

a)  $m_D = 100 \text{ kg}$   $\mu_{RH} = 0.5$   $\mu_{RG} = 0.2$   $\Theta = 20^\circ$

$$\vec{F}_{GH} = m_D \cdot g \cdot \sin \Theta = 100 \text{ kg} \cdot 9.81 \frac{\text{N}}{\text{kg}} = \underline{\underline{981 \text{ N}}}$$

$$|\vec{F}_R| = F_N \cdot \mu_R = m_D \cdot g \cdot \cos \Theta \cdot \mu =$$

$$|\vec{F}_{RH}| = F_N \cdot \mu_{RH} = \underline{\underline{460.9 \text{ N}}}$$

$$|\vec{F}_{RG}| = F_N \cdot \mu_{RG} = \underline{\underline{276.6 \text{ N}}}$$

$$|\vec{F}_{GH}| > |\vec{F}_{RG}| + m \cdot g$$

$$m < \frac{|\vec{F}_{GH}| - |\vec{F}_{RG}|}{g} = m_D (\sin \Theta - \cos \Theta \cdot \mu_{RG})$$

$$m < 100 \text{ kg} \cdot (\sin 20^\circ - \cos 20^\circ \cdot 0.2)$$

$$m < 6 \text{ kg}$$

$$\underline{\underline{0 < m < 6 \text{ kg}}}$$

b)  $m \cdot g > |\vec{F}_{GH}| + |\vec{F}_{RG}|$

$$m > \frac{|\vec{F}_{GH}| + |\vec{F}_{RG}|}{g} = m_D (\sin \Theta + \cos \Theta \cdot \mu_{RG})$$

$$m > 62.4 \text{ kg}$$

$$m < \frac{|\vec{F}_{GH}| + |\vec{F}_{RH}|}{g} = m_D (\sin \Theta + \cos \Theta \cdot \mu_{RH})$$

$$m < 81.2 \text{ kg}$$

$$\underline{\underline{62.4 \text{ kg} < m < 81.2 \text{ kg}}}$$



B4/A1

Gegeben:  $v_A = 16 \frac{m}{s}$   $\Theta = 60^\circ$   $h = 12m$

mit Energieerhaltungssatz:

a)

$$E_S = E_A \quad \leftarrow \text{Ende}$$

$$\frac{1}{2} \cdot m \cdot v_A^2 + m \cdot g \cdot h = \frac{1}{2} \cdot m \cdot v_E^2 + m \cdot g \cdot h$$

$$\frac{1}{2} \cdot m \cdot v_A^2 = \frac{1}{2} \cdot m \cdot v_E^2 + m \cdot g \cdot y_S$$

$$y_S = \frac{v_A^2 - v_E^2}{2g}$$

$$v_S = v_A \cdot \cos \Theta$$

$$= \frac{v_A^2 (1 - \cos^2 \Theta)}{2g} = \frac{16 \frac{m}{s} \cdot \sin^2(60^\circ)}{2 \cdot 9.81 \frac{N}{kg}} = \underline{\underline{9.8m}}$$

b)

$v_E$

$$y = y_E = -12m$$

Energie d. Ball:

$$E_E = \frac{1}{2} \cdot v_E^2 + m \cdot g \cdot y_E$$

Energieerhaltung:

$$E_A = E_E$$

$$\frac{1}{2} \cdot m \cdot v_E^2 + m \cdot g \cdot y_E = \frac{1}{2} \cdot m \cdot v_A^2$$

$$v_E = \sqrt{v_A^2 - 2 \cdot g \cdot y_E} = \underline{\underline{22 \frac{m}{s}}}$$



b) Ges:  $\mu_{RG}$ ?

$$|\vec{F}_{RG}| = |\vec{F}_N| \cdot \mu_{RG}$$

$m \cdot g$

$$\Rightarrow \mu_{RG} = \frac{|\vec{F}_{RG}|}{m \cdot g} = \frac{\Delta E_{\text{Wärme}}}{\Delta s \cdot m \cdot g} = \frac{6,3 \cdot 10^{-3} \text{ J}}{60 \text{ m} \cdot 2000 \cdot 9,81} = \underline{\underline{0,53}}$$



B4 A2

Geg.:  $m = 40 \text{ kg}$   
 $s = 8 \text{ m}$

$\Delta h = 4 \text{ m}$   
 $\Theta = 30^\circ$

$\mu_{RG} = 0,25$

$E_{kin} = E_{pot}$

$\Delta E_{pot} = m \cdot g \cdot \Delta h$

$\Delta E_{kin} = \frac{1}{2} \cdot m \cdot v^2$

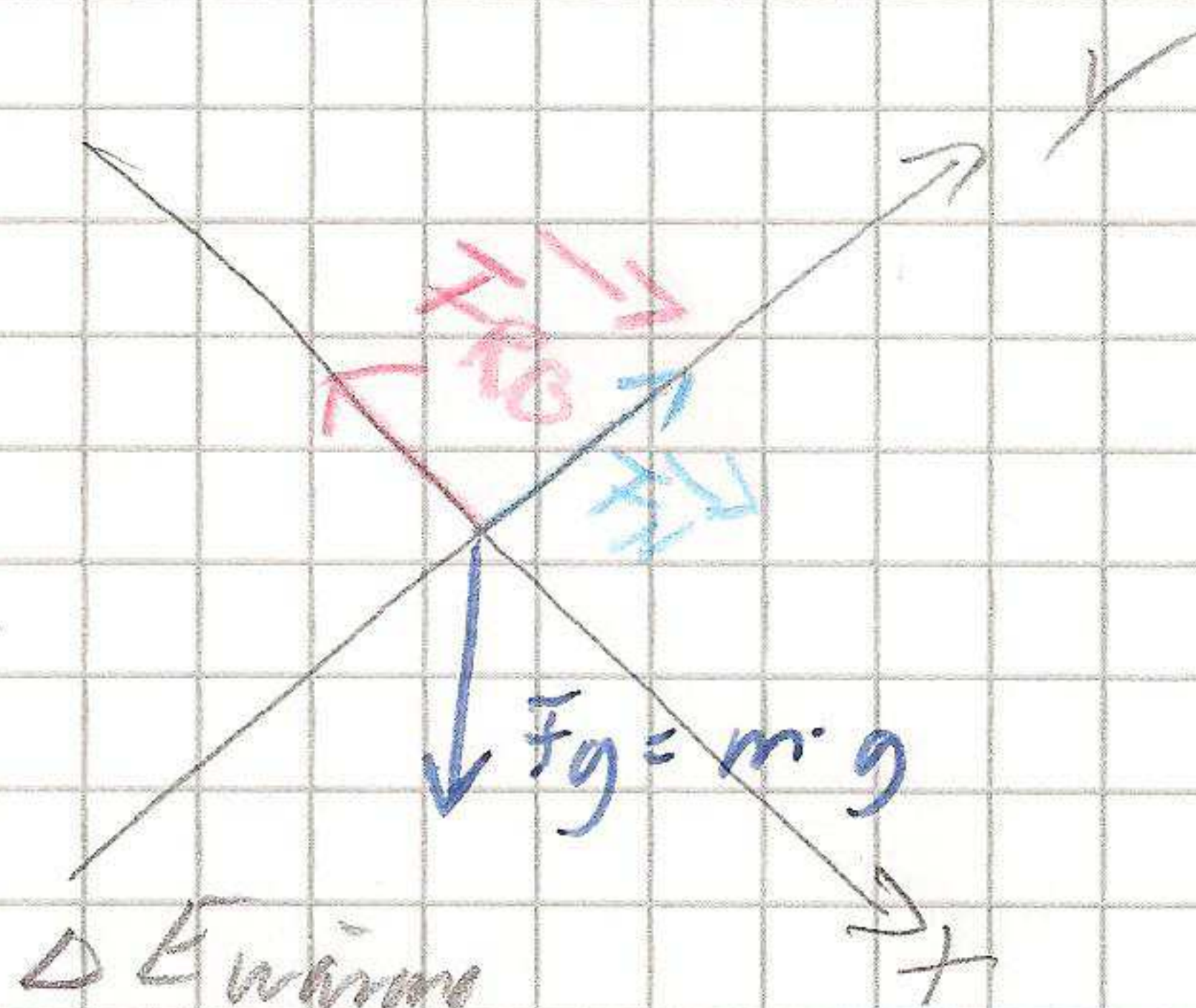
$\Delta E_{w\u00e4rme} = |\vec{F}_{RG}| \cdot s$

$W_{ext} = \Delta E = \Delta E_{pot} + \Delta E_{kin} + \Delta E_{w\u00e4rme}$

$|\vec{F}_{RG}| = \mu_{RG} \cdot |\vec{F}_N|$

$= \mu_{RG} \cdot \cos \Theta \cdot m \cdot g$

$\Delta h = s \cdot \sin \Theta$



$0 = \overbrace{m \cdot g \cdot \Delta h}^{\Delta E_{pot}} + \overbrace{\frac{1}{2} m v^2}^{\Delta E_{kin}} + \overbrace{\mu_{RG} \cdot m \cdot g \cdot \cos \Theta \cdot s}^{\Delta E_{w\u00e4rme}}$

$v^2 = 2 \cdot g \cdot s (\sin \Theta - \mu_{RG} \cdot \cos \Theta)$

$= \underline{\underline{5,6 \frac{\text{m}}{\text{s}}}}$

B4 A3

Geg.:  $m = 2000 \text{ kg}$

$v_A = 25 \frac{\text{m}}{\text{s}}$

$\Delta s = 60 \text{ m}$

a)  $\Delta E = 0$  nicht vorhanden

$\Delta E = \Delta E_{kin} + \Delta E_{pot} + \Delta E_{w\u00e4rme}$

$\Delta E_{kin} = E_{kinE} - E_{kinA} = 0 - E_{kinA} = -E_{kinA}$

$\Delta E_{w\u00e4rme} = |\vec{F}_{RG}| \cdot \Delta s$

$0 = -\frac{1}{2} \cdot m v_A^2 + |\vec{F}_{RG}| \cdot \Delta s$

$F_{RG} \cdot \Delta s = \frac{1}{2} \cdot m v_A^2 = \frac{1}{2} \cdot 2000 \text{ kg} \cdot (25 \frac{\text{m}}{\text{s}})^2 = \underline{\underline{6,3 \cdot 10^5 \text{ J}}}$