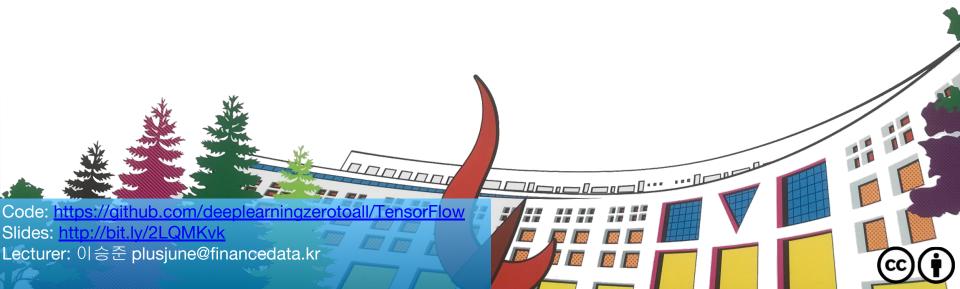
# ML/DL for Everyone Season2



03 - How to minimize cost LAB



# Simplified hypothesis

Hypothesis H(x)=Wx

Cost  $cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$ 

### **Cost function in pure Python**

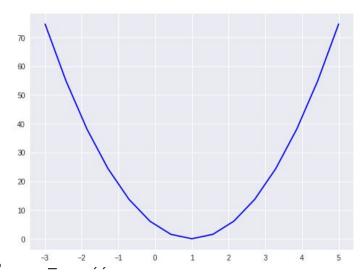
$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

```
import numpy as np
X = np.array([1, 2, 3])
                                                                W
                                                                          cost
Y = np.array([1, 2, 3])
                                                              -3.000 I
                                                                       74.66667
def cost_func(W, X, Y):
                                                              -2.429 | 54.85714
                                                              -1.857 | 38.09524
    c = 0
                                                              -1.286 | 24.38095
    for i in range(len(X)):
                                                              -0.714 \mid 13.71429
        c += (W * X[i] - Y[i]) ** 2
                                                              -0.143 | 6.09524
    return c / len(X)
                                                              0.429 | 1.52381
                                                               1.000 | 0.00000
for feed W in np.linspace(-3, 5, num=15):
                                                               1.571 I 1.52381
    curr cost = cost func(feed W, X, Y)
                                                               2.143 | 6.09524
    print("{:6.3f} | {:10.5f}".format(feed W, curr cost))
                                                               2.714 |
                                                                       13.71429
                                                               3.286 |
                                                                       24.38095
                                                               3.857 | 38.09524
                                                               4.429 |
                                                                       54.85714
                                                               5.000 I
                                                                       74.66667
```

# **Cost function in pure Python**

$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

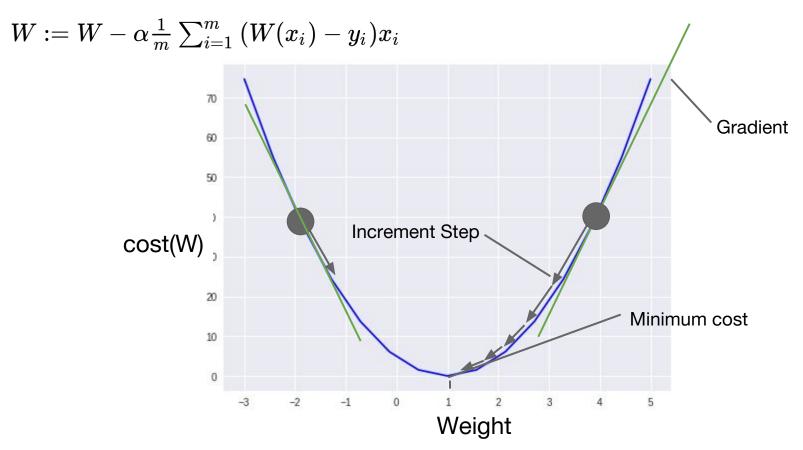
```
import numpy as np
X = np.array([1, 2, 3])
Y = np.array([1, 2, 3])
def cost_func(W, X, Y):
    c = 0
    for i in range(len(X)):
        c += (W * X[i] - Y[i]) ** 2
    return c / len(X)
for feed W in np.linspace(-3, 5, num=15):
    curr cost = cost func(feed W, X, Y)
    print("{:6.3f} | {:10.5f}".format(feed W,
```



#### **Cost function in TensorFlow**

$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

```
X = np.array([1, 2, 3])
Y = np.array([1, 2, 3])
                                                       70
                                                       60
def cost_func(W, X, Y):
  hypothesis = X * W
  return tf.reduce mean(tf.square(hypothesis - Y))
                                                      40
W values = np.linspace(-3, 5, num=15)
                                                       30
cost values = []
                                                       20
for feed W in W values:
    curr cost = cost func(feed W, X, Y)
                                                       10
    cost values.append(curr cost)
    print("{:6.3f} | {:10.5f}".format(feed W, curr ())
```



$$cost(W) = rac{1}{m} \sum_{i=1}^m (Wx_i - y_i)^2$$

$$W := W - lpha rac{1}{m} \sum_{i=1}^m \left(W(x_i) - y_i
ight) x_i$$

```
alpha = 0.01
gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X))
descent = W - tf.multiply(alpha, gradient)
W.assign(descent)
```

```
tf.set random seed(0) # for reproducibility
x data = [1., 2., 3., 4.]
y_{data} = [1., 3., 5., 7.]
W = tf.Variable(tf.random normal([1], -100., 100.))
for step in range(300):
    hypothesis = W * X
    cost = tf.reduce mean(tf.square(hypothesis - Y))
    alpha = 0.01
    gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X))
    descent = W - tf.multiply(alpha, gradient)
                                                         W := W - lpha rac{1}{m} \sum_{i=1}^m \left(W(x_i) - y_i
ight) x_i
    W.assign(descent)
    if step % 10 == 0:
        print('{:5} | {:10.4f} | {:10.6f}'.format(
            step, cost.numpy(), W.numpy()[0]))
```

```
W
tf.set random seed(0) # for reproducibility
                                                               step
                                                                          cost
                                                                  0 | 11716.3086 |
                                                                                    48.767971
x data = [1., 2., 3., 4.]
                                                                       4504.9126 I
                                                                                    30.619968
                                                                 10 I
y data = [1., 3., 5., 7.]
                                                                 20 | 1732.1364 |
                                                                                   19.366755
                                                                 30 | 666.0052 | 12.388859
W = tf.Variable(tf.random normal([1], -100., 100.))
                                                                 40 | 256.0785 | 8.062004
                                                                 50 | 98.4620 | 5.379007
for step in range(300):
                                                                 60 I
                                                                        37.8586 | 3.715335
   hypothesis = W * X
                                                                 70 | 14.5566 |
                                                                                   2.683725
   cost = tf.reduce mean(tf.square(hypothesis - Y))
                                                                                     2.044044
                                                                 80 | 5.5970 |
   alpha = 0.01
                                                                240 |
                                                                         0.0000 |
                                                                                     1.000499
   gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X)
                                                                250 I
                                                                         0.0000 |
                                                                                    1.000309
   descent = W - tf.multiply(alpha, gradient)
                                                                260 I
                                                                         0.0000 |
                                                                                    1.000192
   W.assign(descent)
                                                                270 I
                                                                         0.0000 |
                                                                                    1.000119
                                                                                    1.000074
                                                                280 I
                                                                         0.0000 |
   if step % 10 == 0:
                                                                290 I
                                                                         0.0000 |
                                                                                     1.000046
       print('{:5} | {:10.4f} | {:10.6f}'.format(
           step, cost.numpy(), W.numpy()[0]))
```

# Output when W=5

W=5

W = -3

60 50

```
tf.set random seed(0) # for reproducibility
x data = [1., 2., 3., 4.]
y data = [1., 3., 5., 7.]
W = tf.Variable([5.0])
for step in range(300):
    hypothesis = W * X
                                                                               cost
                                                                                             W
                                                                        step
    cost = tf.reduce mean(tf.square(hypothesis - Y))
                                                                        0 1
                                                                               74.6667 |
                                                                                            4.813334
                                                                       10 I
                                                                               28.7093 I
                                                                                            3.364572
    alpha = 0.01
                                                                       20 1
                                                                               11.0387 |
                                                                                            2.466224
    gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X)
                                                                               4.2444
                                                                       30 I
                                                                                            1.909177
    descent = W - tf.multiply(alpha, gradient)
                                                                                1.6320 |
                                                                                            1.563762
                                                                       40
    W.assign(descent)
                                                                       50 I
                                                                                0.6275 |
                                                                                            1.349578
                                                                       60 I
                                                                                0.2413 |
                                                                                            1.216766
    if step % 10 == 0:
                                                                       70 I
                                                                                0.0928 |
                                                                                            1.134412
        print('{:5} | {:10.4f} | {:10.6f}'.format(
                                                                                0.0357 |
                                                                                            1.083346
                                                                       80 |
            step, cost.numpy(), W.numpy()[0]))
                                                                      270 I
                                                                                0.0000 |
                                                                                            1.000009
                                                                      280 I
                                                                                0.0000 |
                                                                                            1.000006
                                                                      290 I
                                                                                0.0000
                                                                                            1.000004
```

### What's Next?

• Multi-Variable Linear regression