

AIM-CU

Version 1.0.0

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AIM-CU documentation

A CUSUM-based tool for AI Monitoring

AIM-CU is a statistical tool for AI monitoring using cumulative sum (AIM-CU). AIM-CU computes:

- The parameter choices for change-point detection based on an acceptable false alarm rate
- Detection delay estimates for a given displacement of the performance metric from the target for those parameter choices.

Code execution

Clone AIM-CU repository.

```
git clone https://github.com/DIDSR/AIM-CU.git
```

Run the following commands to install required dependencies (Python = 3.10 is used).

```
apt-get -y install python3  
apt-get -y install pip  
cd AIM-CU  
pip install -r requirements.txt
```

Run AIM-CU.

```
python3 app.py
```

Open the URL <http://0.0.0.0:7860> that is running the AIM-CU locally.

Demo

AIM-CU can also be run through the demo available at <https://huggingface.co/spaces/didsr/AIM-CU>. If Space is paused, click on Restart button.

Methods

A two-sided CUSUM control chart computes the cumulative differences or deviations of individual observations from the target mean (or in-control mean, μ_{in}). The positive and negative cumulative sums are calculated:

$$\begin{aligned} S_{hi}(d) &= \max(0, S_{hi}(d-1) + x_d - \mu_{in} - K) \\ S_{lo}(d) &= \max(0, S_{lo}(d-1) - x_d + \mu_{in} - K) \end{aligned}$$

where d denotes a unit of time, x_d is the value of quantity being monitored at time d , μ_{in} is the in-control mean of x_d , and K is a “reference value” related to the magnitude of change that one is interested in detecting. S_{hi} and S_{lo} are the cumulative sum of positive and negative changes. To detect a change in the observed values from the in-control mean, the CUSUM scheme accumulates deviations that are K units away from the in-control mean. Let σ_{in} denote the in-control standard deviation of x_d .

CUSUM

Cumulative Sum (CUSUM)

@author: smriti.prathapan

class package.cusum. CUSUM

CUSUM class and its functionalities.

change_detection (*normalized_ref_value* : float = 0.5 , *normalized_threshold* : float = 4) → None

Detects a change in the process.

Parameters :

- **pre_change_days** (int) – Number of days for in-control phase.

- **normalized_ref_value** (*float* , *optional*) – Normalized reference value for detecting a unit standard deviation change in mean of the process. Defaults to 0.5.
- **normalized_threshold** (*float* , *optional*) – Normalized threshold. Defaults to 4.

compute_cusum (*x* : *list* [*float*] , *mu_0* : *float* , *k* : *float*) → tuple [list [float] , list [float] , list [float]]

Compute CUSUM for the observations in x

Parameters :

- **x** (*list* [*float*]) – Performance metric to be monitored
- **mu_0** (*float*) – In-control mean of the observations/ performance metric
- **k** (*float*) – Reference value related to the magnitude of change that one is interested in detecting

Returns :

Positive cumulative sum, negative cumulative sum, and CUSUM

Return type :

tuple[list[float], list[float], list[float]]

initialize () → None

Initialize with the configuration file.

plot_cusum_plotly () → Figure

Plot CUSUM value using Plotly

Returns :

CUSUM plot using Plotly graph object.

Return type :

go.Figure

`plot_histogram_plotly (data , xlabel , title = ")` → Figure

Plot the histogram of the observations/performance metric being monitored using plotly

Parameters :

- `data (_type_)` – Data values to show in histogram.
- `xlabel (_type_)` – Title of the label for X-axis.
- `title (str , optional)` – Title of the plot. Defaults to "".

Returns :

Histogram as Plotly graph object.

Return type :

go.Figure

`plot_input_metric_plotly ()` → Figure

Plot the input metric using Plotly.

Returns :

Scatter plot as Plotly graph object.

Return type :

go.Figure

`set_df_metric_csv (data_csv : DataFrame)` → None

Assign the performance metric data to be used for CUSUM.

Parameters :

`data_csv (DataFrame or TextFileReader)` – A comma-separated values (csv) file is returned as two-dimensional data structure with labeled axes.

`set_df_metric_default ()` → None

Read the provided performance metric data to be used for CUSUM for an example.

`set_init_stats (init_days : int = 30)` → None

Use initial days to find in-control mean and standard deviation.

Parameters :

`init_days` (*int* , *optional*) – Initial days when observations are considered stable. Defaults to 30.

`set_timeline` (*data : ndarray*) → `None`

Set the timeline of observations.

Parameters :

`data` (*np.ndarray*) – Data of the metric values across the observations.

ARLTheoretical

ARLTheoretical

@author: smriti.prathapan

`package.ARLTheoretical.get_ARL_1` (*h : float* , *shift_in_mean : list [float]* , *dict_ARL0_k : OrderedDict*) → `DataFrame`

Get the ARL1 along with k values.

Parameters :

- `h` (*float*) – Normalized threshold.
- `shift_in_mean` (*list [float]*) – List of the values of shift in mean.
- `dict_ARL0_k` (*OrderedDict*) – Data dictionary of ARL0 and k

Returns :

Table for ARL1 and k values.

Return type :

`pd.DataFrame`

`package.ARLTheoretical.get_ARL_1_h_mu1_k (h : float , k : float , mu1 : float) → float`

Calculate ARL₁ with given Shift in Mean (mu1) and k.

Parameters :

- *h* (float) – Normalized threshold.
- *k* (float) – Normalized reference value.
- *mu1* (float) – Intended shift in mean.

Returns :

Detection delay (ARL₁).

Return type :

float

`package.ARLTheoretical.get_ref_value (h : float , list_ARL_0 : list [float]) → tuple [DataFrame , OrderedDict]`

provides normalized reference values k for provided list of ARL₀, given the value of normalized threshold h.

Parameters :

- *h* (float) – Normalized threshold.
- *list_ARL_0* (list) – List of ARL₀ values.

Returns :

Dataframe of ARL₀ and k, Data dictionary of ARL₀ and k;
where k is normalized reference value.

Return type :

tuple[pd.DataFrame, OrderedDict]

`package.ARLTheoretical.get_ref_value_k (h : float , ARL_0 : float) → float`

Calculation for the reference value for given h and ARL₀.

Parameters :

- `h (float)` – Normalized threshold.
- `ARL_0 (float)` – ARL0 value.

Returns :

Normalized reference value `k`.

Return type :

float

Utils

Utilities to handle different operations

`package.utils.get_greatable_as_html (df: DataFrame) → GT`

Get the `great_table` as HTML from Pandas dataframe.

Parameters :

`df (pd.DataFrame)` – Dataframe to render as a table.

Returns :

Table in HTML format.

Return type :

gt.GT

`package.utils.populate_summary_table_ARL0_k (summary_table_df_ARL0_k: DataFrame , h) → GT`

Populate `ARLTheoretical.summary_table_df_ARL0_k`.

Parameters :

- `summary_table_df_ARL0_k (pd.DataFrame)` – Dataframe of ARL0 and its respective values of `k`.

- `h (float)` – Normalized threshold.

Returns :

Table of ARL0 and k in HTML format.

Return type :

gt.GT

`package.utils.populate_summary_table_ARL1_k (summary_table_df_ARL1_k : DataFrame , dict_ARL0_k : OrderedDict , h) → GT`

Populate Multiindex table specific for ARLTheoretical.summary_table_df_ARL1_k

Parameters :

- `summary_table_df_ARL1_k (pd.DataFrame)` – Dataframe with ARL1 and k values.
- `dict_ARL0_k (OrderedDict)` – Data Dictionary with the mapping between ARL0 and k.
- `h (float)` – Normalized threshold.

Returns :

Table for ARL1 and k in HTML format.

Return type :

gt.GT

