

Compiler Design

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Compiler :- Executes whole code in one time

↳ C, C++, ... → Languages for software development

Interpreter :- line by line execution

↳ Small Code Use → Web based Language

→ Compiler execute whole program at a time.

↳ Large Code Use

Ex. C, C++, Java, Pascal, COBOL, BASIC,

↳ Programming Language

* Interpreter example :- Ruby, Python, ASP.NET, Perl

↓
Scripting language

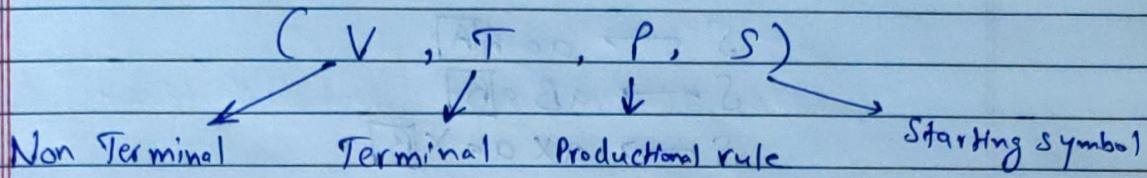
COBOL → Common Business oriented Language

BASIC → Beginner All Purpose symbolic Instruction Code.

* Markup Language → HTML, XML → No use
they just help

in ~~Interpre~~
with scripting language

* Grammar :- 4 Tuple



① Terminal :- Small letter
 $(a-z), (0-9)$

② Non Terminal :-
 $(A-Z)$

③ Production Rule :- $S \rightarrow abc$
 ↓
 P.R.

④ Starting Symbol :- $S \rightarrow abc$
 ↓
 S.S.

Regular Grammar (R.G.) → Finite length.
 Least Powerful

↳ 4 Tuple (V, T, P, S)

↳ Two form ↳ left linear Regular Grammar **
 ↳ Right linear Regular Grammar **

① left linear Regular Grammar :-

$S \rightarrow Aaa$ ↳ Non Terminal on left
 $S \rightarrow Bba$
 $S \rightarrow Xaaa$

(2)

Right linear Regular Grammar I -

$$S \rightarrow aa A[A]$$

$$S \rightarrow aB a[B]$$

$$S \rightarrow ax a = X[B]$$

★

$$S \rightarrow [A]aa[A]$$

$$S \rightarrow [B]B$$

$$S \rightarrow [Z]XAB[B]$$

$$S \rightarrow [A]aXa[B]$$

N.T.

left, Right both

Q.

$$\begin{array}{l} S \rightarrow aa \\ S \rightarrow \epsilon \\ S \rightarrow aaaa \end{array} \quad \begin{array}{c} \times \\ \times \\ \times \end{array} \quad \left. \begin{array}{c} N.T. \\ R.G. \end{array} \right\} \quad \begin{array}{c} X \\ X \end{array}$$

★

If it is R.G., then it will be C.F.G., C.R.S.G.,
Unrestricted grammar

Q. ①

$$\begin{array}{l} S \rightarrow aAA \\ S \rightarrow aab \\ A \rightarrow a \end{array} \quad \left. \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \right\} \quad \begin{array}{c} \text{Right linear grammar} \\ \text{R.G.} \end{array}$$

ii

$$\begin{array}{l} S \rightarrow aaAa \\ S \rightarrow (AA) \\ S \rightarrow B \\ S \rightarrow a \\ B \rightarrow b \end{array} \quad \left. \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \right\} \quad \begin{array}{c} \text{Both linear grammar} \\ \text{Regular Grammar} \end{array}$$

(i) $S \rightarrow aAa$
 $S \rightarrow aBa$

R.G. X

(ii) (i) $A \rightarrow aaAa$ \boxed{A} } R.G. ✓ (Right Linear)
 $B \rightarrow bb$

(ii) $B \rightarrow b$
 $A \rightarrow aAa$
 $A \rightarrow aa$

} R.G. X

(iii) $A \rightarrow aAA$
 $B \rightarrow BB\epsilon$
 \downarrow
Empty

} Both Linear
} R.G. ✓

(i) Derivation Tree

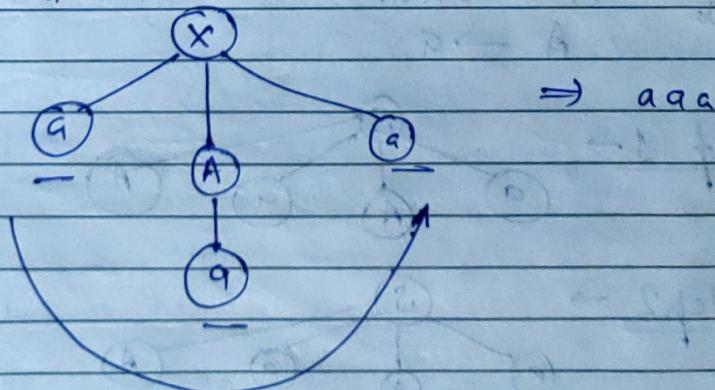
Starting Node \rightarrow Root Node

Vertex \rightarrow Non Terminal

leaf Node (leaves) \rightarrow Terminal

$X \rightarrow aAa$

$A \rightarrow a$

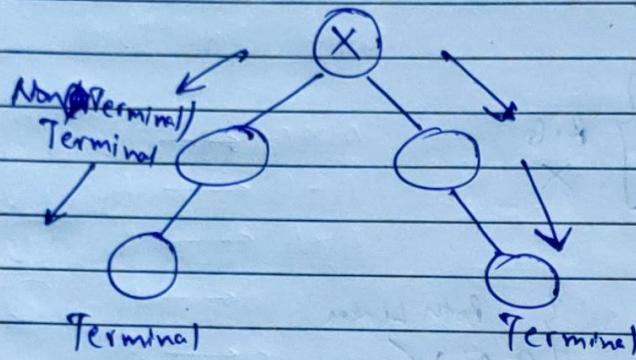


(i)

Top-down derivation tree :-

i) Start with Root Node.

ii) Goes down toward Leaf Node (leaves)



(ii)

Bottom-up derivation tree :-

i) Start with leaf Node (leaves Node)

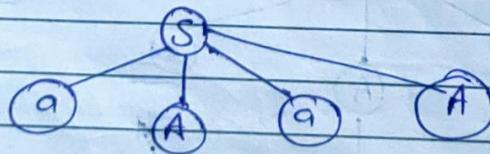
ii) Towards Root Node.

(i)

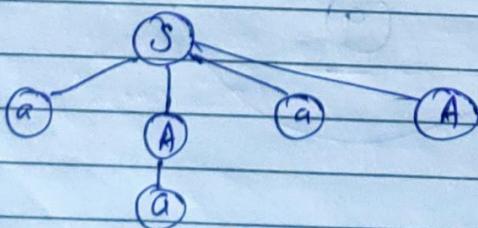
left linear derivation tree :-

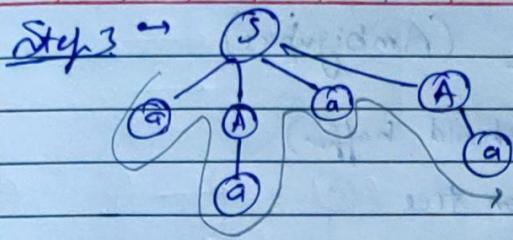
$$\begin{array}{l} \text{Root} \\ \text{Node} \end{array} \leftarrow S \rightarrow aAaA \\ A \rightarrow a$$

Step 1 →



Step 2 →





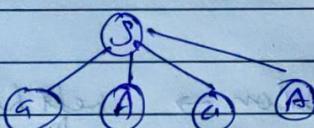
$$S \rightarrow aaaa$$

(ii) Right linear derivation tree :- (Right to left)

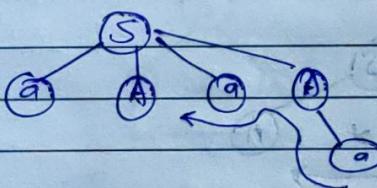
$$S \rightarrow aAaA$$

~~$A \rightarrow a$~~

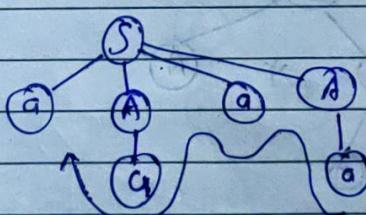
Step 1 :-



Step 2 :-



Step 3 :-



$$S \rightarrow aaaa$$

#

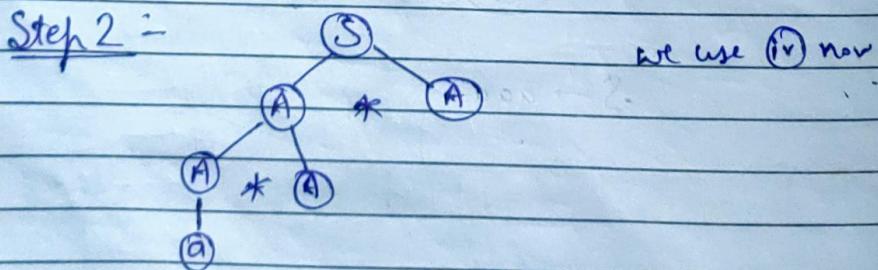
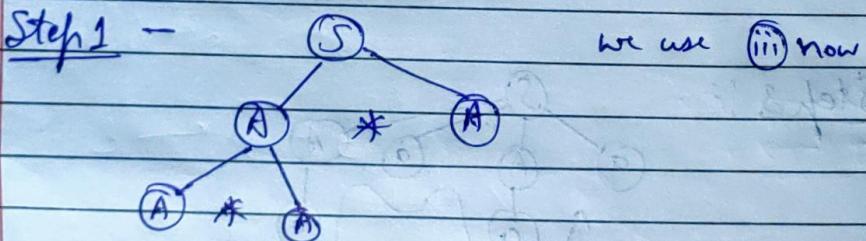
Ambiguity (Grammar) (Ambigibus)

(Any one should happen)

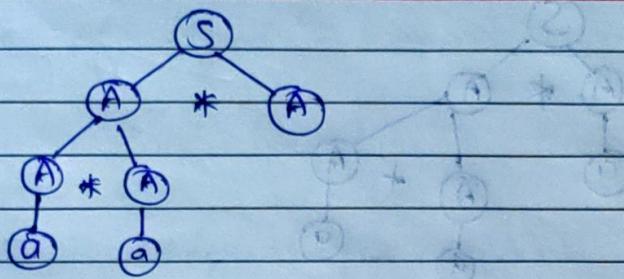
- (i) left linear derivation tree
- (ii) Right " " " "
- (iii) left and right " " " "

- Q. i) $S \rightarrow A * A$
- ii) $A \rightarrow A + A$
 - iii) $A \rightarrow A * A$
 - iv) $A \rightarrow a$
 - v) $B \rightarrow b$

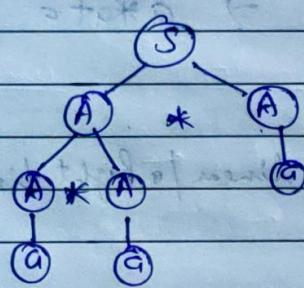
Take any expression \rightarrow left linear \rightarrow
we take (i)



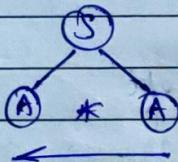
Step 3 :-



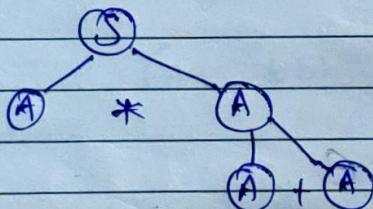
Step 4 :-



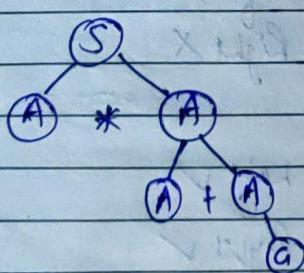
Right Linear :-



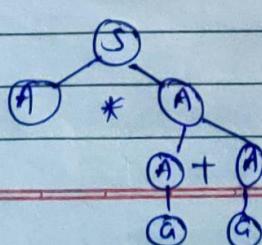
Step 1 :-



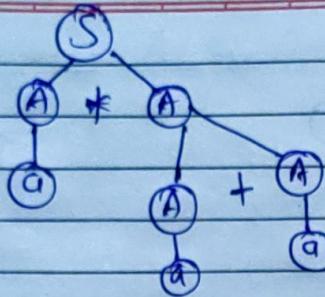
Step 2 :-



Step 3 :-



Step 4:-



$\Rightarrow a * a + a$

Q. Find out left linear / Right Linear Regular Grammar.

$$① \quad S \rightarrow a = A B$$

$$S \rightarrow a A B$$

Right

$$A \rightarrow a$$

$$B \rightarrow b$$

$$② \quad S \rightarrow A a a \text{ left}$$

$$S \rightarrow B b$$

$$A \rightarrow a$$

$$B \rightarrow b$$

$$③ \quad S \rightarrow E + E$$

left X

right X

$$④ \quad S \rightarrow A a a A$$

$$S \rightarrow B A$$

$$A \rightarrow a$$

$$B \rightarrow b$$

left ✓

right ✓

#

Power of Sigma :-

$$\Sigma = \{a, b\}$$

i) $\Sigma^0 \rightarrow$ only Empty string
 $\Sigma^0 \rightarrow$ Empty

ii) $\Sigma^1 \rightarrow$ Set of all string of length 1

$$\Sigma^1 \rightarrow (a, b)$$

iii) $\Sigma^2 \rightarrow$ Set of all string of length 2

$$\Sigma^2 \rightarrow (aa, ab, ba, bb)$$

iv) $\Sigma^3 \rightarrow$ Set of all string of length 3

$$\Sigma^3 \rightarrow (aaa, bbb, abb, baa, bab, aba, aab, bba)$$

v) $\Sigma^4 \rightarrow$ Set of all string of length 4

$$\Sigma^4 \rightarrow (aaaa, \dots)$$

vi) $\Sigma^n \rightarrow$ Set of all string of length n

① Kleene Closure (*)

$$\Sigma = (a, b)$$

$$\Sigma^* = (\text{Empty}, a, b, aa, ab, \dots)$$

② Kleene Plus (+)

$$\Sigma = (a, b)$$

$$\boxed{\Sigma^+ = \Sigma^* - (\text{Empty})}$$

$$\Sigma^+ = (a, b, aa, bb, \dots)$$

Regular Language :- (L)

Language accepted by Regular grammar is called Regular Language.

$$\Sigma = (a, b)$$

$$a^* = (\text{Empty}, a, aa, aaa, \dots)$$

$$a^+ = (a, aa, aaa, \dots)$$

$$\Sigma = (a, b)$$

$$L^1 = (a, b)$$

$$L^2 = (aa, bb, ab, ba)$$

$$L^3 = (aaa, aab, abb, bbb, \dots)$$

$$L^4 = (aaaa, aaab, aabb, abbb, \dots)$$

$$\Sigma = (a, b, c, d)$$

$$L' = (a, b, c, d)$$

$$L^2 = (ab, ac, ad, ba, bd, \dots)$$

$$L^3 = (abc, bcd, \dots)$$

* Five Properties of Regular Language :-

(1) Union - if we have 2 Regular language L_1 and L_2 . Then Union of L_1, UL_2 are Regular Language.

Ex: $L_1 = (a, b)$

$$L_2 = (a, c)$$

$$L_1 \cup L_2 = (a, b, c)$$

(2) Complement - if we have 2 Regular language L_1 and L_2 . Then complement of L_1 and L_2 are Regular Language.

$$L_1 = (a, b)$$

$$L_2 = (a, c)$$

$$L_1' = (b, a)$$

$$L_2' = (c, a)$$

(3) Concatenation - if we have 2 regular language L_1 and L_2 . Then concatenation of L_1, L_2 are regular language.

$$L_1 = (a, b)$$

$$L_2 = (a, c)$$

$$L_1 \cdot L_2 = (aa, ac, ba, bc)$$

(4)

Kleene Closure (*) :- if we have 2 Regular language L_1 and L_2 . Then Kleene closure of L_1^* and L_2^* are Regular language.

$$L_1 = (a, b)$$

$$L_2 = (a, c)$$

$$L_1^* = (\text{Empty}, a, b, aa, bb, ab, ba, \dots)$$

$$L_2^* = (\text{Empty}, a, c, aa, ac, cc, ca, \dots)$$

(5)

Intersection (\cap) :- if we have 2 Regular language L_1 and L_2 . Then intersection of $L_1 \cap L_2$ are regular language.

$$L_1 = (a, b)$$

$$L_2 = (a, c)$$

$$L_1 \cap L_2 = (a)$$



Precedence \rightarrow

(1) Kleene Closure (*) Highest Priority

(2) Second Concatenation

(3) Union (lowest)

Normal Form

\nwarrow CNF (Chomsky Normal Form)

\searrow GNF (Greibach Normal form)

1) CNF :-

Conditions -

- (i) Non-Terminal Represent to empty symbol.

$$A \rightarrow \epsilon$$

- (ii) Non-Terminal Represent to Terminal.

$$A \rightarrow b, A \rightarrow c$$

- (iii) Non-Terminal represent atleast to 2 Non Terminal
($V \rightarrow V_1V_2$)

$$A \rightarrow BC, A \rightarrow AB, A \rightarrow BD$$

2) GNF :-

Conditions -

- (i) Non-Terminal Represent to empty symbol.

$$A \rightarrow \epsilon$$

- (ii) Non-Terminal Represent to Terminal

$$A \rightarrow b, A \rightarrow c$$

(iii)

Non-Terminal Represent Terminal followed by Non Terminals. $(a\alpha^*)$

$$A \rightarrow aB, A \rightarrow aBC, A \rightarrow aBCD, A \rightarrow aABCD$$



Only one terminal followed by terminals

(i)

$$A \rightarrow d \checkmark$$

$$A \rightarrow \epsilon \checkmark$$

$$A \rightarrow Aa X$$

$$A \rightarrow a \checkmark$$

CNF X

GNF X

Regular Grammar
(VTPS) \checkmark

(ii)

$$A \rightarrow a \checkmark$$

$$A \rightarrow \epsilon \checkmark$$

$$A \rightarrow BC \checkmark$$

CNF \checkmark

GNF X

(iii)

$$A \rightarrow a \checkmark$$

$$A \rightarrow b \checkmark$$

$$A \rightarrow aaA X$$

$$A \rightarrow \epsilon \checkmark$$

CNF X

GNF X

(iv)

$$A \rightarrow a \checkmark$$

$$A \rightarrow \epsilon \checkmark$$

$$A \rightarrow aBCDEF GHIJ \checkmark$$

CNF X

GNF \checkmark

(v)

$$A \rightarrow a \checkmark$$

$$A \rightarrow \epsilon \checkmark$$

$$A \rightarrow BC \checkmark$$

CNF \checkmark

GNF X

(vi)

$$A \rightarrow S \quad \checkmark \quad CNR X$$

$$A \rightarrow b \quad \checkmark \quad G.N.P. \quad \checkmark$$

$$A \rightarrow aBC \quad \checkmark$$

CFL (Context free Language) :-

Properties :-

- (i) Union :- if we have 2 Context free language L_1 and L_2 then union of ~~Context free~~ $L_1 \cup L_2$ are CFL.
- (ii) Complement :- if we have 2 Context free language L_1 and L_2 then complement of L_1 and L_2 are ~~CFL~~ NOT CFL.
- (iii) Concatenation :- if we have 2 CFLs L_1 and L_2 then concatenation of $L_1 \cdot L_2$ are CFL.
- (iv) Kleene Closure (*) :- if we have 2 CFLs L_1 and L_2 then Kleene Closure L_1^* and L_2^* are CFL.
- (v) Intersection :- if we have 2 CFLs L_1 and L_2 then intersection of $L_1 \cap L_2$ are NOT CFL.

(Parse Tree)

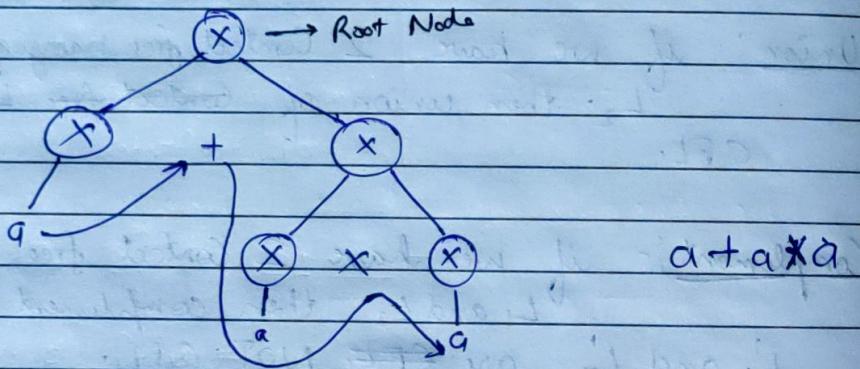
- Q. Find out Left Most Derivation tree
 Final string "a + a * a"

$$X \rightarrow X + X \quad - \textcircled{1}$$

$$X \rightarrow X$$

$$X \rightarrow X \times X \quad - \textcircled{3}$$

$$X \rightarrow a$$



Right

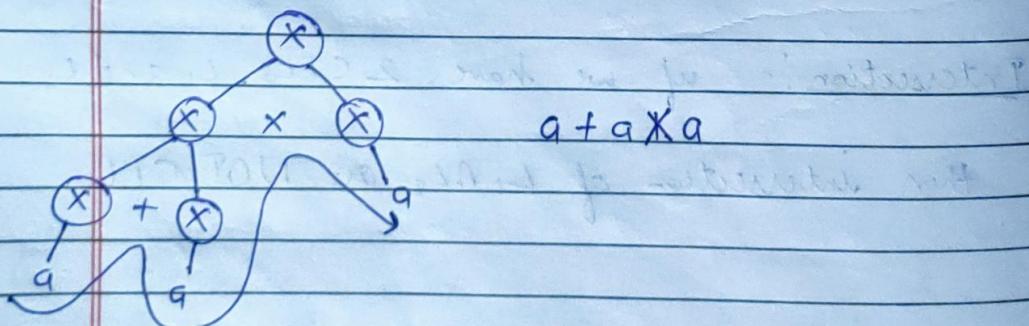
- Q. ~~Left~~ Most Derivation tree → ^(Parse)_{tree}

$$X \rightarrow X + X \quad - \textcircled{3}$$

$$X \rightarrow X$$

$$X \rightarrow X \times X \quad - \textcircled{1}$$

$$X \rightarrow a$$



* If more than one parse tree are possible, like in this example left & right derivation tree are

different), therefore this is Ambiguous Grammar.

* If the structure of left and Right derivation tree are same then grammar is Unambiguous grammar.

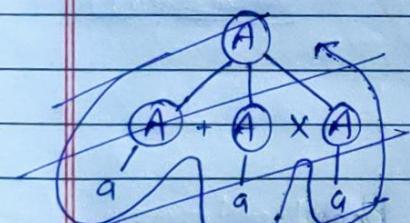
Q. Find out left most derivation tree and right.

$$A \rightarrow A + A \cdot X A \Rightarrow A \rightarrow A + (AXA)$$

$$A \rightarrow AXA + A$$

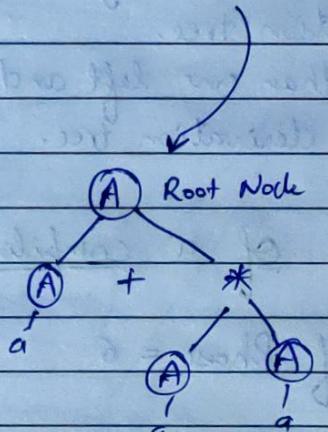
$$A \rightarrow a$$

left most \rightarrow



$a + a \cdot X a$

Sahi tha yeh bhi



diff. structure & diff. strings \rightarrow Ambiguous

* For Unambiguous -

(i) ek se jyada left ban jaayen

(ii) " " " right " "

(iii) ek se jyada dono ban jaayen

Ambiguous

- (i) More than one left and right derivation tree.
- (ii) Different structure of Derivation tree.
- (iii)
 - (1) More than one left derivation tree.
 - (2) More than one right derivation tree.
 - (3) More than one left and right derivation tree.

Unambiguous

- (i) Only one left and one right derivation tree.
- (ii) Same structure of derivation tree.

$A \rightarrow A + A \leftarrow A$
 $A + A \rightarrow A \leftarrow A$
 $\vdots \leftarrow A$

Phases of a compiler -

* No. of Phase = 6

* First 3 Phase called Analysis Phase.

* Last 3 Phase called Synthesis Phase.

Analysis Phase -

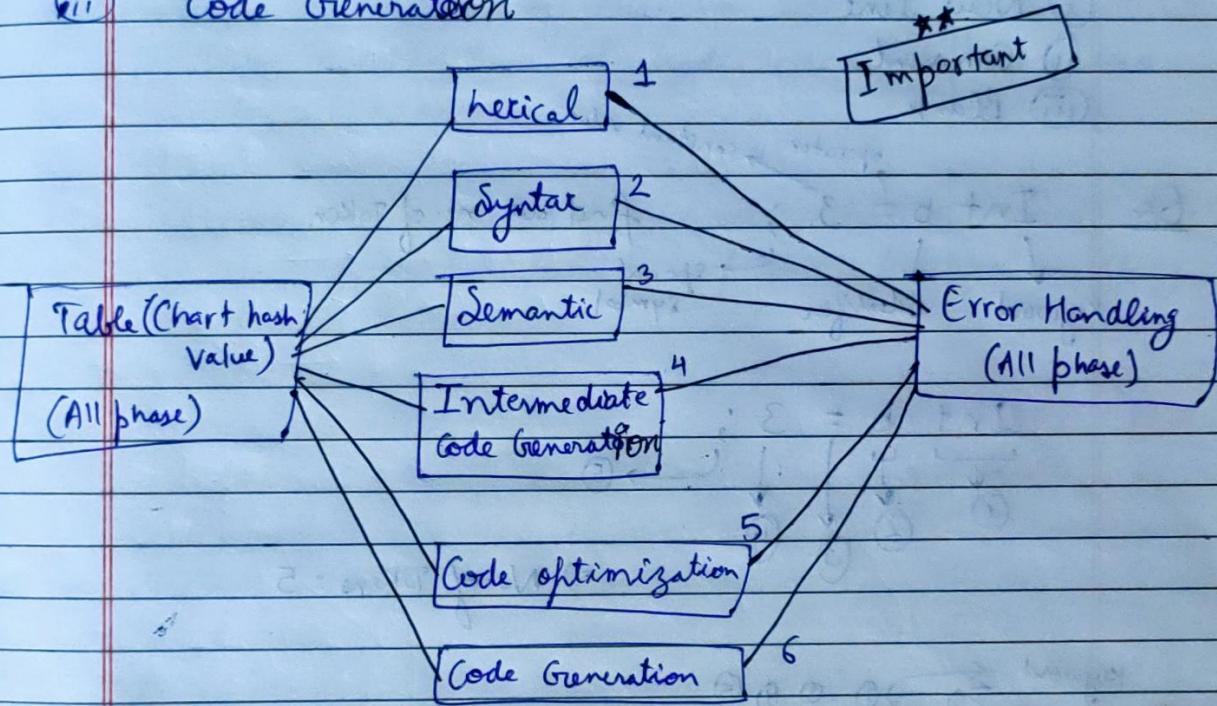
- (i) Lexical Phase
- (ii) Syntax Phase
- (iii) Semantic Phase

Synthesis Phase -

- (i) Intermediate Code Generation

ii) Code optimization

iii) Code Generation



* Token :- Sequence of character which represent unit of Information in the code.

i) Identifier :- (a, b)

ii) Keyword → INT, VOID

(iii) Constant value \rightarrow 5, 6, 0, 1

① operator → Bitwise, Arithmetic



Non-Tokens :-

i) New line

ii) Comment,

iii) Blank

Ex:-

Int b = 3 ;

Keyword

operator

Identifier

constant value

special symbol

find out no. of Token

Int b = 3 ;

①

②

③

④

⑤

⇒ No. of Tokens = 5

Ex:-

Int main () {

Keyword

Print f (" My Name is _____ ");

⑥ ⑦ ⑧ ⑨ ⑩

⑪ return ⑫ ⑬

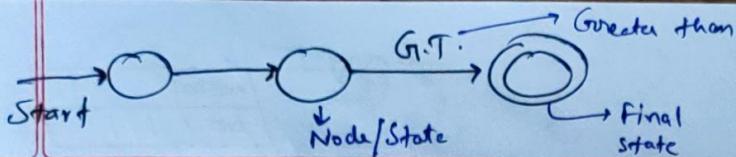
⑭

→ ⑭ ~~ans~~

1,2,3 ← entry tokens

- which line

printed first ← answer

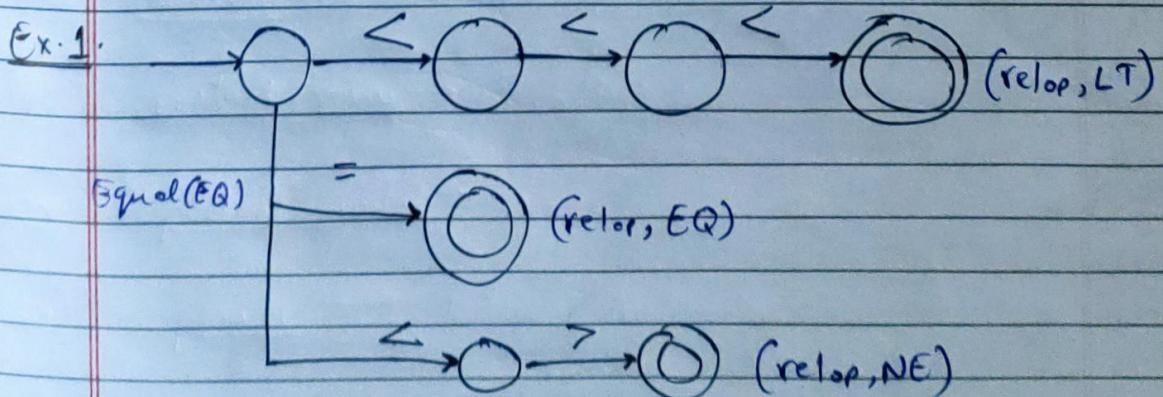


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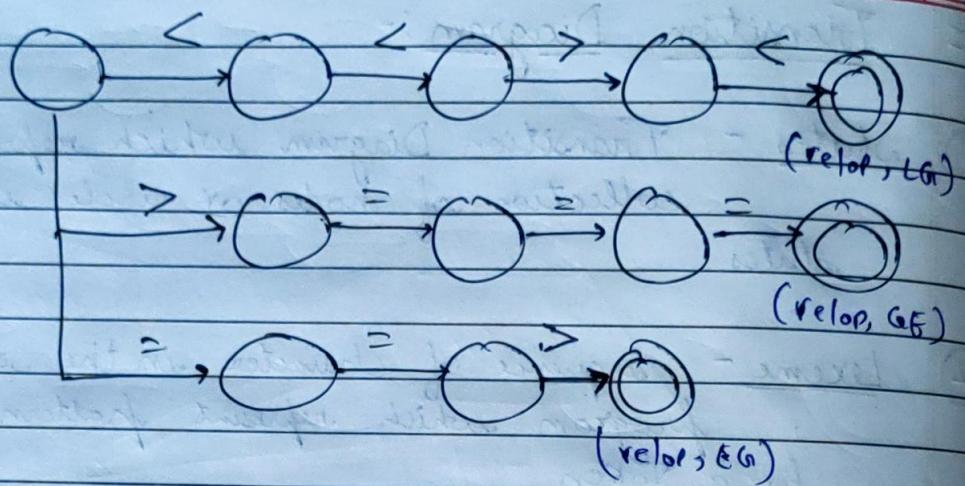
Transition Diagram :-

- ① States - Transition Diagram which represent collection of nodes or circle is called states.
- ② Lexeme - Sequence of character in the source program which represent pattern matching for a Token.

lexeme	Token Name	Attribute
if	if	—
Then	Then	—
else	else	—
Any Identifier	Id	—
Any Number	Number(Num)	—
<	relOp	LT
>	relOp	GT
=	relOp	EQ
<=	relOp	LE
>=	relOp	GE
<u><></u>	relOp	NE (Not Equal) <u><></u>



Ex-2.



① (LT, GT)

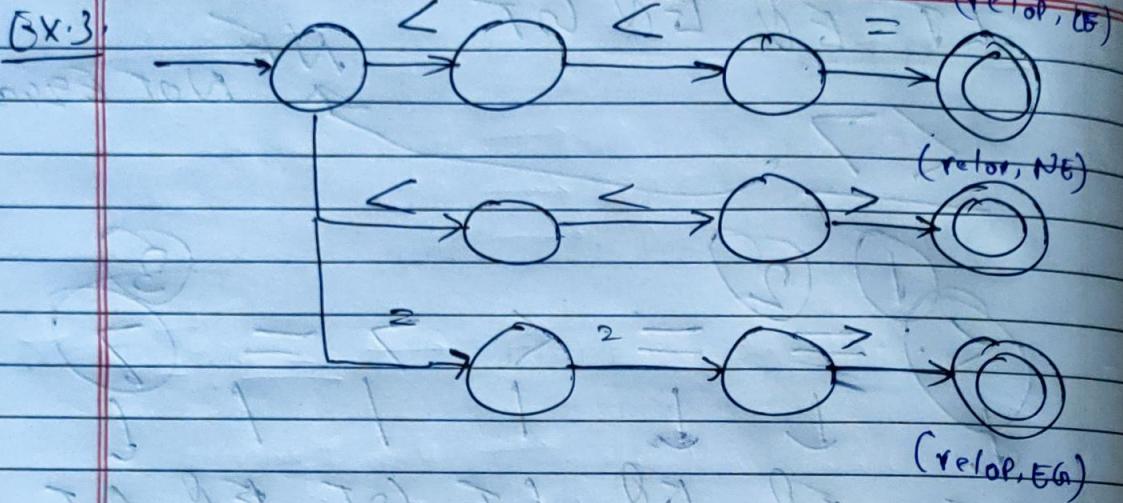
$\downarrow \quad \downarrow$
~~LG~~(NE)

② (GT, EQ)

$\downarrow \quad \downarrow$
(GE)

③ (EQ, GT)

(EG)

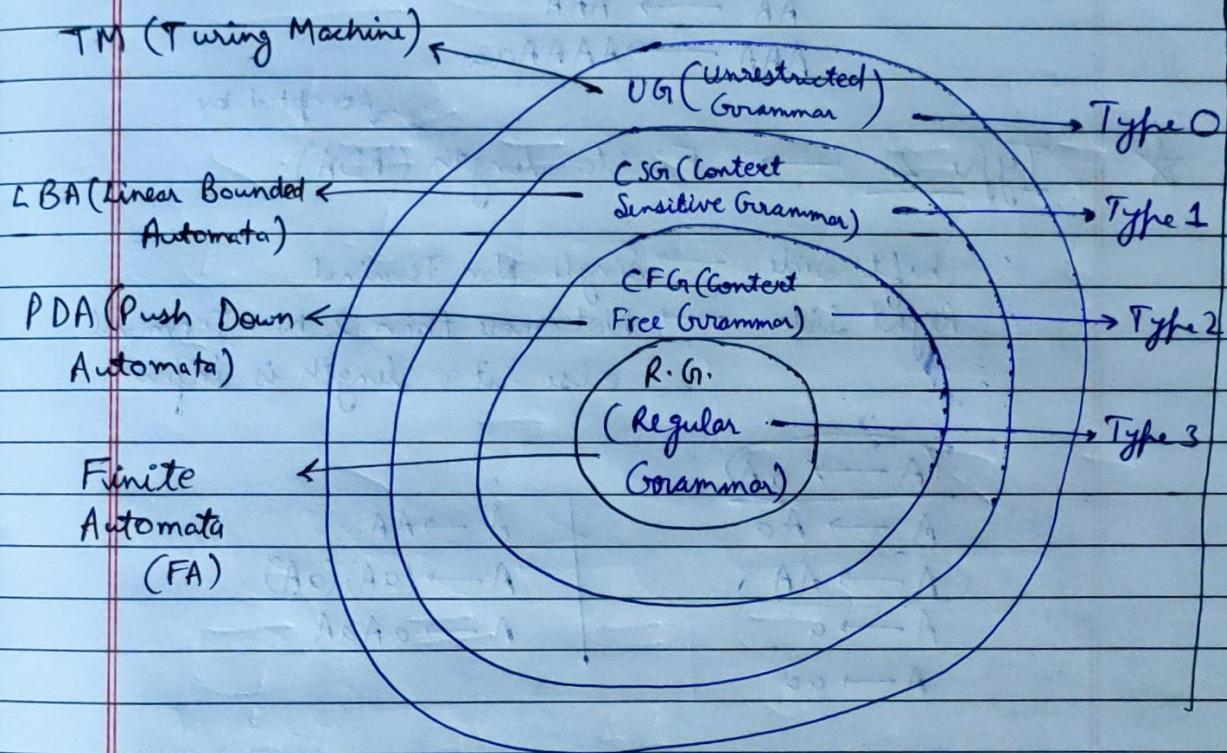


① (LT, EQ)
 (LE)

② (LT, GT) < >
 (EG) ↓
 N6

③ (EQ, GT)
 (EG)

More Complex
More Powerful



* Type 0 → Infinite length (TM)

Example →

$$\begin{array}{l}
 A \rightarrow \text{AAAA} \\
 AA \rightarrow A \\
 AAA \rightarrow A \\
 AA \rightarrow AA
 \end{array}
 \quad \mid \quad
 \begin{array}{l}
 \text{AAA} \rightarrow A \\
 \text{AA} \rightarrow \text{AaA} \\
 aA \rightarrow a
 \end{array}$$

* Type 1 → Infinite length (LBA)

left < Right

A → AA

PAGE NO.

A → A(AA)

DATE

A → AA

Example →

AA → AAA

A → AA

AA → AAA

AAA → AAAAaA

A → (Aa)GA → AaAa

Accepted by

★ Type 2 → Finite length (PDA)

left Side → Single Non Terminal

Right Side → Not more than 2 Non Terminal
else it's length is infinite

A → aA

A → AA

A → AA

A → a

A → aa

A → AA

A → (aA)(aA)

A → aAaA

★ Type 3 → Finite length (FA)

A → a

A → aA ✓

A → Aa

A → aa

Type

Grammar

Language

Automata

Type 3

RG

Regular Language

FA

Type 2

CRG

CFL

PDA

Type 1

CSG

CSL

LBA

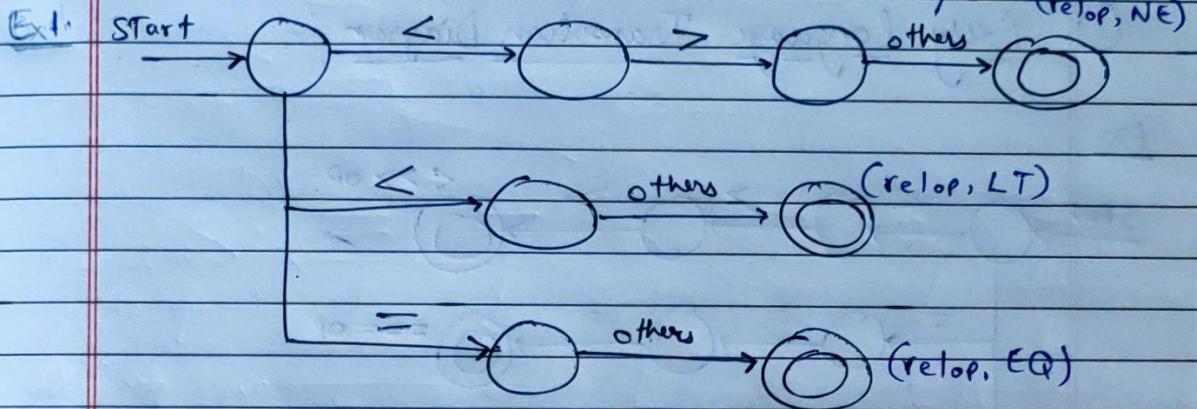
Type 0

UG

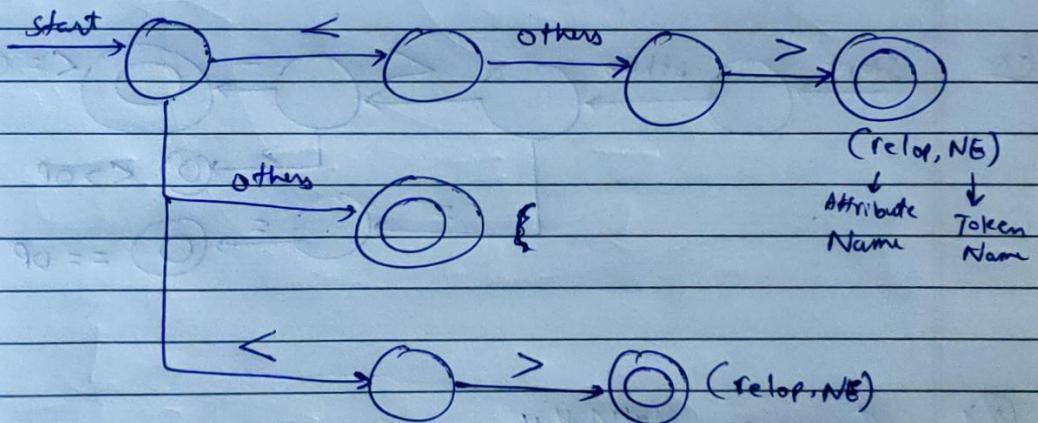
Recursive
language

TM

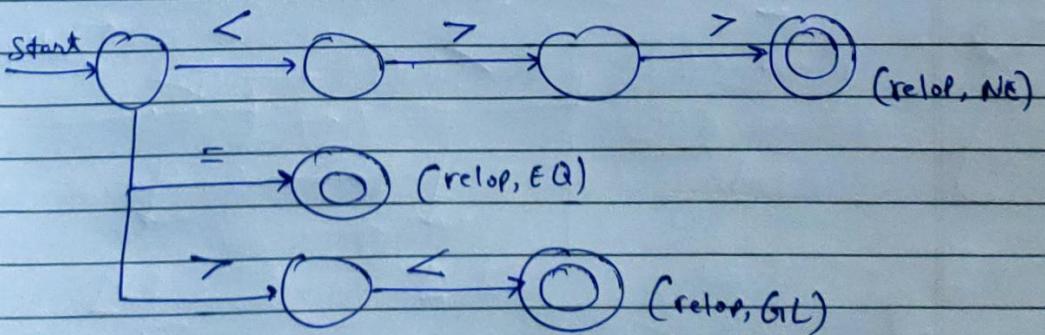
Transition Diagram :- (Leevin Method) Ignore it



Ex.2.



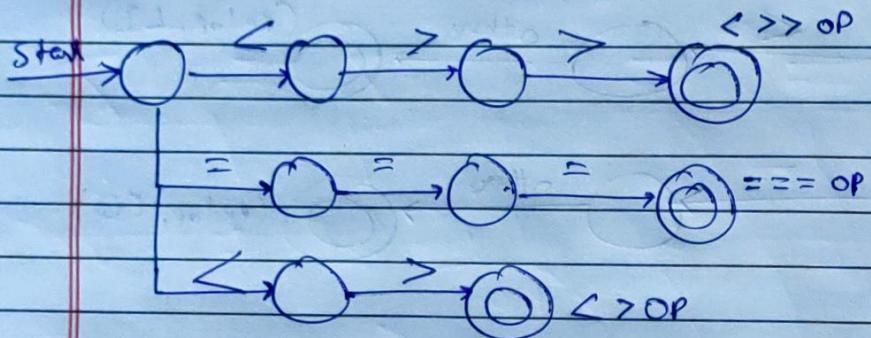
Ex.3.



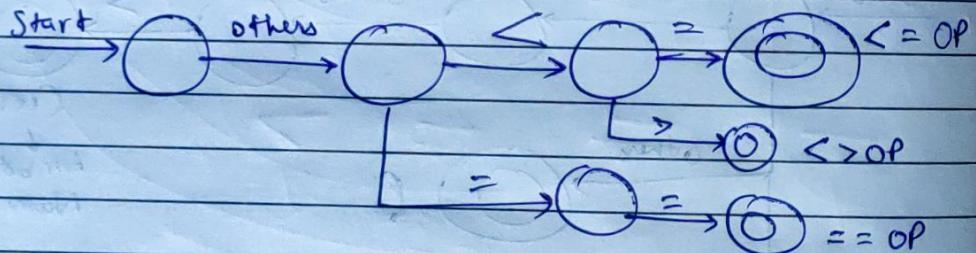
* Transition Diagram :-

① Easy Language Transition Diagram :-

Ex.



Ex.



②

Language Method