
S_hi	Cumulative sum of positive changes in the metric
h	The normalized threshold or control limit (default =4). This threshold determines when the control chart signals a detection
S_lo	Cumulative sum of negative changes in the metric

3.1.2 CUSUM chart

A two-sided CUSUM control chart computes the cumulative differences or deviations of individual observations from the target mean (or in-control mean, μ_{in}). The positive and negative cumulative sums are calculated:

$$S_{hi}(d) = max(0, S_{hi}(d-1) + x_d - \hat{\mu}_{in} - K)$$
$$S_{lo}(d) = max(0, S_{lo}(d-1) - x_d + \hat{\mu}_{in} - K)$$

where d denotes a unit of time, x_d is the value of quantity being monitored at time d, $\hat{\mu}_{in}$ is the in-control mean of x_d, and K is a "reference value" related to the magnitude of change that one is interested in detecting. S_{hi} and S_{lo} are the cumulative sum of positive and negative changes. To detect a change in the observed values from the in-control mean, the CUSUM scheme accumulates deviations that are K units away from the in-control mean. Let σ_{in} denote the in-control standard deviation of x_d.

3.2 CUSUM

Cumulative Sum (CUSUM)

@author: smriti.prathapan

class package.cusum.**CUSUM**

CUSUM class and its functionalities.

change_detection(*normalized_ref_value: float = 0.5*, *normalized_threshold: float = 4*) → None

Detects a change in the process.

Parameters

- **pre_change_days** (*int*) – Number of days for in-control phase.
- **normalized_ref_value** (*float, optional*) – Normalized reference value for detecting a unit standard deviation change in mean of the process. Defaults to 0.5.
- **normalized_threshold** (*float, optional*) – Normalized threshold. Defaults to 4.

compute_cusum(*x: list[float]*, *mu_0: float*, *k: float*) → tuple[list[float], list[float], list[float]]

Compute CUSUM for the observations in x

Parameters

- **x** (*list[float]*) – Performance metric to be monitored
- **mu_0** (*float*) – In-control mean of the observations/performance metric
- **k** (*float*) – Reference value related to the magnitude of change that one is interested in detecting

Returns
Positive cumulative sum, negative cumulative sum, and CUSUM

Return type
tuple[list[float], list[float], list[float]]

initialize() → None

Initialize with the configuration file.

plot_cusum_plotly() → Figure

Plot CUSUM value using Plotly

Returns
CUSUM plot using Plotly graph object.

Return type
go.Figure

plot_input_metric_plotly() → Figure

Plot the input metric using Plotly.

Returns
Scatter plot as Plotly graph object.

Return type
go.Figure

plot_input_metric_plotly_raw() → Figure

Plot AI output using Plotly.

Returns
Scatter plot as Plotly graph object.

Return type
go.Figure

set_df_metric_csv(*data_csv: DataFrame*) → None

Assign the performance metric data to be used for CUSUM.

Parameters
data_csv (*DataFrame or TextFileReader*) – A comma-separated values (csv) file is returned as two-dimensional data structure with labeled axes.

set_df_metric_default() → None

Read the provided performance metric data to be used for CUSUM for an example.

set_init_stats(*init_days: int*) → None

Use initial days to calculate in-control mean and standard deviation.

Parameters
init_days (*int, optional*) – Initial days when observations are considered stable. Defaults to 30.

set_timeline(*data: ndarray*) → None

Set the timeline of observations.

Parameters
data (*np.ndarray*) – Data of the metric values across the observations.

3.3 ARLTheoretical

ARLTheoretical

@author: smriti.prathapan

package.ARLTheoretical.**get_ARL_1**(*h: float*, *shift_in_mean: list[float]*, *dict_ARL0_k: OrderedDict*) → DataFrame

Get the ARL1 along with k values.

Parameters

- **h** (*float*) – Normalized threshold.
- **shift_in_mean** (*list[float]*) – List of the values of shift in mean.
- **dict_ARL0_k** (*OrderedDict*) – Data dictionary of ARL0 and k

Returns
Table for ARL1 and k values.

Return type
pd.DataFrame

package.ARLTheoretical.**get_ARL_1_h_mu1_k**(*h: float*, *k: float*, *mu1: float*) → float

Calculate ARL_1 with given Shift in Mean (mu1) and k.

Parameters

- **h** (*float*) – Normalized threshold.
- **k** (*float*) – Normalized reference value.

- **mu1** (*float*) – Intended shift in mean.

Returns
Detection delay (ARL1).

Return type
float

package.ARLTheoretical.**get_ref_value**(*h: float*, *list_ARL_0: list[float]*) → tuple[DataFrame, OrderedDict]

provides normalized reference values k for provided list of ARL0, given the value of normalized threshold h.

Parameters

- **h** (*float*) – Normalized threshold.
- **list_ARL_0** (*list*) – List of ARL0 values.

Returns
Dataframe of ARL0 and k, Data dictionary of ARL0 and k; where k is normalized reference value.

Return type
tuple[pd.Dataframe, OrderedDict]

package.ARLTheoretical.**get_ref_value_k**(*h: float*, *ARL_0: float*) → float

Calculation for the reference value for given h and ARL_0.

Parameters

- **h** (*float*) – Normalized threshold.
- **ARL_0** (*float*) – ARL0 value.

Returns
Normalized reference value k.

Return type
float

3.4 Utils

Utilities to handle different operations

package.utils.**get_greattable_as_html**(*df: DataFrame*) → GT

Get the great_table as HTML from Pandas dataframe.

Parameters
df (*pd.DataFrame*) – Dataframe to rendera as a table.

Returns
Table in HTML format.

Return type
gt.GT

package.utils.**populate_summary_table_ARL0_k**(*summary_table_df_ARL0_k: DataFrame*, *h*) → GT

Populate ARLTheoretical.summary_table_df_ARL0_k.

Parameters

- **summary_table_df_ARL0_k** (*pd.DataFrame*) – Dataframe of ARL0 and its respective values of k.

- **h** (*float*) – Normalized threshold.

Returns
Table of ARL0 and k in HTML format.

Return type
gt.GT

package.utils.**populate_summary_table_ARL1_k**(*summary_table_df_ARL1_k: DataFrame*, *dict_ARL0_k: OrderedDict*, *h*) → GT

Populate Multiindex table specific for ARLTheoretical.summary_table_df_ARL1_k

Parameters

- **summary_table_df_ARL1_k** (*pd.DataFrame*) – Dataframe with ARL1 and k values.
- **dict_ARL0_k** (*OrderedDict*) – Data Dictionary with the mapping between ARL0 and k.
- **h** (*float*) – Normalized threshold.

Returns
Table for ARL1 and k in HTML format.

Return type
gt.GT

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