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**AIM-CU**  
*Release 1.0.0*

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## A CUSUM-based tool for AI Monitoring

AIM-CU is a statistical tool for AI monitoring using cumulative sum (AIM-CU). AIM-CU computes:

- The parameter choices for change-point detection based on an acceptable false alarm rate
- Detection delay estimates for a given displacement of the performance metric from the target for those parameter choices.



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**CHAPTER  
ONE**

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## **CODE EXECUTION**

Clone AIM-CU repository.

```
git clone https://github.com/DIDSR/AIM-CU.git
```

Run the following commands to install required dependencies (Python = 3.10 is used).

```
apt-get -y install python3
apt-get -y install pip
cd AIM-CU
pip install -r requirements.txt
```

Run AIM-CU.

```
python3 app.py
```

Open the URL <http://0.0.0.0:7860> that is running the AIM-CU locally.



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**CHAPTER  
TWO**

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**DEMO**

AIM-CU can also be run through the demo available at <https://huggingface.co/spaces/didsr/AIM-CU>. If Space is paused, click on Restart button.

## 2.1 Methods

### 2.1.1 CUSUM parameters

Table 1: CUSUM parameters

Parameter	Description
$\mu_{in}$	The mean of the performance metric when the process is in-control, i.e., when there is no performance drift
ARL_0	Number of observations before the control chart signals a false detection
$\sigma_{in}$	The in-control standard deviation of the metric
ARL_1	Number of observations before the control chart signals a true detection
k	The normalized reference value, which is related to the magnitude of change that one is interested in detecting. k = 0.5 is the default choice for detecting a unit standard deviation change
S_hi	Cumulative sum of positive changes in the metric
h	The normalized threshold or control limit (default =4). This threshold determines when the control chart signals a detection
S_lo	Cumulative sum of negative changes in the metric

### 2.1.2 CUSUM chart

A two-sided CUSUM control chart computes the cumulative differences or deviations of individual observations from the target mean (or in-control mean,  $\mu_{in}$ ). The positive and negative cumulative sums are calculated:

$$\begin{aligned} S_{hi}(d) &= \max(0, S_{hi}(d-1) + x_d - \hat{\mu}_{in} - K) \\ S_{lo}(d) &= \max(0, S_{lo}(d-1) - x_d + \hat{\mu}_{in} - K) \end{aligned}$$

where  $d$  denotes a unit of time,  $x_d$  is the value of quantity being monitored at time  $d$ ,  $\hat{\mu}_{in}$  is the in-control mean of  $x_d$ , and  $K$  is a “reference value” related to the magnitude of change that one is interested in detecting.  $S_{hi}$  and  $S_{lo}$  are the cumulative sum of positive and negative changes. To detect a change in the observed values from the in-control mean, the CUSUM scheme accumulates deviations that are  $K$  units away from the in-control mean. Let  $\sigma_{in}$  denote the in-control standard deviation of  $x_d$ .

## 2.2 CUSUM

Cumulative Sum (CUSUM)

@author: smriti.prathapan

**class** package.cusum.CUSUM

CUSUM class and its functionalities.

**change\_detection**(normalized\_ref\_value: float = 0.5, normalized\_threshold: float = 4) → None

Detects a change in the process.

### Parameters

- **pre\_change\_days** (int) – Number of days for in-control phase.
- **normalized\_ref\_value** (float, optional) – Normalized reference value for detecting a unit standard deviation change in mean of the process. Defaults to 0.5.
- **normalized\_threshold** (float, optional) – Normalized threshold. Defaults to 4.

**compute\_cusum**(x: list[float], mu\_0: float, k: float) → tuple[list[float], list[float], list[float]]

Compute CUSUM for the observations in x

### Parameters

- **x** (list[float]) – Performance metric to be monitored
- **mu\_0** (float) – In-control mean of the observations/performance metric
- **k** (float) – Reference value related to the magnitude of change that one is interested in detecting

### Returns

Positive cumulative sum, negative cumulative sum, and CUSUM

### Return type

tuple[list[float], list[float], list[float]]

**initialize()** → None

Initialize with the configuration file.

**plot\_cusum\_plotly()** → Figure

Plot CUSUM value using Plotly

### Returns

CUSUM plot using Plotly graph object.

### Return type

go.Figure

**plot\_input\_metric\_plotly()** → Figure

Plot the input metric using Plotly.

### Returns

Scatter plot as Plotly graph object.

### Return type

go.Figure

**set\_df\_metric\_csv**(data\_csv: DataFrame) → None

Assign the performance metric data to be used for CUSUM.

**Parameters**

**data\_csv** (*DataFrame or TextFileReader*) – A comma-separated values (csv) file is returned as two-dimensional data structure with labeled axes.

**set\_df\_metric\_default()** → None

Read the provided performance metric data to be used for CUSUM for an example.

**set\_init\_stats(*init\_days*: int)** → None

Use initial days to calculate in-control mean and standard deviation.

**Parameters**

**init\_days** (*int, optional*) – Initial days when observations are considered stable. Defaults to 30.

**set\_timeline(*data*: ndarray)** → None

Set the timeline of observations.

**Parameters**

**data** (*np.ndarray*) – Data of the metric values across the observations.

## 2.3 ARLTheoretical

ARLTheoretical

@author: smriti.prathapan

package.ARLTheoretical.**get\_ARL\_1**(*h: float, shift\_in\_mean: list[float], dict\_ARL0\_k: OrderedDict*) → DataFrame

Get the ARL1 along with k values.

**Parameters**

- **h** (*float*) – Normalized threshold.
- **shift\_in\_mean** (*list[float]*) – List of the values of shift in mean.
- **dict\_ARL0\_k** (*OrderedDict*) – Data dictionary of ARL0 and k

**Returns**

Table for ARL1 and k values.

**Return type**

pd.DataFrame

package.ARLTheoretical.**get\_ARL\_1\_h\_mu1\_k**(*h: float, k: float, mu1: float*) → float

Calculate ARL\_1 with given Shift in Mean (mu1) and k.

**Parameters**

- **h** (*float*) – Normalized threshold.
- **k** (*float*) – Normalized reference value.
- **mu1** (*float*) – Intended shift in mean.

**Returns**

Detection delay (ARL1).

**Return type**

float

package .ARLTheoretical.**get\_ref\_value**(*h: float, list\_ARL\_0: list[float]*) → tuple[DataFrame, OrderedDict]  
provides normalized reference values k for provided list of ARL0, given the value of normalized threshold h.

**Parameters**

- **h (float)** – Normalized threshold.
- **list\_ARL\_0 (list)** – List of ARL0 values.

**Returns**

Dataframe of ARL0 and k, Data dictionary of ARL0 and k; where k is normalized reference value.

**Return type**

tuple[pd.DataFrame, OrderedDict]

package .ARLTheoretical.**get\_ref\_value\_k**(*h: float, ARL\_0: float*) → float

Calculation for the reference value for given h and ARL\_0.

**Parameters**

- **h (float)** – Normalized threshold.
- **ARL\_0 (float)** – ARL0 value.

**Returns**

Normalized reference value k.

**Return type**

float

## 2.4 Utils

Utilities to handle different operations

package.utils.**get\_greatable\_as\_html**(*df: DataFrame*) → GT

Get the great\_table as HTML from Pandas dataframe.

**Parameters**

**df (pd.DataFrame)** – Dataframe to render as a table.

**Returns**

Table in HTML format.

**Return type**

gt.GT

package.utils.**populate\_summary\_table\_ARL0\_k**(*summary\_table\_df\_ARL0\_k: DataFrame, h*) → GT

Populate ARLTheoretical.summary\_table\_df\_ARL0\_k.

**Parameters**

- **summary\_table\_df\_ARL0\_k (pd.DataFrame)** – Dataframe of ARL0 and its respective values of k.
- **h (float)** – Normalized threshold.

**Returns**

Table of ARL0 and k in HTML format.

**Return type**

gt.GT

```
package.utils.populate_summary_table_ARL1_k(summary_table_df_ARL1_k: DataFrame, dict_ARL0_k:  
OrderedDict, h) → GT
```

Populate Multiindex table specific for ARLTheoretical.summary\_table\_df\_ARL1\_k

**Parameters**

- **summary\_table\_df\_ARL1\_k** (*pd.DataFrame*) – Dataframe with ARL1 and k values.
- **dict\_ARL0\_k** (*OrderedDict*) – Data Dictionary with the mapping between ARL0 and k.
- **h** (*float*) – Normalized threshold.

**Returns**

Table for ARL1 and k in HTML format.

**Return type**

gt.GT



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