


```
calibrateDebevec = cv2.createCalibrateDebevec()
responseDebevec = calibrateDebevec.process(images, times)
```

The figure below shows the CRF recovered using the images for the red, green and blue channels. Note that the calibrated intensity is after an exponential operation.



Please write your own code for recovering CRF using Debevec's algorithm. Note that the image has RGB three channels, and you need to precess each channel separately.

The most important part is to resemble the matrix for the linear system.



```
In [ ]: ### TODO: implementation of Debevec's CRF recovering algorithm. You need to return the crf (descrete array) for each channel.
import math
from matplotlib import pyplot as plt
import numpy.matlib
import warnings
warnings.filterwarnings("ignore")

def gsolve(Z):
    """
    Z(i, j) is the pixel values of pixel locations number i in image j
    B(j)   is the log delta t for image j
    l      is lambda, the constant that determines the amount of smoothness
    w(z)   is the weighting function value for pixel value z

    Returns:
    g(z)   is the log exposure corresponding to pixel value z
    lE(i)  is the log film irradiance at pixel location i
    """

    n = 256

    s1, s2 = Z.shape
    # Secondly, generate the matrix A and b
    A = np.zeros((s1 * s2 + n + 1, n + s1))
    b = np.zeros((A.shape[0], 1))

    # include the data-fitting equations
    k = 0
    for i in range(s1):
        for j in range(s2):
            wij = w[Z[i, j]]
            A[k, Z[i, j]] = wij
            A[k, n + i] = -wij
            b[k] = wij * B[i, j]
            k += 1

    # fix the curve by setting its middle value to 0
    A[k, 129] = 0
    k += 1

    # include the smoothness equations
    for i in range(1, n - 2):
        A[k, i] = 1 * w[i + 1]
        A[k, i + 1] = -2 * 1 * w[i + 1]
        A[k, i + 2] = 1 * w[i + 1]
        k += 1

    # Solve the system using SVD
    x = np.linalg.lstsq(A, b)
    x = x[0]
    g = x[0 : n]
    lE = x[n: len(x)]

    return g, lE

## some param required to use
N = len(images)          #N指照片个数
row = len(images[0])     #len(images[0])获得的是images列表中第一个项的shape[0],也就是图像的width
col = len(images[0][0])  #len(images[0][0])获得的是images列表中第一个项的shape[1],也就是图像的height
l = 10

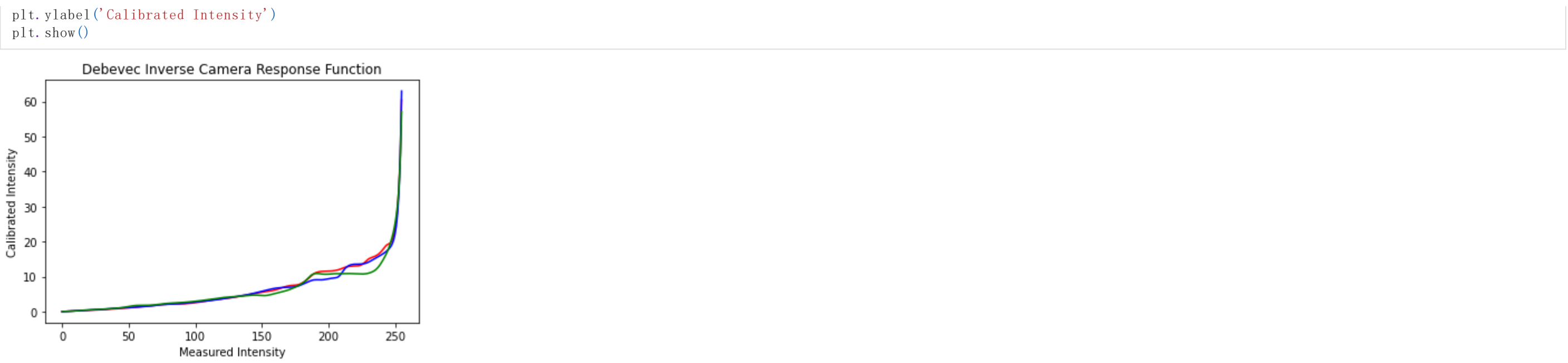
## add a hat weighting function
Zmin = 0
Zmax = 255
w = np.zeros((Zmax - Zmin + 1))
for z in range(Zmin, Zmax + 1):
    if z <= (Zmax + Zmin) // 2:
        w[z] = z - Zmin + 1
    else:
        w[z] = Zmax - z + 1

# Firstly, randomly select N points
##
numSamples = math.ceil(255 * 2 / (N - 1)) * 2
numPixels = row * col          #一张图片上总的像素个数
step = int(numPixels / numSamples)
sampleIndices = list(range(0, numPixels, step))[:-1] #每张图像选择len(sampleIndices)个点,即numSamples个
flattenImage = np.zeros((N, 3, numPixels), dtype=np.uint8) #flattenImage[i, j]表示第i张图像的第j通道的所有像素
for i in range(N): #遍历每张图像
    for j in range(3): #遍历每个通道
        flattenImage[i, j] = np.reshape(images[i][:, :, j], (numPixels,)) #取出每张图像在每个通道的所有像素点,将其flatten成一维
Z_r = np.zeros((numSamples, N), dtype=np.uint8) #Z[i, j]表示在第j个图像上的第i个像素位置
Z_g = np.zeros((numSamples, N), dtype=np.uint8)
Z_b = np.zeros((numSamples, N), dtype=np.uint8)
for i in range(N):
    Z_b[:, i] = flattenImage[i, 0][sampleIndices]
    Z_g[:, i] = flattenImage[i, 1][sampleIndices]
    Z_r[:, i] = flattenImage[i, 2][sampleIndices]
index_ = np.arange(0, numSamples) #要保留的位置
idx = [] #要剔除的位置
for i in range(numSamples):
    for k in range(N - 1):
        if Z_g[i, k] > Z_g[i, k + 1]: #这里让像素值呈升序排列(输入图像是从低曝光时间到高曝光时间的顺序排列的,所以后一张图像的一个位置的像素值要高于前一张图像的对应位置的像素值),所以将不按升序排列的
            idx.append(i)
            break
index_ = np.delete(index_, idx, 0)
Z_b = Z_b[index_]
Z_g = Z_g[index_]
Z_r = Z_r[index_]
B = np.matlib.repmat(np.log(times), Z_b.shape[0] * Z_b.shape[1], 1) #dim=0方向np.log(times)要重复Z_b.shape[0] * Z_b.shape[1]次,dim=1方向重复1次.

# Thirdly, solve the linear system using SVD
# this part is in the function 'gsolve'

# Finally, return the crf, which should be a numpy array of shape (3, 256) as we have 3 channels
##
g_b, lE_b = gsolve(Z_b) #gsolve函数就对应Debevec的论文最后面的gsolve.m代码的python实现形式
g_g, lE_g = gsolve(Z_g)
g_r, lE_r = gsolve(Z_r)
```

```
In [ ]: ### TODO: plot the CRF (3 plots for 3 channels) you have recovered.
xx = list(range(0, 256))
plt.title('Debevec Inverse Camera Response Function')
plt.plot(xx, np.exp(g_r), 'r')
plt.plot(xx, np.exp(g_g), 'b')
plt.plot(xx, np.exp(g_b), 'g')
plt.xlabel('Measured Intensity')
```



Step 3: Merge Images

Once the CRF has been estimated, we can merge the exposure images into one HDR image using MergeDebevec with OpenCV.

```
In [ ]: # Merge images into an HDR linear image using OpenCV's function
mergeDebevec = cv2.createMergeDebevec()
hdrDebevec = mergeDebevec.process(images, times, responseDebevec)
# You may want to save the HDR image (radiance map).
# cv2.imwrite("hdrDebevec.hdr", hdrDebevec)

import matplotlib.pyplot as plt
plt.imshow(hdrDebevec)
plt.show()
```

Clipping input data to the valid range for imshow with RGB data ([0..1] for floats or [0..255] for integers).



And you should implement your own code according to the equation below. The w is the hat weighting function we used before.

$$\ln E_i = \frac{\sum_{j=1}^P w(Z_{ij})(g(Z_{ij}) - \ln \Delta t_j)}{\sum_{j=1}^P w(Z_{ij})}$$

```
In [ ]: ### TODO: recover the radiance map

m = np.zeros(flattenImage.shape[1:])
wsum = np.zeros(flattenImage.shape[1:])
hdr = np.zeros(flattenImage.shape[1:])

lnDt = np.log(times) #ln delta t
for i in range(N):
    wij_b = w[flattenImage[i,0]]
    wij_g = w[flattenImage[i,1]]
    wij_r = w[flattenImage[i,2]]
    wsum[0,:] += wij_b
    wsum[1,:] += wij_g
    wsum[2,:] += wij_r
    m0 = np.subtract(g_b[flattenImage[i,0]], lnDt[i][:,0])
    m1 = np.subtract(g_g[flattenImage[i,1]], lnDt[i][:,0])
    m2 = np.subtract(g_r[flattenImage[i,2]], lnDt[i][:,0])
    hdr[0] += np.multiply(m0, wij_b)
    hdr[1] += np.multiply(m1, wij_g)
    hdr[2] += np.multiply(m2, wij_r)
hdr = np.divide(hdr, wsum)
hdr = np.exp(hdr)
hdr = np.reshape(np.transpose(hdr), (row, col, 3))

radiancemap = (hdr / np.amax(hdr) * 255).astype(np.float32)

# plot your radiance map
plt.imshow(cv2.cvtColor(radiancemap, cv2.COLOR_BGR2RGB))
plt.show()
```

Clipping input data to the valid range for imshow with RGB data ([0..1] for floats or [0..255] for integers).



Step 4: Tone mapping

Now we have merged our exposure images into one HDR image. Can you guess the minimum and maximum pixel values for this image? The minimum value is obviously 0 for a pitch black condition. What is the theoretical maximum value? Infinite! In practice, the maximum value is different for different situations. If the scene contains a very bright light source, we will see a very large maximum value.

Even though we have recovered the relative brightness information using multiple images, we now have the challenge of saving this information as a 24-bit image for display purposes.

The process of converting a High Dynamic Range (HDR) image to an 8-bit per channel image while preserving as much detail as possible is called Tone mapping.

There are several tone mapping algorithms. OpenCV implements four of them. The thing to keep in mind is that there is no right way to do tone mapping. Usually, we want to see more detail in the tonemapped image than in any one of the exposure images. Sometimes the goal of tone mapping is to produce realistic images and often times the goal is to produce surreal images. The algorithms implemented in OpenCV tend to produce realistic and therefore less dramatic results.

Let's look at the various options. Some of the common parameters of the different tone mapping algorithms are listed below.

- gamma : This parameter compresses the dynamic range by applying a gamma correction. When gamma is equal to 1, no correction is applied. A gamma of less than 1 darkens the image, while a gamma greater than 1 brightens the image.
- saturation : This parameter is used to increase or decrease the amount of saturation. When saturation is high, the colors are richer and more intense. Saturation value closer to zero, makes the colors fade away to grayscale.
- contrast : Controls the contrast (i.e. $\log(\text{maxPixelValue}/\text{minPixelValue})$) of the output image.

Let us explore one of the tone mapping algorithms available in OpenCV.

Reinhard Tonemap

```
createTonemapReinhard
(
  float    gamma = 1.0f,
  float    intensity = 0.0f,
  float    light_adapt = 1.0f,
  float    color_adapt = 0.0f
)
```

The parameter intensity should be in the [-8, 8] range. Greater intensity value produces brighter results. light_adapt controls the light adaptation and is in the [0, 1] range. A value of 1 indicates adaptation based only on pixel value and a value of 0 indicates global adaptation. An in-between value can be used for a weighted combination of the two. The parameter color_adapt controls chromatic adaptation and is in the [0, 1] range. The channels are treated independently if the value is set to 1 and the adaptation level is the same for every channel if the value is set to 0. An in-between value can be used for a weighted combination of the two.

For more details, check out this [paper](#).

```
In [ ]: import matplotlib.pyplot as plt
# Tonemap using Reinhard's method to obtain 24-bit color image
tonemapReinhard = cv2.createTonemapReinhard(1.5, 0,0,0)

### The following two lines is to tone map radiance map "hdrDebevec" from OpenCV's algorithm. Please use this function to tone map your radiance map and plot it.
ldrReinhard = tonemapReinhard.process(hdrDebevec)
plt.imshow(ldrReinhard)
plt.show()
### TODO: Call OpenCV's function to tonemap the radiance map you have recovered.
ldrReinhard = tonemapReinhard.process(radiancemap)
plt.imshow(ldrReinhard)
plt.show()
# You may want to save the tonemapped image to a file.
# cv2.imwrite("ldr-Reinhard.jpg", ldrReinhard * 255)
```



Recent methods

There is a [NTIRE challenge](#) in HDRI, and the methods proposed in year 2021 (almost deep learning based) are summarized in this [paper](#).

References

Book

- High dynamic range imaging: acquisition, display, and image-based lighting
 - Reinhard, Erik, et al. ,2010
 - The bible of the HDR imaging

HDR Image Reconstruction

- Debevec, Paul E., and Jitendra Malik. "Recovering high dynamic range radiance maps from photographs." Proceedings of the 24th annual conference on Computer graphics and interactive techniques. ACM Press/Addison-Wesley Publishing Co., 1997.
 - The basic but effective method for HDR image reconstruction, this paper motivates many works about HDR imaging
 - Matrix form solution(including least square term and smoothness term)
- Robertson, Mark, Sean Borman, and Robert L. Stevenson. "Dynamic range improvement through multiple exposures." Image Processing, 1999. ICIP 99. Proceedings. 1999 International Conference on. Vol. 3. IEEE, 1999.
 - Maximum likelihood solution, consider the additive noise and dequantization error as independent Gaussian random variable
 - Iterative method derived from the partial differential equation results
- Mitsunaga, Tomoo, and Shree K. Nayar. "Radiometric self calibration." Computer Vision and Pattern Recognition, 1999. IEEE Computer Society Conference on.. Vol. 1. IEEE, 1999.
 - Use polynomials to model the CRF
 - Iterative method with rough estimation of exposure time ratio
- Lin, Stephen, et al. "Radiometric calibration from a single image." Computer Vision and Pattern Recognition, 2004. CVPR 2004. Proceedings of the 2004 IEEE Computer Society Conference on. Vol. 2. IEEE, 2004.
 - Single image HDR scheme
 - Based on the edge color distribution

Image Alignment and Registration

- Ward, Greg. "Fast, robust image registration for compositing high dynamic range photographs from hand-held exposures." Journal of graphics tools 8.2 (2003): 17-30.
 - Median threshold bitmap (MTB) for global alignment
 - Very efficient (due to based on bitwise operation)
- Kang, Sing Bing, et al. "High dynamic range video." ACM Transactions on Graphics (TOG) 22.3 (2003): 319-325.
 - Both global and local registration
 - A variant of LK optical flow
 - A strategy to obtain HDR video

Alternative to HDR imaging Exposure Fusion Two series of paper

- Mertens, Tom, Jan Kautz, and Frank Van Reeth. "Exposure fusion." Computer Graphics and Applications, 2007. PG'07. 15th Pacific Conference on. IEEE, 2007.
- Mertens, Tom, Jan Kautz, and Frank Van Reeth. "Exposure fusion: A simple and practical alternative to high dynamic range photography." Computer Graphics Forum. Vol. 28. No. 1. Blackwell Publishing Ltd, 2009.
 - Scalar-weighted map is first generated based on the quality measurement (contrast, saturation, well-exposedness) of the exposure bracketed image, then the fusion is performed in the multiresolution manner (Each layer of the Laplacian pyramid of resulting image is computed by the pixel-based multiplication if Gaussian pyramids of the weighted map with Laplacian pyramids of the original image)