

Chapter 9 Question 2

• given:

$$9.4 \quad \lambda(t) = e^{\beta_0 + \beta_1 x(t) + \beta_2 x(t)^2}$$

$$9.5 \quad \lambda(t) = \alpha e^{\frac{-(x(t) - \mu)^2}{2\sigma^2}}$$

$$\alpha = e^{\beta_0 - \frac{\beta_1^2}{4\beta_2}} \quad \mu = -\frac{\beta_1}{2\beta_2} \quad \sigma^2 = -\frac{1}{2\beta_2}$$

• proof

$$9.5 \quad \lambda(t) = \alpha e^{\frac{-(x(t) - \mu)^2}{2\sigma^2}}$$

$$= e^{\beta_0 - \frac{\beta_1^2}{4\beta_2}} e^{\frac{-(x(t) + \frac{\beta_1}{2\beta_2})^2}{2(-\frac{1}{2\beta_2})}}$$

$$= e^{\beta_0 - \frac{\beta_1^2}{4\beta_2} + \frac{-(x(t) + \frac{\beta_1}{2\beta_2})^2}{2(-\frac{1}{2\beta_2})}}$$

$$= e^{\beta_0 - \frac{\beta_1^2}{4\beta_2} + \beta_2 (x(t) + \frac{\beta_1}{2\beta_2})^2}$$

$$= e^{\beta_0 - \frac{\beta_1^2}{4\beta_2} + \beta_2 [x(t)^2 + 2(\frac{\beta_1}{2\beta_2} x(t)) + \frac{\beta_1^2}{4\beta_2^2}]}$$

$$= e^{\beta_0 - \frac{\beta_1^2}{4\beta_2} + \beta_2 x(t)^2 + \beta_1 x(t) + \frac{\beta_1^2}{4\beta_2}}$$

$$= e^{\beta_0 + \beta_1 x(t) + \beta_2 x(t)^2}$$

$$= \lambda(t) \quad 9.4$$